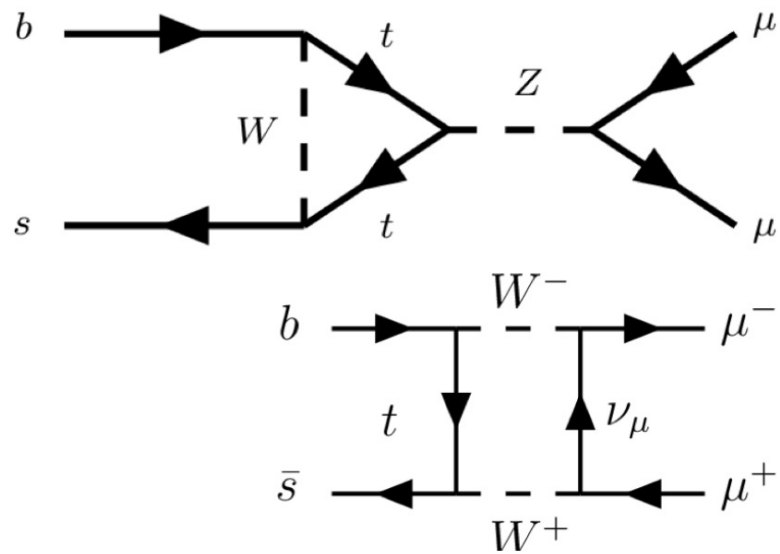


Rare decays

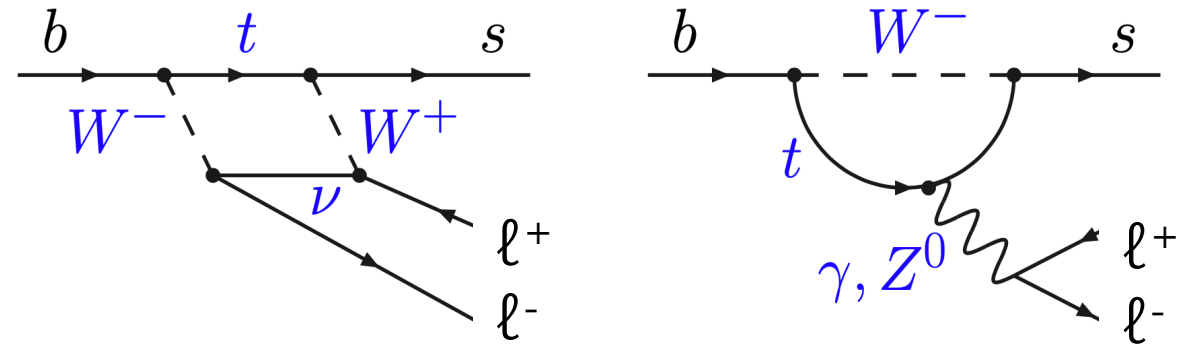


(very) rare decays: $b \rightarrow s \ell^+ \ell^-$ transitions

$B_s \rightarrow \ell^+ \ell^-$



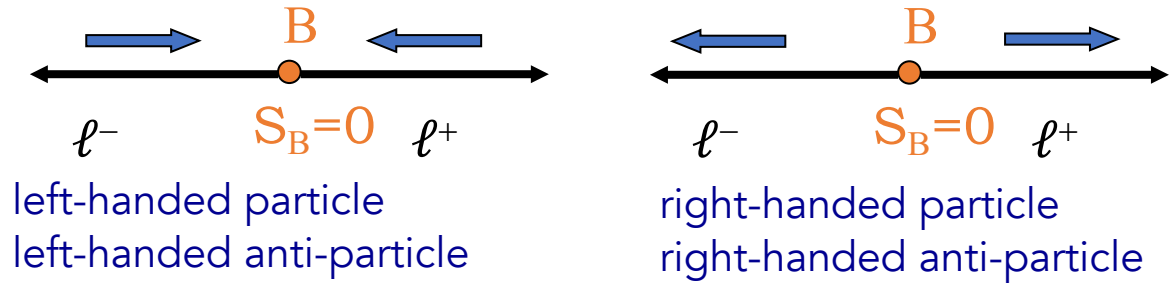
$H_b \rightarrow H_s \ell^+ \ell^-$



$$B_{s/d} \rightarrow \ell^+ \ell^- \quad \ell = e \text{ or } \mu$$

SM : very rare (V_{tq} , helicity suppression)

In the SM, in the massless limit: left-handed anti-particle & right-handed particle are forbidden



$$\mathcal{B}(B_s^0 \rightarrow e^+ e^-) = (8.60 \pm 0.36) \times 10^{-14}$$

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (3.66 \pm 0.14) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow e^+ e^-) = (2.41 \pm 0.13) \times 10^{-15}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) = (1.03 \pm 0.05) \times 10^{-10}$$

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SM

Due to CKM, the B_d modes are further suppressed by a factor 1/30

Sensitive to the scalar sector

New Physics models with an extended Higgs sector

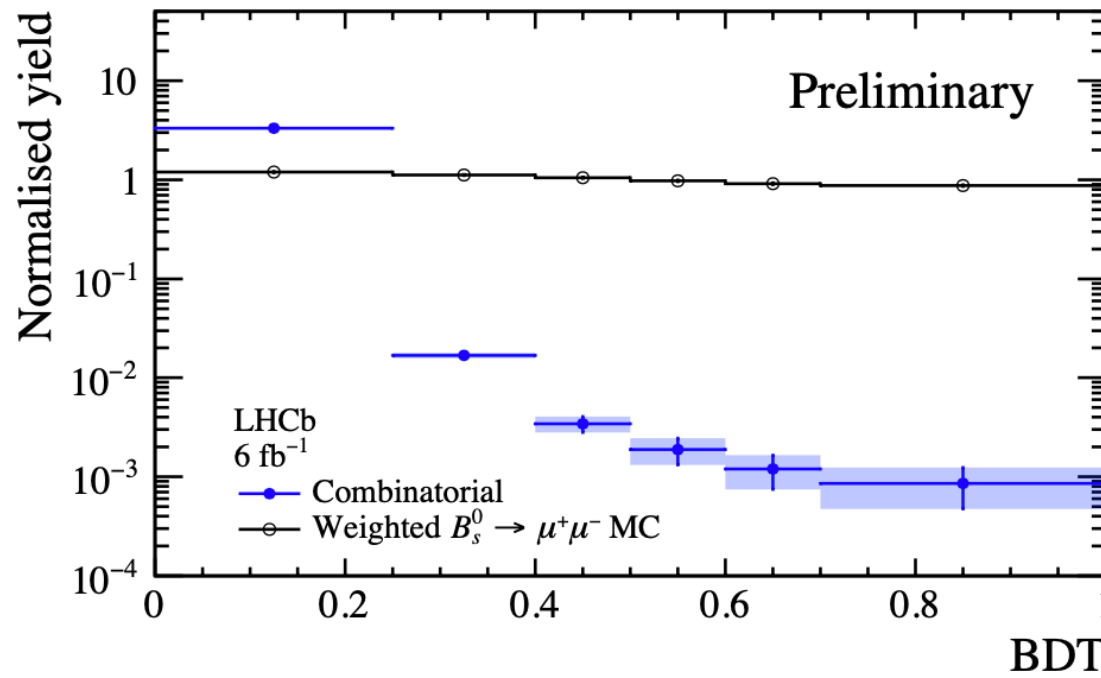
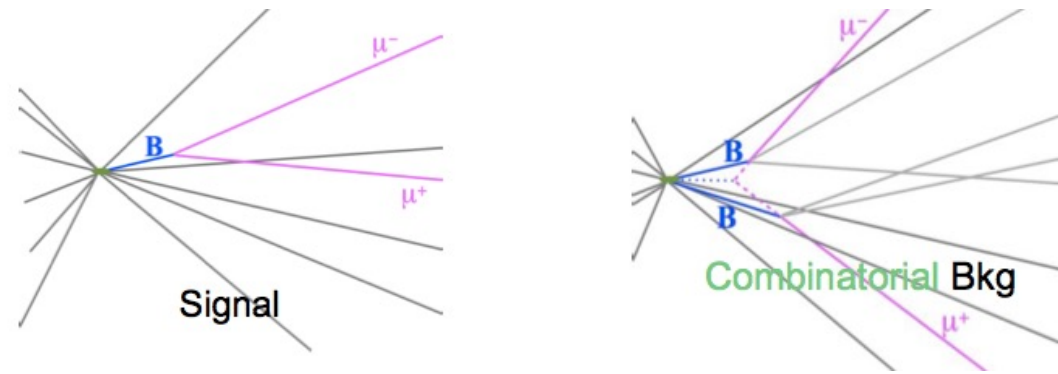
$$\text{BR}^{\text{MSSM}} \propto \tan^6 \beta / M_A^4$$

ratio of the vevs of the two Higgs doublets

First searches in 1985 (!) : CLEO $\text{BR} < 10^{-4}$ @ 90% CL

Analysis in a nutshell

- Huge sample of B mesons
- Efficient trigger
- Powerful selection
 - Vertex resolution
 - Mass resolution
 - Muon ID
- BDT algorithm



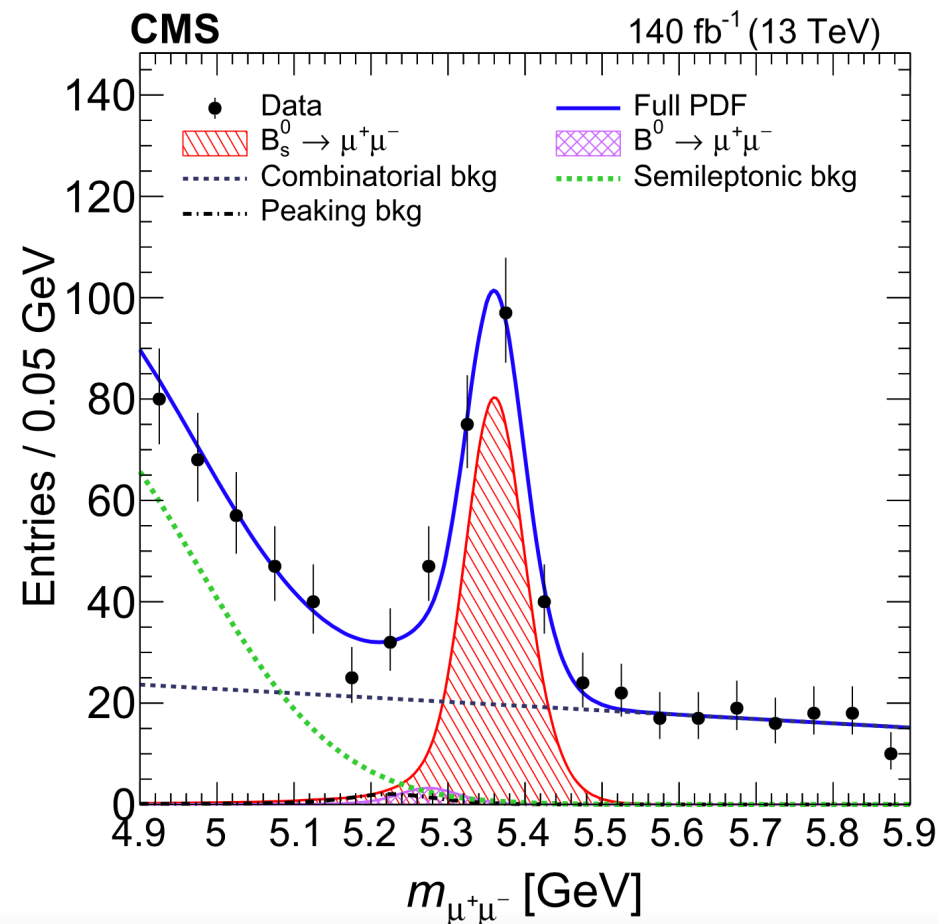
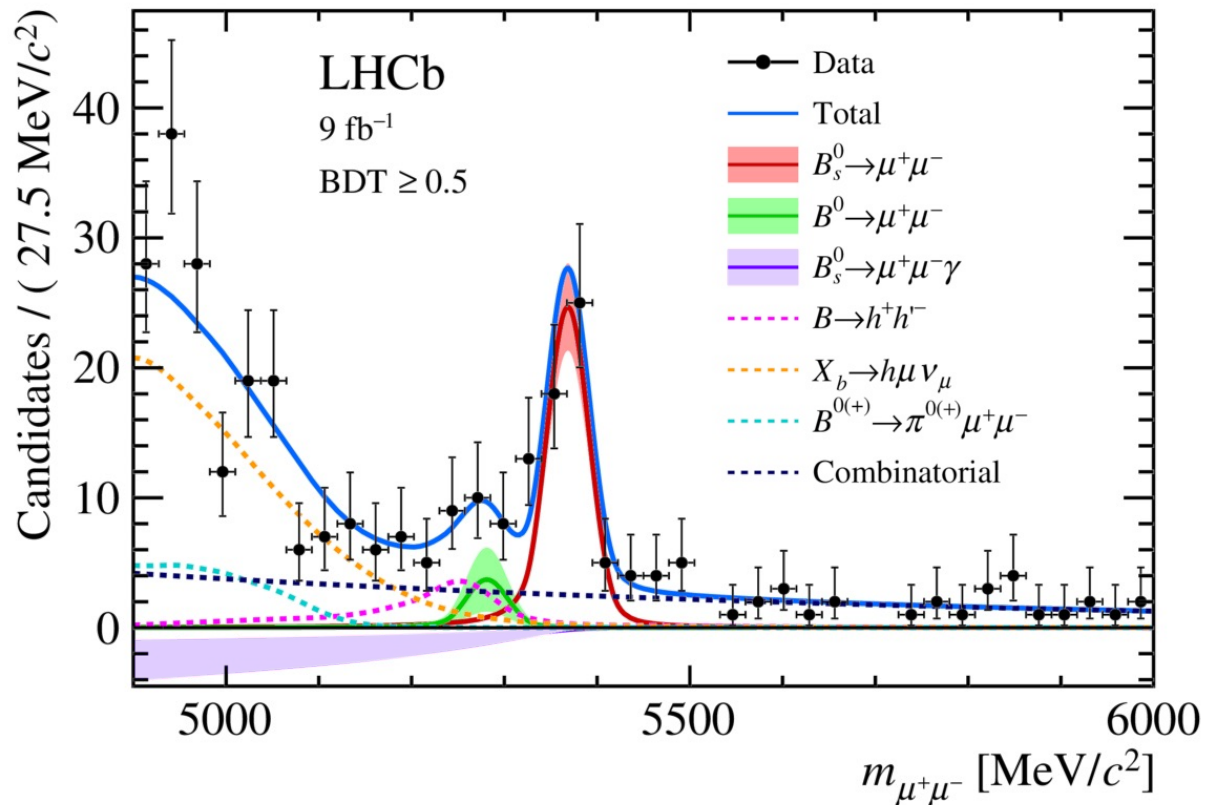
Expectations (from SM)

$$N(B_s^0 \rightarrow \mu^+\mu^-)_{SM} = 147 \pm 8$$

$$N(B^0 \rightarrow \mu^+\mu^-)_{SM} = 16 \pm 1$$

- Branching fraction estimated from a fit in 5 BDT bins (first one excluded since it's background dominated) and two run periods (Run1 & Run2)

Two most precise measurements: CMS & LHCb



[LHCb-PAPER-2021-007](#)

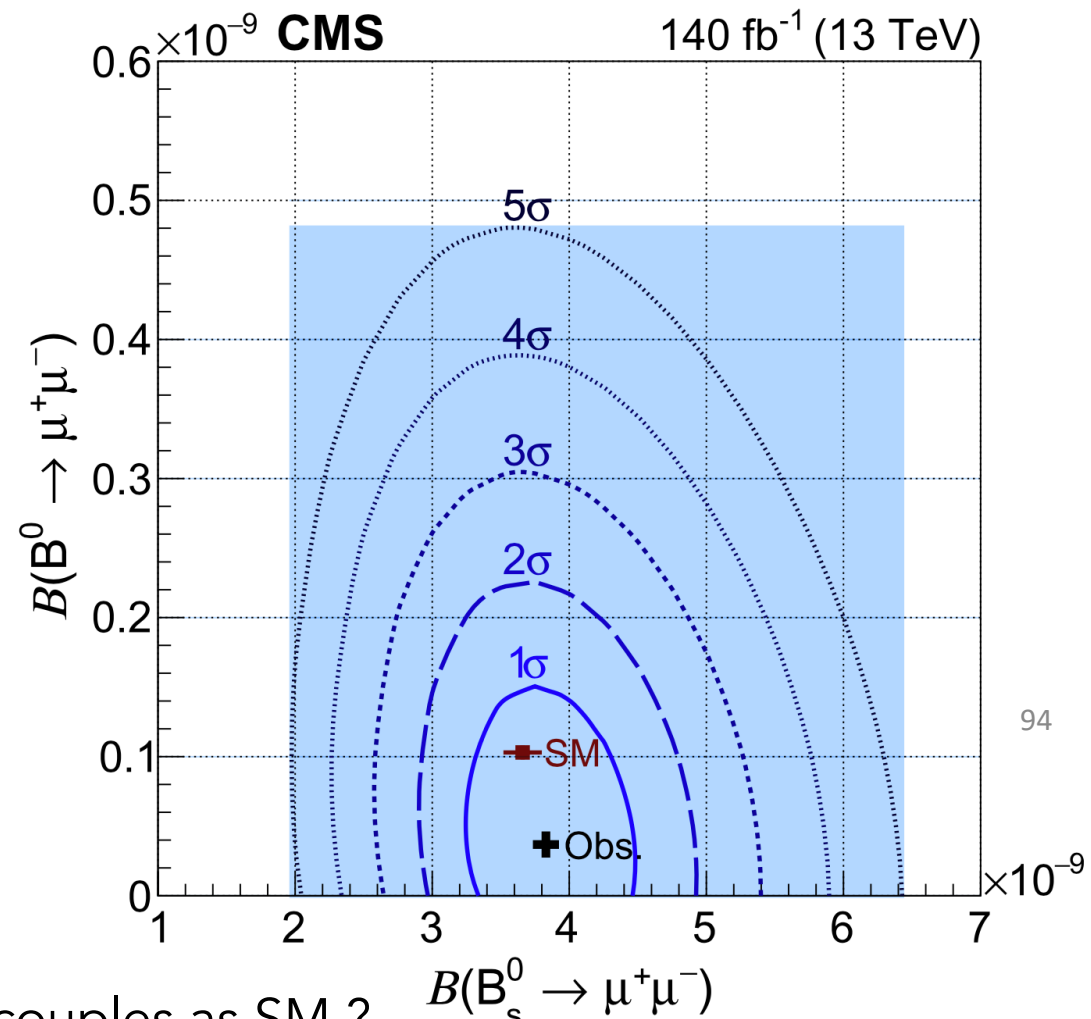
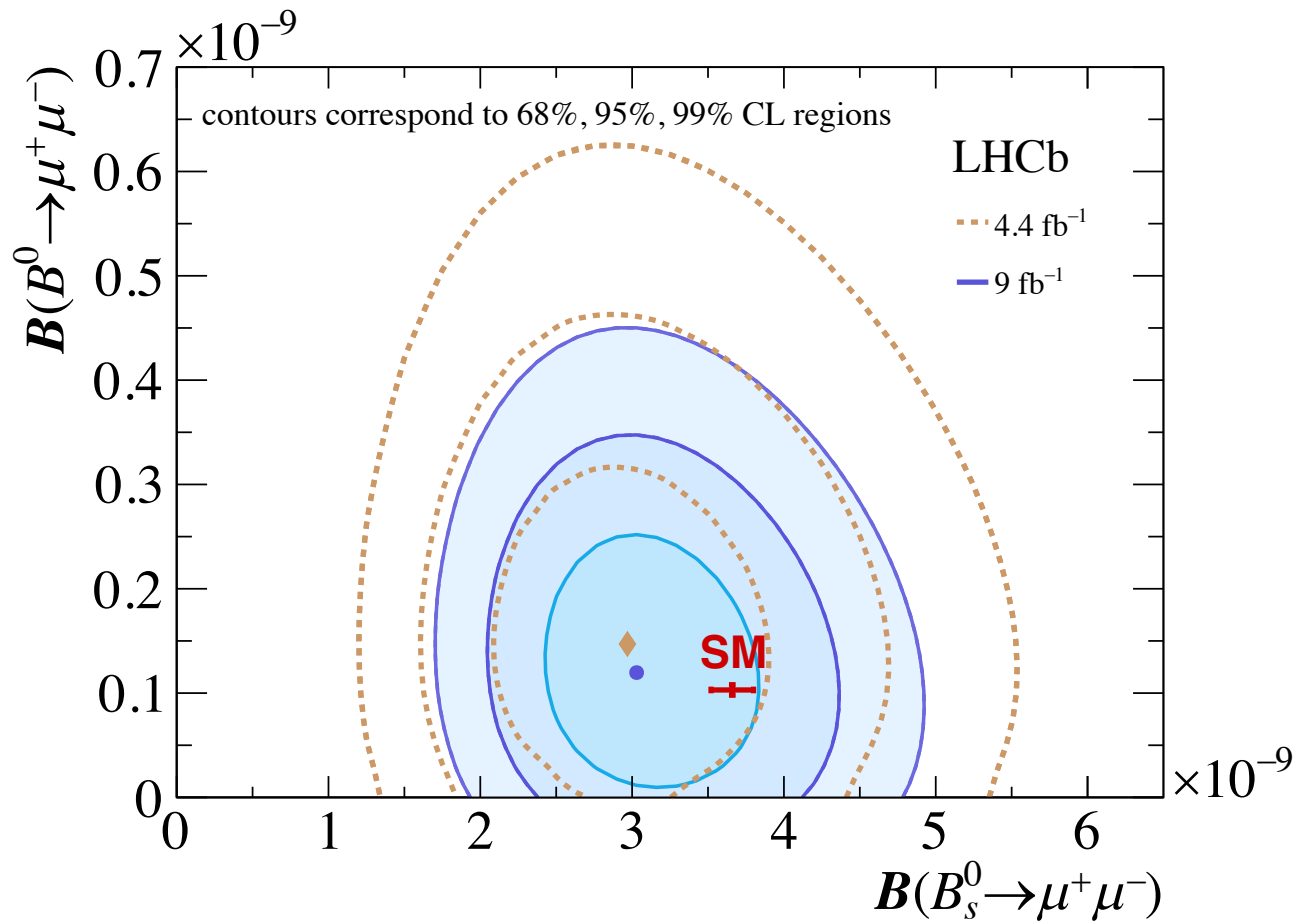
$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (3.09^{+0.46+0.15}_{-0.43-0.11}) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) < 2.6 \times 10^{-10}$$

@ 95 % CL

$$\begin{aligned} \mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) &= \\ &= \left[3.83^{+0.38}_{-0.36} \text{ (stat)}^{+0.19}_{-0.16} \text{ (syst)}^{+0.14}_{-0.13} (f_s/f_u) \right] \times 10^{-9}, \end{aligned}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) < 1.9 \times 10^{-10} \text{ at 95\% CL.}$$



Important to check B_d vs B_s : if there is New Physics does it couples as SM ?

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-) = 3.52^{+0.32}_{-0.30} \times 10^{-9}$$

Combination from arXiv:2210.07221

Color meets Flavor school Bad Honnef March 2024

SM-like given the current precision

$H_b \rightarrow H_s \ell^+ \ell^-$: what do we measure ?

Branching Fractions

Angular observables

Lepton Flavour Universality
observables:
Branching Fractions ratios
angular observables ratios



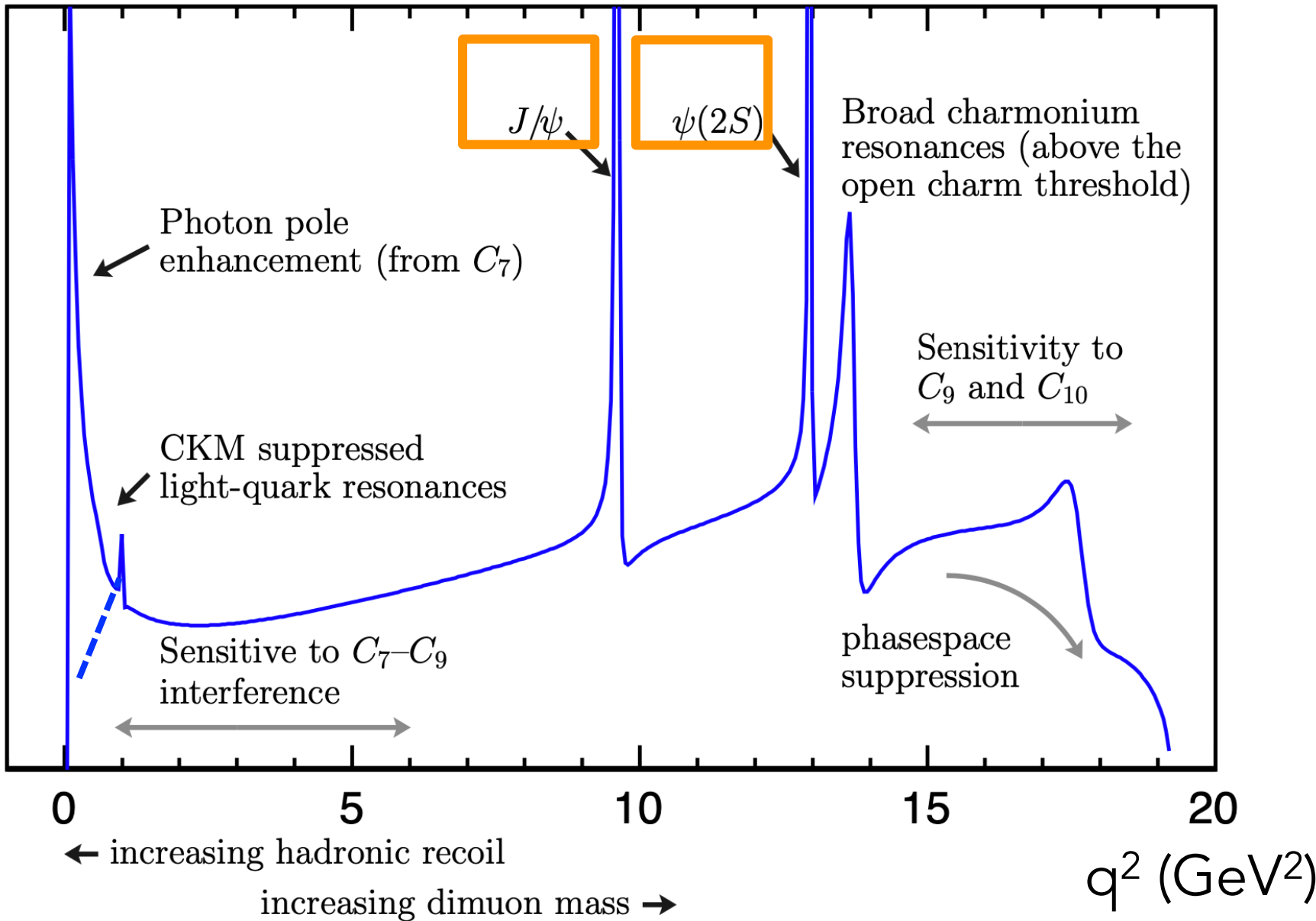
theoretical
cleanness

there is no free lunch



resonant (control) modes

$d\Gamma/dq^2$



— $B \rightarrow K^* \ell \ell$
 - - - $B \rightarrow K \ell \ell$

One example of a BF measurement: $B_s \rightarrow \phi \mu \mu$

$$q^2 = M^2(\mu\mu)$$

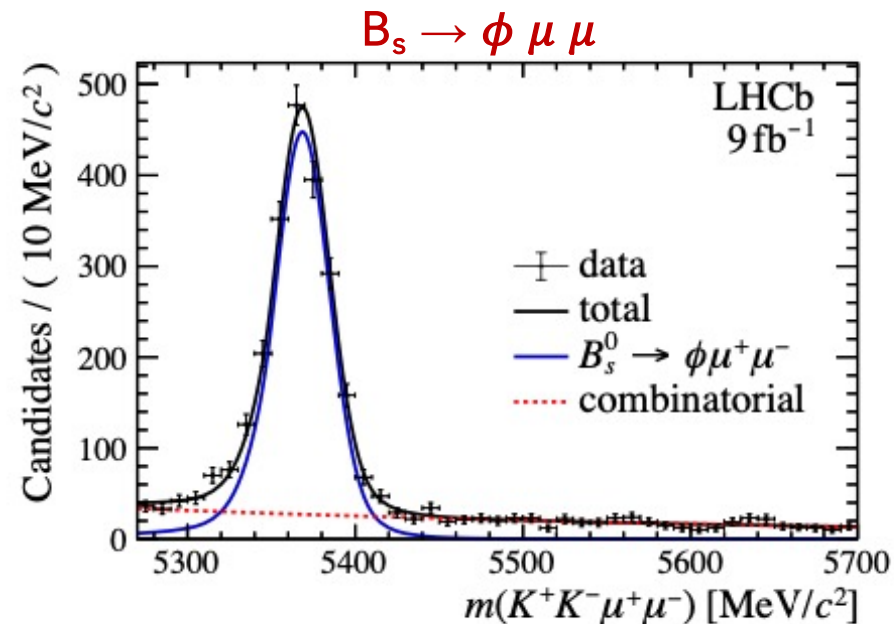
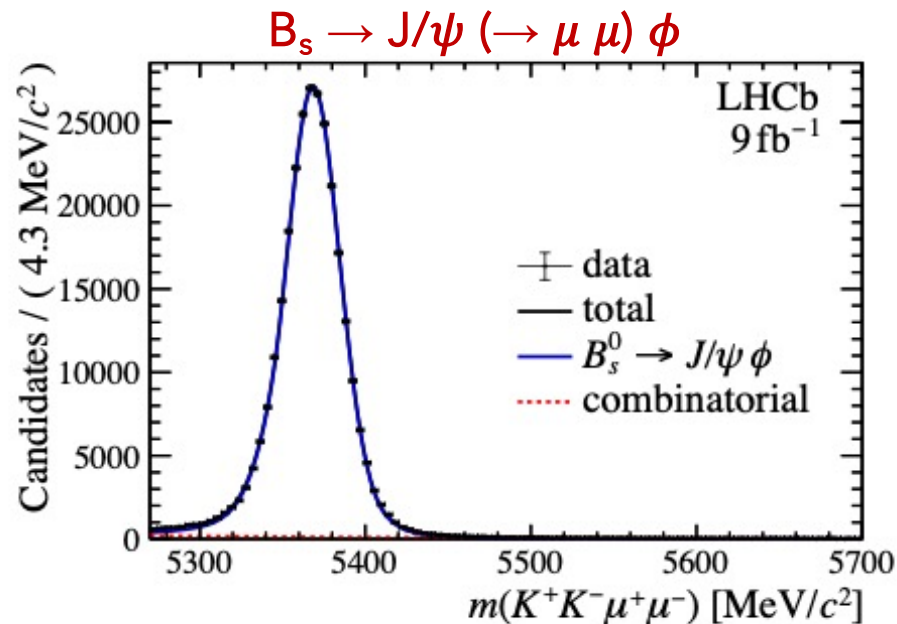
Experimentally 'easy' for LHCb

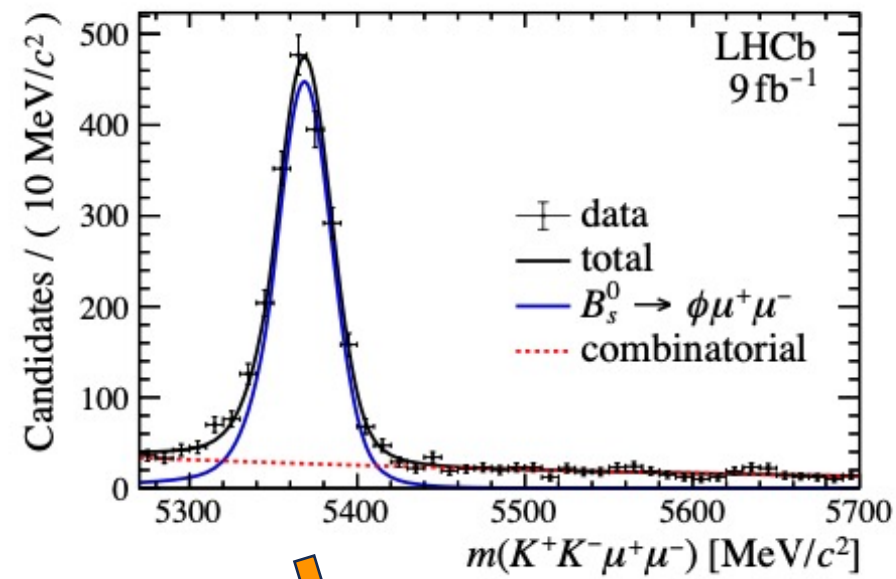
- two muons
- $\phi \rightarrow KK$ and is a narrow resonance

Use of $B_s \rightarrow J/\psi (\rightarrow \mu \mu) \phi$ as a normalisation mode

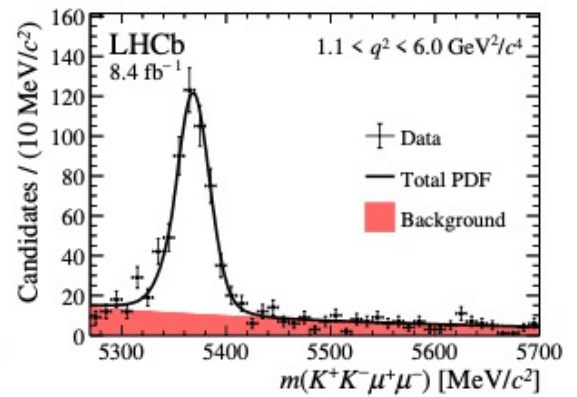
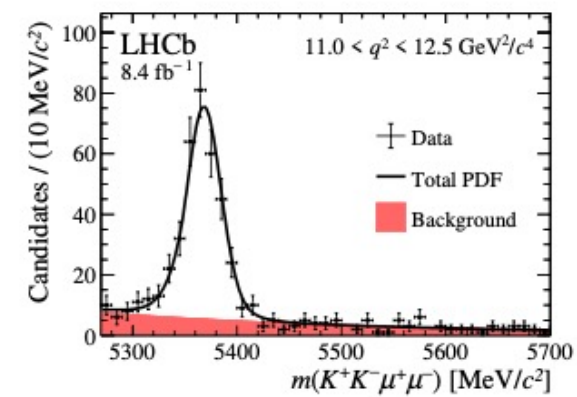
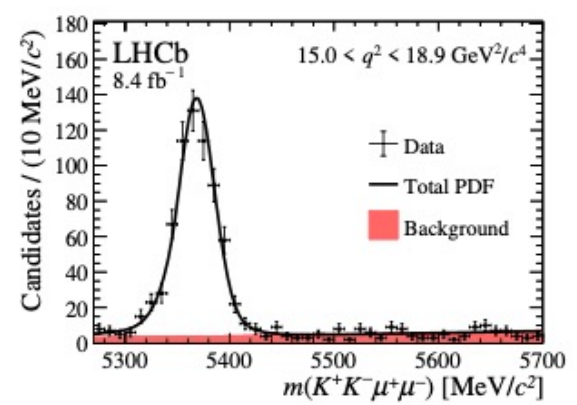
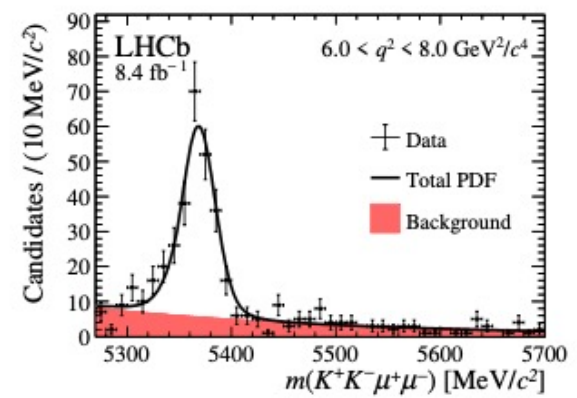
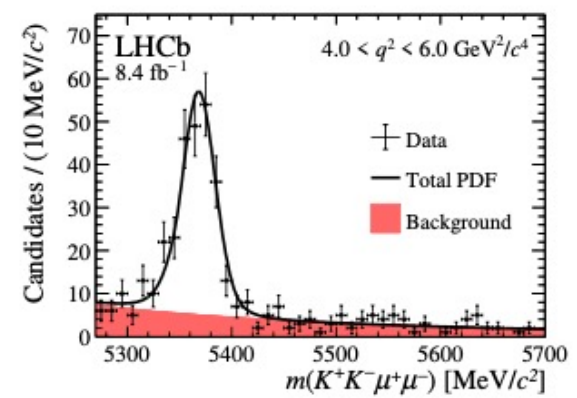
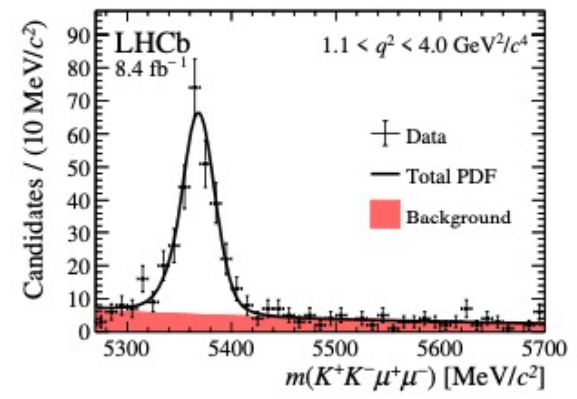
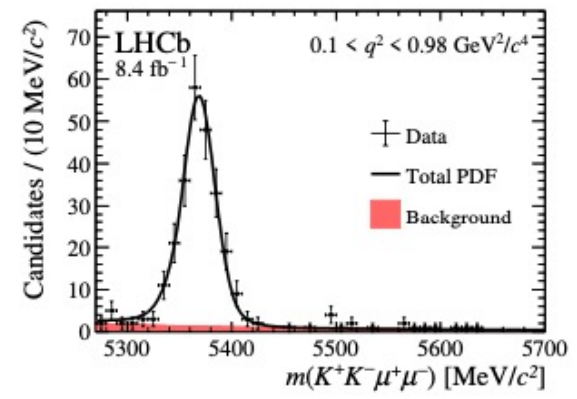
$$\mathcal{B}(B_s^0 \rightarrow J/\psi \phi) = (1.018 \pm 0.032 \pm 0.037) \times 10^{-3}$$

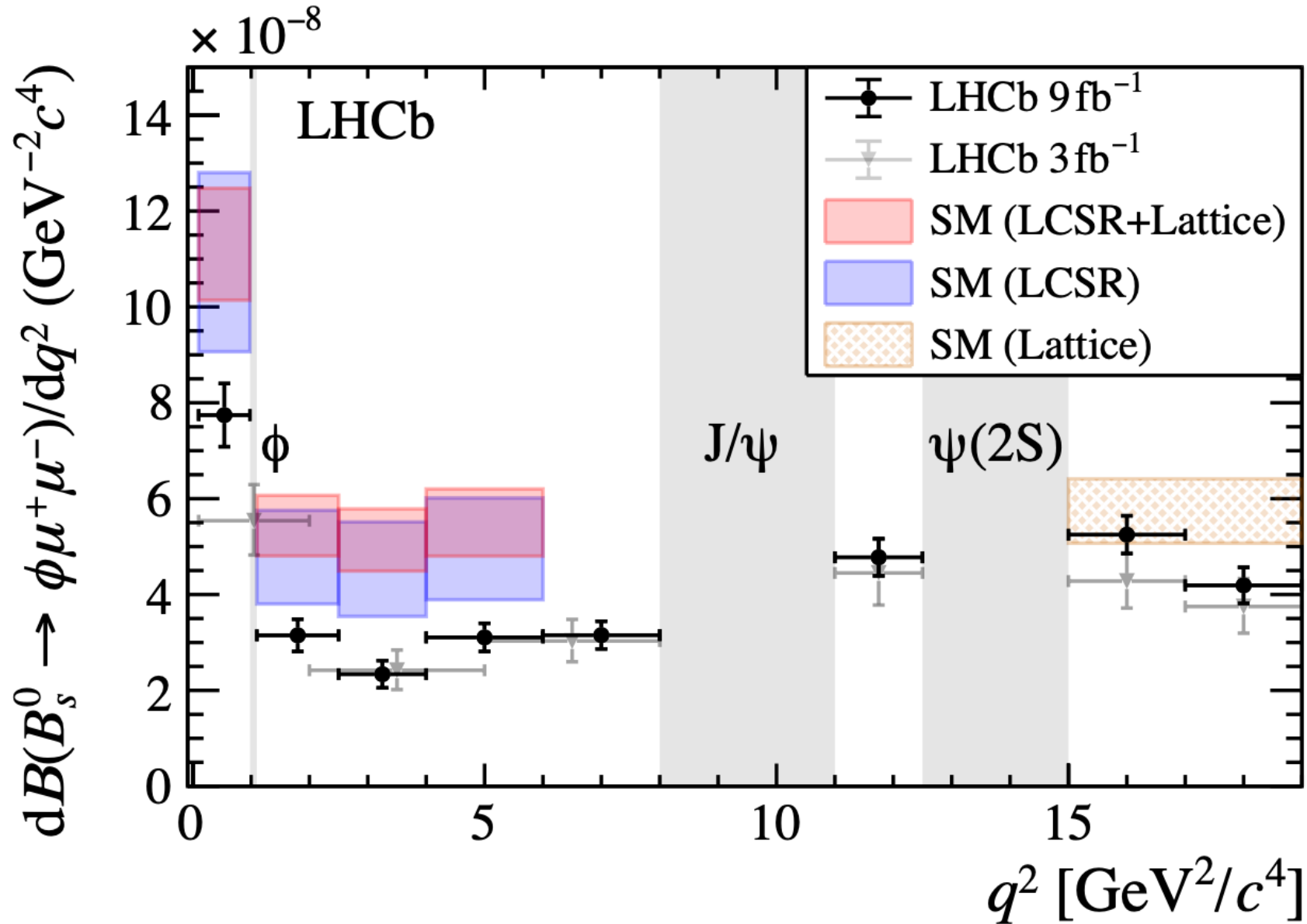
$$\frac{d\mathcal{B}(B_s^0 \rightarrow \phi \mu^+ \mu^-)}{dq^2} = \frac{\mathcal{B}(B_s^0 \rightarrow J/\psi \phi) \times \mathcal{B}(J/\psi \rightarrow \mu^+ \mu^-)}{q_{\max}^2 - q_{\min}^2} \times \frac{N_{\phi \mu^+ \mu^-}}{N_{J/\psi \phi}} \times \frac{\epsilon_{J/\psi \phi}}{\epsilon_{\phi \mu^+ \mu^-}}$$





Split in 7 q^2 bins





Measurements below predictions

Predictions correlated from a bin to another

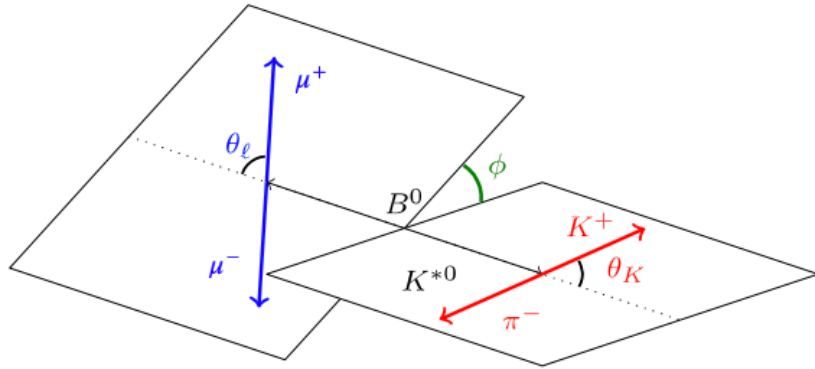
Better agreement at higher- q^2 (LQCD)

Similar patterns for other decay modes

To have more information: angular analyses

3 angles and $q^2 = M^2(\ell\ell)$

$B \rightarrow V \ell\ell$



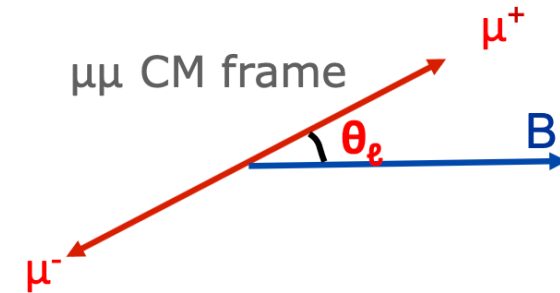
$\Lambda_b \rightarrow \Lambda^* \ell\ell$

$\Lambda_b \rightarrow \Lambda \ell\ell$

Assuming that the Λ_b is produced unpolarized at LHC

one angle and q^2

$B \rightarrow PS \ell\ell$



A set of anomalies in $b \rightarrow s \mu\mu$ transitions

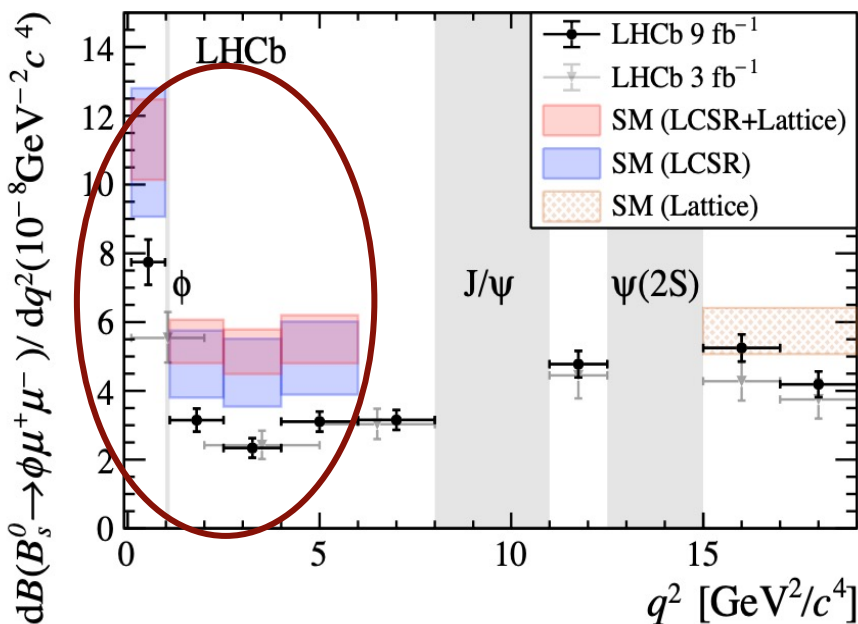
$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ with 6 fb^{-1} (~ 4600 evts.)

$B^+ \rightarrow K^{*+} \mu^+ \mu^-$ with 9 fb^{-1} (~ 700 evts.)

$B_s \rightarrow \phi \mu^+ \mu^-$ with 9 fb^{-1} (~ 1900 evts.)

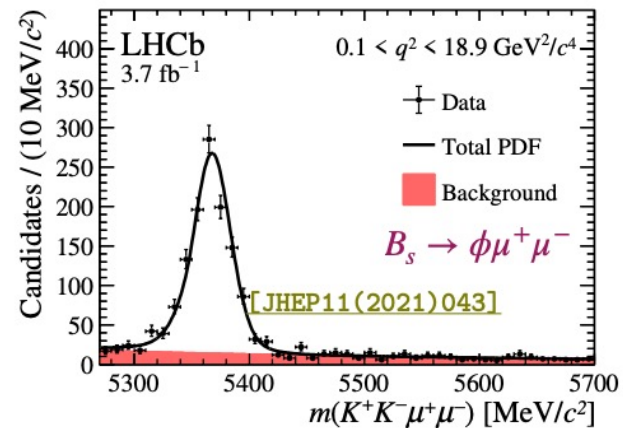
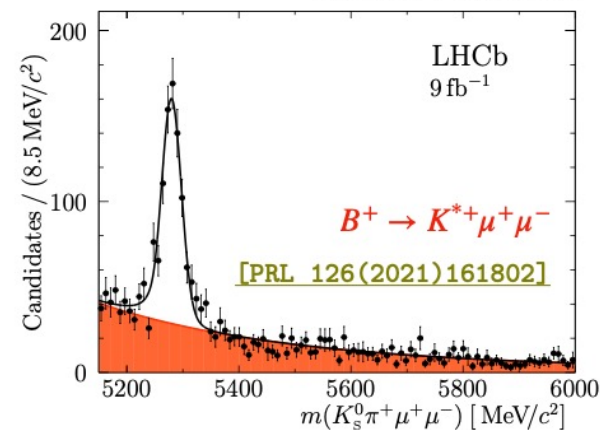
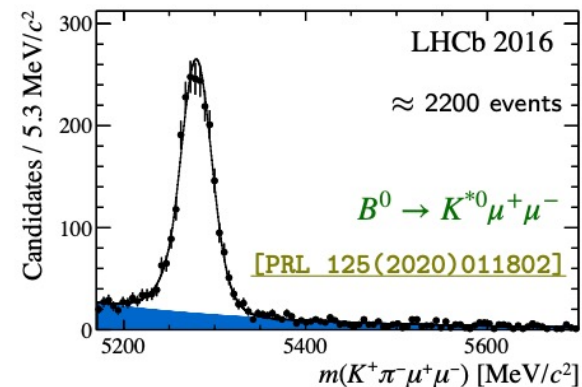
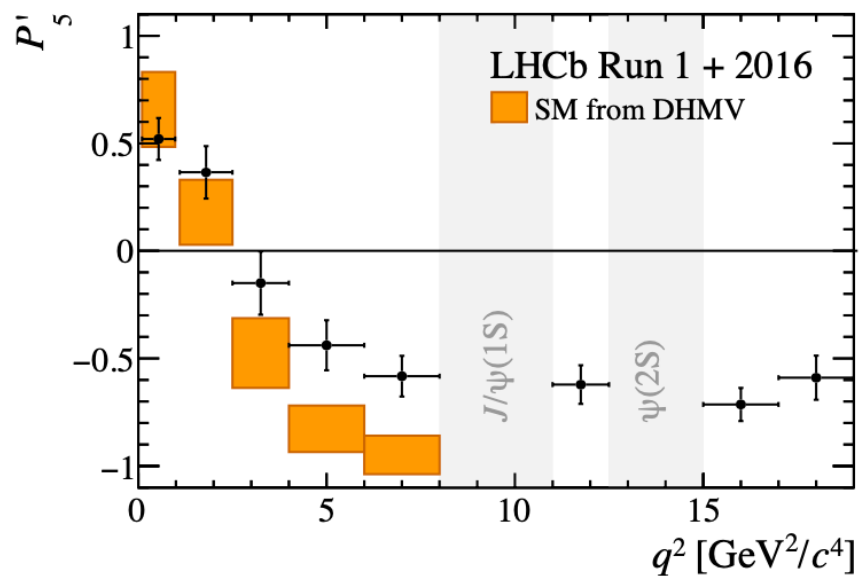
$B_s \rightarrow \phi \mu\mu$ $d\text{BR}/dq^2$

PRL 127 (2021) 151801



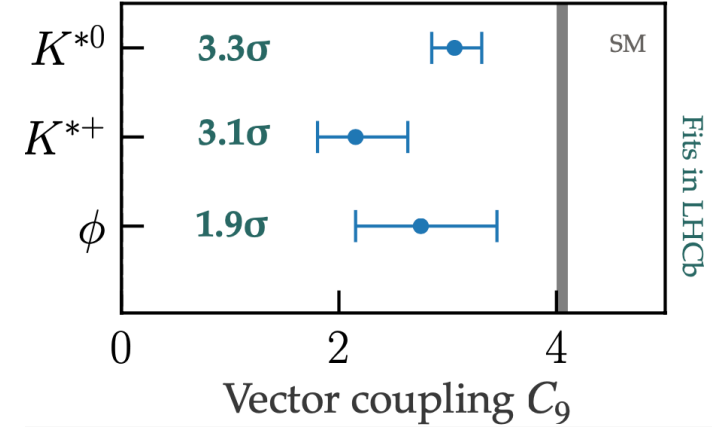
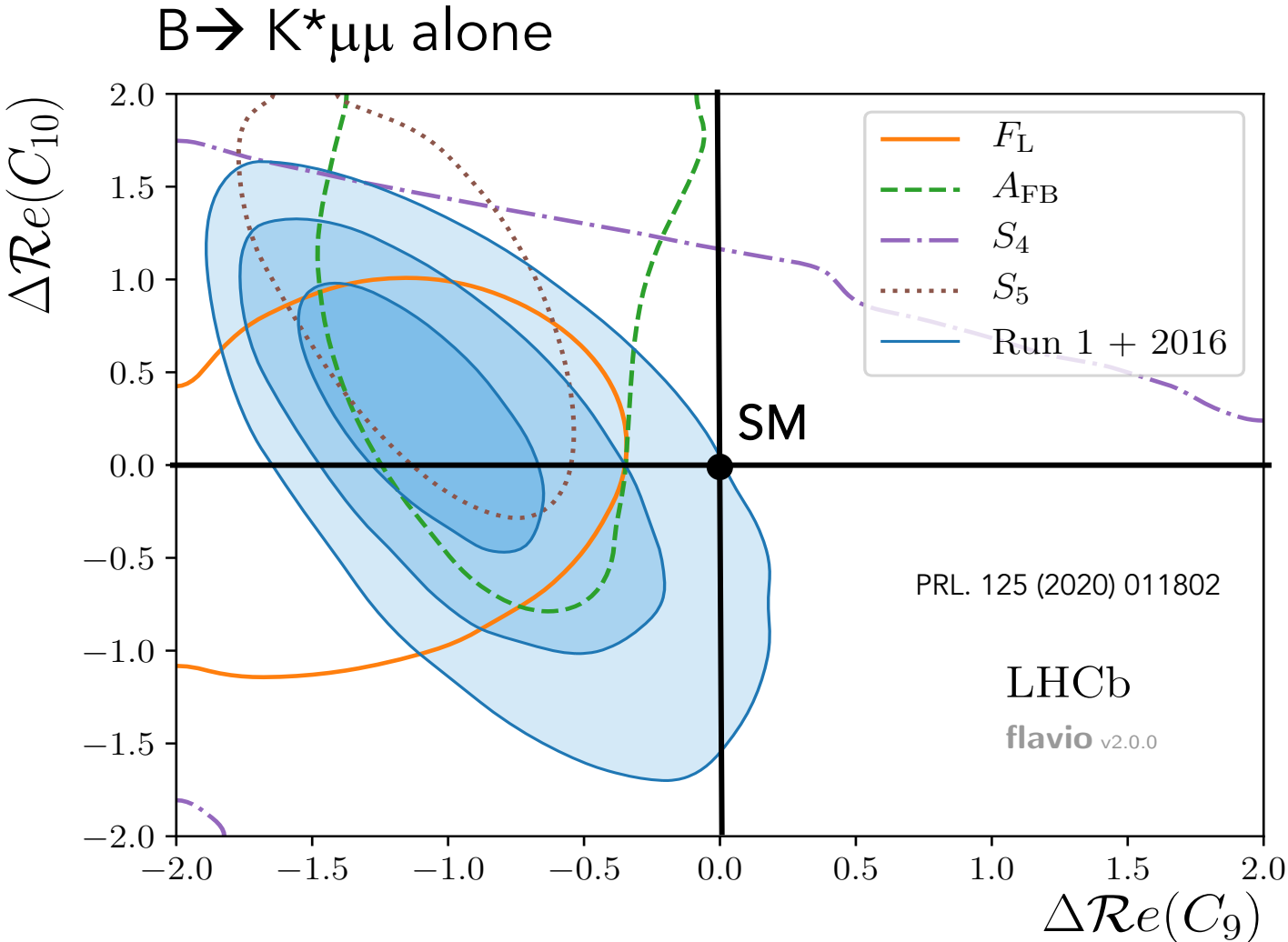
$B_d \rightarrow K^* \mu\mu$ angular fits

[Phys. Rev. Lett. 125 \(2020\) 011802](https://arxiv.org/abs/2001.01802)



$$C_i = C_i^{SM} + C_i^{NP}$$

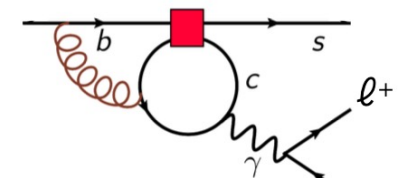
- In the SM Wilson coefficients are real, no necessarily the case for New Physics
- Many parameters fit... reduced configurations



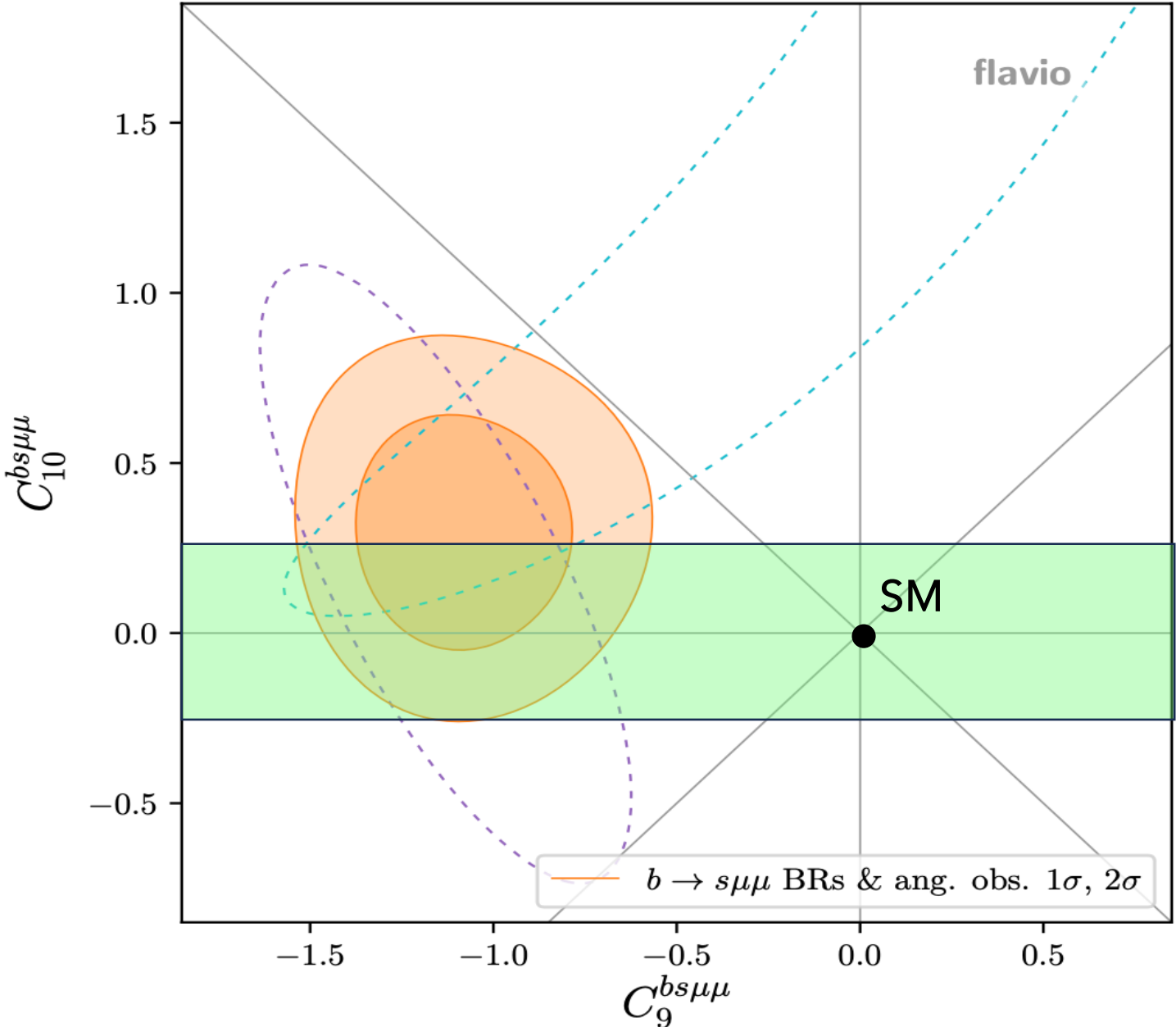
Global Wilson coefficients fit seems to indicate a pattern: different observables give a coherent picture

but

theoretical debate about $c\bar{c}$ loop impact

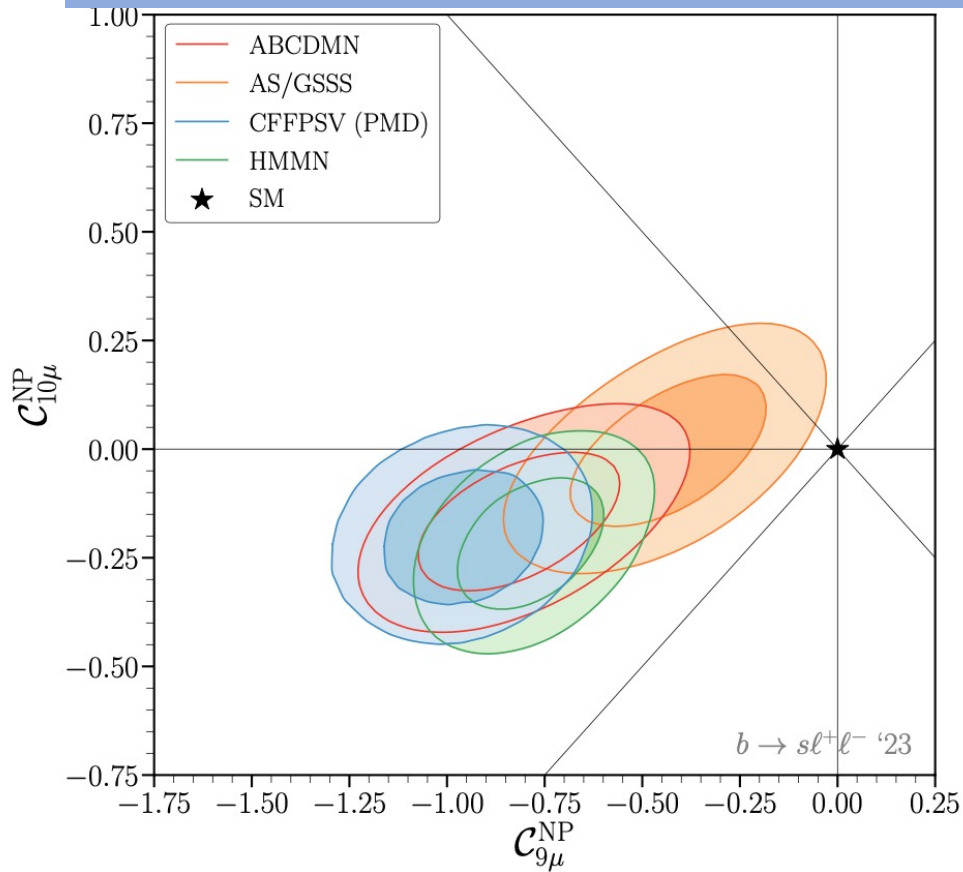


They can mimic C_9 shift

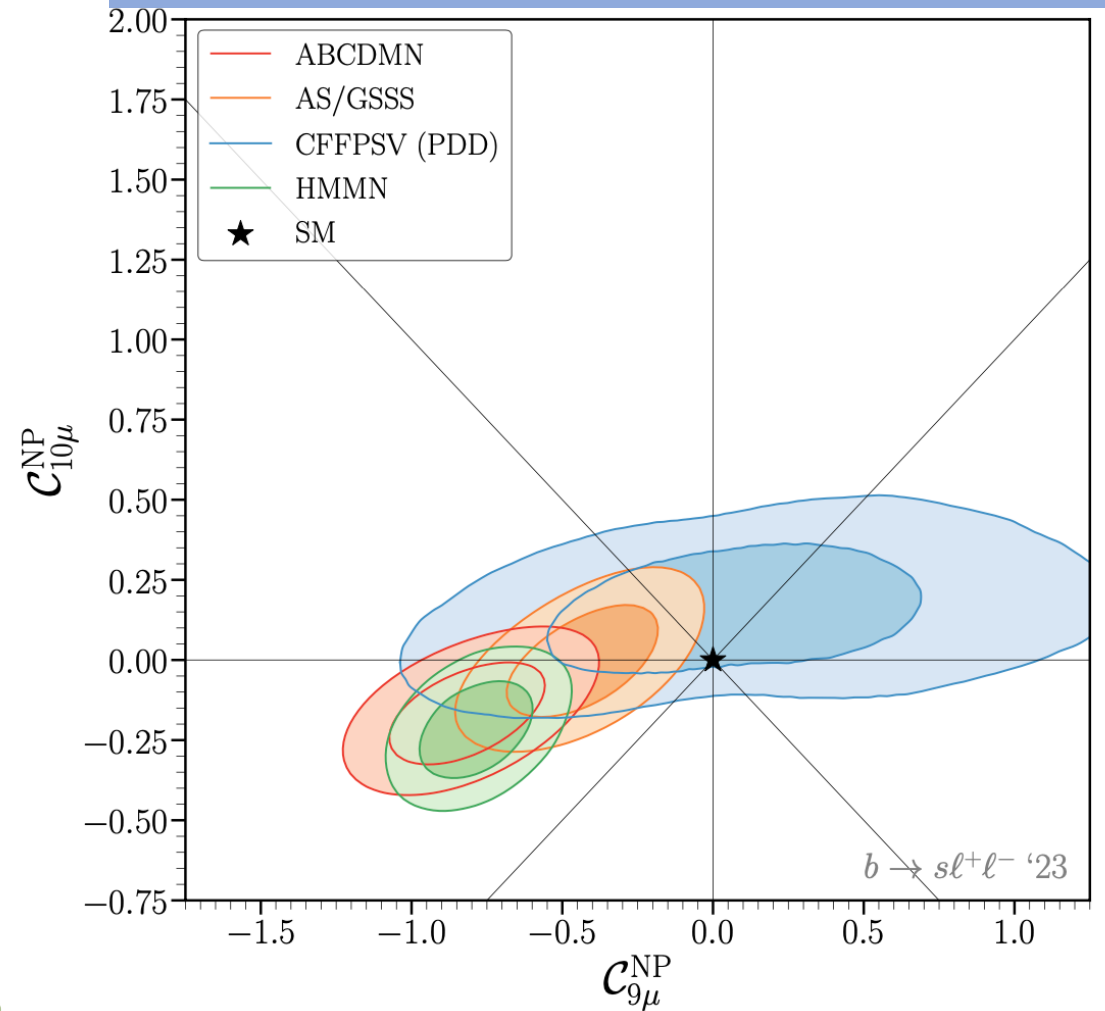


$B_s \rightarrow \mu\mu$

with TH input for the non-local contributions



No TH input for the non-local contributions



- ▶ **ABCDMN** (M. Algueró, A. Biswas, B. Capdevila, S. Descotes-Genon, J. Matias, M. Novoa-Brunet)
Statistical framework: χ^2 -fit, based on private code [arXiv:2304.07330](#)
- ▶ **AS / GSSS** (W. Altmannshofer, P. Stangl / A. Greljo, J. Salko, A. Smolkovic, P. Stangl)
Statistical framework: χ^2 -fit, based on public code `flavio` [arXiv:2212.10497](#).
- ▶ **CFFPSV** (M. Ciuchini, M. Fedele, E. Franco, A. Paul, L. Silvestrini, M. Valli)
Statistical framework: Bayesian MCMC fit, based on public code `HEPfit` [arXiv:2212.10516](#)
- ▶ **HMMN** (T. Hurth, F. Mahmoudi, D. Martínez-Santos, S. Neshatpour)
Statistical framework: χ^2 -fit, based on public code `SuperIso` [arXiv:23xx.xxxxx](#)

From B. Capdevila
FPCP 2023

$B_{s/d} \rightarrow \mu^+ \mu^- :$

- clean prediction (relative precision $\sim 4 - 5 \%$)
- clean measurement for B_s ($\sim 10\%$) ; B_d not yet measured.

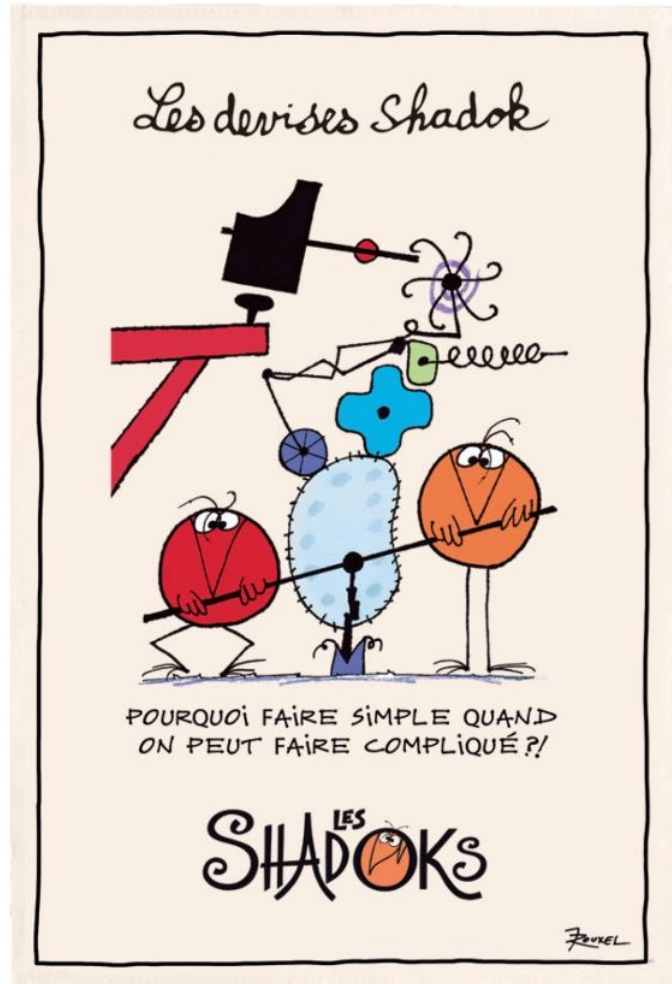
😊 clear road
 C_{10} constraint

$H_b \rightarrow H_s \mu^+ \mu^- :$

- clean measurements ($\sim 10\%$ on BR in various q^2 bins)
- TH predictions not very precise for the BR. Better for angular observables.
- How to mitigate/constraint the impact of non-local contributions ?

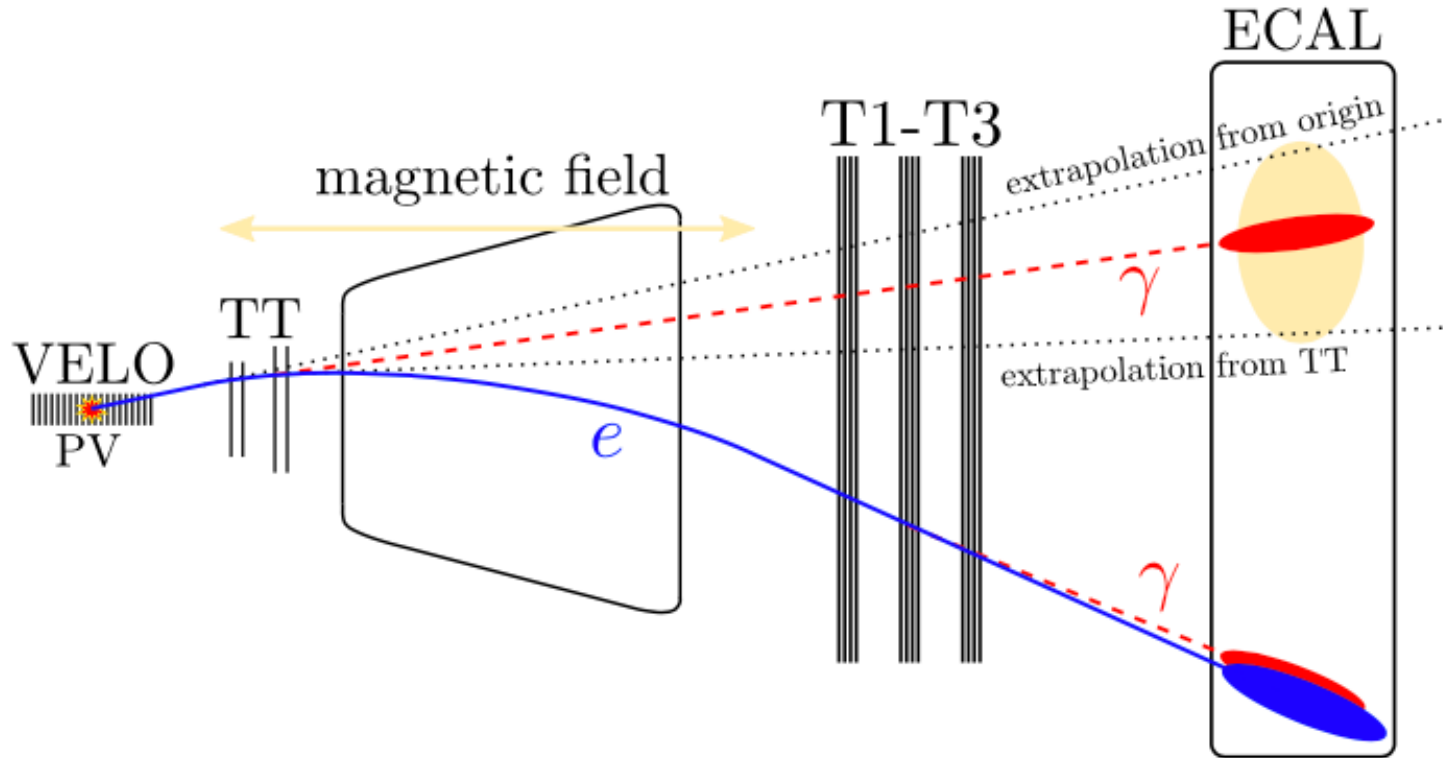
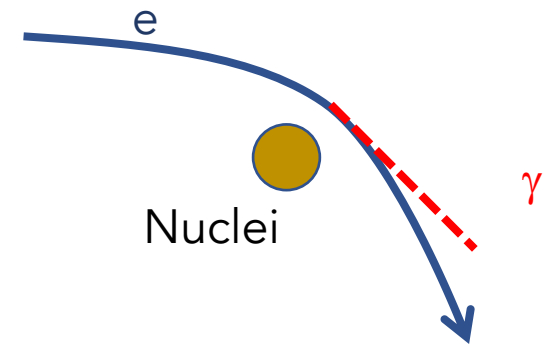
?????

Why not electrons ?



Let's use the electrons and double our statistics !

Electrons emit Bremsstrahlung



Before the magnet

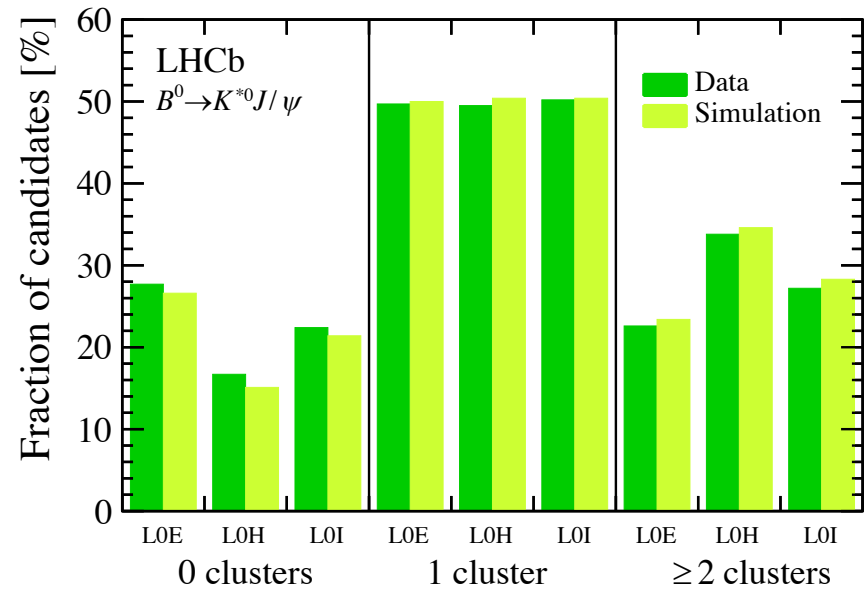
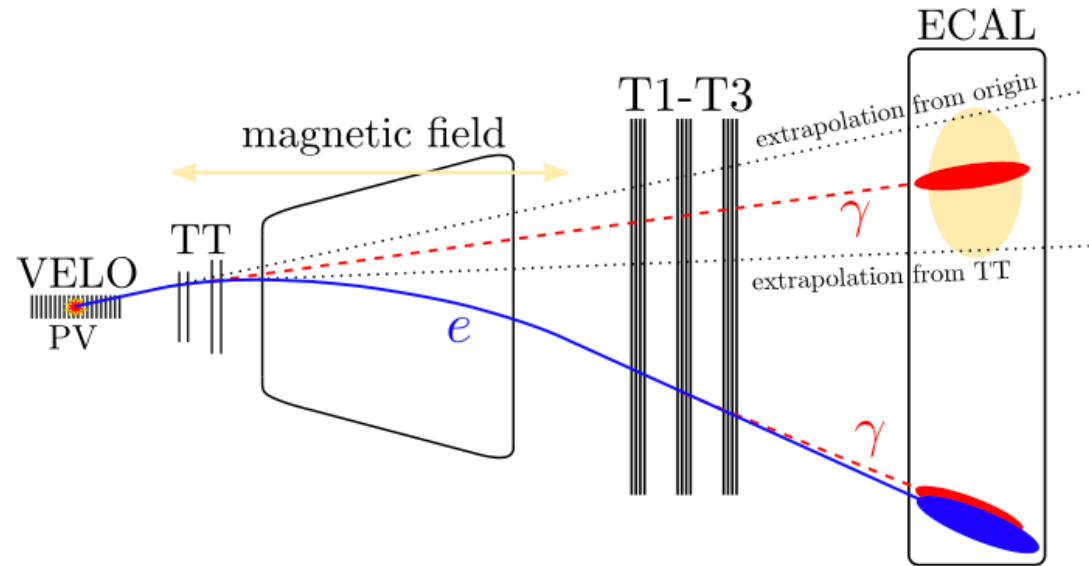
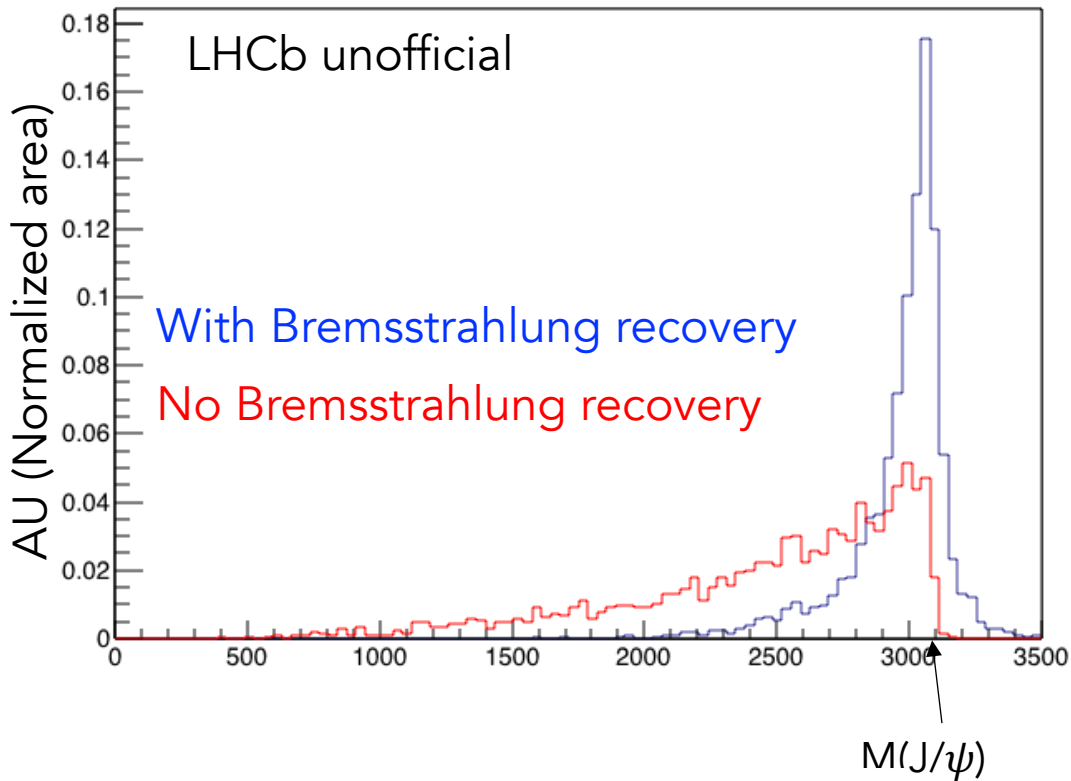
- electron can be swept out (=lost !)
- kinematics are "wrong"

After the magnet

- not an issue

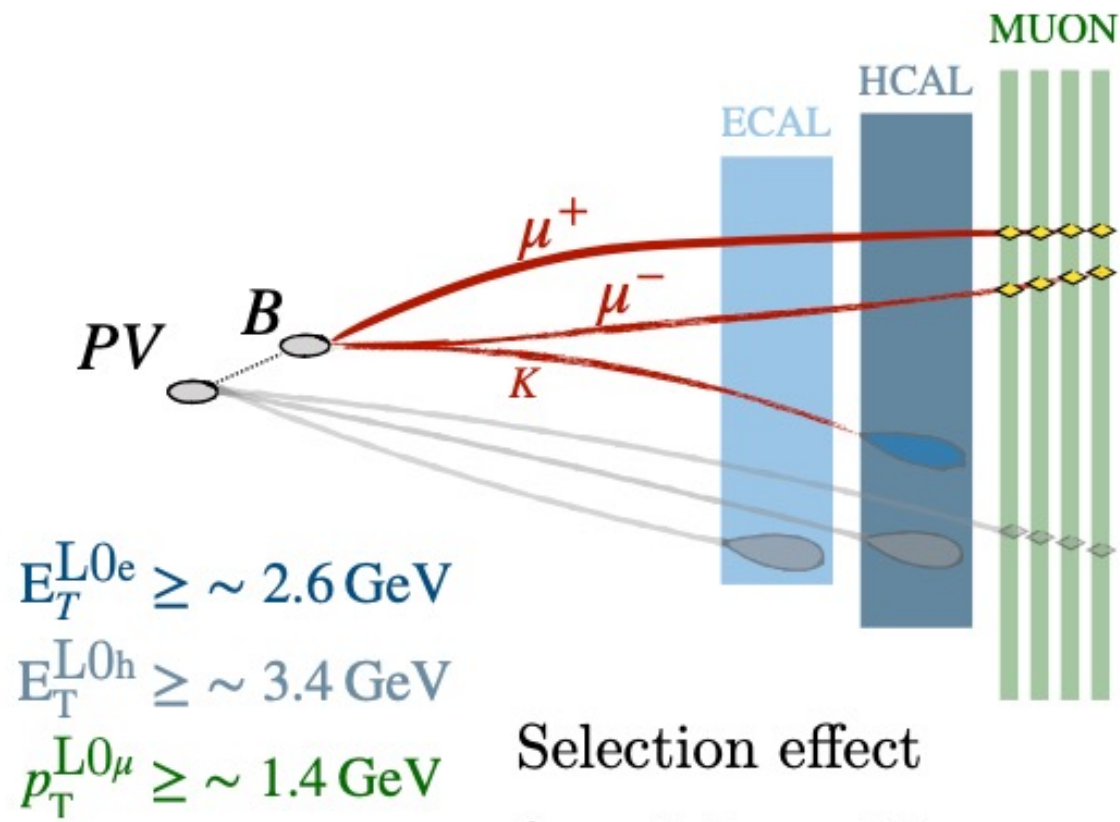
Energy loss $\propto E_e$
 Energy loss \propto material

In both cases E/p is correct



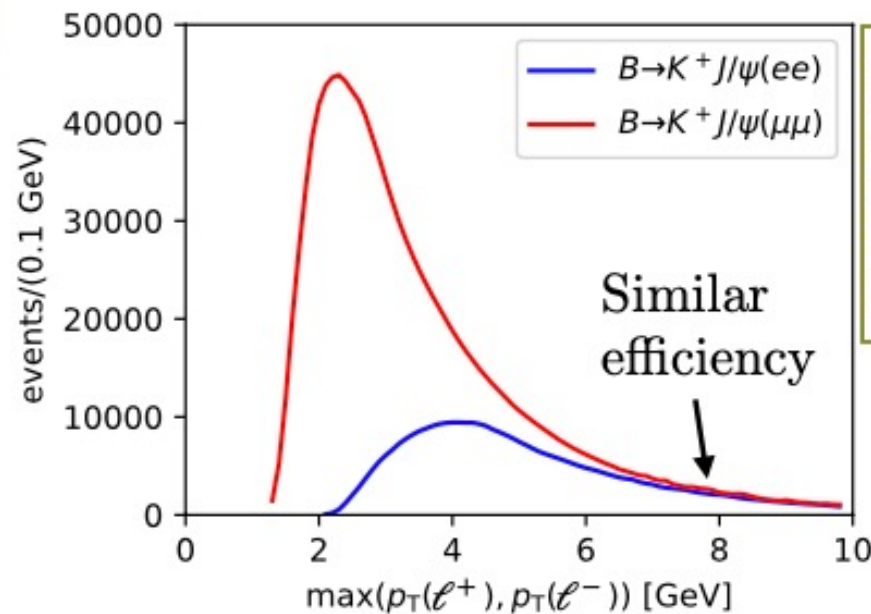
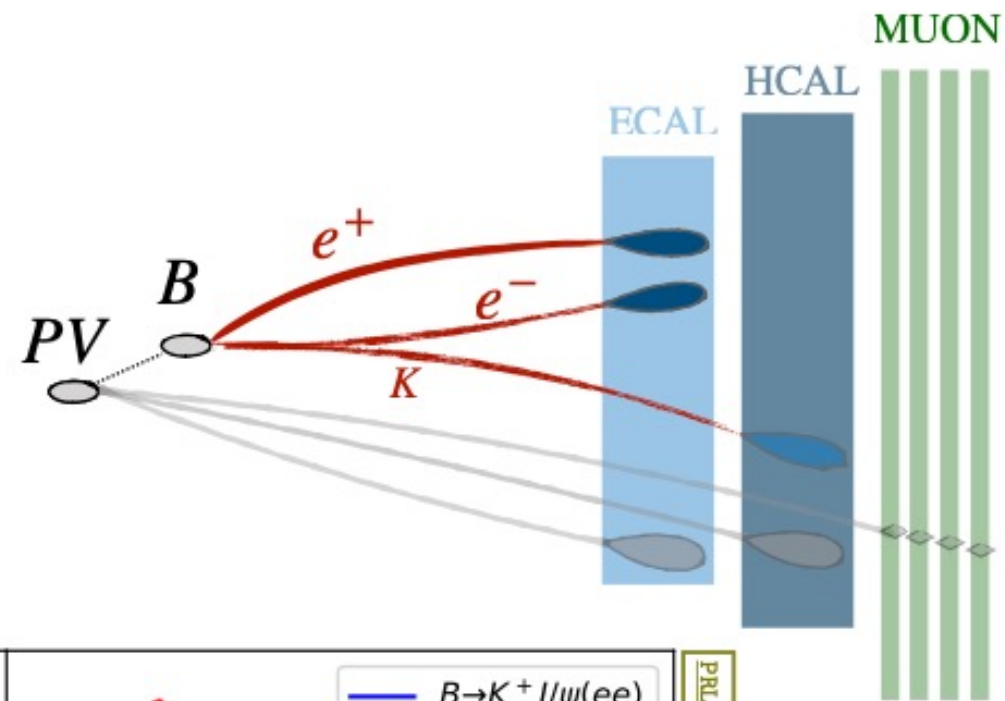
Bremsstrahlung recovery algorithm is $\sim 50\%$ efficient
 Well described in simulation

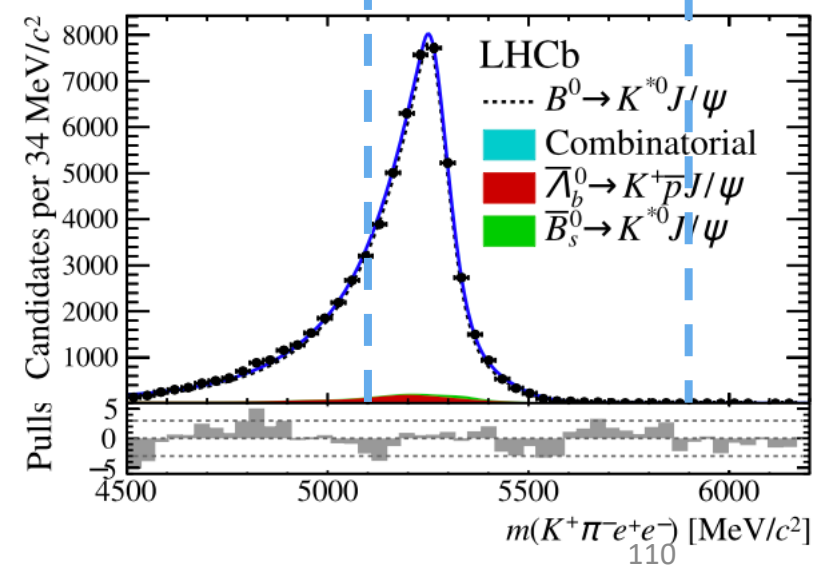
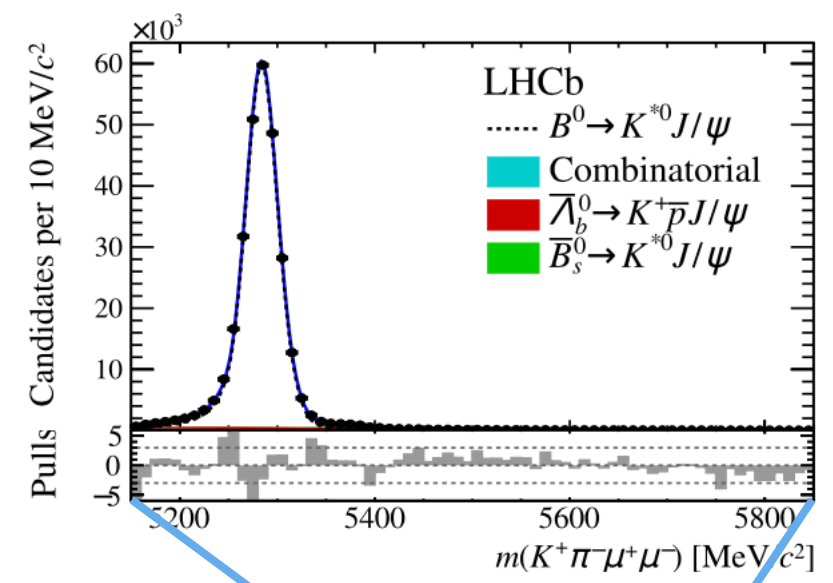
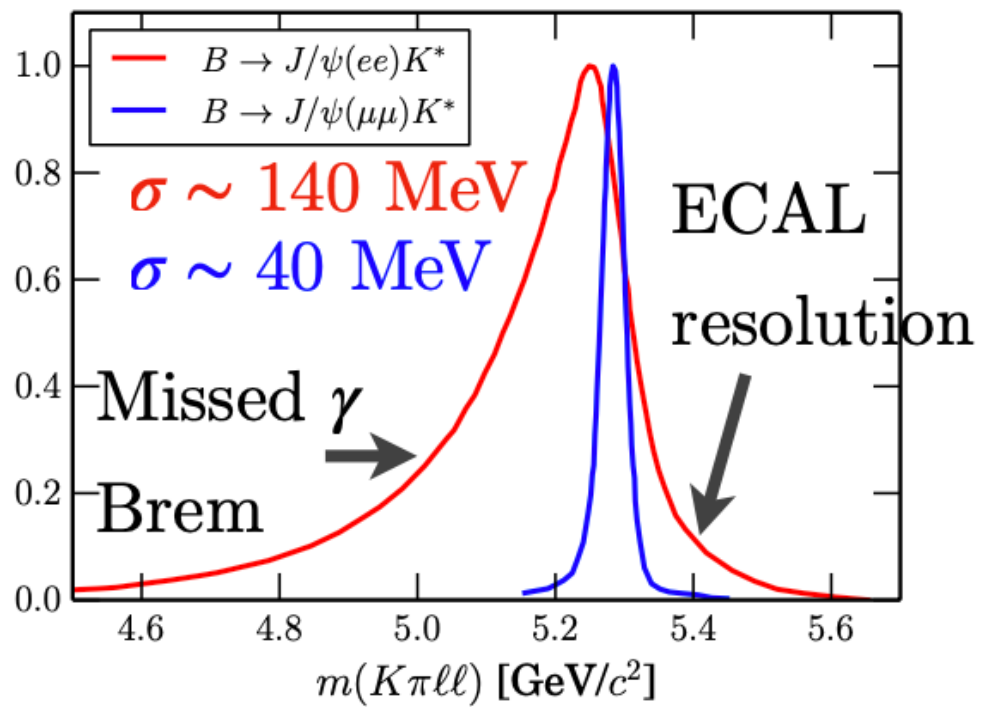
Hardware trigger is very different for electrons and muons



Selection effect
from L0e vs L0 μ

$$\sim \frac{1}{3}$$



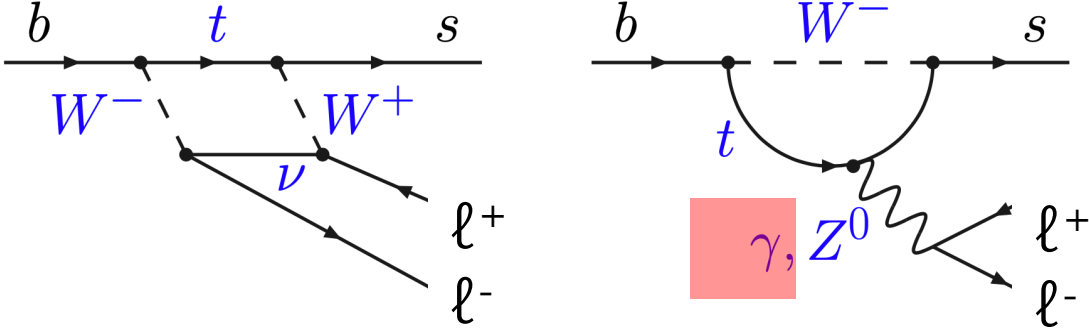


Using modes with electrons to increase the statistics is not the best idea

Use electrons for:

- measurements which **cannot** be done with muons or where the SM contribution is so tiny that any sign of a channel is NP

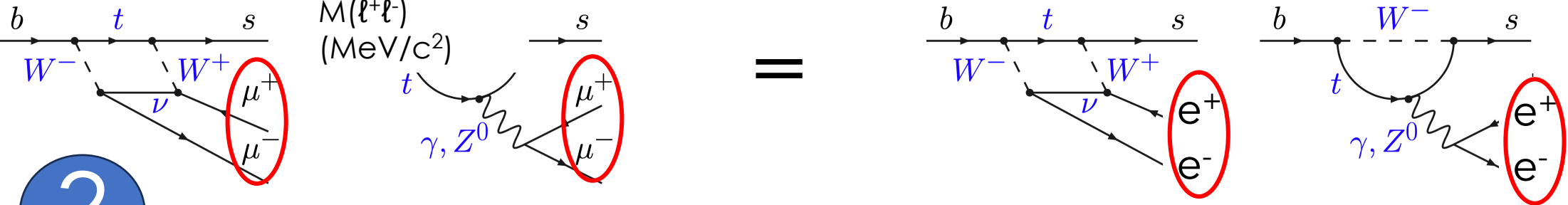
1



- search for New Physics

?

=



2

1a

Why don't you look at $B_s \rightarrow ee$?

SM prediction

$$\mathcal{B}(B_s^0 \rightarrow e^+e^-) = (8.60 \pm 0.36) \times 10^{-14}$$

$$\mathcal{B}(B^0 \rightarrow e^+e^-) = (2.41 \pm 0.13) \times 10^{-15}$$

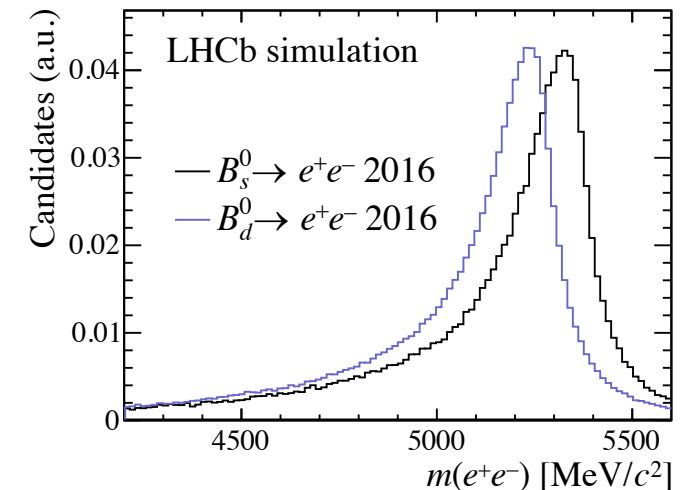
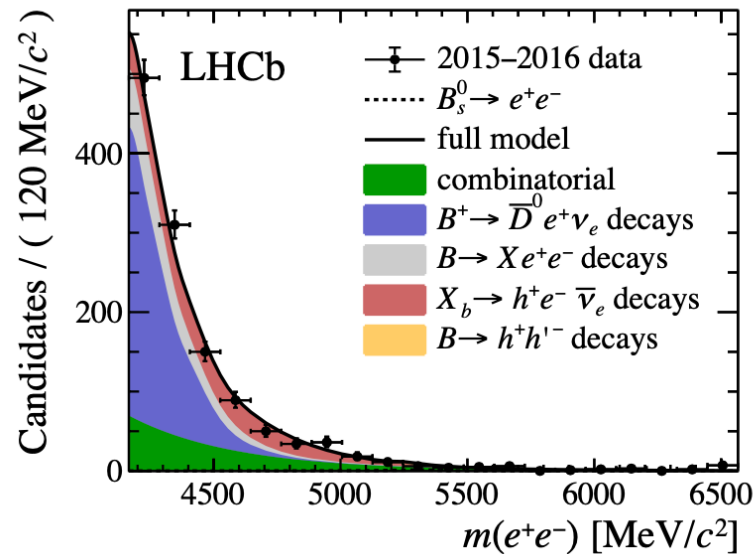
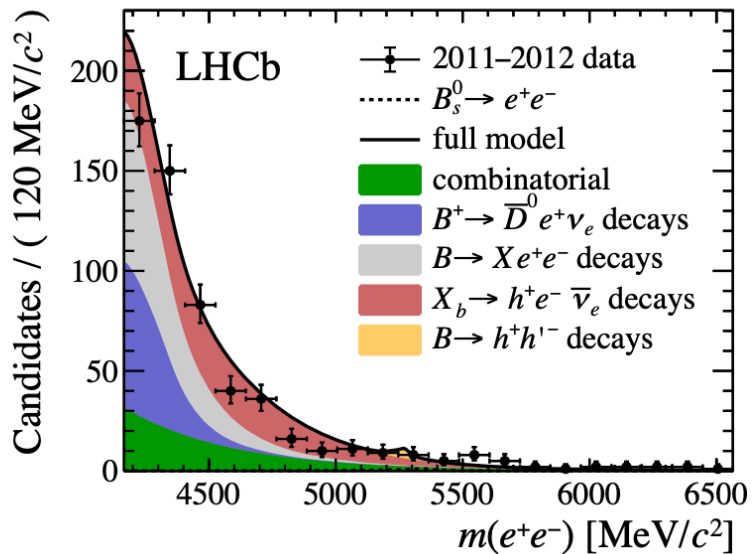
more helicity suppression !

$$\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-) = (3.66 \pm 0.14) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+\mu^-) = (1.03 \pm 0.05) \times 10^{-10}$$

Not enough mass resolution to separate B_d from B_s

(5 fb⁻¹) [LHCb-PAPER-2020-001](#)



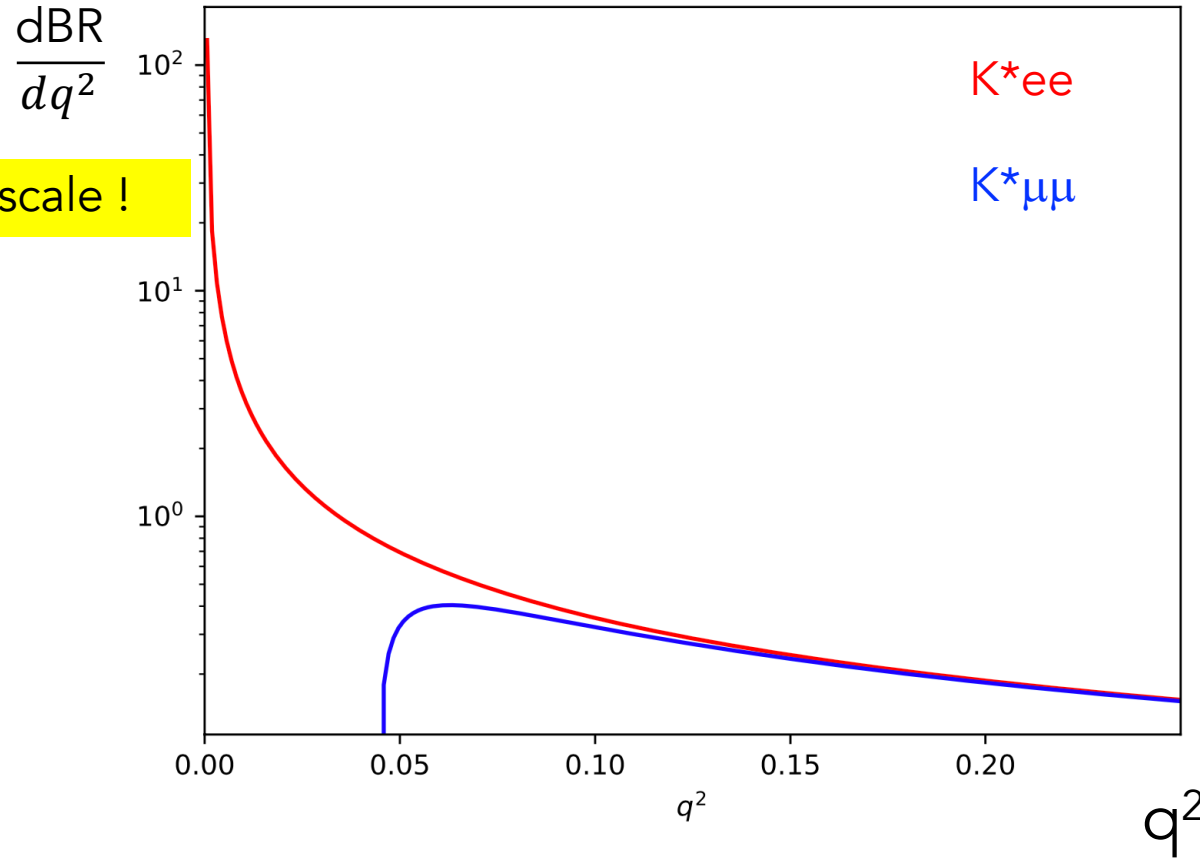
$\mathcal{B}(B_s^0 \rightarrow e^+e^-) < 9.4 (11.2) \times 10^{-9}$ at 90 (95) % confidence level

no results from
ATLAS or CMS

1b

Want to know about the photon polarization in $b \rightarrow s \gamma$?

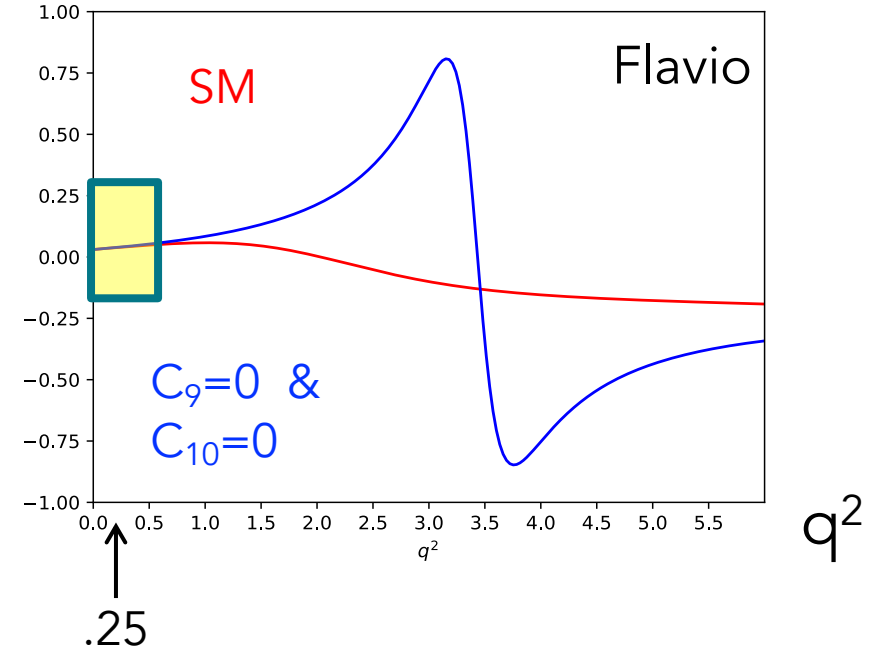
$$B^0 \rightarrow K^{*0} l^+ l^- \times 10^6$$



log scale !

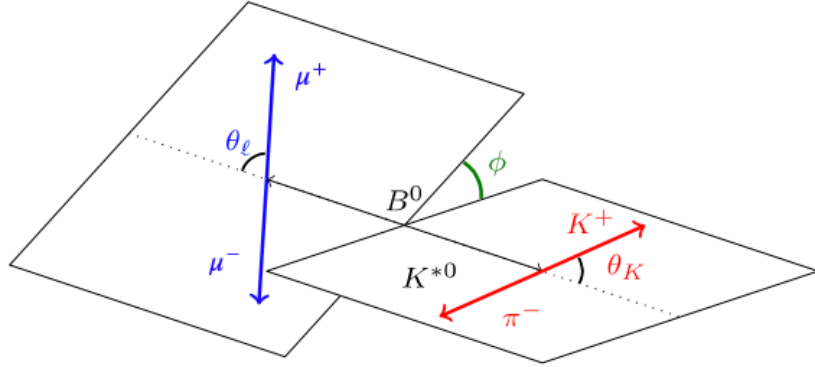
$$A_T^2(q^2)$$

A_T^2 for $B^0 \rightarrow K^{*0} e^+ e^-$



Electrons should give us access to C_7 and C_7' Wilson coefficients

$B \rightarrow V \ell \ell$



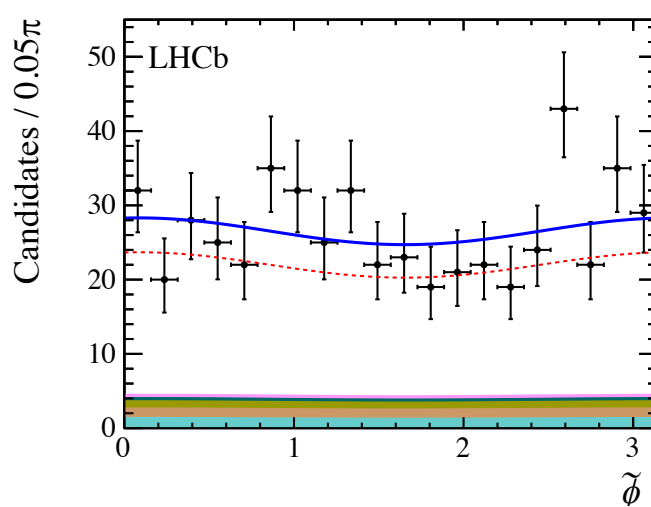
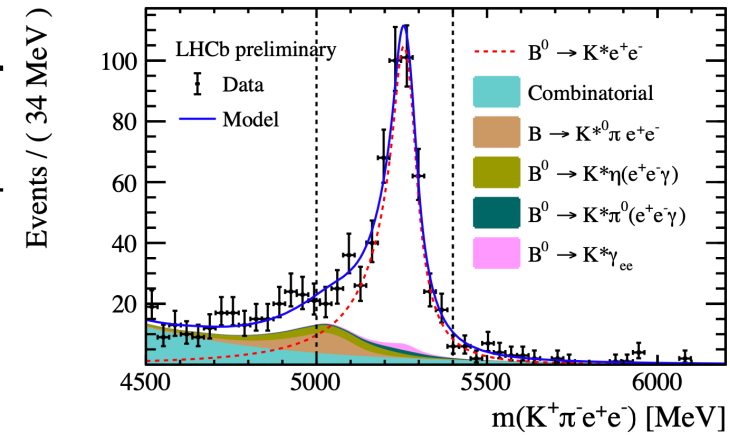
Complicated full $B \rightarrow K^* \mu \mu$ angular fit (8 parameters) can be reduced to the variables of interest to probe the photon pole (4 parameters)

$$\begin{aligned}
 &= \frac{9}{16\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\
 &\quad + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell - F_L \cos^2 \theta_K \cos 2\theta_\ell \\
 &\quad + (1 - F_L) A_T^{Re} \sin^2 \theta_K \cos \theta_\ell \\
 &\quad + \frac{1}{2}(1 - F_L) A_T^{(2)} \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\tilde{\phi} \\
 &\quad \left. + \frac{1}{2}(1 - F_L) A_T^{Im} \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\tilde{\phi} \right].
 \end{aligned}$$

$$A_T^{(2)}(q^2 \rightarrow 0) = \frac{2\text{Re}(C_7 C_7'^*)}{|C_7|^2 + |C_7'|^2}$$

$$A_T^{Im}(q^2 \rightarrow 0) = \frac{2\text{Im}(C_7 C_7'^*)}{|C_7|^2 + |C_7'|^2}$$

→ 0 for purely left-handed photon



$$F_L = 0.044 \pm 0.026 \pm 0.014,$$

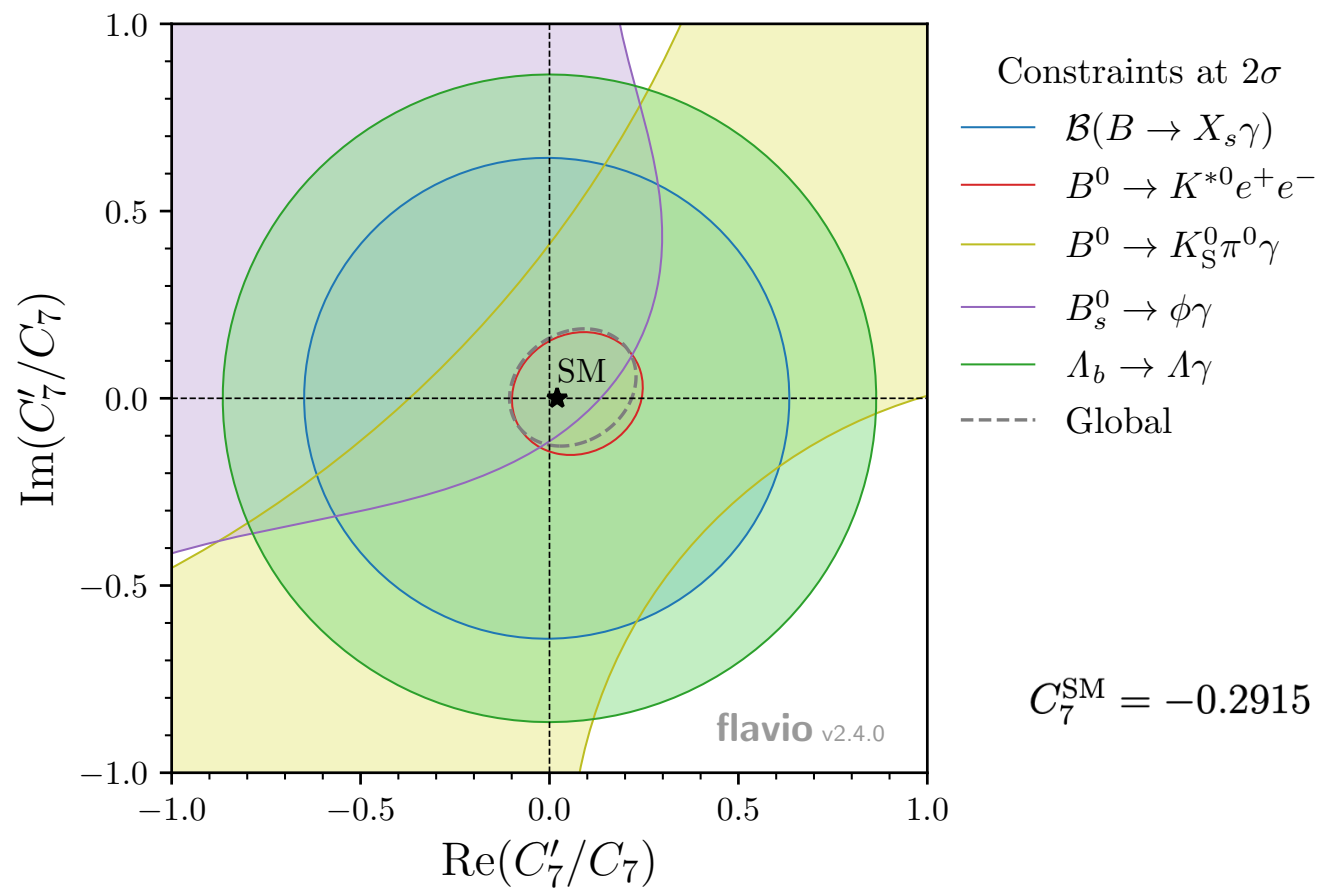
$$A_T^{\text{Re}} = -0.06 \pm 0.08 \pm 0.02,$$

$$A_T^{(2)} = +0.11 \pm 0.10 \pm 0.02,$$

$$A_T^{\text{Im}} = +0.02 \pm 0.10 \pm 0.01,$$

$$A_T^{(2)}(\text{SM}) = 0.033 \pm 0.020,$$

$$A_T^{\text{Im}}(\text{SM}) = -0.00012 \pm 0.00034.$$



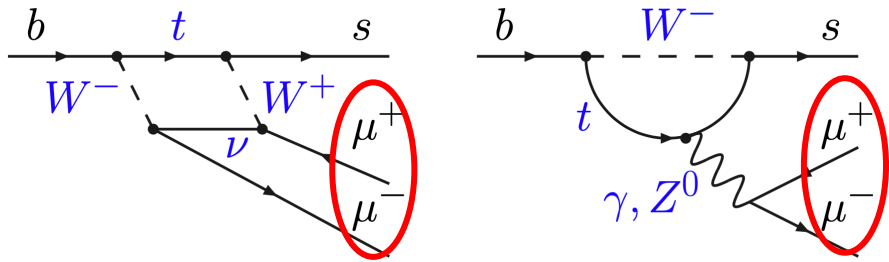
$$C_7^{\text{SM}} = -0.2915$$

5% precision on the photon polarization in $b \rightarrow s\gamma$ transitions

2

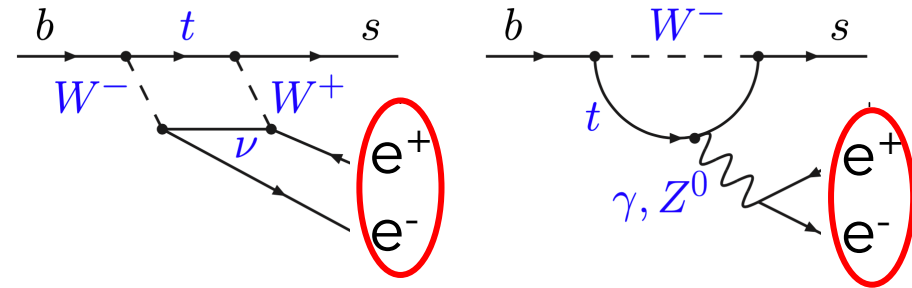
Lepton Flavour Universality tests in $b \rightarrow s \ell \ell$ transitions

$\ell = e, \mu$



?

=



In the SM only difference : kinematics (lepton masses)

Any ratio of observables in principle

Start with the simplest (?) one: ratio of branching fractions

$$R_{H_s} = \frac{\int \frac{d\Gamma(B \rightarrow H_s \mu^+ \mu^-)}{dq^2} dq^2}{\int \frac{d\Gamma(B \rightarrow H_s e^+ e^-)}{dq^2} dq^2} \stackrel{SM}{\approx} 1$$

← $B^{+,0}, B_s, \Lambda_b$ ← $K, K^*, \phi, \rho K \dots$

Practically at LHCb:

$$R_H = \frac{N(B \rightarrow H \mu^+ \mu^-)}{N(B \rightarrow H e^+ e^-)} \times \frac{\epsilon(B \rightarrow H e^+ e^-)}{\epsilon(B \rightarrow H \mu^+ \mu^-)} + r_{J/\psi} = \frac{BR(B \rightarrow H J/\psi(\mu^+ \mu^-))}{BR(B \rightarrow H J/\psi(e^+ e^-))} = 1$$

Yields from mass fits

Efficiencies from
MC & data
calibration samples

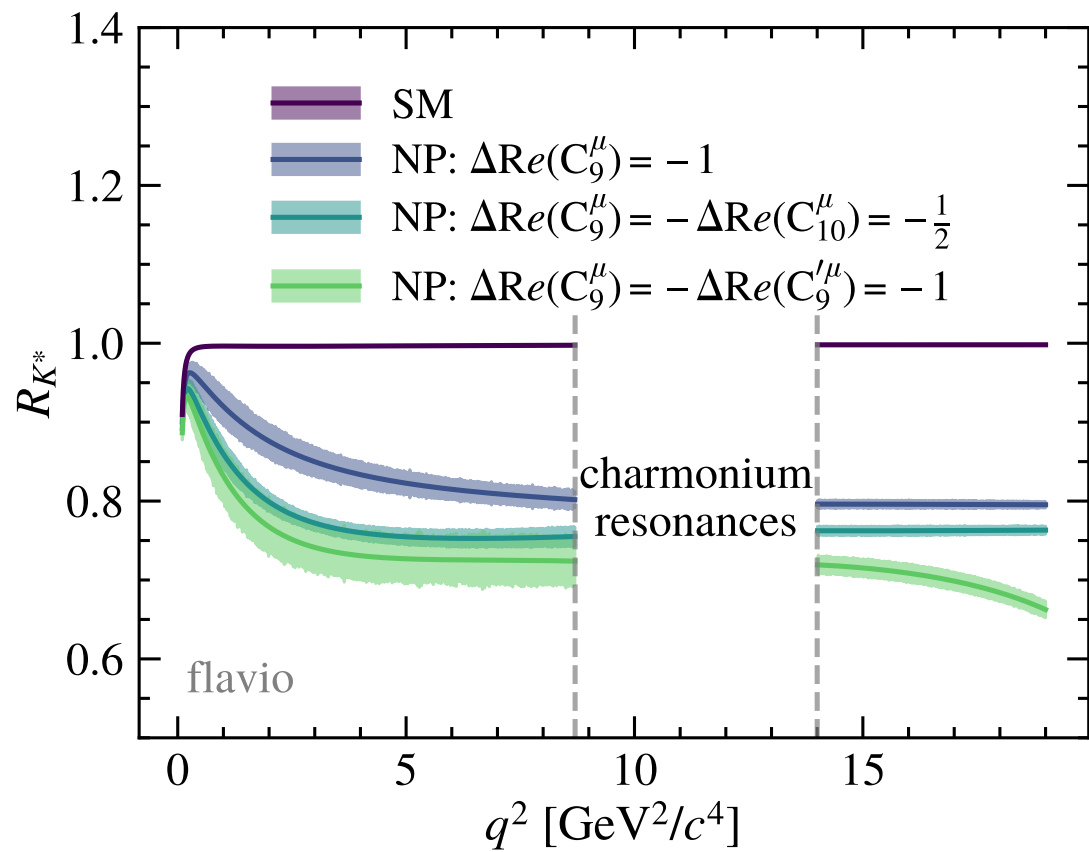
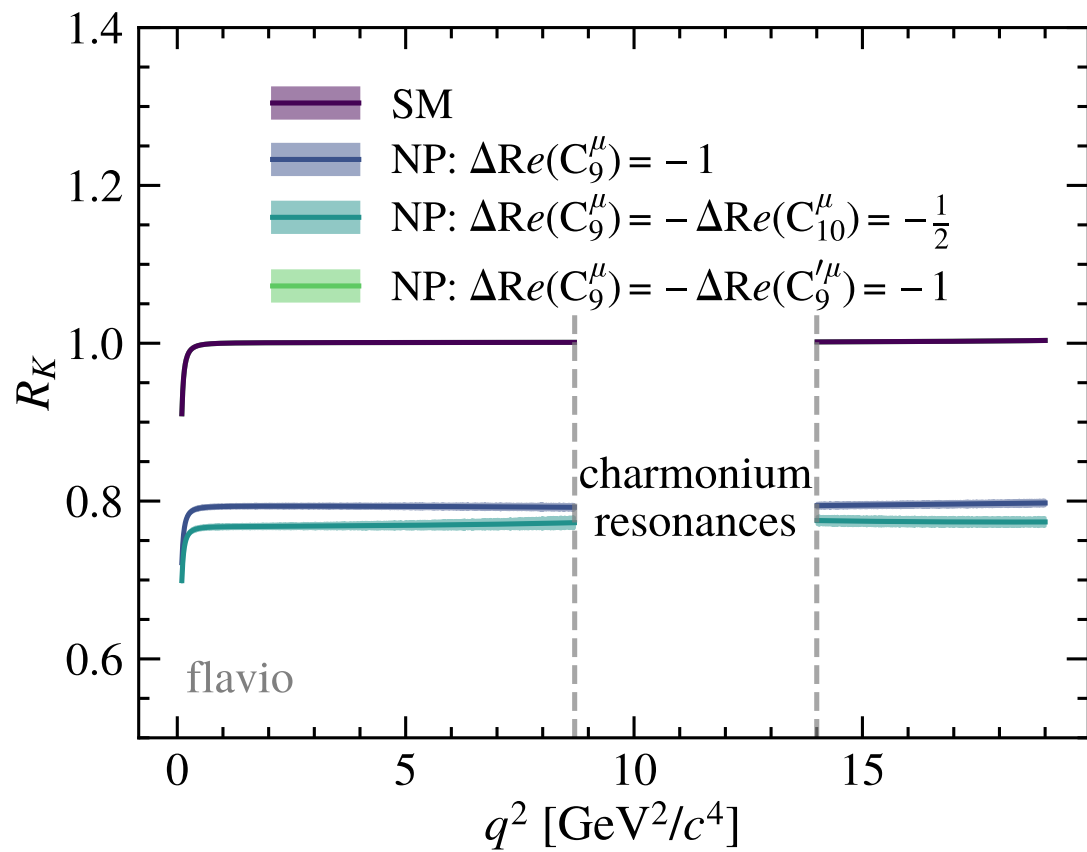
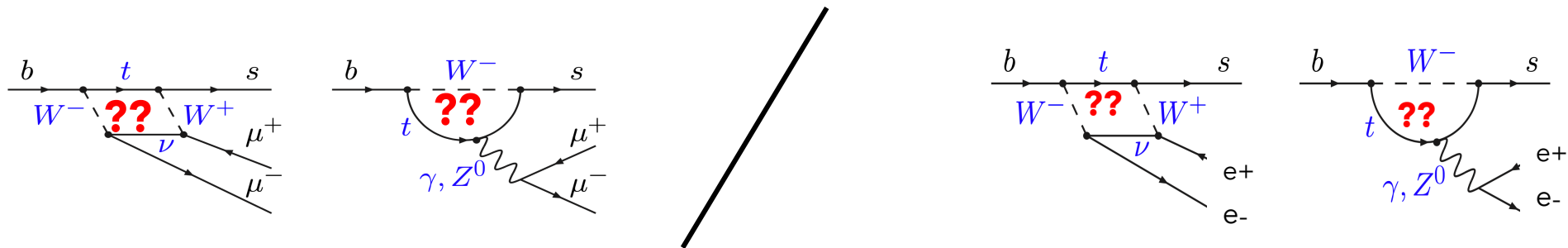
well tested LFU in J/ψ modes

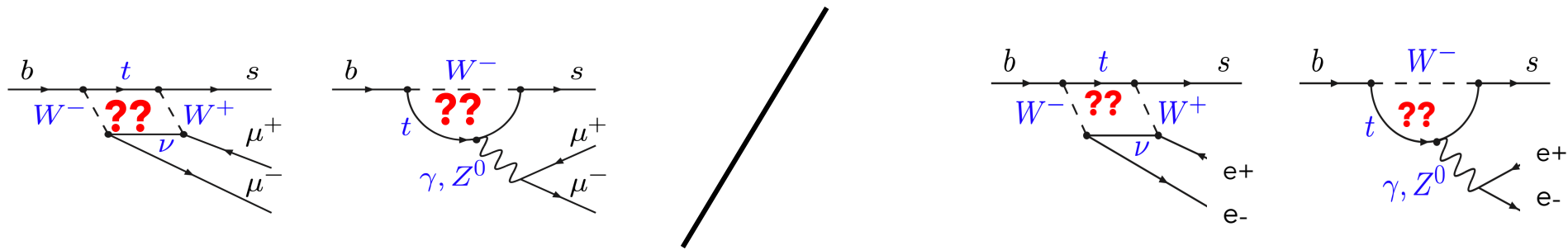
$H = K, K^*, \rho K \dots$

⇒ Use of the double ratio using the resonant channels

$$R_H = \frac{\frac{N(B \rightarrow H \mu^+ \mu^-)}{N(B \rightarrow H J/\psi(\mu^+ \mu^-))}}{\frac{N(B \rightarrow H e^+ e^-)}{N(B \rightarrow H J/\psi(e^+ e^-))}} \times \frac{\frac{\epsilon(B \rightarrow H e^+ e^-)}{\epsilon(B \rightarrow H J/\psi(e^+ e^-))}}{\frac{\epsilon(B \rightarrow H \mu^+ \mu^-)}{\epsilon(B \rightarrow H J/\psi(\mu^+ \mu^-))}}$$

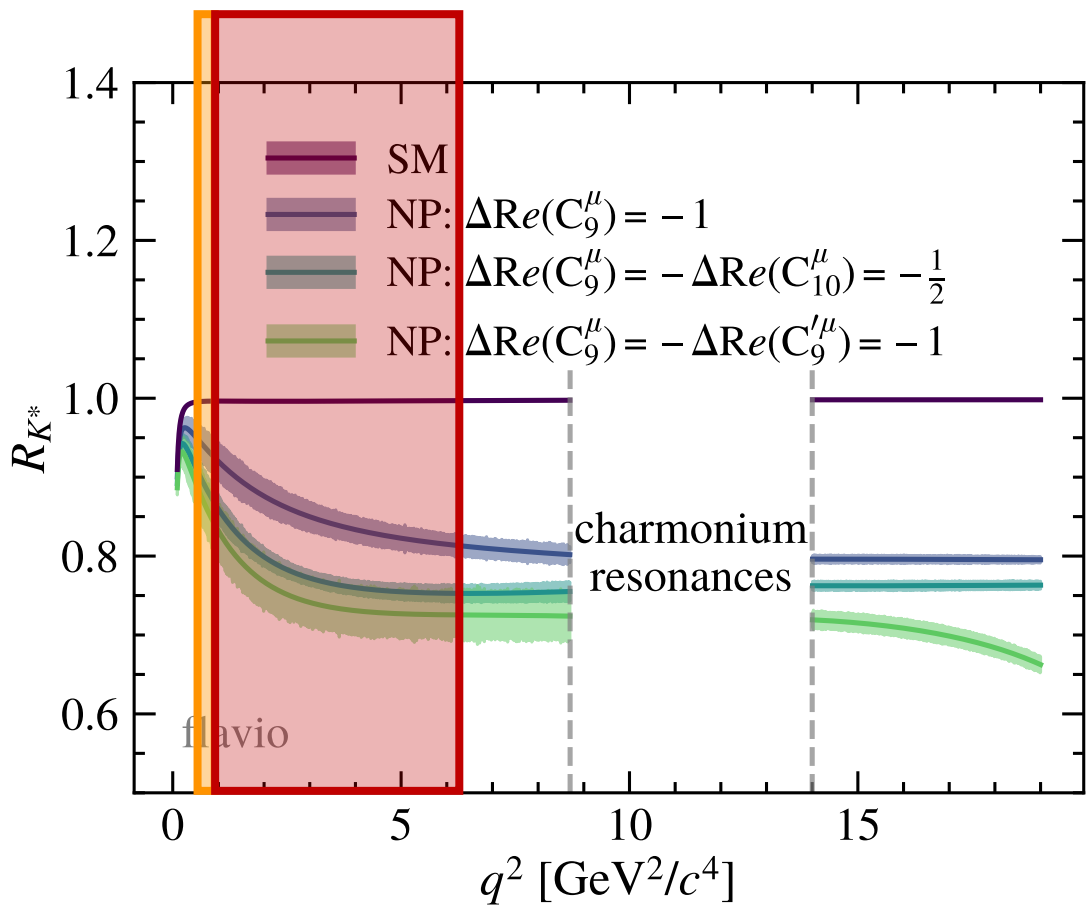
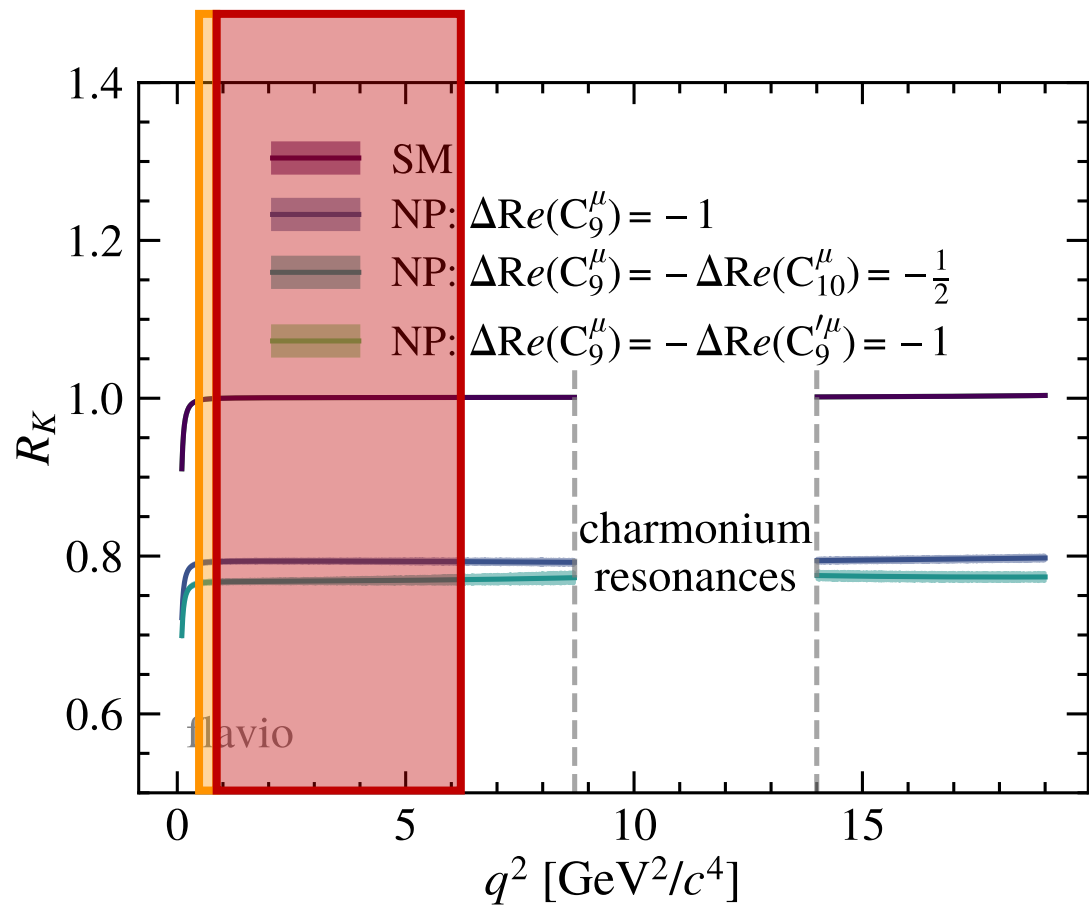
⇒ cancels out most of the systematics due to e/μ differences





low- q^2

central- q^2



⇒ the LHCb R_x analysis

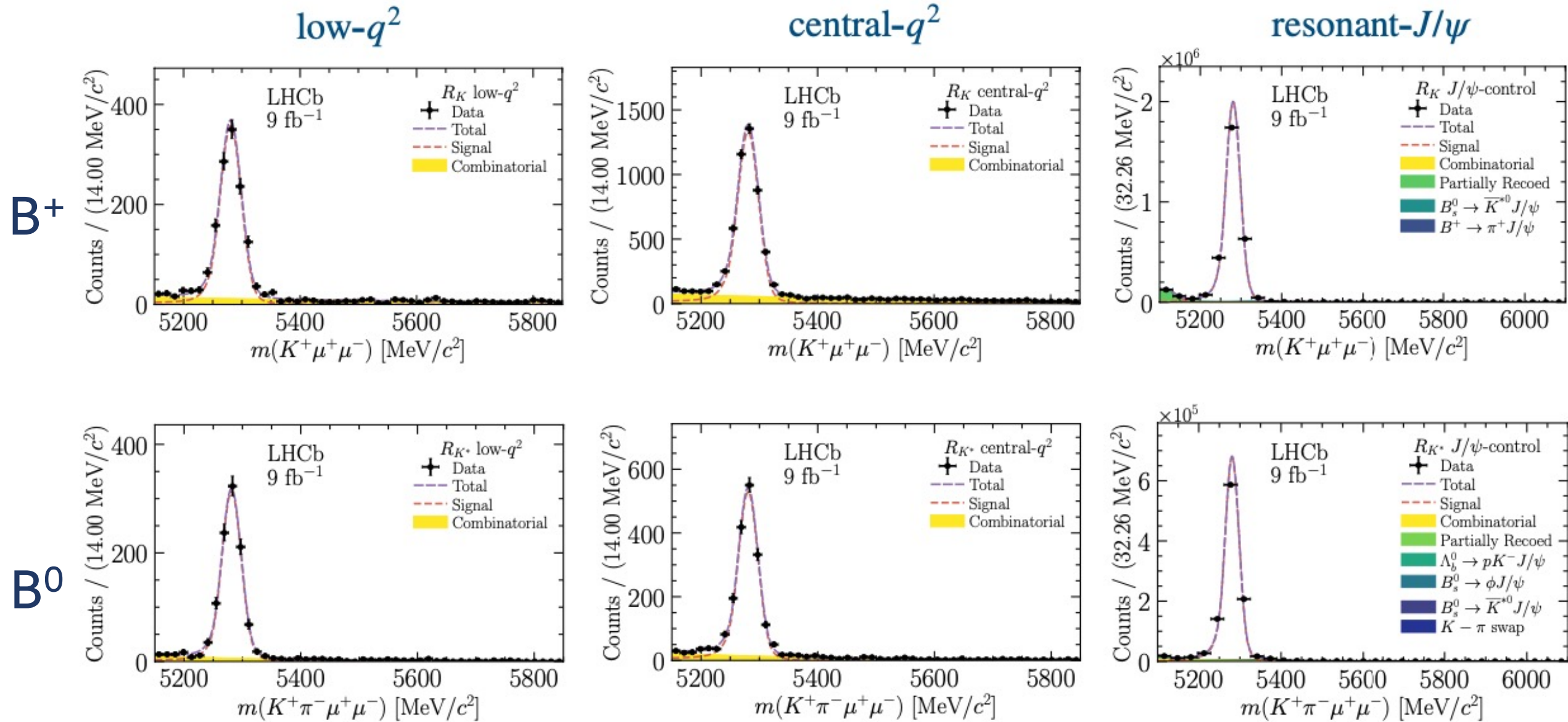
Simultaneous fit of

- $B \rightarrow K \ell \ell$ and $B \rightarrow K^* \ell \ell$
- in 2 kinematical regions (low and central- q^2)

Full correction of the MC samples using data control samples

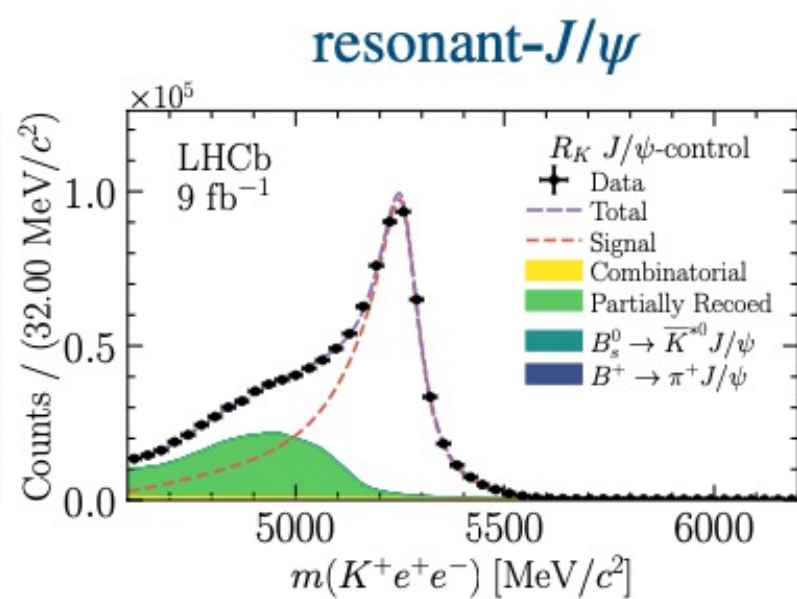
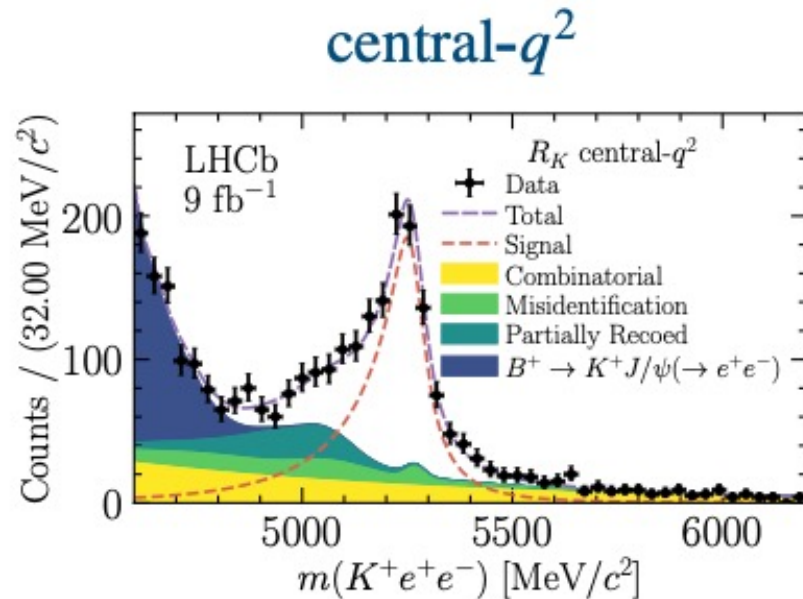
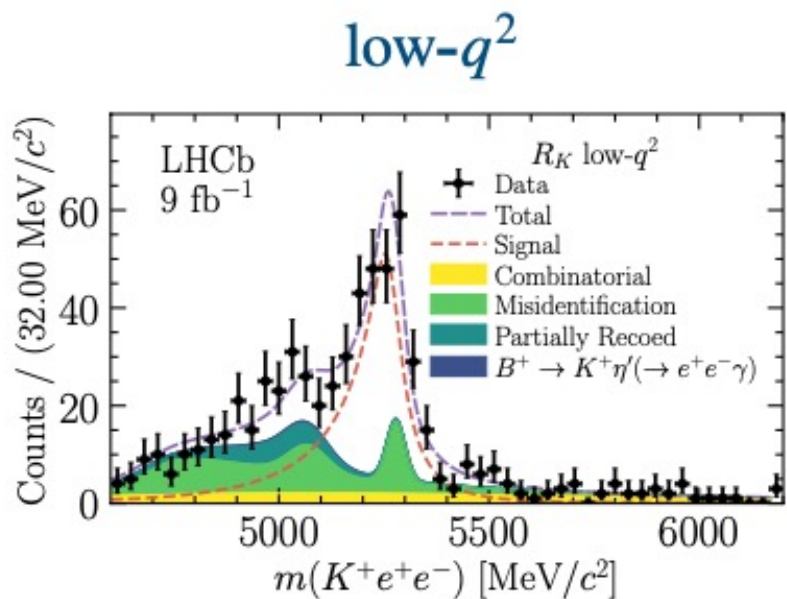
Extraction of the misld background in the ee- samples from the same data

Simultaneous fit for R_x extraction: muon modes

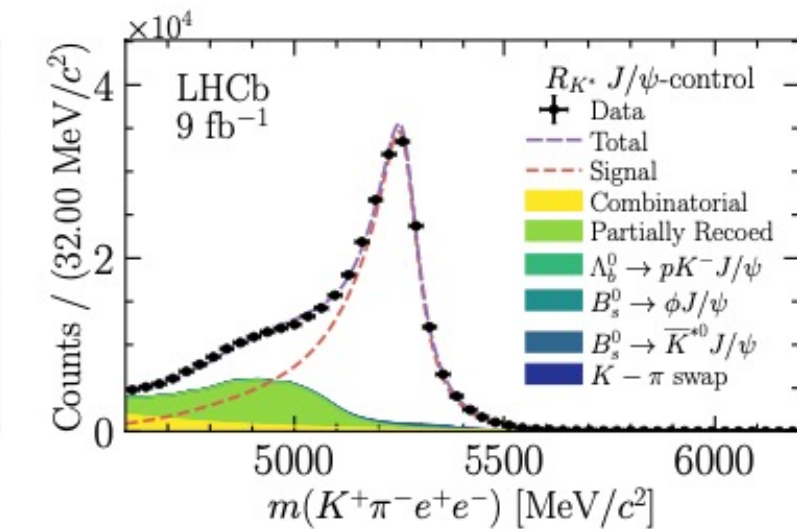
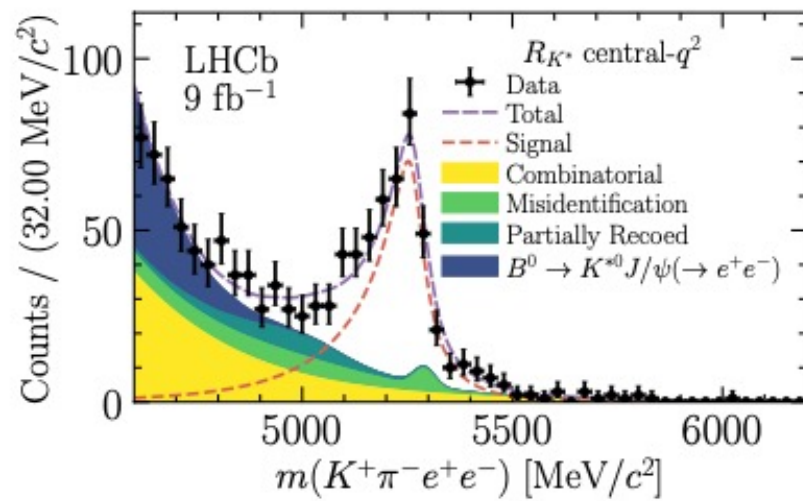
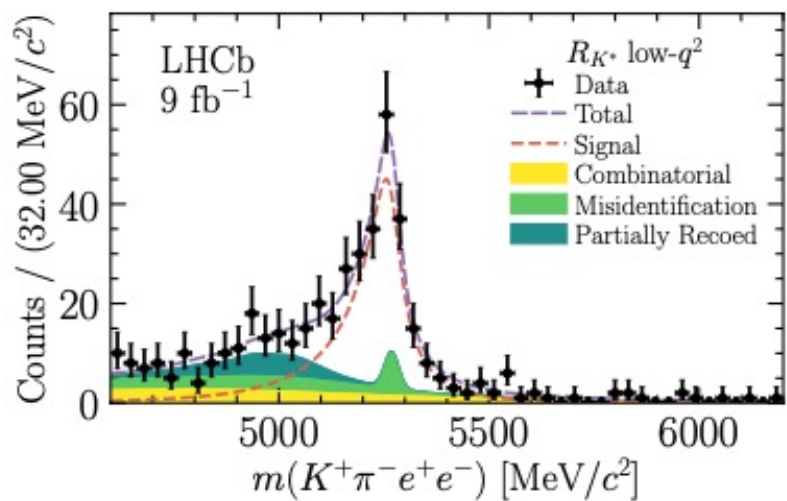


Simultaneous fit for R_x extraction: electron modes

B^+



B^0



A factor ~ 4 in yields between electron and muon modes

Measured yields from simultaneous fit to R_X

LU observable	Muon ($\times 10^3$)	Electron ($\times 10^3$)
low- q^2 R_K	1.25 ± 0.04	0.305 ± 0.024
low- q^2 R_{K^*}	1.001 ± 0.034	0.247 ± 0.022
central- q^2 R_K	4.69 ± 0.08	1.19 ± 0.05
central- q^2 R_{K^*}	1.74 ± 0.05	0.443 ± 0.028
J/ψ R_K	$(2.964 \pm 0.002) \times 10^3$	$(7.189 \pm 0.015) \times 10^2$
J/ψ R_{K^*}	$(9.733 \pm 0.010) \times 10^2$	$(2.517 \pm 0.009) \times 10^2$

Results

CMS

[arXiv:2401.07090](https://arxiv.org/abs/2401.07090)

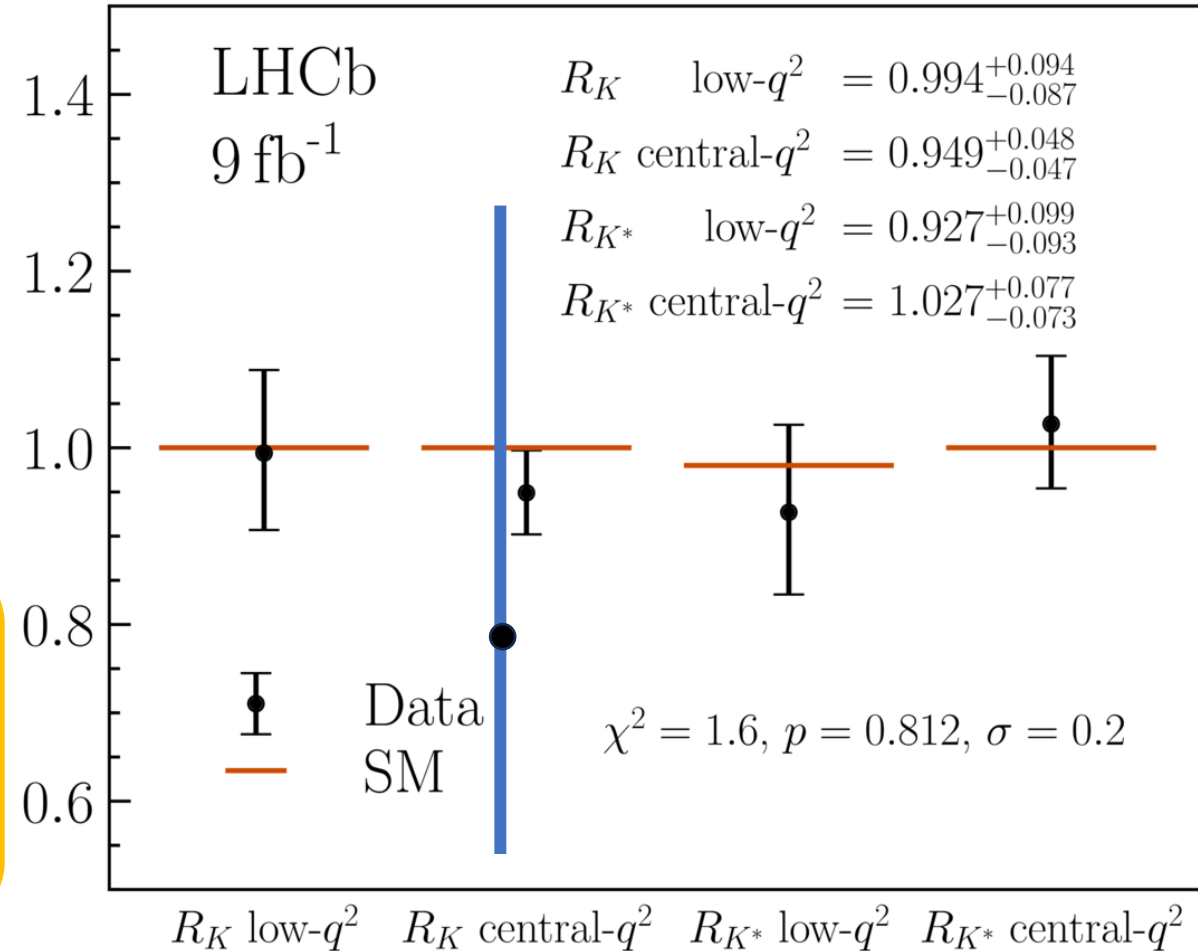
$$\text{low-}q^2 \begin{cases} R_K & = 0.994^{+0.090}_{-0.082} (\text{stat})^{+0.029}_{-0.027} (\text{syst}), \\ R_{K^*} & = 0.927^{+0.093}_{-0.087} (\text{stat})^{+0.036}_{-0.035} (\text{syst}), \end{cases}$$

$$\text{central-}q^2 \begin{cases} R_K & = 0.949^{+0.042}_{-0.041} (\text{stat})^{+0.022}_{-0.022} (\text{syst}), \\ R_{K^*} & = 1.027^{+0.072}_{-0.068} (\text{stat})^{+0.027}_{-0.026} (\text{syst}), \end{cases}$$

First or most precise test of LFU in $b \rightarrow s \ell \ell$

Compatible with the SM at 0.2σ

R_{K,K^*}



$$B \rightarrow K \nu \bar{\nu}$$

B-Factories

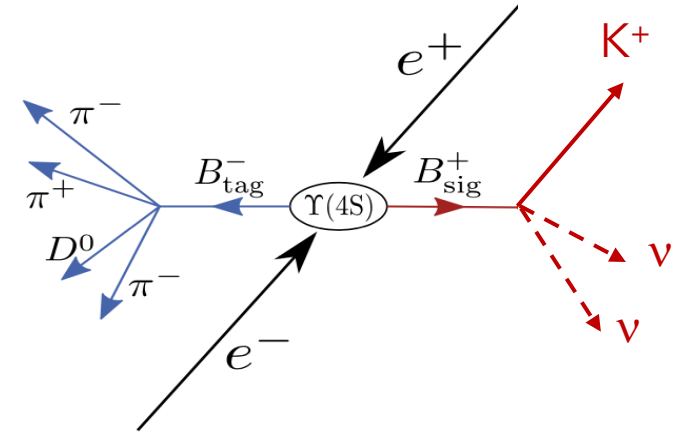
Experimentally very challenging

- Low branching fraction with large backgrounds (eg $K+K_L K_L$)
- No peak

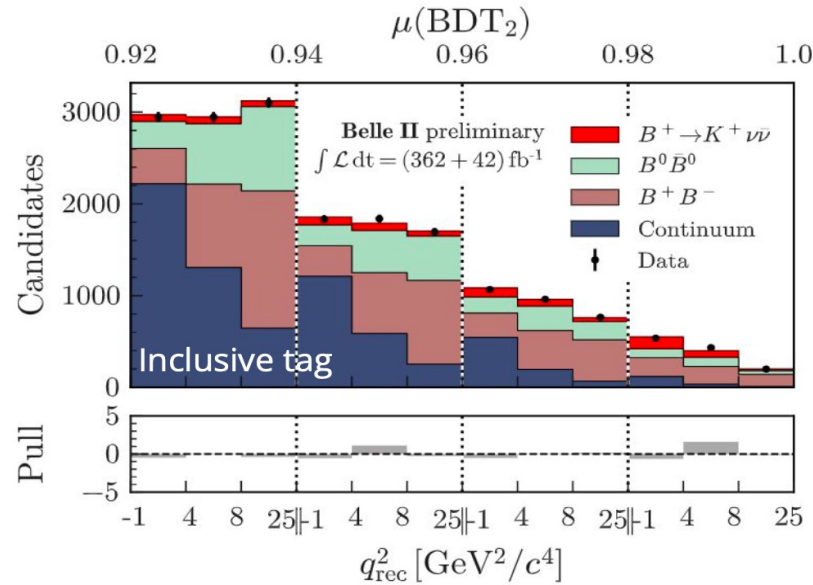
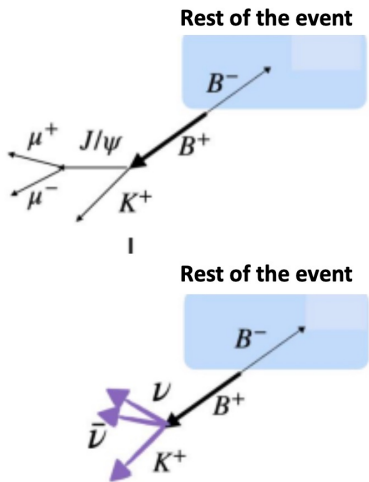
Theoretically cleaner \Rightarrow precise SM prediction:

$$\mathcal{B}(B \rightarrow K \nu \bar{\nu}) = (5.6 \pm 0.4) 10^{-6}$$

PRD 107, 119903 (2023)



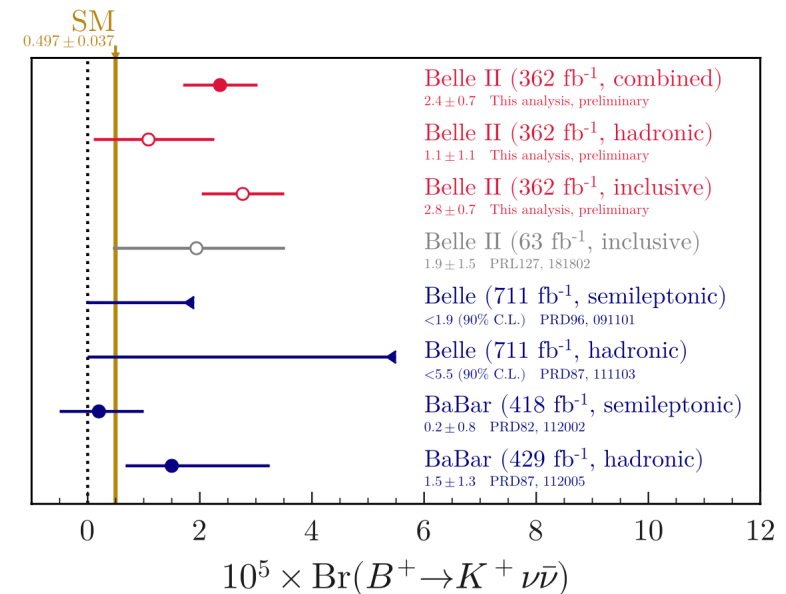
Check of the efficiency



$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = [2.4 \pm 0.5(\text{stat})^{+0.5}_{-0.4}(\text{syst})] \times 10^{-5}$$

arXiv:2311.14647

Color meets Flavor school Bad Honnef March 2024



Conclusion

- Mostly launched by B-factories (BaBar & Belle) even if started before (ARGUS, CLEO, LEP)
- Nowadays mostly LHCb and Belle-II : **complementarity**
- At the electroweak scale, the CKM mechanism dominates CP violation
- Still room for physics beyond SM at $\sim 20\%$ in FCNC
- In 1964 the discovery of the **small** amount of CP violation came as a surprise
- A bunch of tensions in FCNC $b \rightarrow s \ell \ell$ transitions, more data is needed to pin-point the origin.
- Heavy Flavour physics is much more than what I had time to touch upon

Precision !

**new detectors / new data / more sophisticated analyses
⇒ exciting times ahead !**

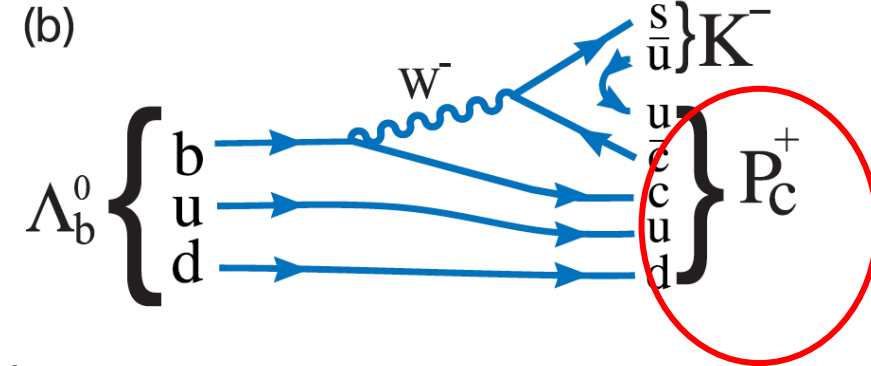
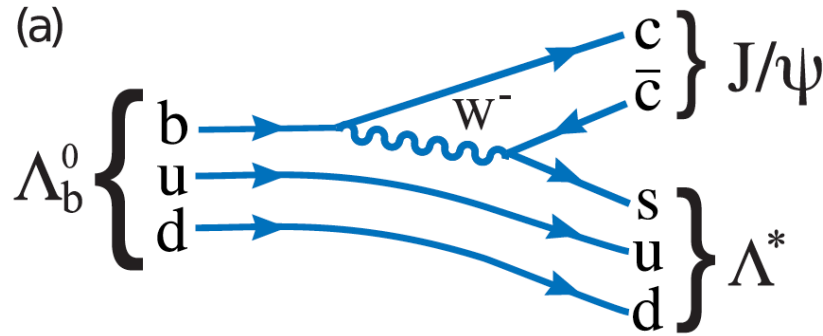
*Many thanks to J. Rouxel &
JP Couturier for the Shadoks*

Back-up slides

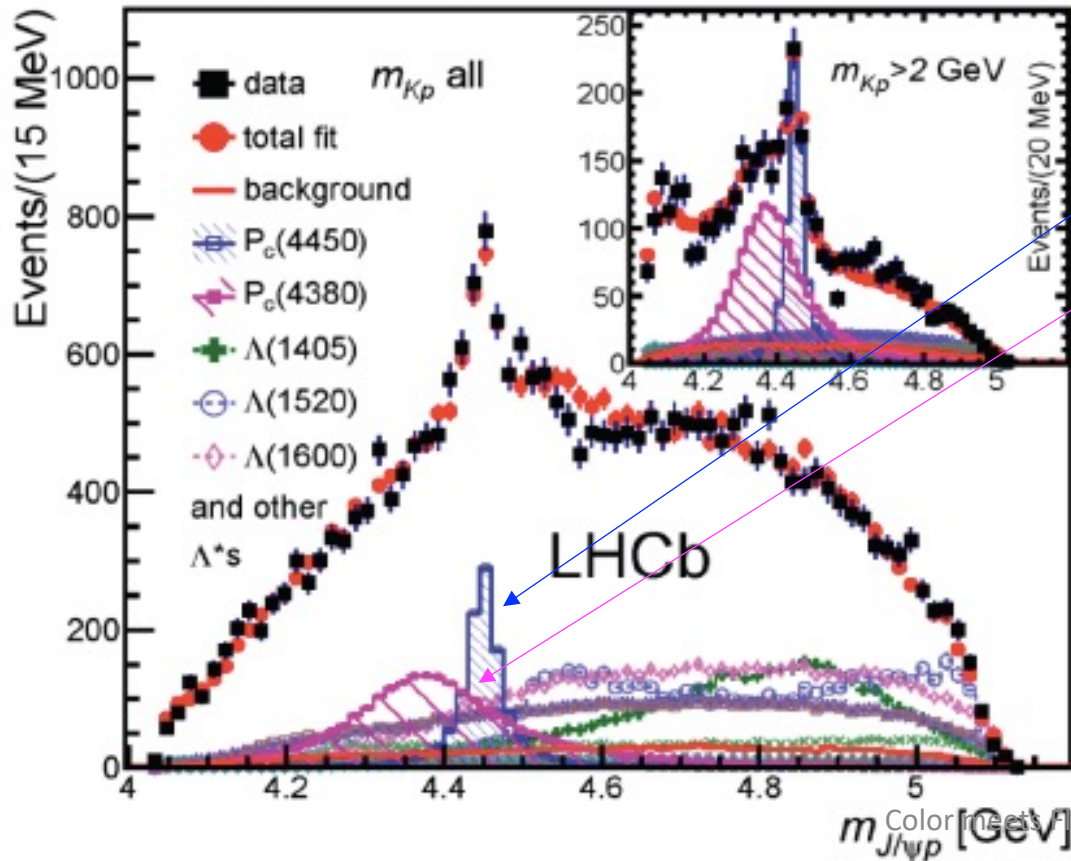
Observed for the first time
4 years ago by LHCb

Pentaquark signals

$\Lambda_b \rightarrow J/\psi p K$ decays



PRL 115 (2015) 072001

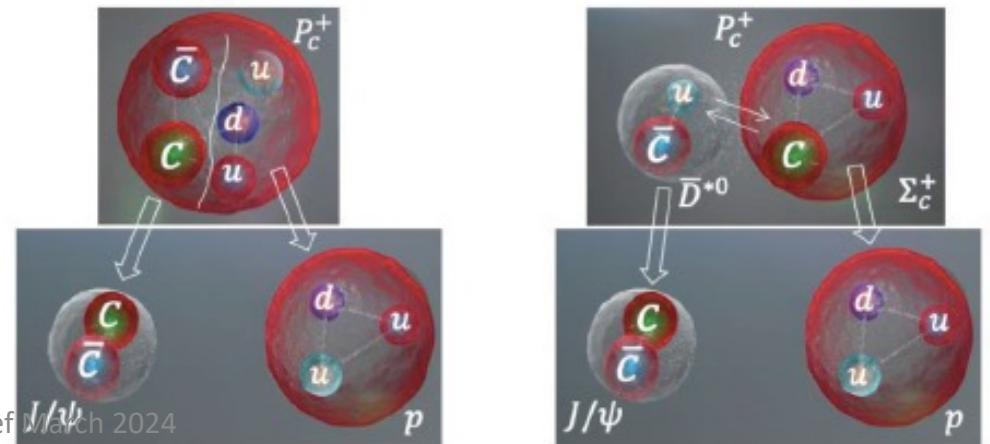


Two charged states:

- $P_c(4450)$ narrow
- $P_c(44380)$ broad

A pentaquark

tightly bound or molecular ?



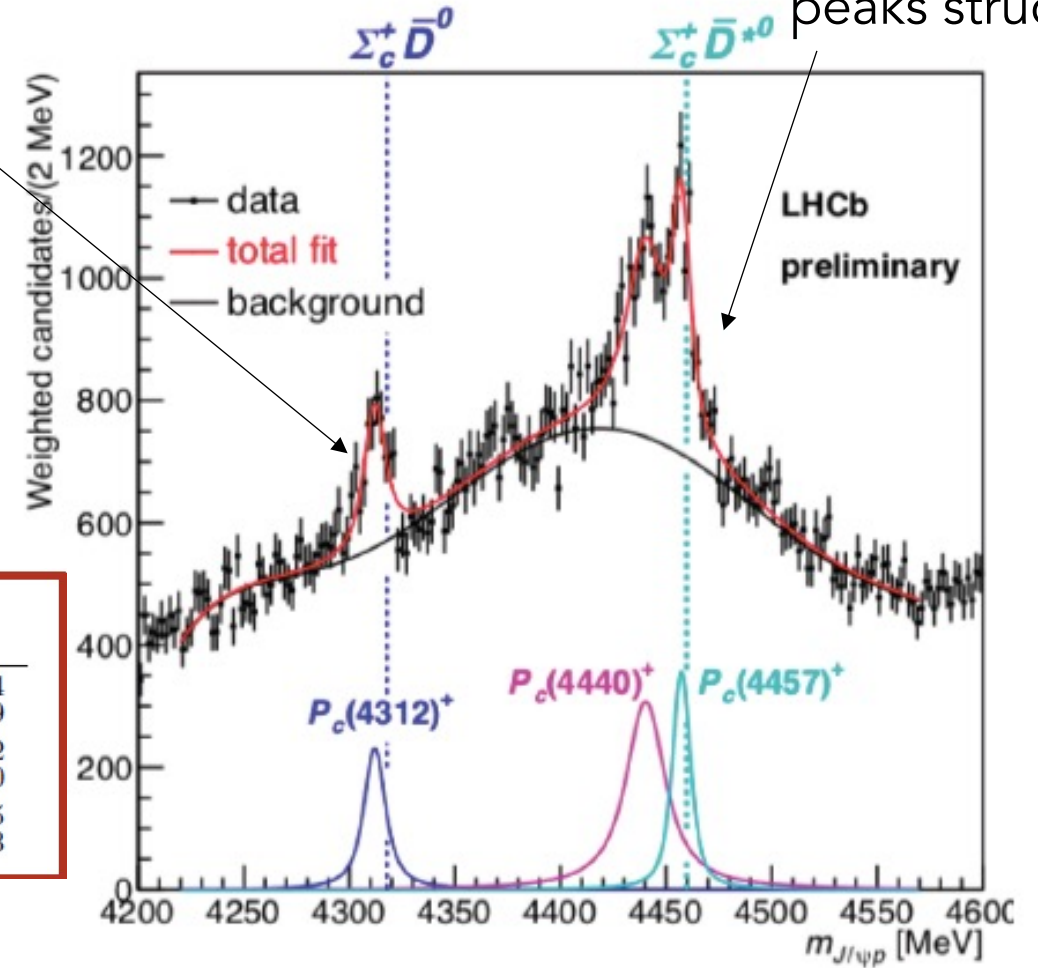
Update using Run2 full statistics \Rightarrow **x 9 statistics of the published result !**
 (x2 selection , x3 integrated luminosity, x cross section changes with energy)

Narrow bump hunting analysis with empirical background shape

$P_c(4450)$: a two peaks structure !

"New" peak at 4312 MeV

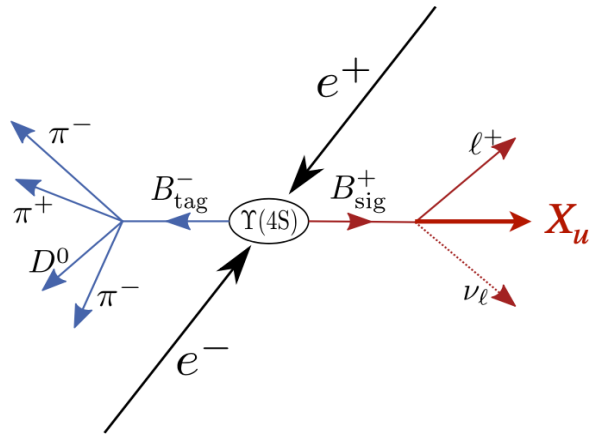
Full amplitude analysis ongoing especially needed to confirm the broad $P_c(4380)$



State	M [MeV]	Γ [MeV]	(95% CL)	\mathcal{R} [%]
$P_c(4312)^+$	$4311.9 \pm 0.7^{+6.8}_{-0.6}$	$9.8 \pm 2.7^{+3.7}_{-4.5}$	(< 27)	$0.30 \pm 0.07^{+0.34}_{-0.09}$
$P_c(4440)^+$	$4440.3 \pm 1.3^{+4.1}_{-4.7}$	$20.6 \pm 4.9^{+8.7}_{-10.1}$	(< 49)	$1.11 \pm 0.33^{+0.22}_{-0.10}$
$P_c(4457)^+$	$4457.3 \pm 0.6^{+4.1}_{-1.7}$	$6.4 \pm 2.0^{+5.7}_{-1.9}$	(< 20)	$0.53 \pm 0.16^{+0.15}_{-0.13}$

$$\mathcal{R} \equiv \frac{\mathcal{B}(\Lambda_b \rightarrow P_c^+ K^-) \mathcal{B}(P_c^+ \rightarrow J/\psi p)}{\mathcal{B}(\Lambda_b \rightarrow J/\psi p K^-)}$$

BFactories (Belle-II)



Beam energy const. + tag-side
 \rightarrow kinematical constraints

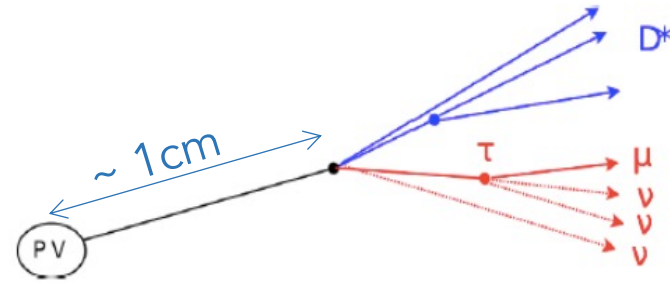
Inclusive decays

Access to absolute BR

BaBar & Belle $\sim 1.1 \text{ ab}^{-1}$

Belle-II (ICHEP2020 schedule) :
 10 ab^{-1} in 2025, 50 ab^{-1} in 2031

LHCb



Very large boost \rightarrow flight distance
 reconstruction
 \rightarrow kinematical constraints

All b-hadrons species

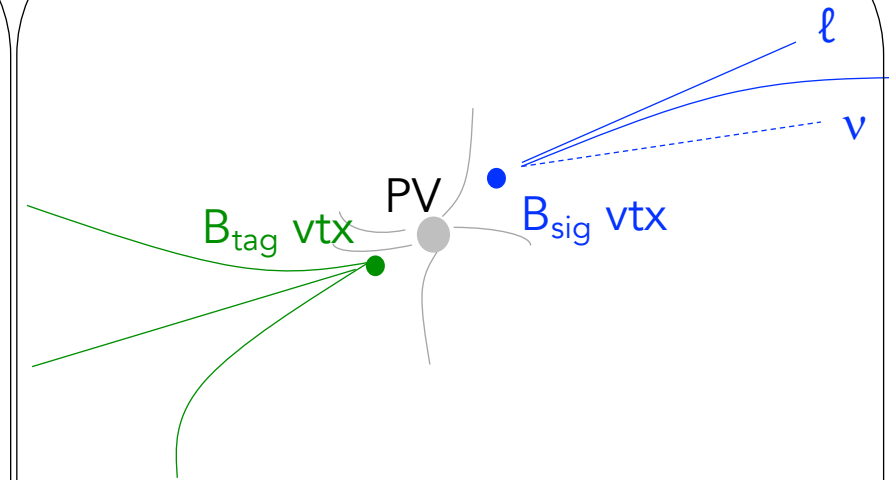
No access to absolute BR

LHCb: 9 fb^{-1} at hand

LHCb-Upgrade 1 (soft. trigger) :
 at the end of Run3 (2024) : 23 fb^{-1}
 at the end of 2020s : 50 fb^{-1}

LHCb-Upgrade 2 : 300 fb^{-1}

FCCee



Flight distance reco. and beam+other
 hemisphere
 \rightarrow kinematical constraints

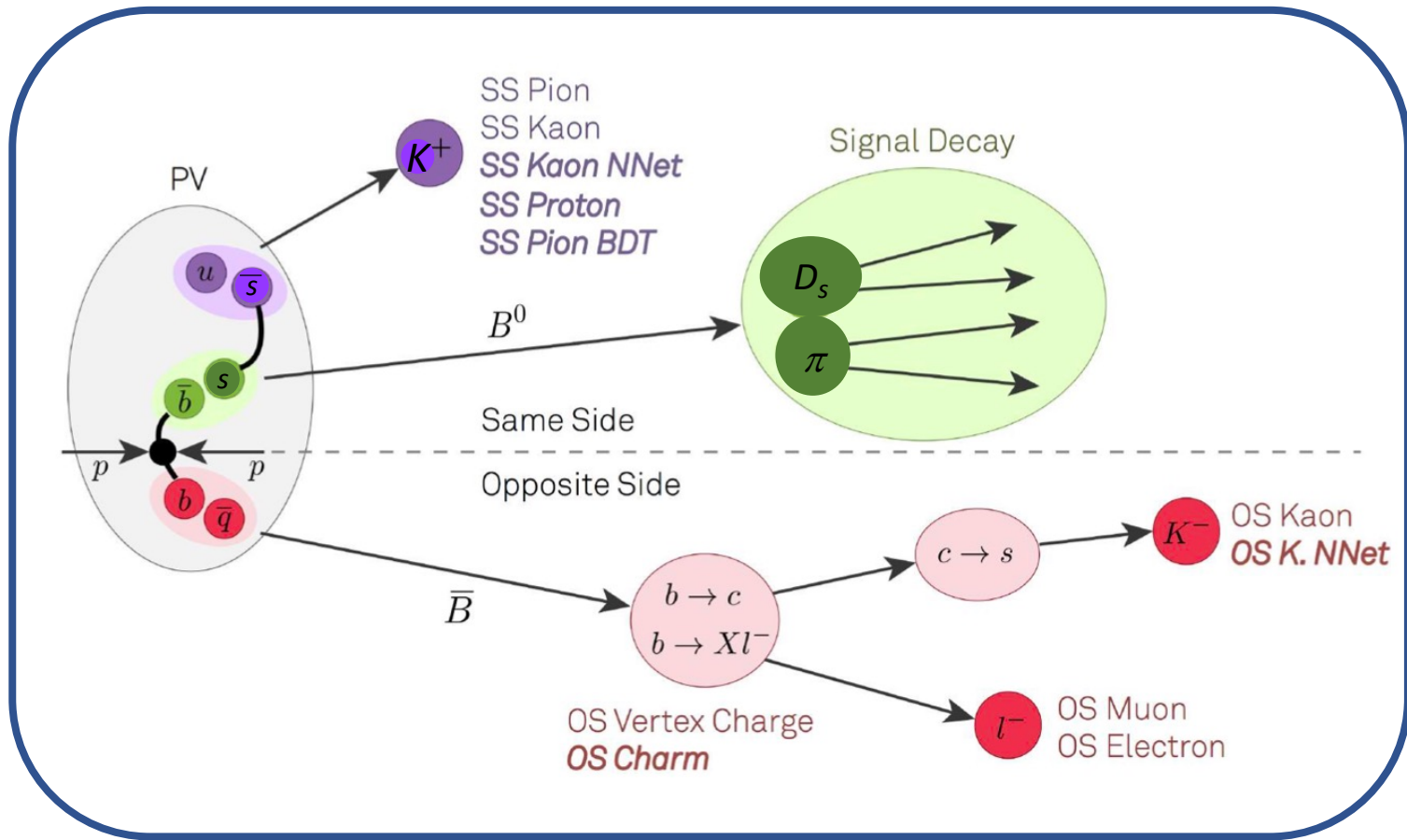
All b-hadrons species

Access to absolute BR

FCCee (from late 2030)

$5 \cdot 10^{12} Z^0$

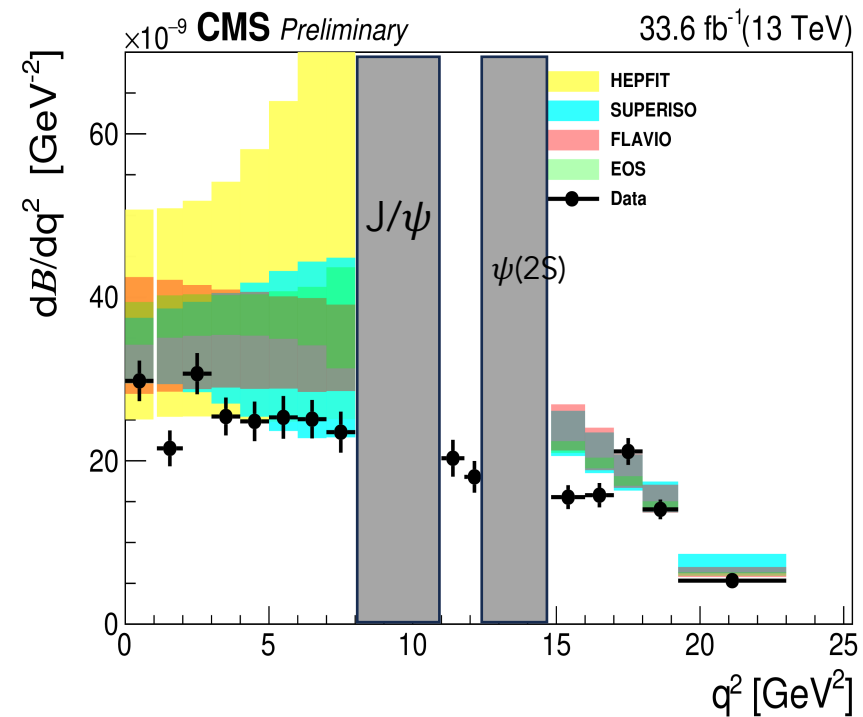
$1.5 \cdot 10^8 \text{ WW}$



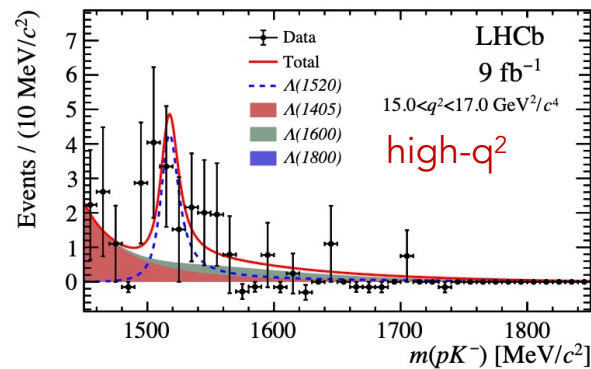
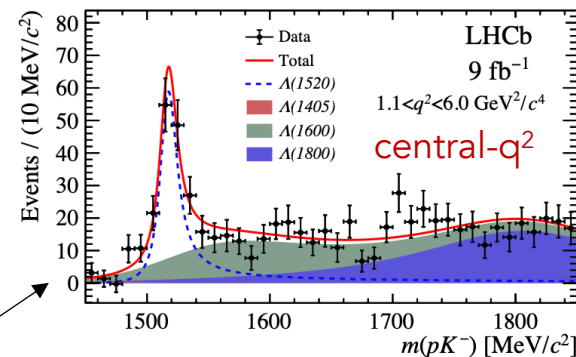
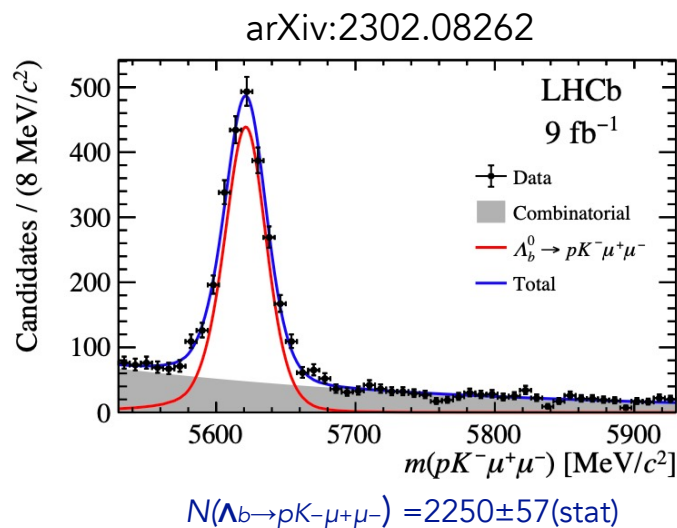
Branching fractions for $b \rightarrow s \mu \mu$ transitions

$$B_d \rightarrow K^{*0} \mu \mu$$

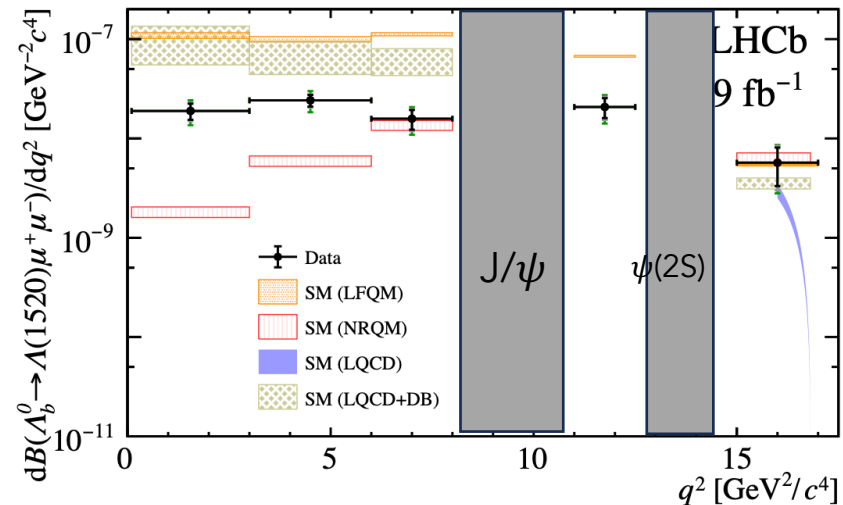
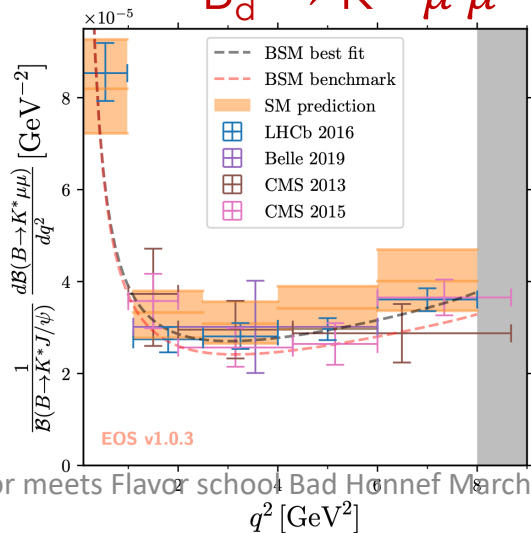
CMS-PAS-BPH-22-005



$$\Lambda_b \rightarrow \Lambda(1520) \mu \mu$$



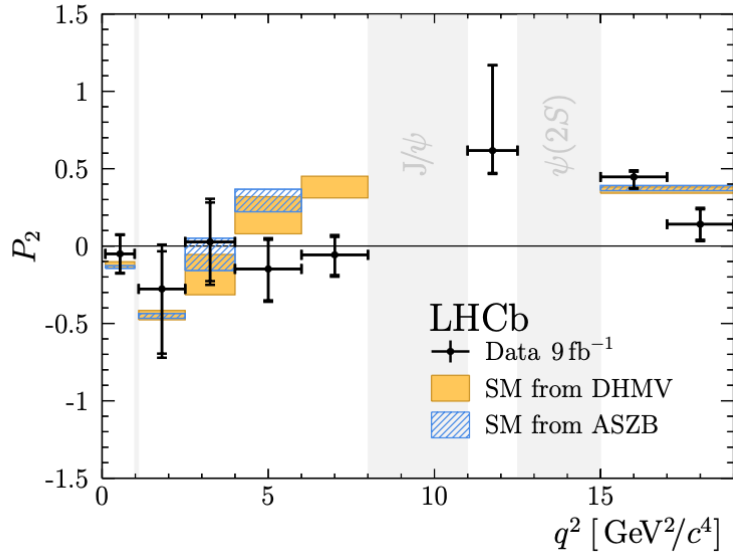
$$B_d \rightarrow K^{*0} \mu \mu$$



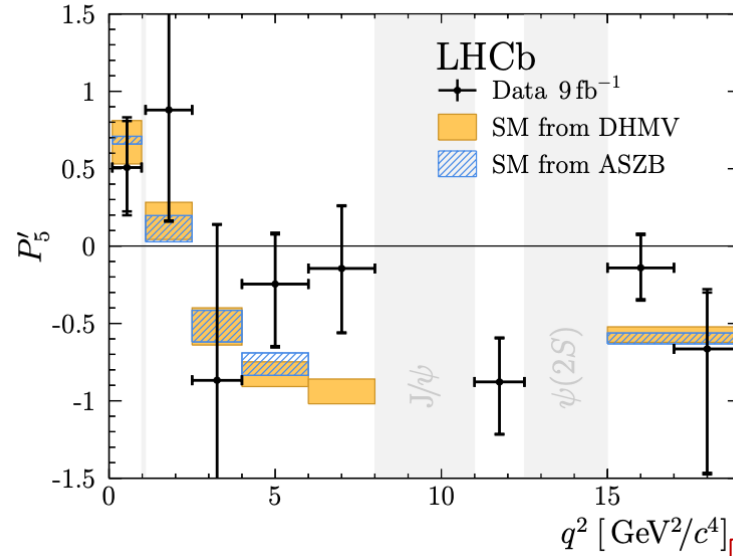
Very clean signal peaks
 Measurements below predictions
 Predictions correlated from a bin to another
 Better agreement at higher- q^2 (LQCD)

Many parameters extracted in a large number of bins

$B^+ \rightarrow K^{*+} \mu\mu$



[Phys. Rev. Lett.126 \(2021\) 161802](#)



Optimized variables
(less FF dependent)

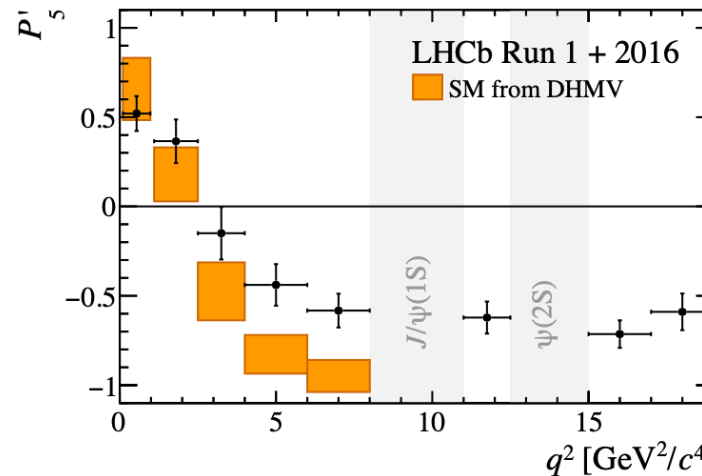
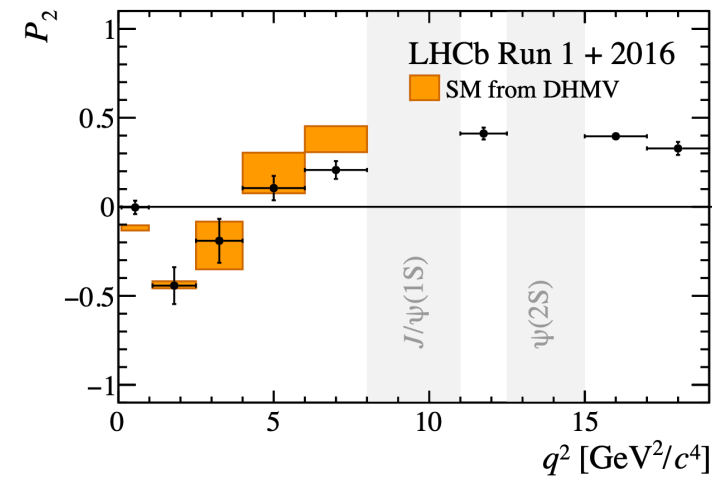
$$P_2 = \frac{2}{3} A_{\text{FB}} / (1 - F_L)$$

$$P'_5 = S_5 / \sqrt{F_L(1 - F_L)}$$

$$P'_5 = \sqrt{2} \frac{\text{Re}(A_0^L A_{\perp}^{L*} - A_0^R A_{\perp}^{R*})}{\sqrt{(|A_0^L|^2 + |A_0^R|^2) (|A_{\parallel}^L|^2 + |A_{\parallel}^R|^2 + |A_{\perp}^L|^2 + |A_{\perp}^R|^2)}}$$

$B^0 \rightarrow K^{*0} \mu\mu$

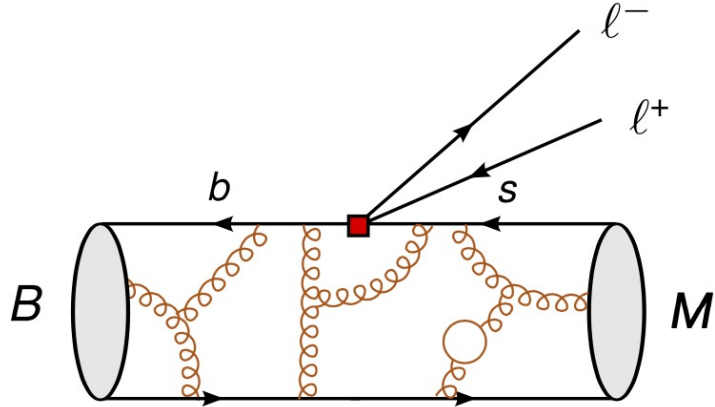
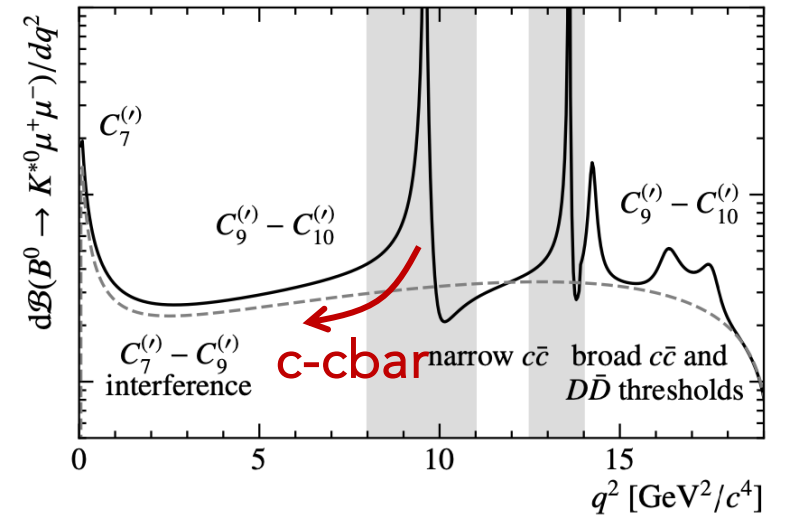
[Phys. Rev. Lett. 125 \(2020\) 011802](#)



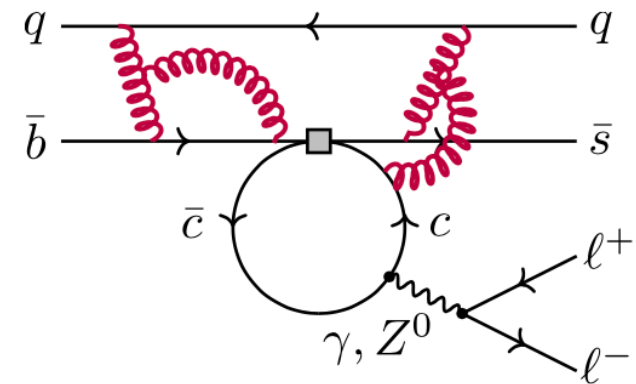
Life is not that simple ...

$$\mathcal{L}_{\text{eff}} \propto G_F V_{tb} V_{ts}^* \sum_{i=7,9,10} (C_i \mathcal{O}_i + C'_i \mathcal{O}'_i)$$

+

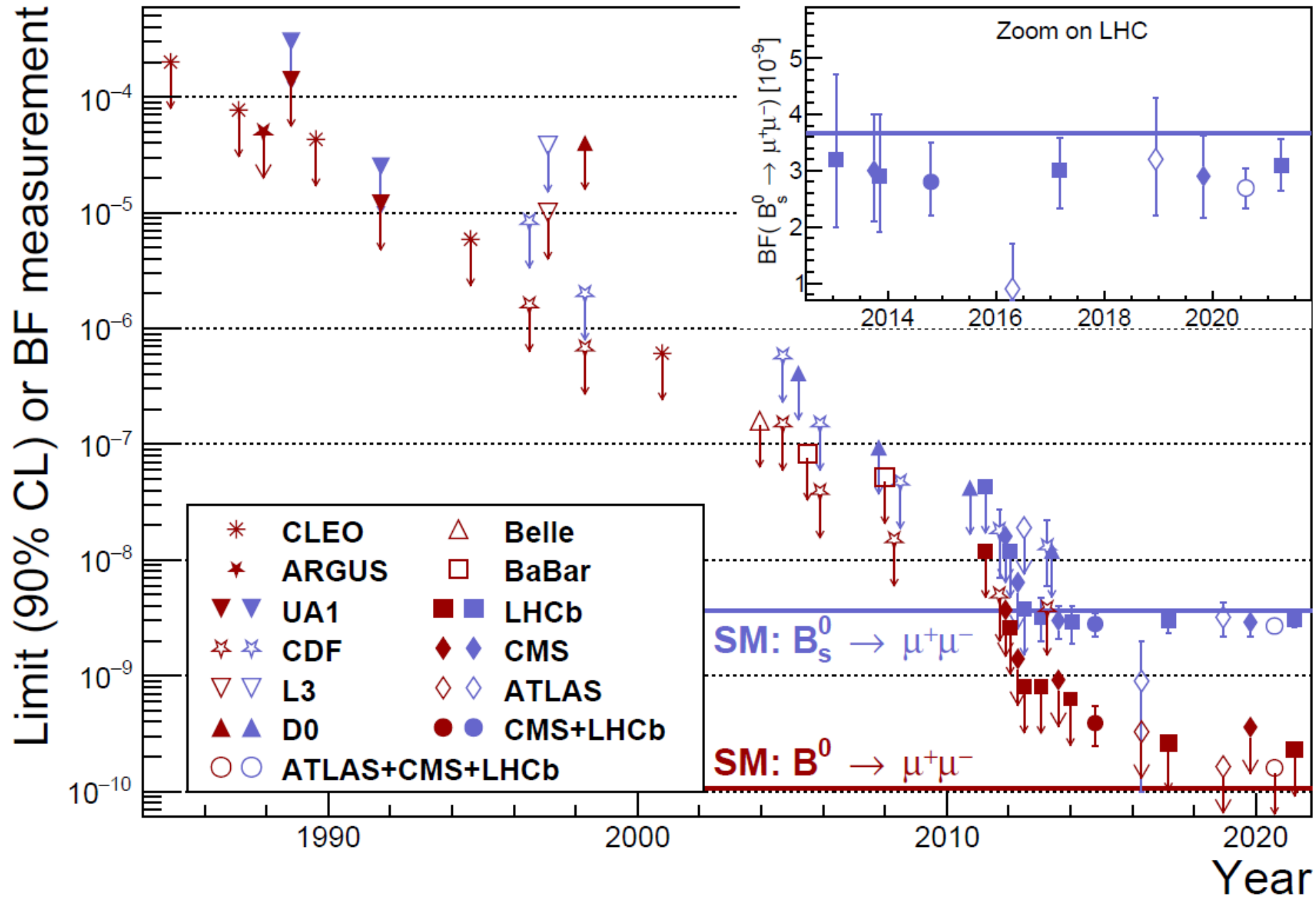


non-local contributions



Would appear as a shift in C_9
 Varying as function of q^2 (not the case for NP)

Searched for during ~ 30 years. First evidence in Nov 2012 (LHCb)



From a yield to a BR

Number of
observed decay

Efficiency

$$BR(B_s \rightarrow \mu\mu) = \frac{N(B_s \rightarrow \mu\mu)_{real}}{N(B_s)_{produced}} = \frac{N(B_s \rightarrow \mu\mu)_{obs} / \epsilon}{L_{int} \times \sigma_{bb} \times f_s}$$

Integrated
luminosity

bb cross
section

Fraction of b quarks
that hadronize into a B_s

$L_{int}, \sigma_{bb}, \epsilon$ have large systematic errors





Normalize with respect to another decay with a very well known BR
(BFactories crucial inputs) :

$$B^+ \rightarrow J/\psi K^+ \text{ or } B^0 \rightarrow K^+ \pi^-$$

$$\frac{BR(B_s \rightarrow \mu\mu)}{BR(B^+ \rightarrow J\psi K^+)} = \frac{N(B_s \rightarrow \mu\mu)_{obs}}{N(B \rightarrow J\psi K)_{obs}} \times \frac{\mathcal{E}_{B \rightarrow J\psi K}}{\mathcal{E}_{B_s \rightarrow \mu\mu}} \times \frac{f_u}{f_s}$$

Most of systematic uncertainties cancel in the ratio of efficiency

This cancellation is very efficient if you have a normalization channel similar to your signal and selected in the same way!

$$B^0 \rightarrow K^{*0} \mu \mu$$

$$\frac{d^4\Gamma[\bar{B}^0 \rightarrow \bar{K}^{*0} \mu^+ \mu^-]}{dq^2 d\vec{\Omega}} = \frac{9}{32\pi} \sum_i I_i(q^2) f_i(\vec{\Omega})$$

$$\vec{\Omega} = (\theta_\ell, \theta_K, \phi)$$

$$\frac{d^4\bar{\Gamma}[B^0 \rightarrow K^{*0} \mu^+ \mu^-]}{dq^2 d\vec{\Omega}} = \frac{9}{32\pi} \sum_i \bar{I}_i(q^2) f_i(\vec{\Omega})$$

I_i ($i=1,9$) are encoding the matrix elements of the decay

$$\begin{aligned} \frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_K d\phi} = \frac{9}{32\pi} & \left[I_1^s \sin^2\theta_K + I_1^c \cos^2\theta_K \right. \\ & + I_2^s \sin^2\theta_K \cos 2\theta_\ell + I_2^c \cos^2\theta_K \cos 2\theta_\ell \\ & + I_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi + I_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi \\ & + I_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + I_6 \sin^2\theta_K \cos \theta_\ell \\ & + I_7 \sin 2\theta_K \sin \theta_\ell \sin \phi + I_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi \\ & \left. + I_9 \sin^2\theta_K \sin^2\theta_\ell \sin 2\phi \right], \end{aligned}$$

The I_i depend on the amplitudes



CP violation in the mixing

Mass eigenstates Flavour eigenstates

$$|M_L\rangle = p|M\rangle + q\bar{M}\rangle$$

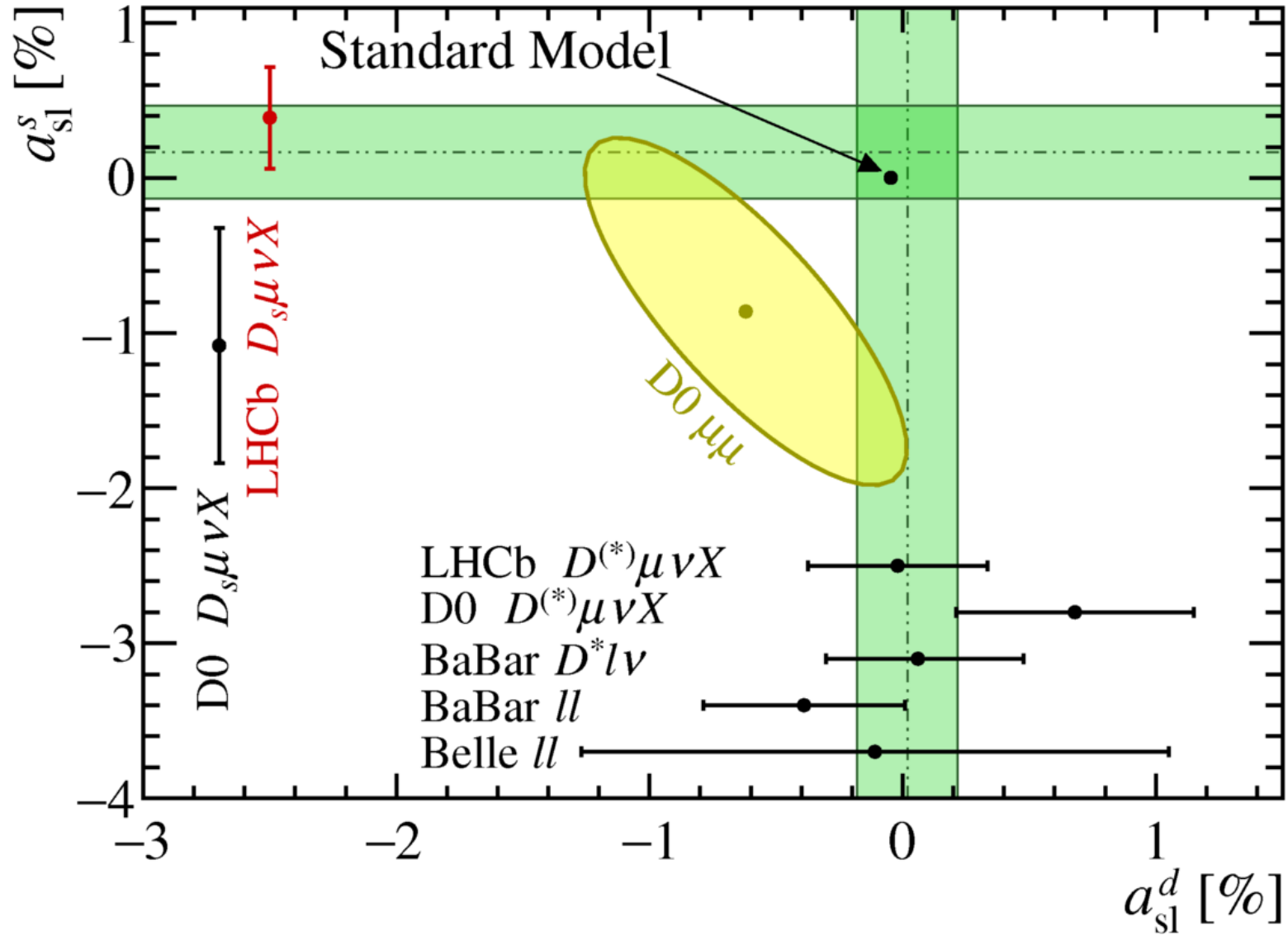
$$|M_H\rangle = p|M\rangle - q\bar{M}\rangle$$

$$\left|\frac{q}{p}\right| \neq 1 \quad P(B \rightarrow \bar{B}) \neq P(\bar{B} \rightarrow B)$$

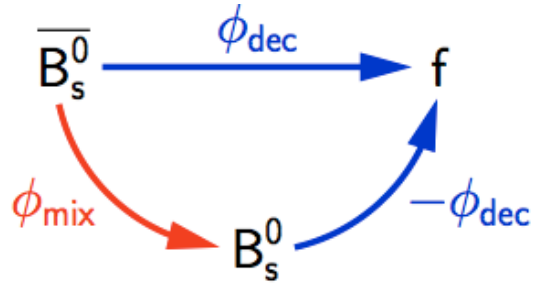
$$a_{sl}^q = \frac{P(\bar{B}_q \rightarrow B_q) - P(B_q \rightarrow \bar{B}_q)}{P(\bar{B}_q \rightarrow B_q) + P(B_q \rightarrow \bar{B}_q)} = \frac{1 - |q/p|^4}{1 + |q/p|^4} \approx \frac{\Delta\Gamma_q}{\Delta m_q} \tan \phi_q^{12}$$

So far only observed in the K system

Expected to be small in the SM ; $\sim -5 \cdot 10^{-4}$ (B_d) and $2 \cdot 10^{-5}$ (B_s)

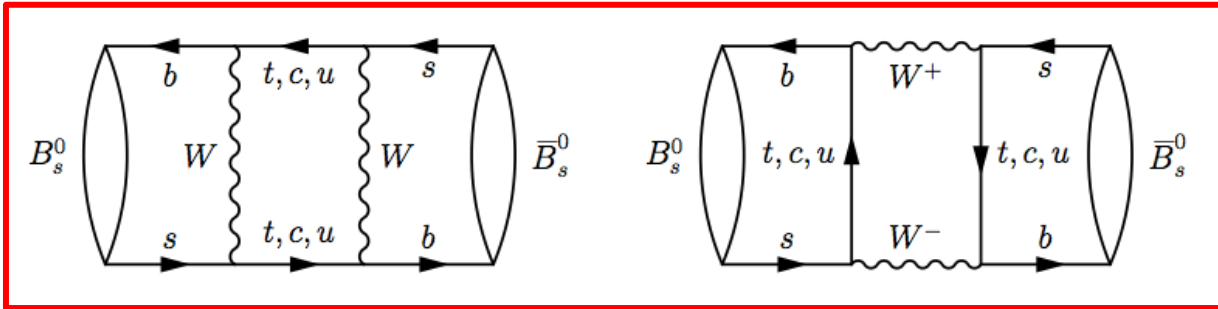


$B_s \rightarrow J/\psi \phi$ analog of the previous case ($B_d \rightarrow J/\psi K_s$)

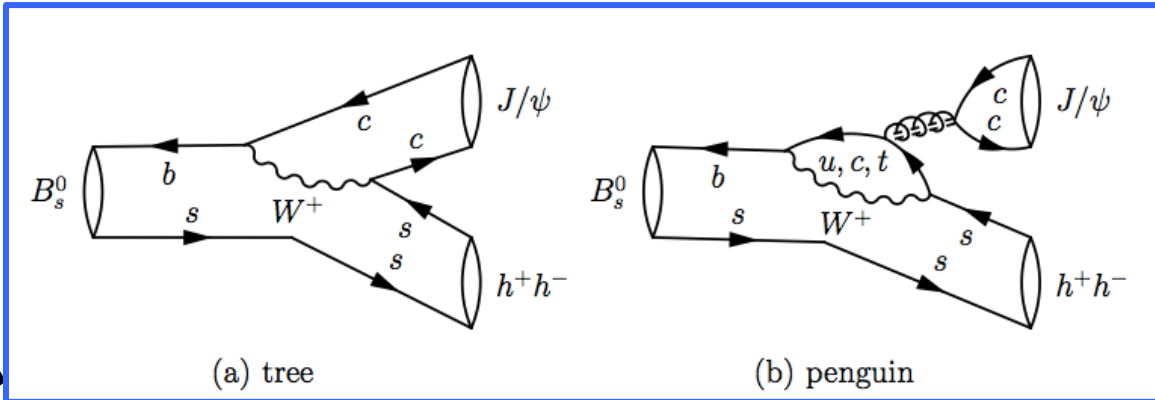


$$\phi_s = \phi_{\text{mix}} - 2\phi_{\text{dec}}$$

- PS \rightarrow VV, admixture of CP-odd and CP-even states, measure also $\Delta\Gamma_s$.
 \Rightarrow 3 "P-wave" amplitudes of KK system
- o 1 "S-wave" amplitude (A_s)
 - o 10 terms with all the interferences
 - o $\phi_s, \Delta\Gamma_s, \Gamma_s$




Mixing



Decay

Probing CKM matrix elements complex at higher order

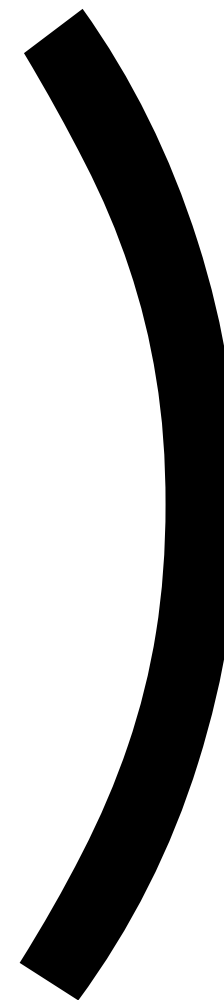
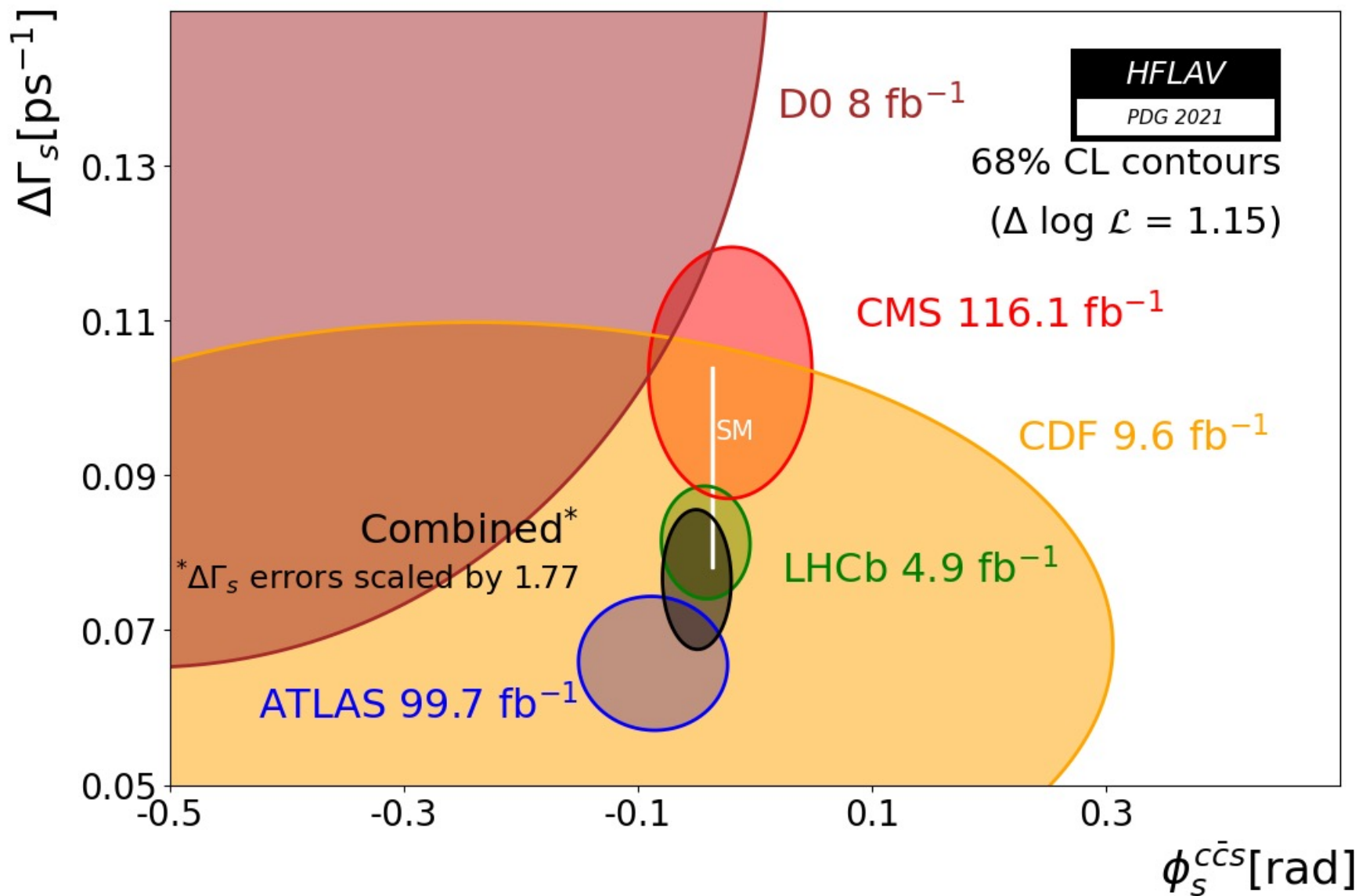
$$V_{\text{CKM}} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$



$$\begin{pmatrix} 1 - \lambda^2/2 - \lambda^4/8 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda + \frac{A^2\lambda^5}{2}(1 - 2\rho) - iA^2\lambda^5\eta & 1 - \lambda^2/2 - \lambda^4\left(\frac{1}{8} + \frac{A^2}{2}\right) & A\lambda^2 \\ A\lambda^3(1 - (1 - \lambda^2/2)(\rho + i\eta)) & -A\lambda^2(1 - \lambda^2/2)(1 + \lambda^2(\rho + i\eta)) & 1 - \frac{A^2\lambda^4}{2} \end{pmatrix} + \mathcal{O}(\lambda^6)$$

SM : $\phi_s = -0.0370 \pm 0.0008$ rad
(prediction from a fit using other measurements)

[HFLAV](#)

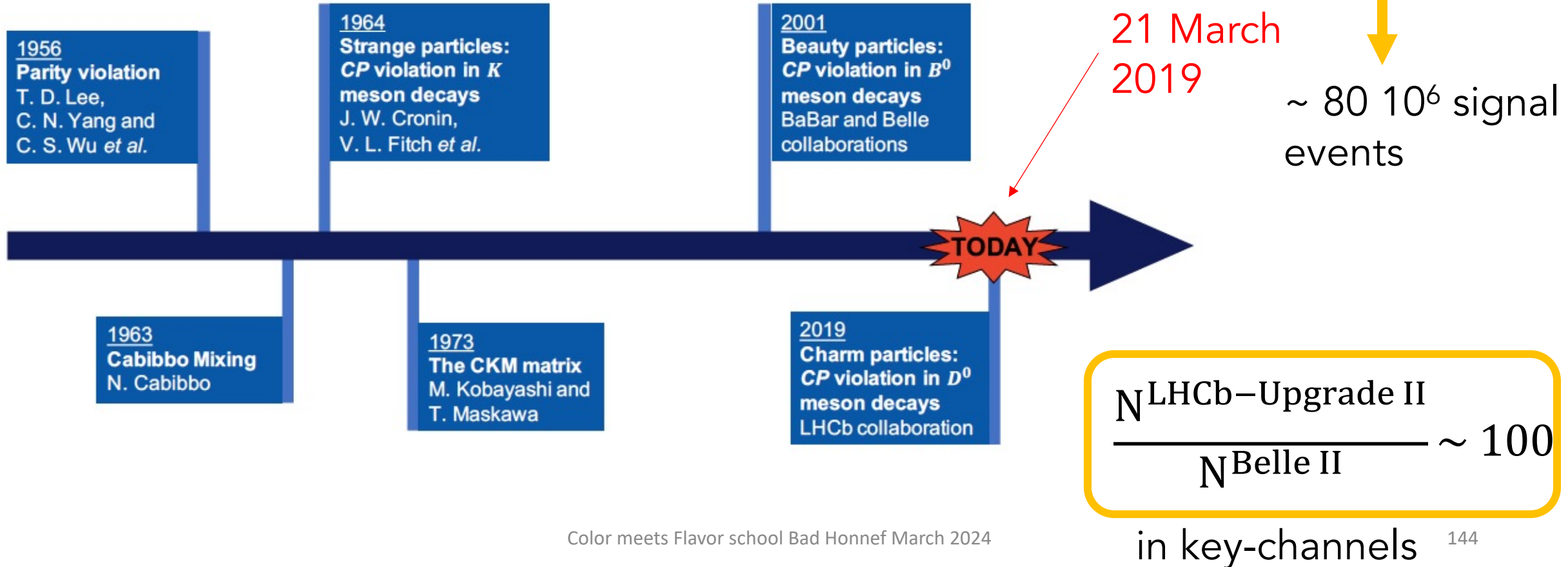


Discovery of CP violation in charm decays

CP violation in up-type sector. SM expectations : $10^{-3} - 10^{-4}$.

$$\sigma_{cc} \approx 20\sigma_{bb} \text{ at LHCb}$$

Extremely large samples needed !



Experimentally:

$$A_{raw} = \frac{N(D^0 \rightarrow f) - N(\bar{D}^0 \rightarrow f)}{N(D^0 \rightarrow f) + N(\bar{D}^0 \rightarrow f)} = A_{CP} + A_D(\pi_s^+ / \mu) + A_P(D^{*+} / D_{\text{from } B}^0)$$

$D^0 \rightarrow KK$ or $\pi\pi$

charge symmetric

$$\Delta A_{CP} = A_{raw}(KK) - A_{raw}(\pi\pi) \cong A_{CP}(KK) - A_{CP}(\pi\pi)$$

Kinematical reweighting \Rightarrow production and detection asymmetries cancel

π tag

$\Delta A_{CP} = (-0.154 \pm 0.029)\%$

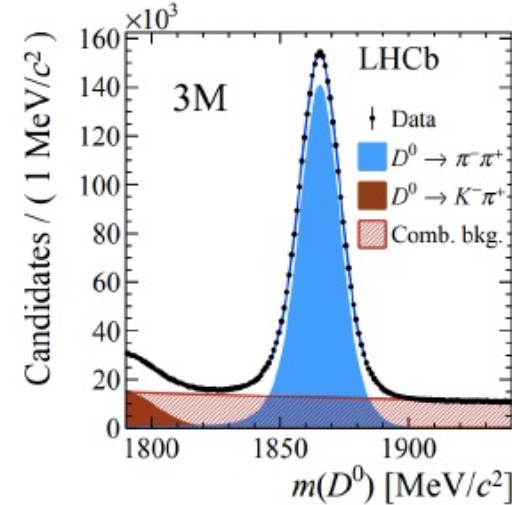
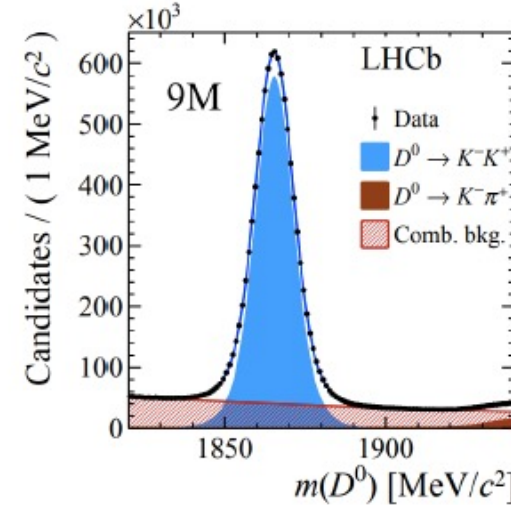
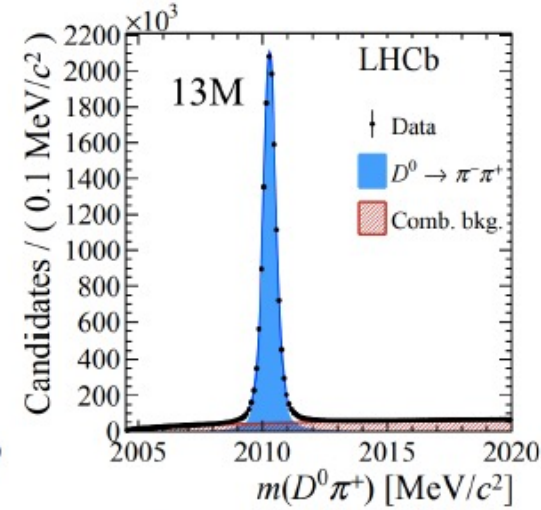
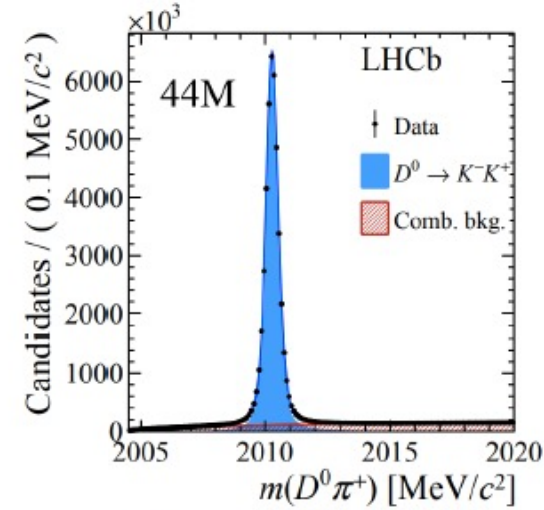
Observation of CP violation at 5.3σ

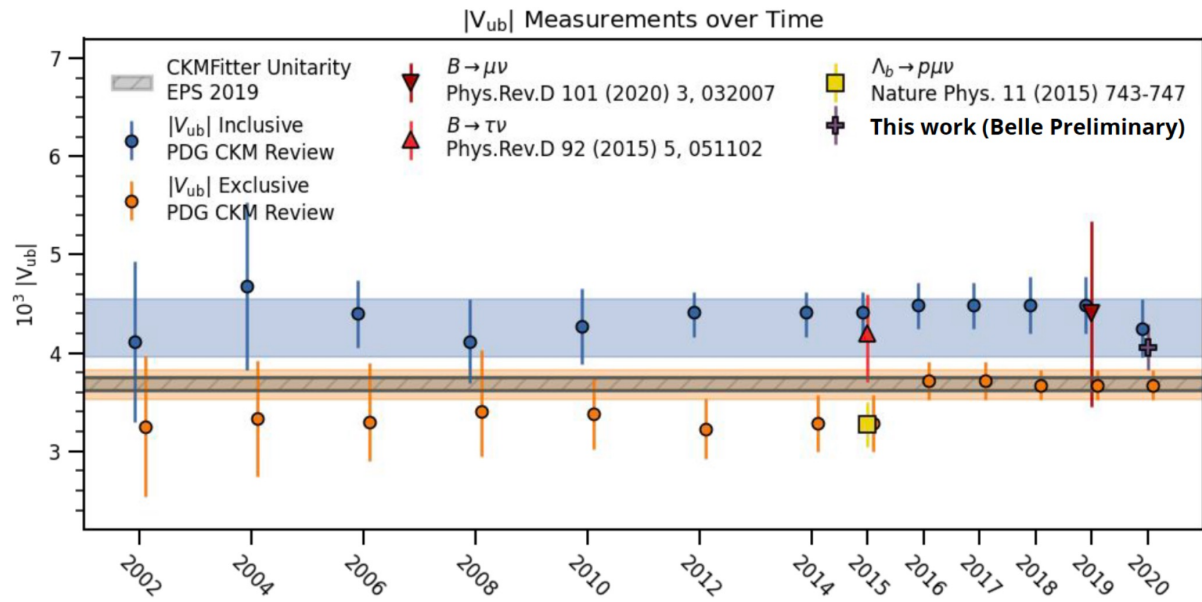
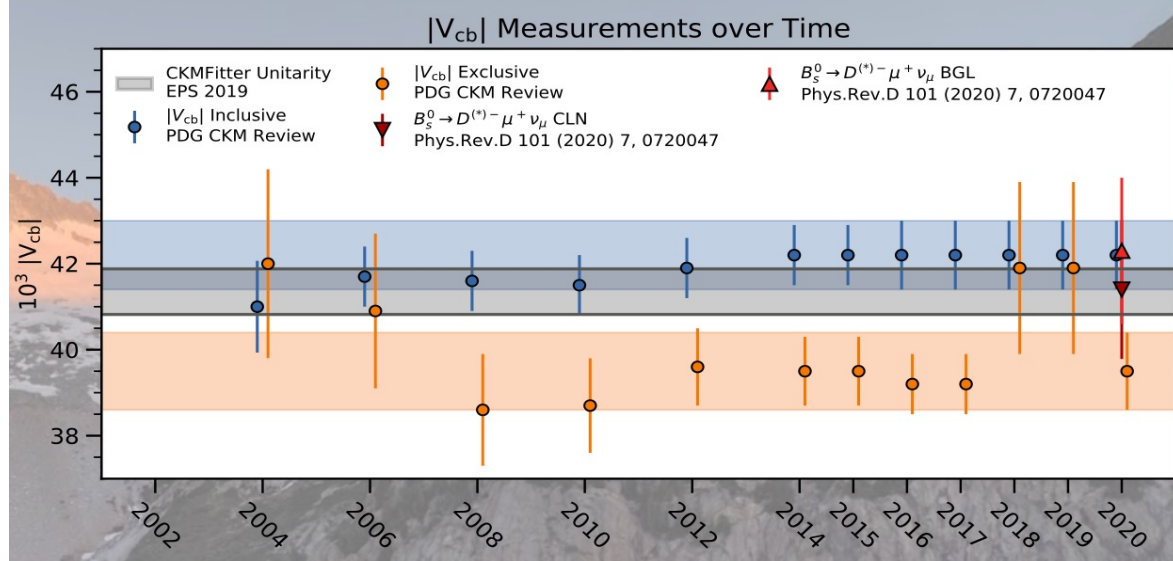
μ tag

Run2 dataset (6 fb^{-1})

Phys. Rev. Lett. 122 (2019) 211803

Color meets Flavor school Bad Honnef IV





Long standing discrepancies ... (not due to statistics)

$|V_{cb}|$: **inclusive** determinations

Not a statistical issue

Kinematical constraints from other B reconstruction

$$|V_{cb}| = (42.2 \pm 0.8) \times 10^{-3} \quad \text{PDG}$$

Using q^2 moments and Belle + Belle-II data

$$|V_{cb}| = (41.69 \pm 0.59|_{\text{fit}} \pm 0.23|_{\text{h.o.}}) \cdot 10^{-3} = (41.69 \pm 0.63) \cdot 10^{-3}$$

$|V_{cb}|$: **exclusive** determinations ($B \rightarrow D^{(*)} | \nu$)

$B \rightarrow D^* | \nu$ extremely clean samples, $B \rightarrow D | \nu$ less clean (D^* feed-down)

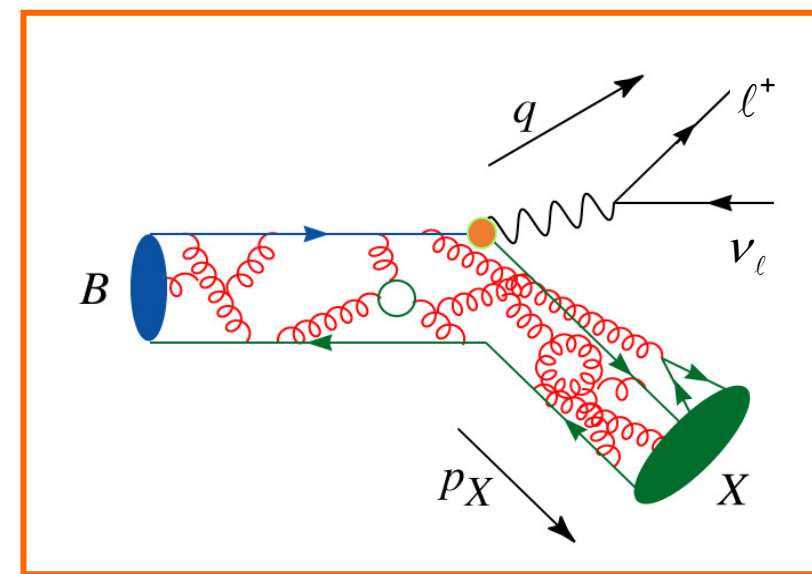
FF parametrization

Measurement of the differential rates

$$|V_{cb}| = (39.4 \pm 0.8) \times 10^{-3}$$

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$$|V_{cb}|_{\text{BGL}} = (40.57 \pm 0.31 \pm 0.95 \pm 0.58) \times 10^{-3},$$



arXiv:2205.10274

$|V_{ub}|/|V_{cb}|$ by LHCb

$$\frac{\mathcal{B}(\Lambda_b \rightarrow p \mu^- \bar{\nu}_\mu)_{q^2 > 15 \text{ GeV}^2/c^4}}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c \mu \nu)_{q^2 > 7 \text{ GeV}^2/c^4}}$$

$$\frac{\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)_{q^2 < 7}}{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)_{\text{Full } q^2}}$$

$$\frac{\mathcal{B}(B_s^0 \rightarrow K^- \mu^+ \nu_\mu)_{q^2 > 7}}{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)_{\text{Full } q^2}}$$

$B_s^0 \rightarrow K^+ \mu^- \nu$ vs $\Lambda_b^0 \rightarrow p \mu \nu$

Decay	Λ_b^0	B_s^0
theory error	5%	~ 5%
prod frac	20%	10%
BF	4×10^{-4}	1×10^{-4}
$\mathcal{B}(X_c)$ error	$\pm 5\%$	$\pm 2.8\%$
background	Λ_c^+	$\Lambda_c^+, D_s, D^+, D^0$

Importance of X_c BF measurements

Importance of FF knowledge for the backgrounds

2012 data !

$$\frac{|V_{ub}|}{|V_{cb}|} = 0.083 \pm 0.004 \pm 0.004$$

$$|V_{ub}|/|V_{cb}|(\text{high}) = 0.0946 \pm 0.0030 (\text{stat})_{-0.0025}^{+0.0024} (\text{syst}) \pm 0.0013 (D_s) \pm 0.0068 (\text{FF})$$