

Compact Multiquarks vs. Hadronic Molecules

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Joint work with Jon Rosner

Exotic multi-quark states and baryon spectroscopy workshop
Bonn University, June 26 2024

Outline

- quarks are fundamental building blocks of protons, neutrons and all hadrons
- all quarks are equal, but heavy quarks are more equal than others

new combinations with heavy quarks, incl. exotics:

- newly discovered T_{cc}^+ tetraquark = $(cc\bar{u}\bar{d})$
- stable $bb\bar{u}\bar{d}$ tetraquark
- hadronic molecules, esp. LHCb pentaquarks 6 by the latest count:
3 nonstrange & 3 strange
- *“like a new layer in the periodic table”*

\exists robust experimental evidence
for multiquark states, a.k.a.
exotic hadrons with heavy Q

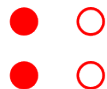
- non $\bar{q}q'$ mesons, e.g. $\bar{Q}Q\bar{q}q$, $QQ\bar{q}\bar{q}$
 $Q = c, b$ $q = u, d, s$
- non $qq'q''$ baryons, e.g. $\bar{Q}Qqq'q''$

two key questions:

- which additional exotics should we expect?
- how are quarks organized inside them?



Tq



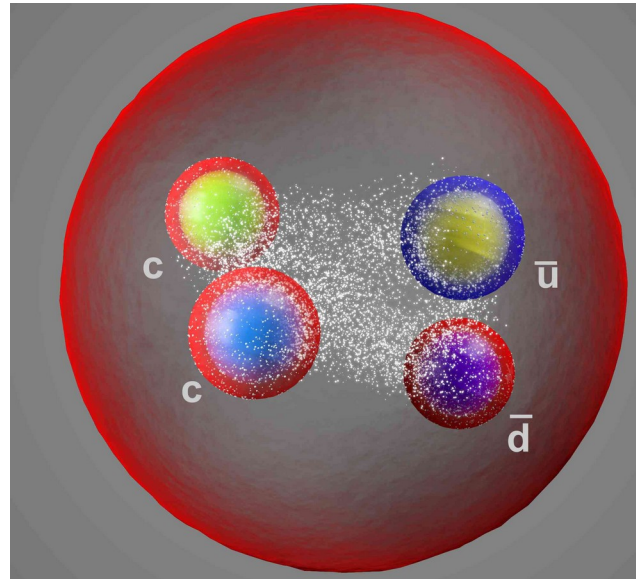
dq-dq



had. mol.

...

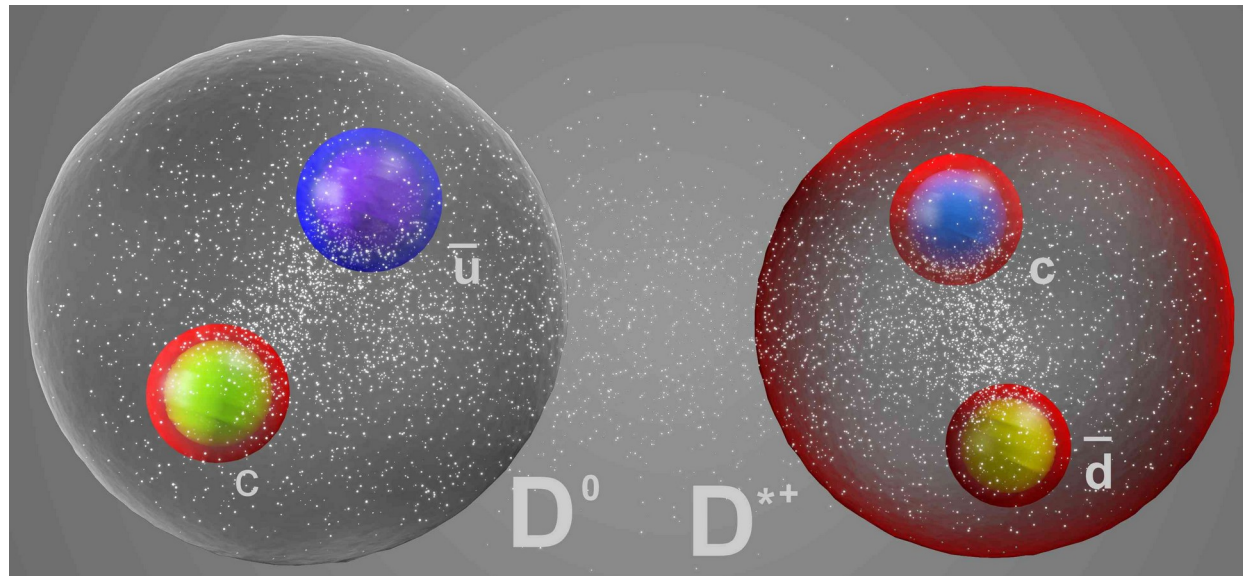
tightly-bound
tetraquark



each quark
sees the color charges
of all other quarks

or

hadronic
molecule?



two color
singlets
interacting
by
light meson
x-change



CERN-EP-2021-165
LHCb-PAPER-2021-031
September 2, 2021

Phys. Rev. Lett. 131 (2023) 041902

Nature Commun. 13 (2022) 3351

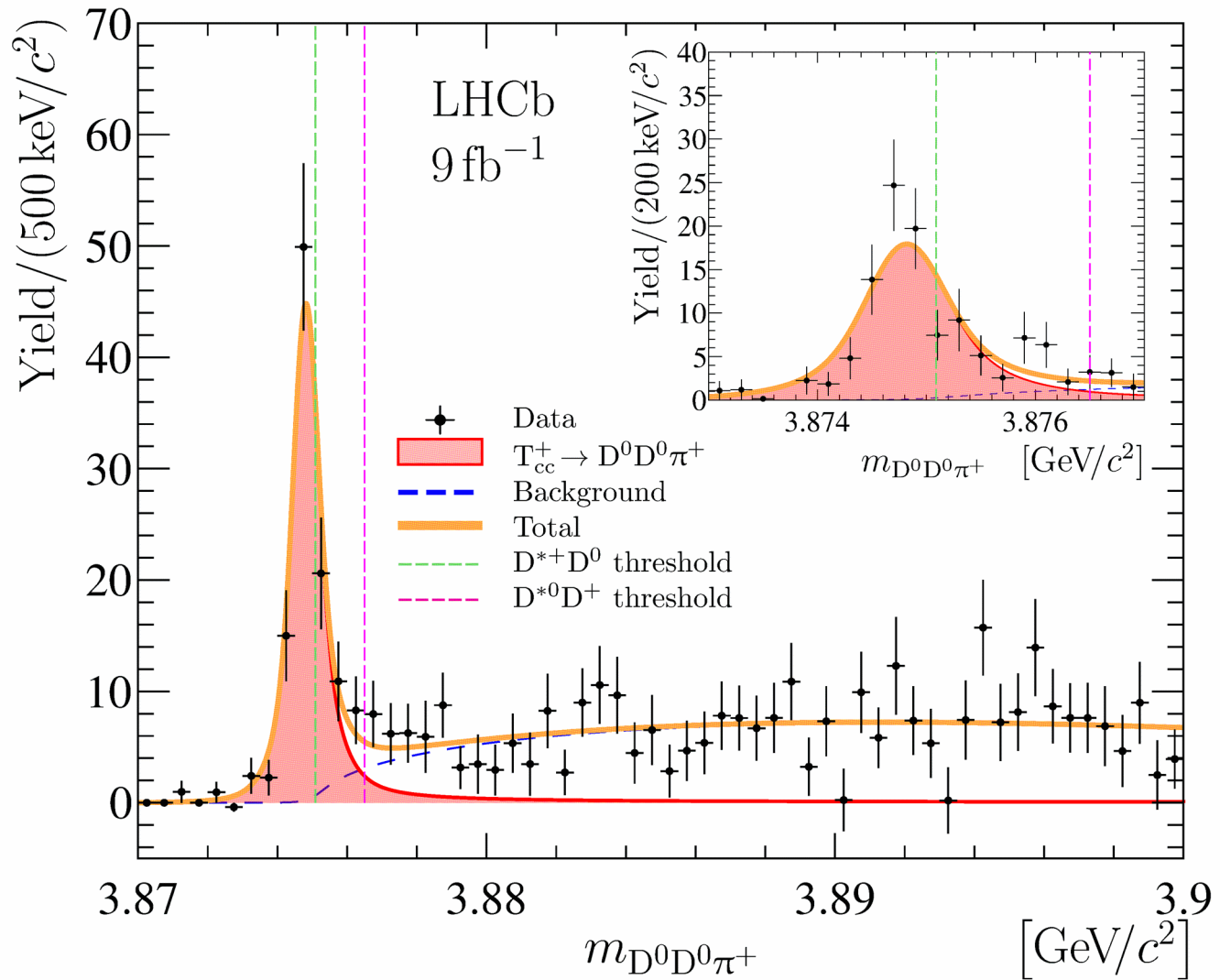
arXiv:2109.01038v1 [hep-ex] 2 Sep 2021

Observation of an exotic narrow doubly charmed tetraquark

LHCb collaboration[†]

Abstract

Conventional hadronic matter consists of baryons and mesons made of three quarks and quark-antiquark pairs, respectively. The observation of a new type of hadronic state, a doubly charmed tetraquark containing two charm quarks, an anti-u and an anti-d quark, is reported using data collected by the LHCb experiment at the Large Hadron Collider. This exotic state with a mass of about $3875 \text{ MeV}/c^2$ manifests itself as a narrow peak in the mass spectrum of $D^0 D^0 \pi^+$ mesons just below the $D^{*+} D^0$ mass threshold. The near-threshold mass together with a strikingly narrow width reveals the resonance nature of the state.



The D⁰D⁰π⁺ mass distribution. The D⁰D⁰π⁺ mass distribution where the contribution of the non-D⁰ background has been statistically subtracted. The result of the fit described in the text is overlaid.

Table 1: Signal yield, N , Breit–Wigner mass relative to $D^{*+}D^0$ mass threshold, δm_{BW} , and width, Γ_{BW} , obtained from the fit to the $D^0D^0\pi^+$ mass spectrum. The uncertainties are statistical only.

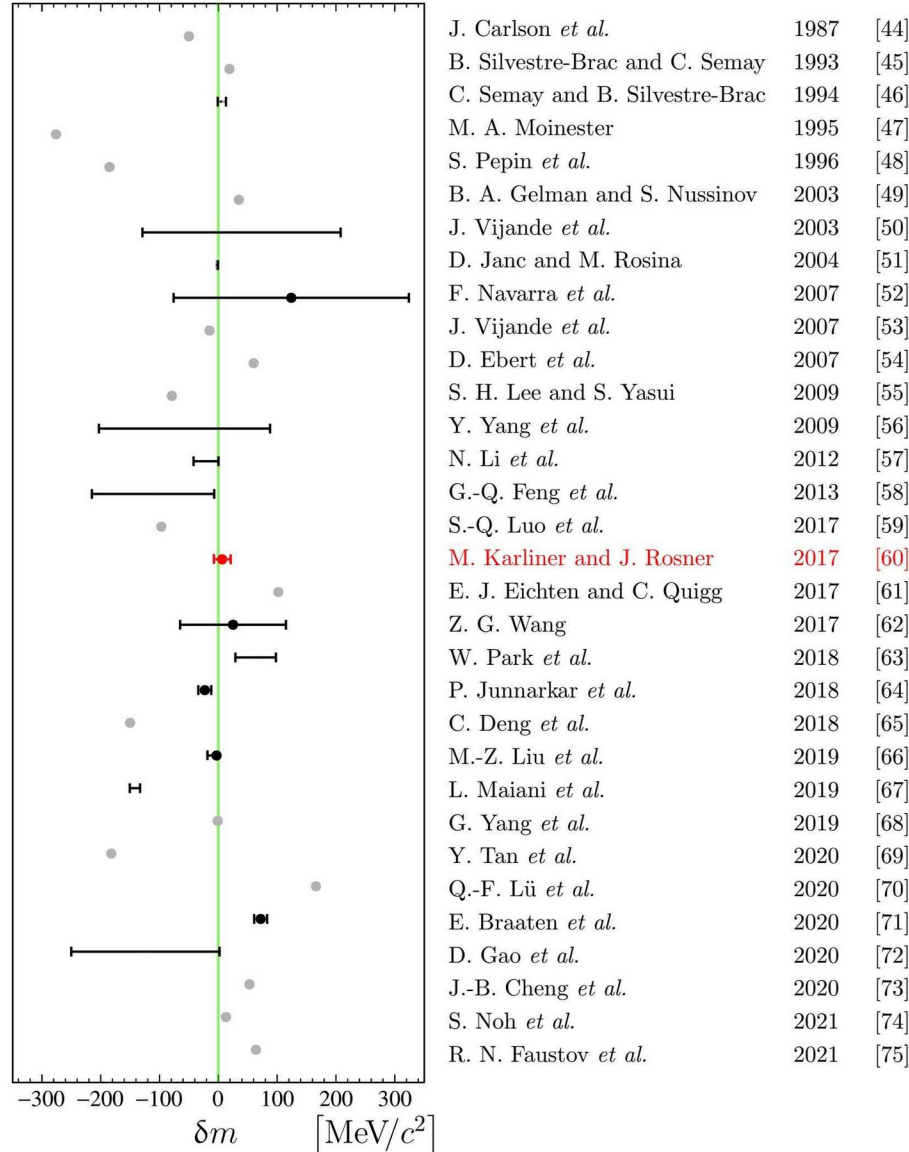
Parameter	Value	
N	117 ± 16	
δm_{BW}	$-273 \pm 61 \text{ keV}/c^2$	@ 4.3 σ
Γ_{BW}	$410 \pm 165 \text{ keV}$	
δm_{pole}	$= -360 \pm 40_{-0}^{+4} \text{ keV}/c^2,$	
Γ_{pole}	$= 48 \pm 2_{-14}^{+0} \text{ keV},$	

$$[M(D^{*0}) + M(D^+)] - [M(D^{*+}) + M(D^0)] = 1.4 \text{ MeV} \gg \Gamma(T_{cc}^+)$$

so $T_{cc}^+ \iff D^{*+}D^0$, with very little $D^{*0}D^+$

TH predictions for T_{cc}^+ mass, $I = 0$, $J^P = 1^+$

$$\delta m_U = -359 \pm 40^{+9}_{-6} \text{ keV}/c^2$$



Theory predictions for the mass of the ground isoscalar $J^P = 1^+$ $cc\bar{u}\bar{d}$ tetraquark T_{cc}^+ state [44–75]. Masses are shown relative to the $D^{*+}D^0$ mass threshold.

Adapted from supplemental material for LHCb-PAPER-2021-032


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important digression: $X(3872)$ observed by CMS in heavy ion collisions

PHYSICAL REVIEW LETTERS **128**, 032001 (2022)

**Evidence for $X(3872)$ in Pb-Pb Collisions and Studies
of its Prompt Production at $\sqrt{s_{NN}} = 5.02$ TeV**

A. M. Sirunyan *et al.**
CMS Collaboration

 (Received 25 February 2021; revised 2 September 2021; accepted 22 December 2021; published 19 January 2022)

The first evidence for $X(3872)$ production in relativistic heavy ion collisions is reported. The $X(3872)$ production is studied in lead-lead (Pb-Pb) collisions at a center-of-mass energy of $\sqrt{s_{NN}} = 5.02$ TeV per nucleon pair, using the decay chain $X(3872) \rightarrow J/\psi \pi^+ \pi^- \rightarrow \mu^+ \mu^- \pi^+ \pi^-$. The data were recorded with the CMS detector in 2018 and correspond to an integrated luminosity of 1.7 nb^{-1} . The measurement is performed in the rapidity and transverse momentum ranges $|y| < 1.6$ and $15 < p_T < 50 \text{ GeV}/c$. The significance of the inclusive $X(3872)$ signal is 4.2 standard deviations. The prompt $X(3872)$ to $\psi(2S)$ yield ratio is found to be $\rho^{\text{Pb-Pb}} = 1.08 \pm 0.49(\text{stat}) \pm 0.52(\text{syst})$, to be compared with typical values of 0.1 for pp collisions. This result provides a unique experimental input to theoretical models of the $X(3872)$ production mechanism, and of the nature of this exotic state.

DOI: [10.1103/PhysRevLett.128.032001](https://doi.org/10.1103/PhysRevLett.128.032001)

The production cross section is much larger, due to multi-parton events, but the huge combinatorial background has been a major challenge. This is a proof that this challenge can be dealt with, at least in some cases,

Prompt production of $X(3872)$ in Pb-Pb collisions. \implies what about T_{cc}^+ ?

10

hadrons w. heavy quarks are *much simpler*:

- heavy quarks almost static
- smaller spin-dep. interaction $\propto 1/m_Q$
- key to accurate prediction of b quark baryons

- Phenomenological approach
- Identify eff. d.o.f. & their interactions
- Extract model parameters from exp
- Then use them to make predictions

apply the toolbox to

doubly-heavy baryons , e.g. ccu

and

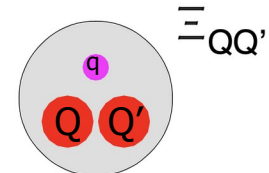
doubly-heavy tetraquarks, e.g. $cc\bar{u}\bar{d}$

in both heavy cc diquark 3_c^* coupled to a light 3_c

doubly-heavy baryons non-exotic, must exist

\Rightarrow excellent testing ground for the toolbox

MK & JR, PRD 90, 094007(2014)



doubly heavy baryons: mass predictions

MK & JR, Phys. Rev. D90, 094007 (2014)

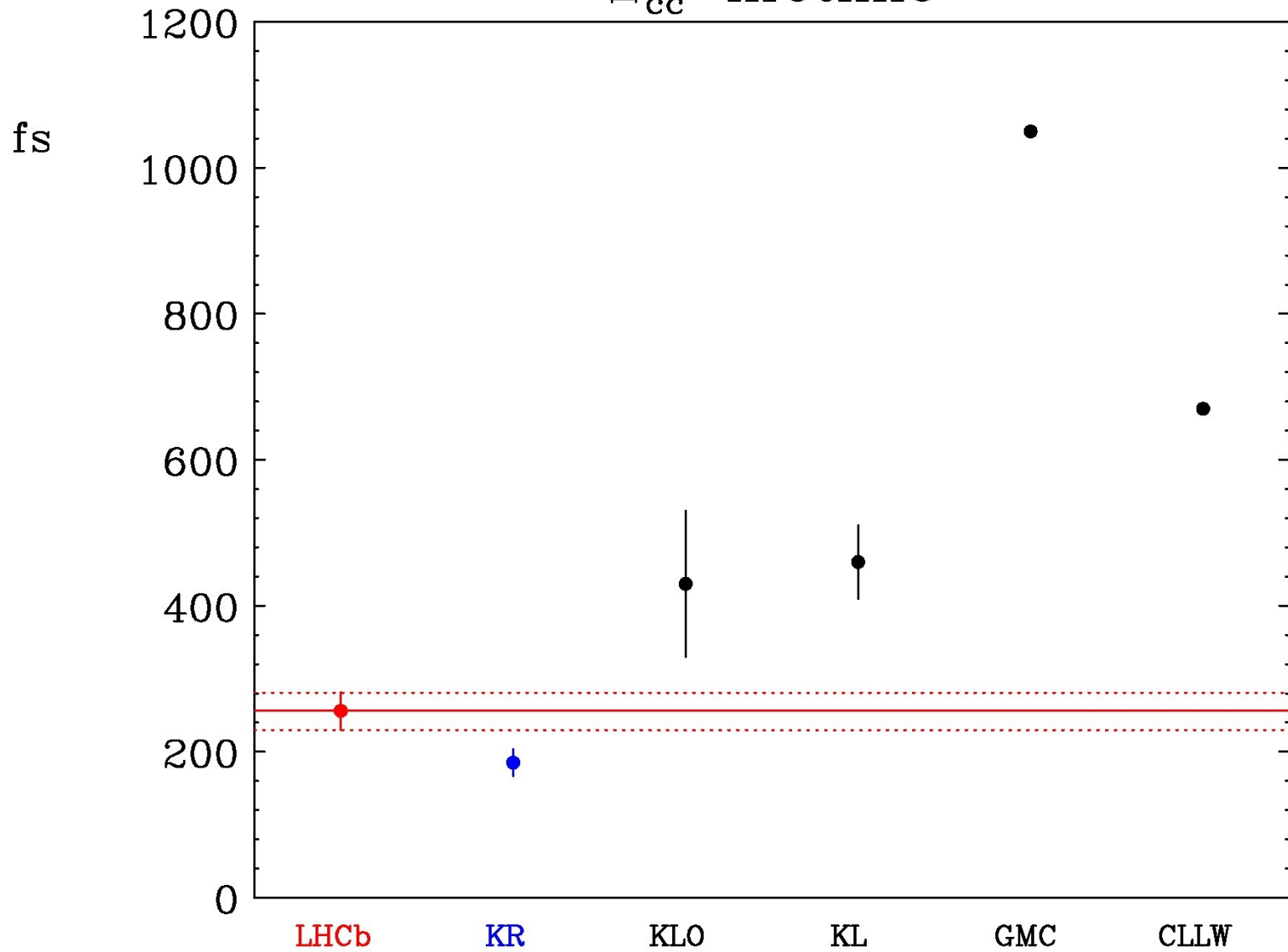
TABLE XVIII. Summary of our mass predictions (in MeV) for lowest-lying baryons with two heavy quarks. States without a star have $J = 1/2$; states with a star are their $J = 3/2$ hyperfine partners. The quark q can be either u or d . The square or curved brackets around cq denote coupling to spin 0 or 1.

State	Quark content	$M(J = 1/2)$	$M(J = 3/2)$
$\Xi_{cc}^{(*)}$	ccq	3627 ± 12	3690 ± 12
$\Xi_{bc}^{(*)}$	$b[cq]$	6914 ± 13	6969 ± 14
Ξ'_{bc}	$b(cq)$	6933 ± 12	...
$\Xi_{bb}^{(*)}$	bbq	10162 ± 12	10184 ± 12

LHCb: 3621.6 ± 0.4

PRL 119,112001, (2017)

Ξ_{cc}^{++} lifetime



$$\tau(\Xi_{cc}^{++}) = 256_{-22}^{+21} \pm 14 \text{ fs}$$

ccq mass calculation

sum of :

- $2m_c$
- V_{cc} in 3_c^*
- $V_{HF}(cc)$
- $V_{HF}(cq)$
- m_q

ccq mass calculation

sum of :

- $2m_c$
 - V_{cc} in 3_c^*
 - $V_{HF}(cc)$
 - $V_{HF}(cq)$
 - m_q
- } no exp info !

Effective masses

in mesons:

$$m_u^m = m_d^m = m_q^m = 310 \text{ MeV}, \quad m_c^m = 1663.3 \text{ MeV}$$

in baryons:

$$m_u^b = m_d^b = m_q^b = 363 \text{ MeV}, \quad m_c^b = 1710.5 \text{ MeV}$$

$V(cc)$ from $V(c\bar{c})$:

$$\bar{M}(c\bar{c} : 1S) \equiv [3M(J/\psi) + M(\eta_c)]/4 = 3068.6 \text{ MeV}$$

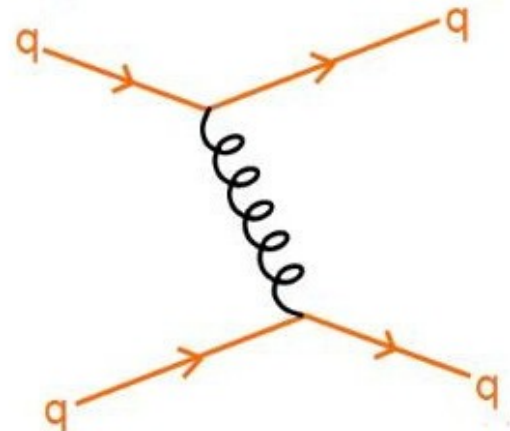
$$V(c\bar{c}) = \bar{M}(c\bar{c} : 1S) - 2m_c^m = -258.0 \text{ MeV.}$$

$$V(cc) = \frac{1}{2} V(c\bar{c}) = -129.0 \text{ MeV.}$$

in weak coupling follows
from color algebra in $1g_x$

here a dynamical assumption:

$V(cc)$ and $V(c\bar{c})$ factorize
into color \times space



gluon exchange by 2 quarks

$V_{HF}(cc)$ from $V_{HF}(c\bar{c})$:

$$V_{HF}(cc) = \frac{a_{cc}}{m_c^2}$$

$$V_{HF}(c\bar{c}) = M(J/\psi) - M(\eta_c) = 113.2 \text{ MeV} = \frac{4a_{\bar{c}c}}{m_c^2}$$

assume $a_{cc} = \frac{1}{2}a_{c\bar{c}}$,

$$\Rightarrow \frac{a_{cc}}{m_c^2} = 1/2 \cdot \frac{M(J/\psi) - M(\eta_c)}{4} = 14.2 \text{ MeV}$$

Contributions to Ξ_{cc} mass

Contribution	Value (MeV)
$2m_c^b + m_q^b$	3783.9
cc binding	-129.0
$a_{cc}/(m_c^b)^2$	14.2
$-4a/m_q^b m_c^b$	-42.4
Total	3627 ± 12

The ± 12 MeV error estimate from
ave. error for Qqq baryons

can the strong QQ interaction stabilize
 H_{QQ} : $(QQuudd)$ hexaquarks,
heavy-quark analogue of the H dibaryon?

\Rightarrow below $2\Lambda_Q$

but above $\Xi_{QQ}N$

\Rightarrow unstable

an ugly duckling...

The same theoretical toolbox
that led to the accurate Ξ_{cc} mass prediction
now predicts
a stable, deeply bound $bb\bar{u}\bar{d}$ tetraquark,
215 MeV below BB^* threshold
the first manifestly exotic stable hadron



Discovery of the Doubly Charmed Ξ_{cc} Baryon Implies a Stable $bb\bar{u}\bar{d}$ Tetraquark

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Recently, the LHCb Collaboration discovered the first doubly charmed baryon $\Xi_{cc}^{++} = ccu$ at 3621.40 ± 0.78 MeV, very close to our theoretical prediction. We use the same methods to **predict a doubly bottom tetraquark $T(bb\bar{u}\bar{d})$ with $J^P = 1^+$ at 10389 ± 12 MeV, 215 MeV below the $B^-\bar{B}^{*0}$ threshold and 170 MeV below the threshold for decay to $B^-\bar{B}^0\gamma$.** The $T(bb\bar{u}\bar{d})$ is therefore stable under strong and electromagnetic interactions and can only decay weakly, the first exotic hadron with such a property. On the other hand, the mass of $T(cc\bar{u}\bar{d})$ with $J^P = 1^+$ is predicted to be 3882 ± 12 MeV, 7 MeV above the D^0D^{*+} threshold and 148 MeV above the $D^0D^+\gamma$ threshold. $T(bc\bar{u}\bar{d})$ with $J^P = 0^+$ is predicted at 7134 ± 13 MeV, 11 MeV below the \bar{B}^0D^0 threshold. Our precision is not sufficient to determine whether $bc\bar{u}\bar{d}$ is actually above or below the threshold. It could manifest itself as a narrow resonance just at threshold.

DOI: 10.1103/PhysRevLett.119.202001

Calculation of tetraquark $bb\bar{u}\bar{d}$ mass

build on accuracy of the Ξ_{cc} mass prediction

$$V(bb) = \frac{1}{2} V(\bar{b}b)$$

to obtain lowest possible mass, assume:

- $bb\bar{u}\bar{d}$ in S -wave
- $\bar{u}\bar{d}$: $\mathbf{3}_c$ “good” antidiq., $S=0$, $I=0$
(it's the lightest one)

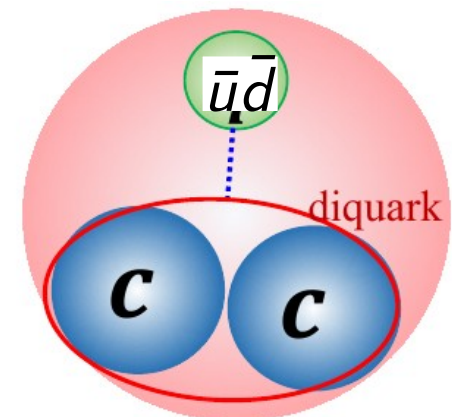
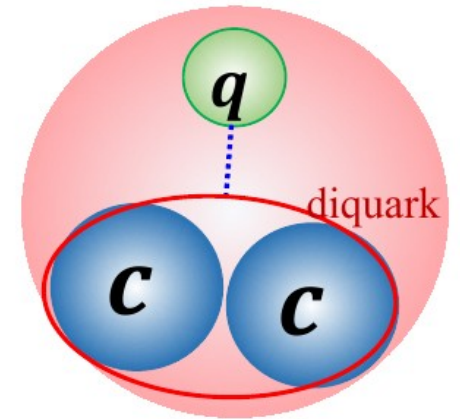
$\Rightarrow bb$ must be $\bar{\mathbf{3}}_c$; Fermi stats: spin 1

$$(bb)_{S=1} (\bar{u}\bar{d})_{S=0} \Rightarrow J^P = 1^+.$$

$\Rightarrow (bb) (\bar{u}\bar{d})$ very similar to bbq baryon:

$$q \leftrightarrow (\bar{u}\bar{d})$$

bbq baryon



Ξ_{cc} discovery \Rightarrow quantitative validation

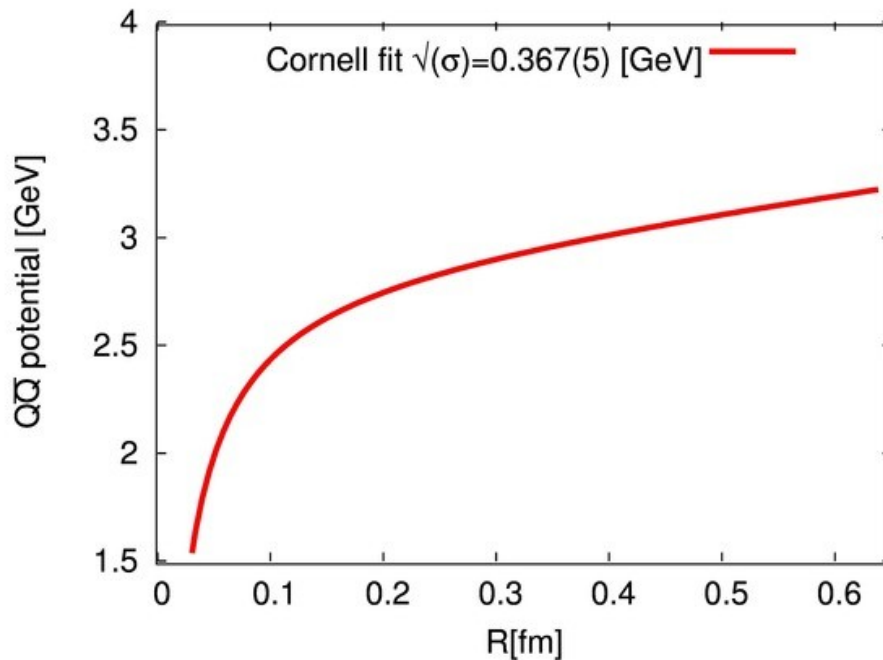
qualitatively $E_{binding} \sim \alpha_s^2 M_Q$

so for $M_Q \rightarrow \infty$

$QQ\bar{u}\bar{d}$ must be bound

Contributions to mass of $(bb\bar{u}\bar{d})$ Tq with $J^P = 1^+$

Contribution	Value (MeV)
$2m_b^b$	10087.0
$2m_q^b$	726.0
$a_{bb}/(m_b^b)^2$	7.8
$-3a/(m_q^b)^2$	-150.0
bb binding	-281.4
Total	10389.4 ± 12



$T(bb\bar{u}\bar{d})$:

$m_b \approx 5$ GeV

$\Rightarrow R(bb) \sim 0.2$ fm

$$V(r) = -\frac{\alpha_s(r)}{r} + \sigma r$$

$\Rightarrow B(bb) \approx -280$ MeV

tightly bound, but $\bar{3}_c$,

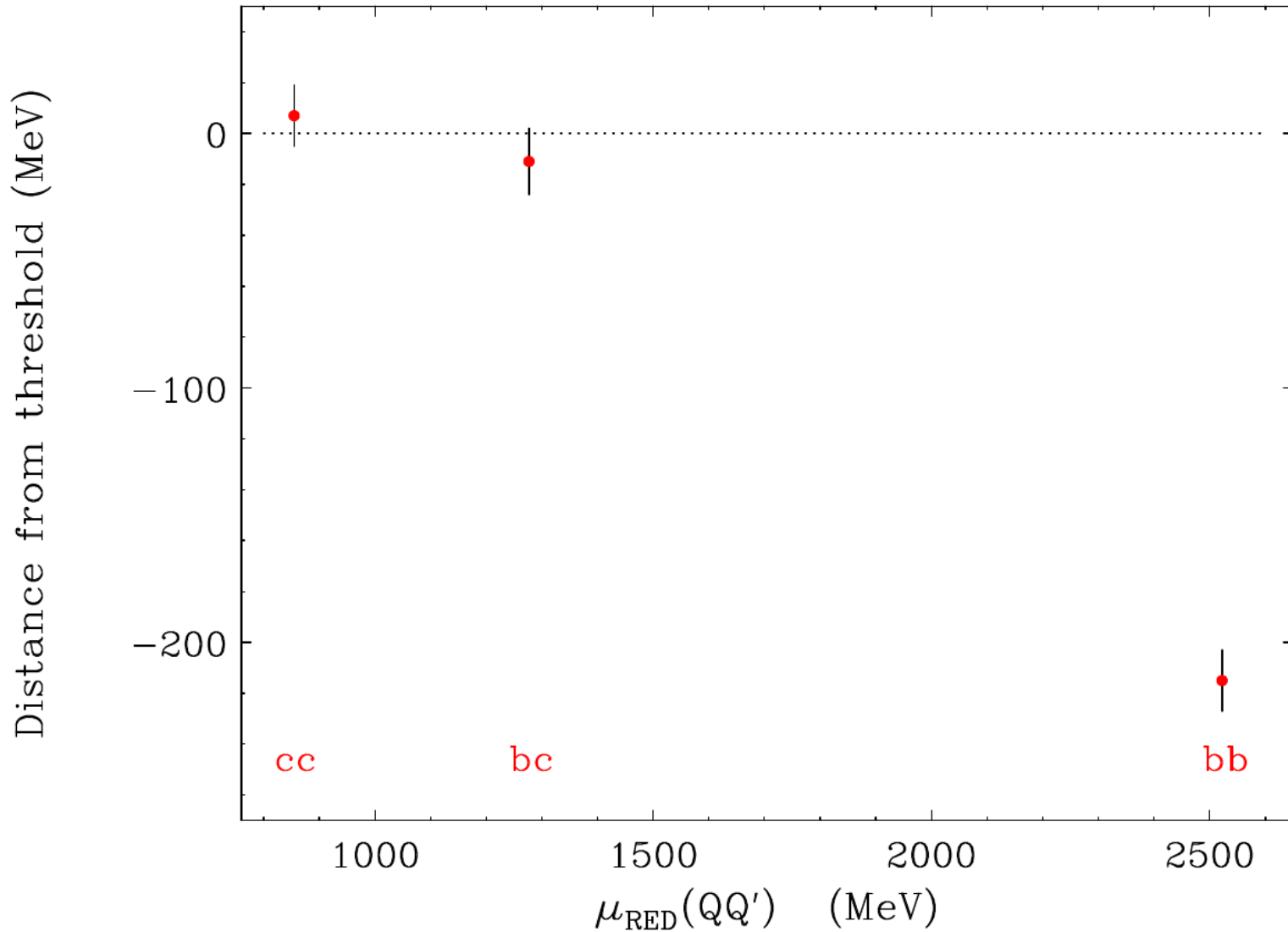
so cannot disengage from $\bar{u}\bar{d}$

The channel $T_{bb} \rightarrow BB^*$ is kinematically closed

because in BB^* the two b quarks are far from each other and the v. large bb binding energy is lost

$\Rightarrow T_{bb}$ is stable against strong decay

Distance of the $QQ'\bar{u}\bar{d}$ Tq masses
from the relevant two-meson thresholds (MeV).



Tetraquark production

$$\sigma(pp \rightarrow T(bb\bar{u}\bar{d}) + X \lesssim \sigma(pp \rightarrow \Xi_{bb} + X)$$

same bottleneck: $\sigma(pp \rightarrow \{bb\} + X)$

hadronization:

$$\left. \begin{array}{l} \{bb\} \rightarrow \{bb\}q \\ \{bb\} \rightarrow \{bb\}\bar{u}\bar{d} \end{array} \right\} \begin{array}{l} P(\bar{u}\bar{d}) \lesssim P(q) \\ \mathbf{3}_c \qquad \mathbf{3}_c \end{array}$$

LHCb observed $ccu = \Xi_{cc}^{+++}$

$$\sigma(pp \rightarrow \Xi_{bb} + X) = (b/c)^2 \cdot \sigma(pp \rightarrow \Xi_{cc} + X)$$

$\Rightarrow \Xi_{bb}$ and $T(bb\bar{u}\bar{d})$ accessible, $T(cc\bar{u}\bar{d})$ near thr. \rightarrow v. narrow accessible
with much more $\int \mathcal{L} dt$ now: $D^0 D^{*+}$, etc.

Inclusive signature of either bbq or $bb\bar{q}\bar{q}$: displaced B_c

T. Gershon & A. Poluektov JHEP 1901 (2019) 019

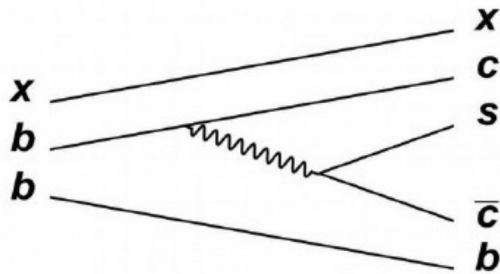
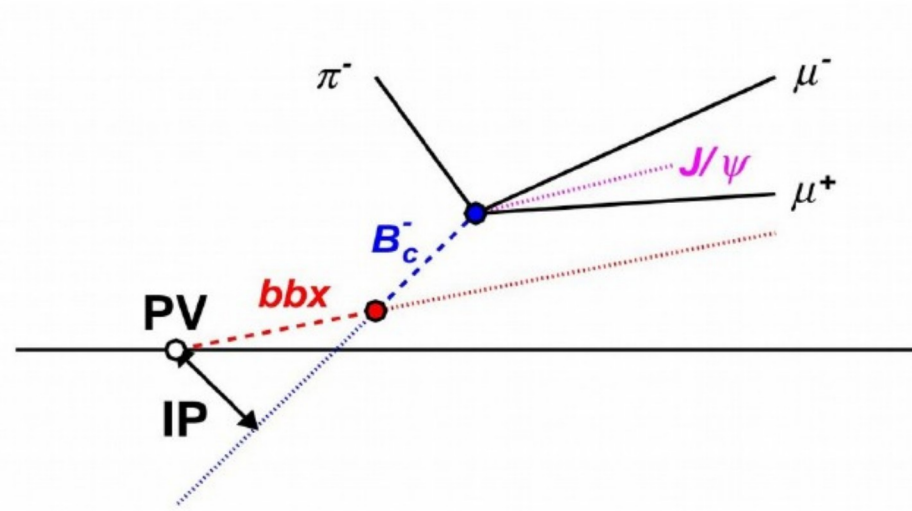


Diagram for production of a B_c^- meson from a double beauty hadron decay.



$\mathcal{O}(1\%)$ of all B_c -s @LHC come from bbx

- major enhancement of eff. bbx rate
- bbq or $bb\bar{u}\bar{d}$?

incl. $\sigma(bb\bar{x})$:
heavy ions $\gg pp$

\Rightarrow displaced B_c @ALICE & RHIC !

crude estimate of $bb\bar{u}\bar{d}$ lifetime

$$M_{initial} = M(bb\bar{u}\bar{d}) = 10,389.4 \text{ MeV}$$

$$M_{final} = M(\bar{B}) + M(D) = 7,144.5 \text{ MeV},$$

$W^{-*} \rightarrow e\bar{\nu}_e, \mu\bar{\nu}_\mu, \tau\bar{\nu}_\tau, 3 \text{ colors of } \bar{u}\bar{d} \text{ and } \bar{c}s,$

a kinematic suppression factor

$$F(x) = 1 - 8x + 8x^3 - x^4 + 12x^2 \ln(1/x),$$

$$x \equiv \{[M(\bar{B}) + M(D)]/M(bb\bar{u}\bar{d})\}^2,$$

$|V_{cb}| = 0.04$, factor of 2 to count each decaying b quark.

$$\Rightarrow \Gamma(bb\bar{u}\bar{d}) = \frac{18 G_F^2 M(bb\bar{u}\bar{d})^5}{192\pi^3} F(x) |V_{cb}|^2 = 17.9 \times 10^{-13} \text{ GeV},$$

$$\tau(bb\bar{u}\bar{d}) = 367 \text{ fs.}$$

$bb\bar{u}\bar{d}$ decay channels

(a) “standard process” $bb\bar{u}\bar{d} \rightarrow cb\bar{u}\bar{d} + W^{*-}$.

$(bb\bar{u}\bar{d}) \rightarrow D^0 \bar{B}^0 \pi^-, D^+ B^- \pi^-$

$(bb\bar{u}\bar{d}) \rightarrow J/\psi K^- \bar{B}^0, J/\psi \bar{K}^0 B^-.$

$(bb\bar{u}\bar{d}) \rightarrow \Omega_{bc} \bar{p}, \Omega_{bc} \bar{\Lambda}_c, \Xi_{bc}^0 \bar{p}, \Xi_{bc}^0 \bar{\Lambda}_c$

In addition, a rare process where *both* $b \rightarrow c\bar{c}s$,

$(bb\bar{u}\bar{d}) \rightarrow J/\psi J/\psi K^- \bar{K}^0.$

striking signature: $2J/\psi$ -s from same 2ndary vertex

(b) The W -exchange $b\bar{d} \rightarrow c\bar{u}$

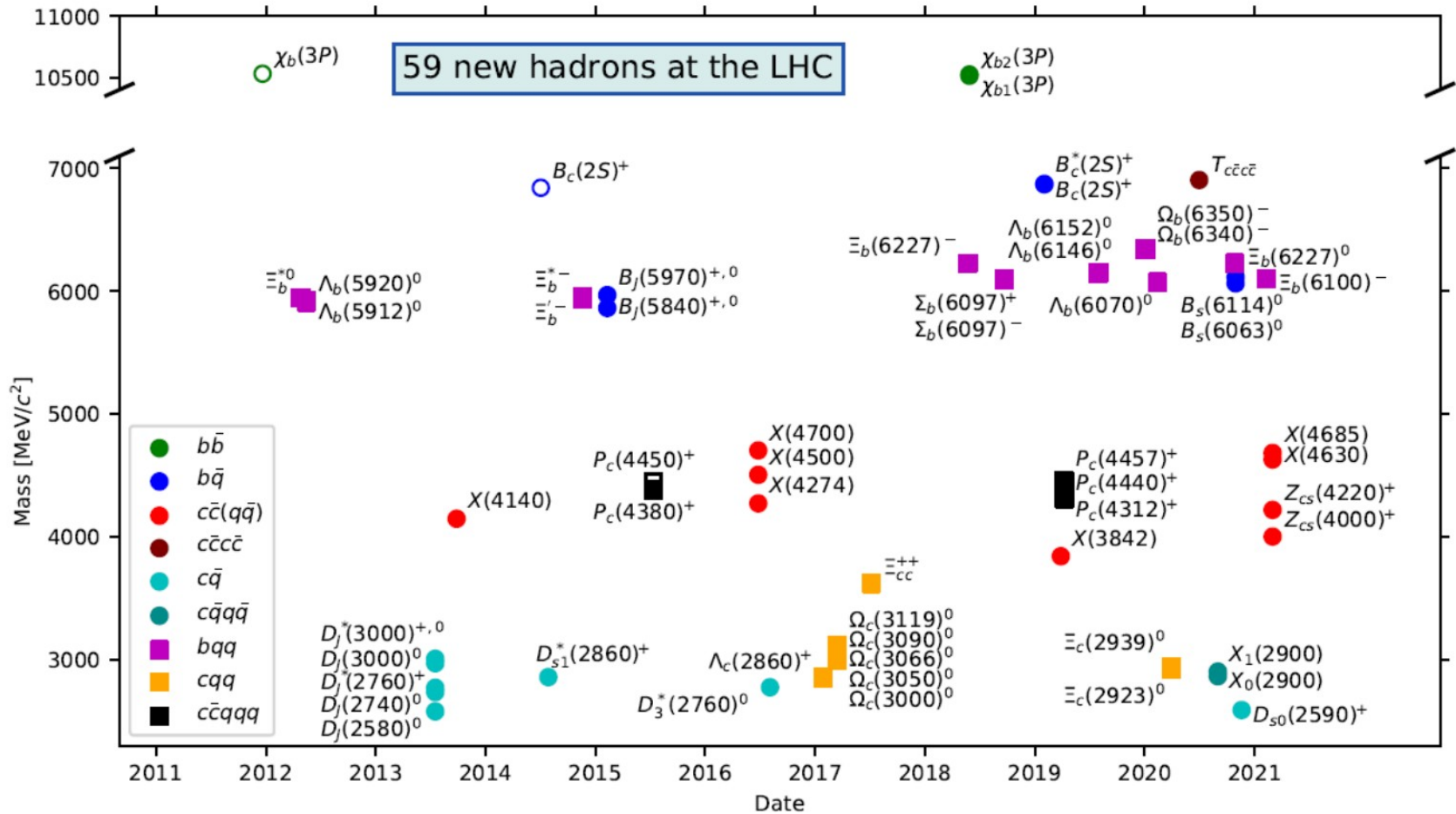
e.g. $(bb\bar{u}\bar{d}) \rightarrow D^0 B^-.$

$T(bb\bar{u}\bar{d})$ Summary

- stable, deeply bound $bb\bar{u}\bar{d}$ tetraquark
- $J^P = 1^+$, $M(bb\bar{u}\bar{d}) = 10389 \pm 12$ MeV
- 215 MeV below BB^* threshold
- first manifesty exotic stable hadron
- $(bb\bar{u}\bar{d}) \rightarrow \bar{B}D\pi^-, J/\psi\bar{K}\bar{B},$
 $J/\psi J/\psi K^- \bar{K}^0, D^0 B^-$

$bb\bar{u}\bar{d}$
cousins

- $(bc\bar{u}\bar{d})$: $J^P = 0^+$, borderline bound 7134 ± 13 MeV, 11 MeV below $\bar{B}^0 D^0$
- $(cc\bar{u}\bar{d})$: $J^P = 1^+$, **observed**: 3875 MeV, just $\mathcal{O}(300)$ keV below $D^0 D^{*+}$, $\Gamma \ll 1$ MeV



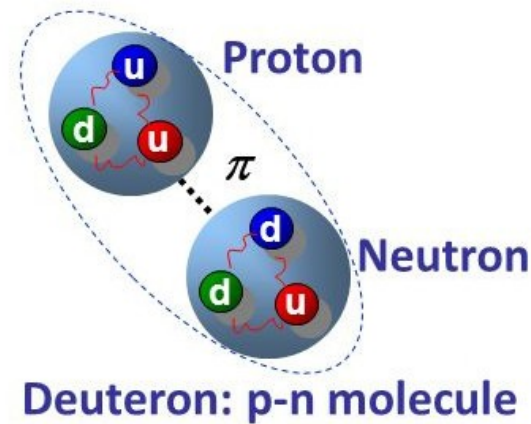
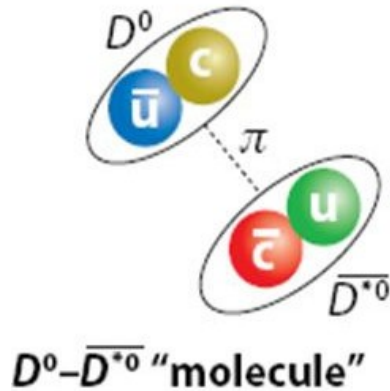
The full list of new hadrons found at the LHC, organised by year of discovery (horizontal axis) and particle mass (vertical axis). The colours and shapes denote the quark content of these states. (Image: LHCb/CERN)

5 narrow exotic states close to meson-meson thresholds

state	mass MeV	width MeV	$\bar{Q}Q$ decay mode	phase space MeV	nearby threshold	ΔE MeV
$X(3872)$	3872	< 1.2	$J/\psi \pi^+ \pi^-$	495	$\bar{D}D^*$	< 1
$Z_b(10610)$	10608	21	$\Upsilon \pi$	1008	$\bar{B}B^*$	2 ± 2
$Z_b(10650)$	10651	10	$\Upsilon \pi$	1051	\bar{B}^*B^*	2 ± 2
$Z_c(3900)$	3900	24 – 46	$J/\psi \pi$	663	$\bar{D}D^*$	24
$Z_c(4020)$	4020	8 – 25	$J/\psi \pi$	783	\bar{D}^*D^*	6
\times					$\bar{D}D$	
\times					$\bar{B}B$	

- masses and widths approximate
- quarkonium decays mode listed have max phase space
- offset from threshold for orientation only, v. sensitive to exact mass

Hadronic molecules: deuteron-like

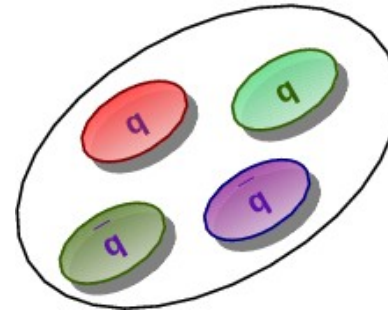
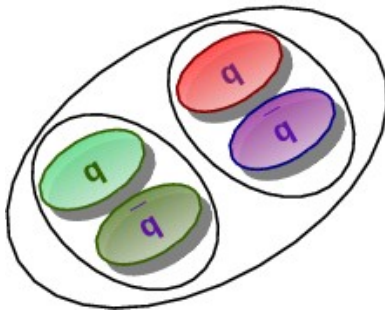


Tetraquarks: same 4 quarks, but tightly bound:

Hadronic Molecule

Tetraquark

two color singlets attract through residual forces



each quark sees color charges of all the other quarks

Belle, PRL 116, 212001 (2016):

$$\frac{\Gamma(Z_b(10610) \rightarrow \bar{B}B^*)}{\Gamma(Z_b(10610) \rightarrow \Upsilon(1S)\pi)} \approx \frac{86\%}{0.54\%} = \mathcal{O}(100)$$

despite 1000 MeV of phase space
for $\Upsilon(1S)\pi$ vs few MeV for $\bar{B}B^*$!

overlap of Z_b wave function with $\Upsilon\pi$
dramatically smaller than with $\bar{B}B^*$

similarly

$$\frac{\Gamma(X(3872) \rightarrow \bar{D}D^*)}{\Gamma(X(3872) \rightarrow J/\psi\pi^+\pi^-)} = 9.1^{+3.4}_{-2.0}$$

$$\frac{\Gamma(Z_c(3885) \rightarrow \bar{D}D^*)}{\Gamma(Z_c(3885) \rightarrow J/\psi\pi)} = 6.2 \pm 1.1 \pm 2.7$$

4 pieces of experimental evidence in support of molecular interpretation of Z_Q and $X(3872)$:

1. masses near thresholds and J^P of S-wave
2. narrow width despite very large phase space
3. $\text{BR}(\text{fall apart mode}) \gg \text{BR}(\text{quarkonium} + X)$
4. no states which require binding through 3 pseudoscalar coupling

the binding mechanism can in principle
apply to any two heavy hadrons
which couple to isospin
and are heavy enough,
be they mesons or baryons

doubly-heavy hadronic molecules:

most likely candidates with $Q\bar{Q}'$, $Q = c, b$, $\bar{Q}' = \bar{c}, \bar{b}$:

$D\bar{D}^*$, $D^*\bar{D}^*$, D^*B^* , $\bar{B}B^*$, \bar{B}^*B^* ,

$\Sigma_c\bar{D}^*$, $\Sigma_c B^*$, $\Sigma_b\bar{D}^*$, $\Sigma_b B^*$, **the lightest of new kind**

$\Sigma_c\bar{\Sigma}_c$, $\Sigma_c\bar{\Lambda}_c$, $\Sigma_c\bar{\Lambda}_b$, $\Sigma_b\bar{\Sigma}_b$, $\Sigma_b\bar{\Lambda}_b$, and $\Sigma_b\bar{\Lambda}_c$.

$c\bar{c}$ and $b\bar{b}$ states decay strongly to $\bar{c}c$ or $\bar{b}b$ and π -(s)

$b\bar{c}$ and $c\bar{b}$ states decay strongly to B_c^\pm and π -(s)

QQ' candidates – dibaryons

$\Sigma_c\Sigma_c$, $\Sigma_c\Lambda_c$, $\Sigma_c\Lambda_b$, $\Sigma_b\Sigma_b$, $\Sigma_b\Lambda_b$, and $\Sigma_b\Lambda_c$.

like a whole new periodic table

Thresholds for $Q\bar{Q}'$ molecular states

Channel	Minimum isospin	Minimal quark content ^{a,b}	Threshold (MeV) ^c	Example of decay mode
$D\bar{D}^*$	0	$c\bar{c}q\bar{q}$	3875.8	$J/\psi \pi\pi$
$D^*\bar{D}^*$	0	$c\bar{c}q\bar{q}$	4017.2	$J/\psi \pi\pi$
D^*B^*	0	$c\bar{b}q\bar{q}$	7333.8	$B_c^+ \pi\pi$
$\bar{B}B^*$	0	$b\bar{b}q\bar{q}$	10604.6	$\Upsilon(nS)\pi\pi$
\bar{B}^*B^*	0	$b\bar{b}q\bar{q}$	10650.4	$\Upsilon(nS)\pi\pi$
$\Sigma_c\bar{D}^*$	1/2	$c\bar{c}qqq'$	4462.4	$J/\psi p$
$\Sigma_c B^*$	1/2	$c\bar{b}qqq'$	7779.5	$B_c^+ p$
$\Sigma_b\bar{D}^*$	1/2	$b\bar{c}qqq'$	7823.0	$B_c^- p$
$\Sigma_b B^*$	1/2	$b\bar{b}qqq'$	11139.6	$\Upsilon(nS)p$
$\Sigma_c\bar{\Lambda}_c$	1	$c\bar{c}qq' \bar{u}\bar{d}$	4740.3	$J/\psi \pi$
$\Sigma_c\bar{\Sigma}_c$	0	$c\bar{c}qq' \bar{q}\bar{q}'$	4907.6	$J/\psi \pi\pi$
$\Sigma_c\bar{\Lambda}_b$	1	$c\bar{b}qq' \bar{u}\bar{d}$	8073.3 ^d	$B_c^+ \pi$
$\Sigma_b\bar{\Lambda}_c$	1	$b\bar{c}qq' \bar{u}\bar{d}$	8100.9 ^d	$B_c^- \pi$
$\Sigma_b\bar{\Lambda}_b$	1	$b\bar{b}qq' \bar{u}\bar{d}$	11433.9	$\Upsilon(nS)\pi$
$\Sigma_b\bar{\Sigma}_b$	0	$b\bar{b}qq' \bar{q}\bar{q}'$	11628.8	$\Upsilon(nS)\pi\pi$

^aIgnoring annihilation of quarks.

^bPlus other charge states when $I \neq 0$.

^cBased on isospin-averaged masses.

^dThresholds differ by 27.6 MeV.

New Exotic Meson and Baryon Resonances from Doubly Heavy Hadronic Molecules

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(Received 13 July 2015; published 14 September 2015)

We predict several new exotic doubly heavy hadronic resonances, inferring from the observed exotic bottomoniumlike and charmoniumlike narrow states $X(3872)$, $Z_b(10610)$, $Z_b(10650)$, $Z_c(3900)$, and $Z_c(4020/4025)$. We interpret the binding mechanism as mostly molecularlike isospin-exchange attraction between two heavy-light mesons in a relative S -wave state. We then generalize it to other systems containing two heavy hadrons which can couple through isospin exchange. The new predicted states include resonances in meson-meson, meson-baryon, baryon-baryon, and baryon-antibaryon channels. These include those giving rise to final states involving a heavy quark $Q = c, b$ and antiquark $\bar{Q}' = \bar{c}, \bar{b}$, namely, $D\bar{D}^*$, $D^*\bar{D}^*$, D^*B^* , $\bar{B}B^*$, \bar{B}^*B^* , $\Sigma_c\bar{D}^*$, $\Sigma_c B^*$, $\Sigma_b\bar{D}^*$, $\Sigma_b B^*$, $\Sigma_c\bar{\Sigma}_c$, $\Sigma_c\bar{\Lambda}_c$, $\Sigma_c\bar{\Lambda}_b$, $\Sigma_b\bar{\Sigma}_b$, $\Sigma_b\bar{\Lambda}_b$, and $\Sigma_b\bar{\Lambda}_c$, as well as corresponding S -wave states giving rise to QQ' or $\bar{Q}\bar{Q}'$.

DOI: 10.1103/PhysRevLett.115.122001

PACS numbers: 14.20.Pt, 12.39.Hg, 12.39.Jh, 14.40.Rt

 Selected for a Viewpoint in *Physics*

Observation of $J/\psi p$ Resonances Consistent with Pentaquark States in $\Lambda_b^0 \rightarrow J/\psi K^- p$ Decays

R. Aaij *et al.**

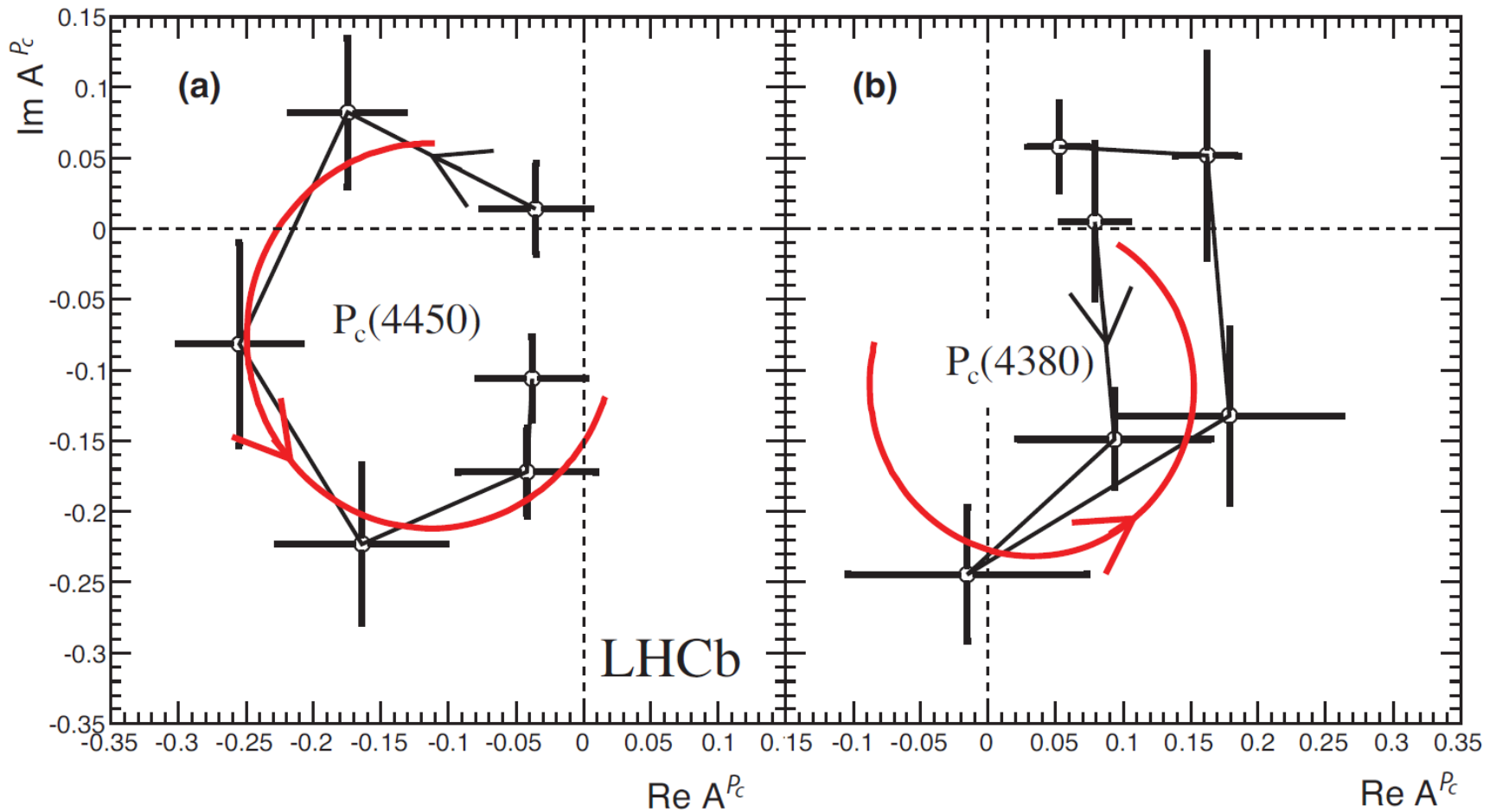
(LHCb Collaboration)

(Received 13 July 2015; published 12 August 2015)

Observations of exotic structures in the $J/\psi p$ channel, which we refer to as charmonium-pentaquark states, in $\Lambda_b^0 \rightarrow J/\psi K^- p$ decays are presented. The data sample corresponds to an integrated luminosity of 3 fb^{-1} acquired with the LHCb detector from 7 and 8 TeV pp collisions. An amplitude analysis of the three-body final state reproduces the two-body mass and angular distributions. To obtain a satisfactory fit of the structures seen in the $J/\psi p$ mass spectrum, it is necessary to include two Breit-Wigner amplitudes that each describe a resonant state. The significance of each of these resonances is more than 9 standard deviations. One has a mass of $4380 \pm 8 \pm 29 \text{ MeV}$ and a width of $205 \pm 18 \pm 86 \text{ MeV}$, while the second is narrower, with a mass of $4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$ and a width of $39 \pm 5 \pm 19 \text{ MeV}$. The preferred J^P assignments are of opposite parity, with one state having spin $3/2$ and the other $5/2$.

DOI: 10.1103/PhysRevLett.115.072001

PACS numbers: 14.40.Pq, 13.25.Gv

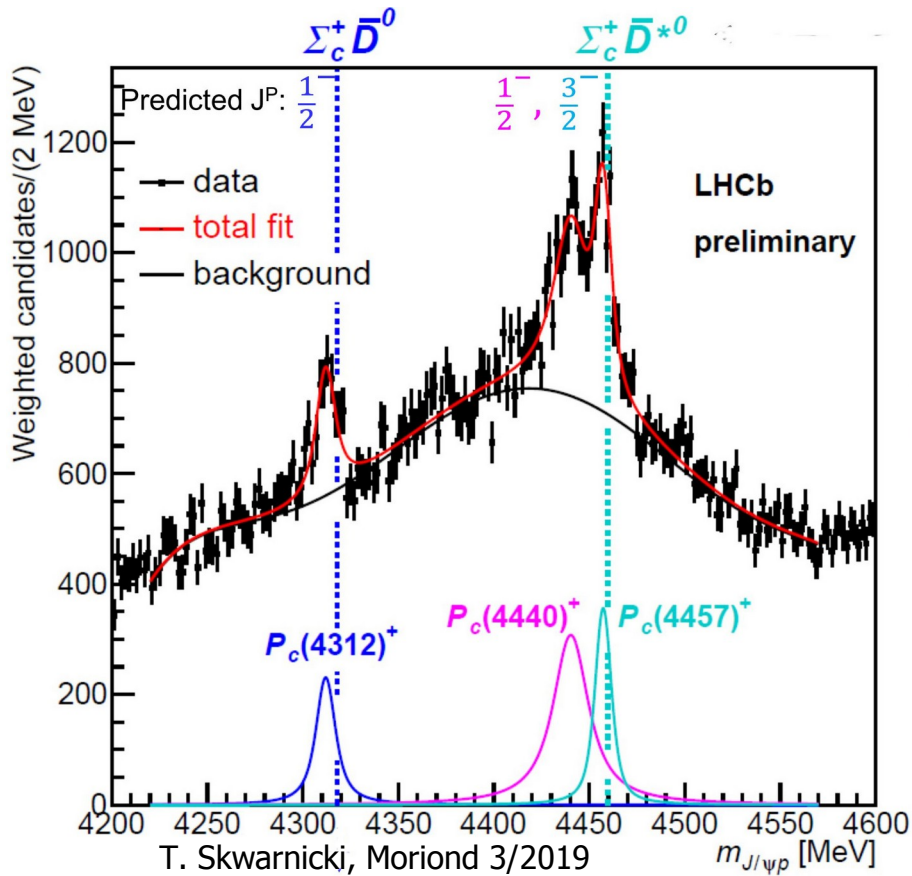


$P_c(4450)$: predicted,
 narrow: $\Gamma = 39 \pm 5 \pm 19$,
 10 MeV from $\Sigma_c \bar{D}^*$ threshold
 perfect Argand plot: a molecule

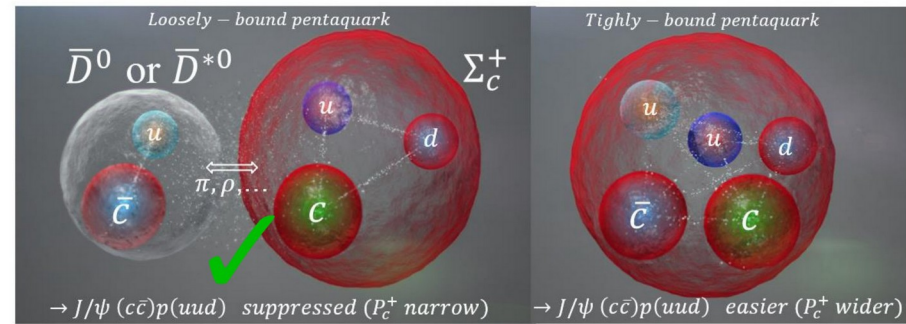
$P_c(4380)$: not predicted,
 wide: $\Gamma = 205 \pm 18 \pm 86$ MeV,
 Argand plot not resonance-like
 ???

$P_c(4450)$ might be just the first of many “heavy deuterons”

as of 2015



The near-threshold masses and the narrow widths of $P_c(4312)^+$, $P_c(4440)^+$ and $P_c(4457)^+$ favor “molecular” pentaquarks with meson-baryon substructure!



observe all 3 S -wave states:

$$\Sigma_c \bar{D}; \quad J^P = \frac{1}{2}^-,$$

$$\Sigma_c \bar{D}^*; \quad J^P = \frac{1}{2}^-, \frac{3}{2}^-$$

for $Q \rightarrow \infty$ 4 more S -wave states:

$$\Sigma_c^* \bar{D}; \quad J^P = \frac{3}{2}^-$$

$$\Sigma_c^* \bar{D}^*; \quad J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$$

but $\Gamma(\Sigma_c^* \rightarrow \Lambda_c \pi) \approx 15 \text{ MeV} \dots$

two v. different types of exotics:

$$Q\bar{Q}q\bar{q}$$
$$QQ\bar{q}\bar{q}$$

e.g.

$$Z_b(10610)$$
$$T(bb\bar{u}\bar{d})$$
$$\bar{B}B^*$$

molecule

tightly-bound

tetraquark

why is it so ?

Exotics with $\bar{Q}Q$ vs. QQ : very different

$$V(\bar{Q}Q) = 2V(QQ), \text{ hundreds of MeV}$$

but *only* if $\bar{Q}Q$ color singlet

$\Rightarrow \bar{Q}Q$ can immediately hadronize as quarkonium

\Rightarrow exotics: \bar{Q} in one hadron and Q in the other

\Rightarrow deuteron-like "hadronic molecules"

vs. QQ *never* a color singlet,

\Rightarrow tightly bound exotics, tetraquarks

$T(bb\bar{u}\bar{d})$:

$m_b \approx 5 \text{ GeV}$

$\Rightarrow R(bb) \sim 0.2 \text{ fm}$

$$V(r) = -\frac{\alpha_s(r)}{r} + \sigma r$$

$\Rightarrow B(bb) \approx -280 \text{ MeV}$

tightly bound, but $\bar{3}_c$,

so cannot disengage from $\bar{u}\bar{d}$

$Z_b(10610)$: $b\bar{b}u\bar{d}$

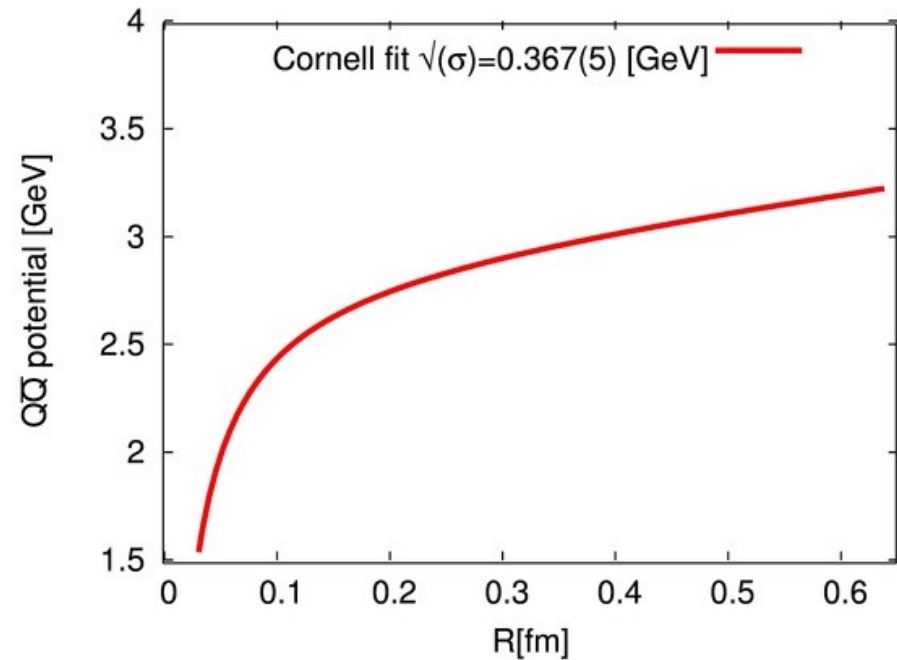
if $b\bar{b}$ compact \Rightarrow color singlet:

decouple from $u\bar{d}$, $Z_b \rightarrow \Upsilon\pi^+$

so only semi-stable config.,

“hadronic molecule:” $\bar{B}B^* \sim 1 \text{ GeV}$ above $\Upsilon\pi$

yet narrow $\sim 15 \text{ MeV}$, because $r(\Upsilon)/r(\bar{B}B^*) \ll 1$



very different!

Upshot:

$bb\bar{u}\bar{d}$: tightly bound tetraquark

$b\bar{b}q\bar{q}$: a molecule

recent news from LHCb: new strange Pq-s

J/ψ Λ resonances in

$$B^- \rightarrow J/\psi \Lambda \bar{p}, \quad \Xi_b^- \rightarrow J/\psi \Lambda K^-$$

\implies new “molecular” pentaquarks:

$$(c\bar{c}sud) \approx \Xi_c^0(csd)\bar{D}^{*0}(\bar{c}u) \rightarrow J/\psi \Lambda$$

vs. $(c\bar{c}uud) \approx \Sigma_c^+(cud)\bar{D}^{*0}(\bar{c}u) \rightarrow J/\psi p$

LHCb arXiv:2012.10380, Sci. Bull. **66**, 1278-1287 (2021)

LHC seminar “Particle Zoo 2.0: New tetra- and pentaquarks at LHCb”,
July 5, 2022, <https://indico.cern.ch/event/1176505/>
and LHCb-PAPER-2022-031, in preparation.

$$\Xi_c \bar{D}^{(*)} \text{ molecules} \implies \Xi'_c \bar{D}^{(*)} \text{ molecules}$$

PHYSICAL REVIEW D **106**, 036024 (2022)

New strange pentaquarks

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Tel Aviv University, Tel Aviv 69978, Israel*

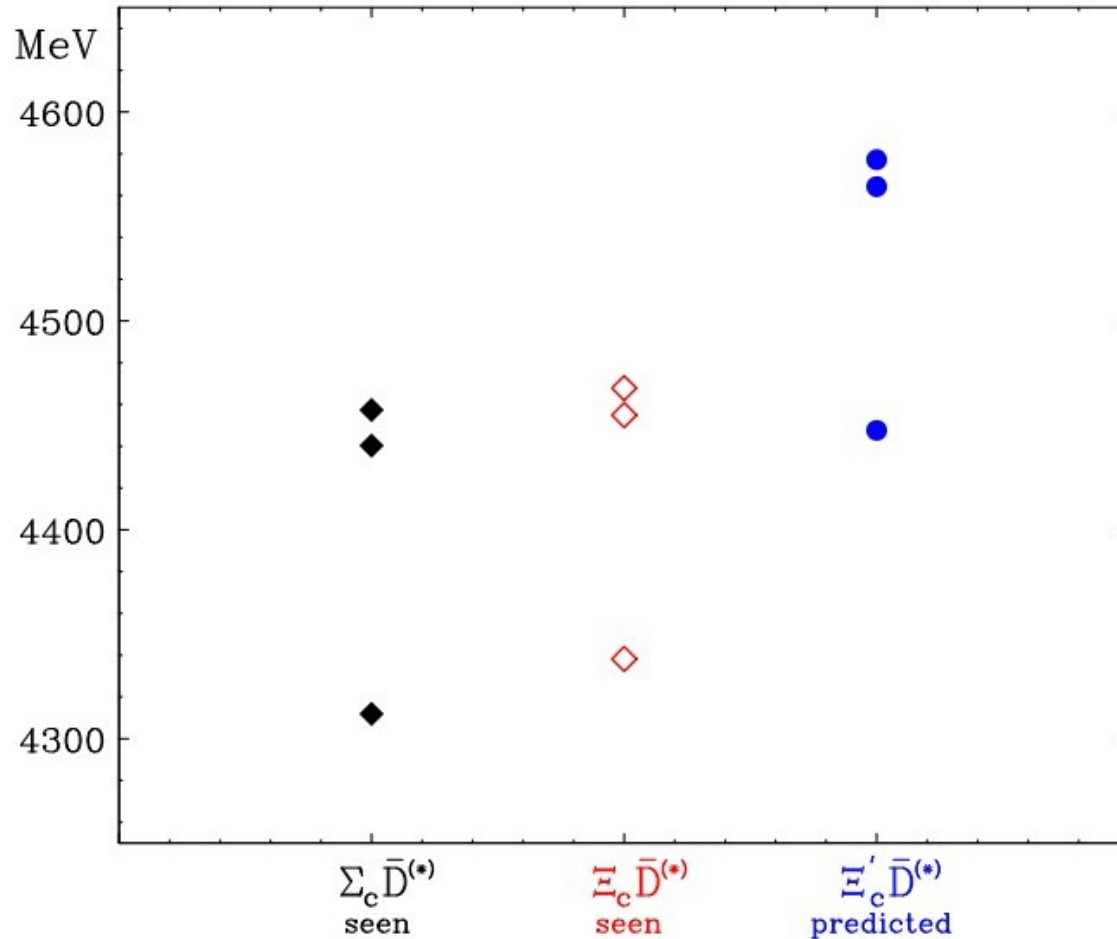
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(Received 25 July 2022; accepted 8 August 2022; published 25 August 2022)

The new strange pentaquarks observed by LHCb are very likely hadronic molecules consisting of $\Xi_c \bar{D}$ and $\Xi_c \bar{D}^*$. We discuss the experimental evidence supporting this conclusion, pointing out the similarities and differences with the $P_c(4312)$, $P_c(4440)$ and $P_c(4457)$ pentaquarks in the nonstrange sector. The latter clearly are hadronic molecules consisting of $\Sigma_c \bar{D}$ and $\Sigma_c \bar{D}^*$. **Following this line of thought, we predict three additional strange pentaquarks consisting of $\Xi'_c \bar{D}$ and $\Xi'_c \bar{D}^*$. The masses of these states are expected to be shifted upward by $M(\Xi'_c) = M(\Xi_c) \approx 110$ MeV with respect to the corresponding known strange pentaquarks.**

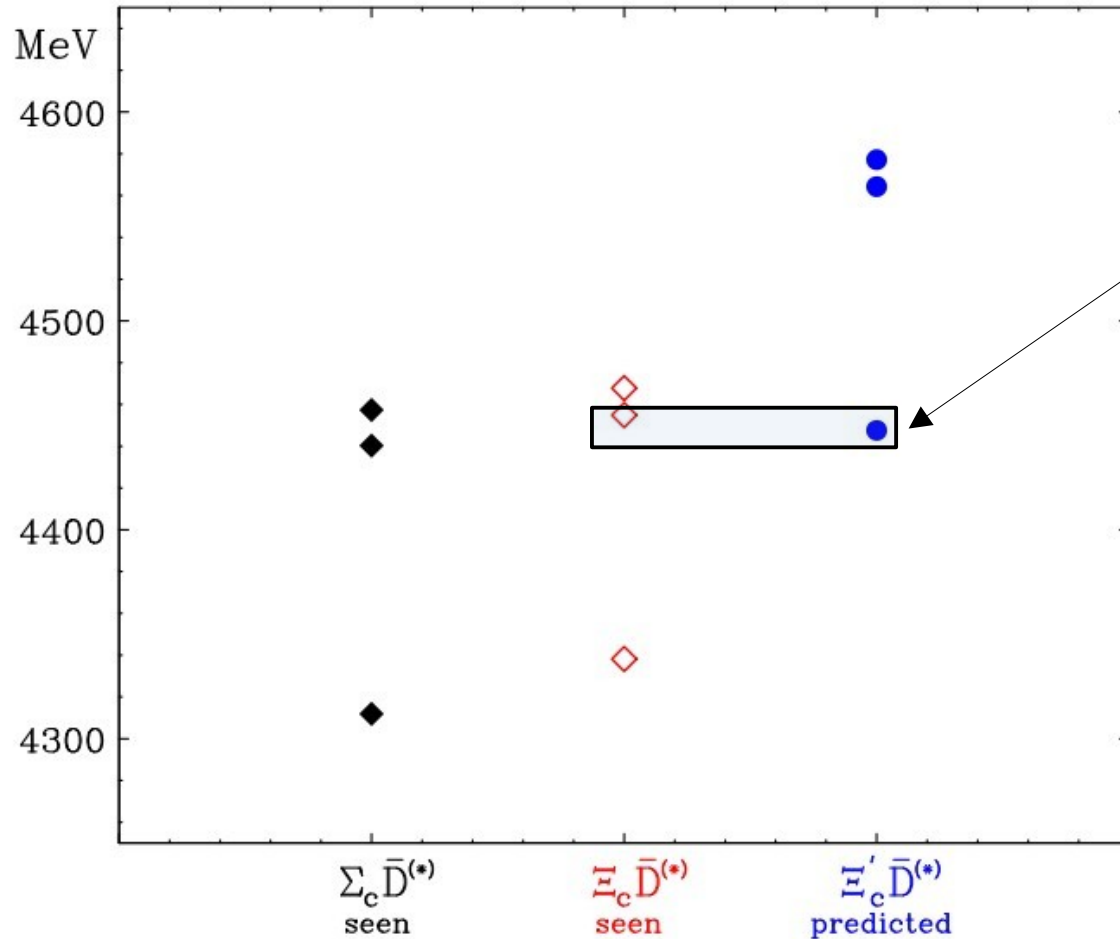
DOI: [10.1103/PhysRevD.106.036024](https://doi.org/10.1103/PhysRevD.106.036024)

Pentaquarks as hadronic molecules



Pentaquarks as hadronic molecules. $\Sigma_c \bar{D}^{(*)}$ states are denoted by black diamonds, $\Xi_c \bar{D}^{(*)}$ states by open red diamonds and $\Xi_c' \bar{D}^{(*)}$ states by blue circles.

Pentaquarks as hadronic molecules



only 7 MeV
difference;
 $\Xi_c' \bar{D}$ spin- $\frac{1}{2}$
if $P_{\psi_s}^\Lambda(4455)$
spin- $\frac{1}{2}$,
 \Rightarrow mixing

Pentaquarks as hadronic molecules. $\Sigma_c \bar{D}^{(*)}$ states are denoted by black diamonds, $\Xi_c \bar{D}^{(*)}$ states by open red diamonds and $\Xi_c' \bar{D}^{(*)}$ states by blue circles.

LHCb, 08/2020: PRL 125 (2020) 242001, PRD 102 (2020) 112003

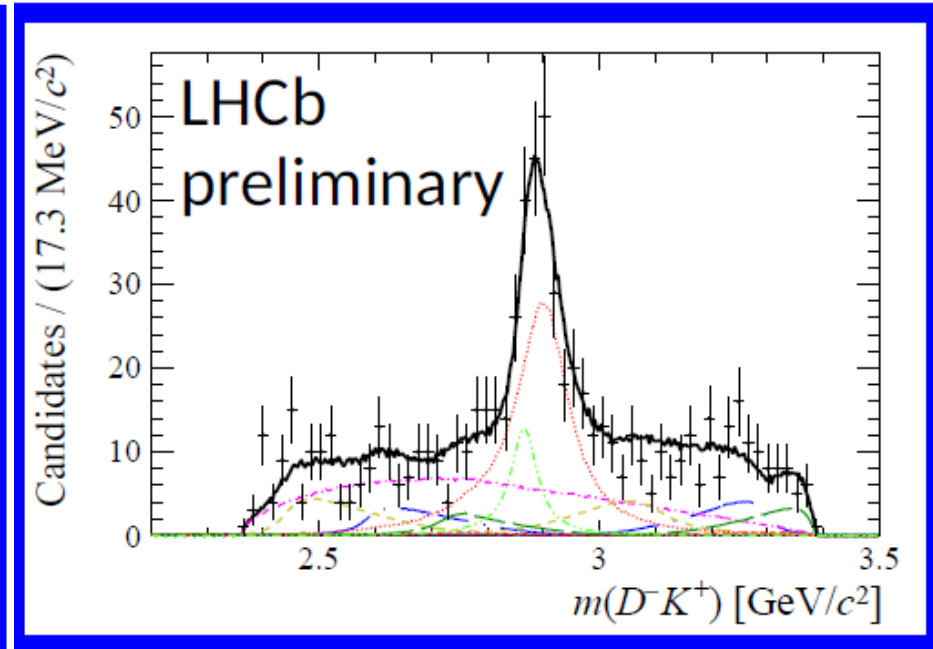
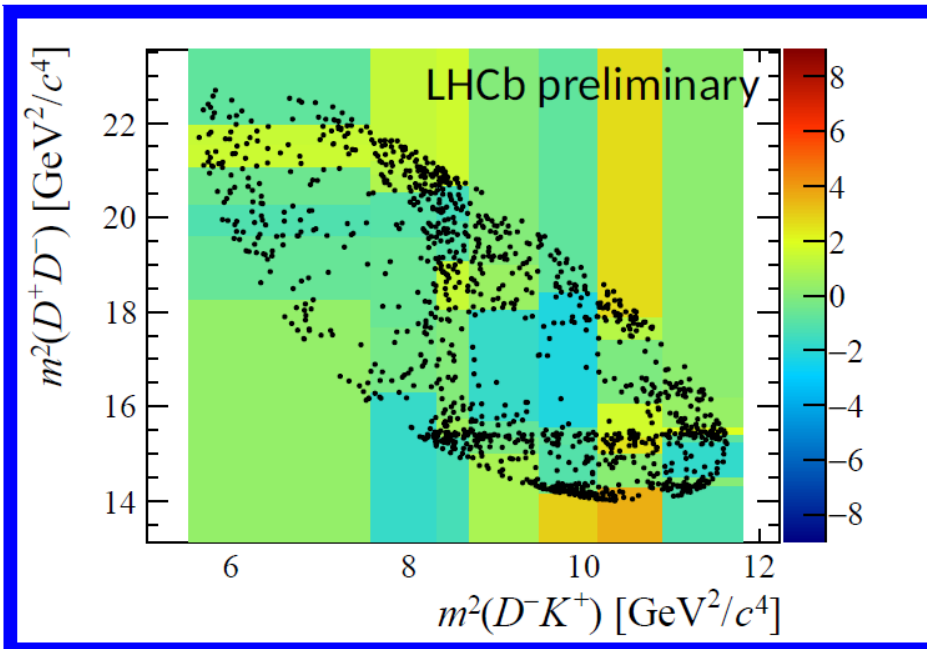
narrow $D^+ K^-$ resonance in $B^- \rightarrow D^- D^+ K^-$

first exotic hadron with open heavy flavor:

$cs\bar{u}\bar{d}$ tetraquark

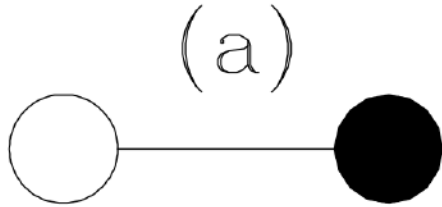
$cc\bar{u}\bar{d}$: found ϵ^- two meson threshold

\Rightarrow expect $cs\bar{u}\bar{d}$ well above $D^+ K^-$ threshold

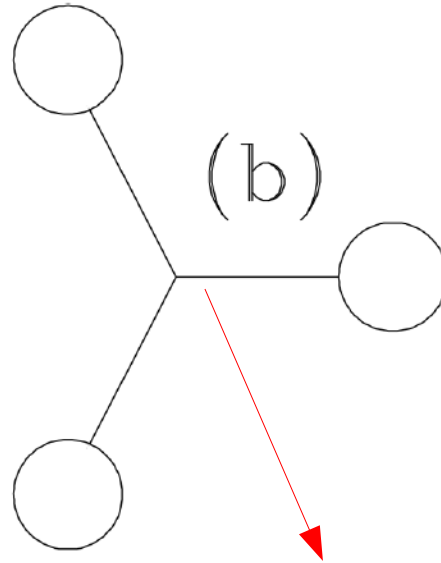


- two BW-s:
 $X_0(2900)$, $J^P = 0^+$ at 2866 ± 7 MeV, $\Gamma_0 = 57 \pm 13$ MeV
 $X_1(2900)$, $J^P = 1^-$ at 2904 ± 7 MeV $\Gamma_1 = 110 \pm 12$ MeV.
- our interpretation:
 $X_0(2900) = cs\bar{u}\bar{d}$ isosinglet compact tetraquark,
mass = 2863 ± 12 MeV, from quark model incl. 2 string junctions
- **the first exotic hadron with open heavy flavor**
- analogous $bs\bar{u}\bar{d}$ Tq predicted at 6213 ± 12 MeV
- $X_1(2900)$: ?
currently $J^P = 1^-$ preferred, but if $J^P = 2^+$,
possibly a D^*K^* molecule, c.f. threshold at 2902 MeV

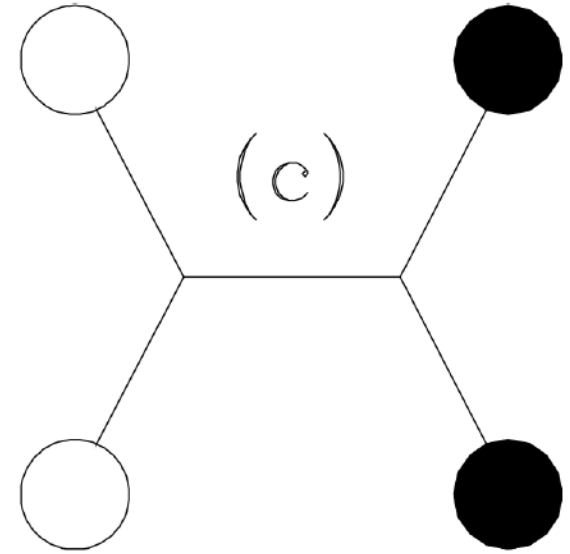
meson
no string junction



baryon
one string junction



tetraquark
two string junctions



string junction mass: $S = 165.1 \text{ MeV}$

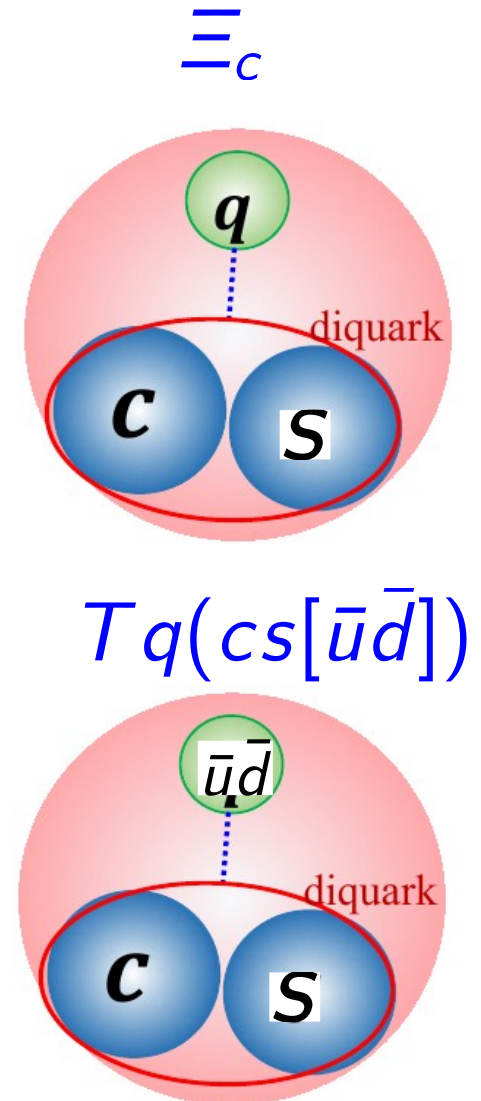
FIG. 1: QCD strings connecting quarks (open circles) and antiquarks (filled circles). (a) Quark-antiquark meson with one string and no junctions; (b) Three-quark baryon with three strings and one junction; (c) Baryonium (tetraquark) with five strings and two junctions.

$\Xi_c(csq)$ baryon vs. $cs[\bar{u}\bar{d}]$ tetraquark

- cs color antitriplet diquark in both
- $3_c^* [cs]$ $S = 0$ interacts with 3_c : q or $[\bar{u}\bar{d}]$
- $\bar{u}\bar{d}$: $S = 0, I = 0$ “good” diquark $[\bar{u}\bar{d}]$ much lighter than $S = 1, I = 1$ ($\bar{u}\bar{d}$), due to strong spin-dep. interaction between light quarks, c.f.

$$\Sigma_b(b(ud)) - \Lambda_b(b[ud]) \approx 194 \text{ MeV}$$

- $J^P = 0^+$
- all parameters from ordinary hadrons



$T(cs\bar{u}\bar{d})$ mass in the string-junction picture:

cs : spin-0 diquark $[cs] \Rightarrow \Delta E_{HF}(cs)$: attractive color HF

$B(cs)$: binding energy in 3_c^*

$$M[T(cs\bar{u}\bar{d})] = m_c + m_s + m_{[ud]} + 2S + B(cs) + \Delta E_{HF}(cs) ,$$

use $M(\Lambda_c) = m_c + m_{[ud]} + S = 2286.5$ MeV, and

values from fits to ordinary hadronic spectra:

$$m_s = 482.2 \text{ MeV}, \quad B(cs) = -35.0 \text{ MeV}, \quad \Delta E_{HF}(cs) = -35.4 \text{ MeV}$$

so

$$\begin{aligned} M[T(cs\bar{u}\bar{d})] &= \Lambda_c + m_s + S + B(cs) + \Delta E_{HF}(cs) = \\ &= 2863.4 \pm 12 \text{ MeV} \end{aligned}$$

LHCb, June 2020:

- a narrow resonance decaying into two J/ψ -s
- quark content $cc\bar{c}\bar{c}$, confirmed by CMS
- $M \approx 6.9$ GeV: $X(6900)$
- tetraquark-like
- ~ 700 MeV above $J/\psi J/\psi$ threshold
 \Rightarrow probably a $2S$ excited $cc\bar{c}\bar{c}$ state
- first exotic containing both QQ and $\bar{Q}\bar{Q}$
- \Rightarrow bottom analogue: $\Upsilon\Upsilon$ at $\gtrsim 19.4$ GeV ?
- stimulating challenge for EXP and TH

Interpretation of structure in di- J/ψ spectrum

- structure in LHCb di- J/ψ spectrum around 6.9 and 7.2 GeV
- interpreted in terms of $J^{PC} = 0^{++} (cc)-(\bar{c}\bar{c})$ Tq resonances
- Tq masses from recently confirmed string-junction picture
- main peak around 6.9 GeV likely dominated by the $0^{++}(2S)$, radial exc. of $(cc)-(\bar{c}\bar{c})$ Tq, predicted at 6.871 ± 0.025 GeV
- dip around 6.75 GeV: opening of S -wave di- χ_{c0} channel
- dip around 7.2 GeV: opening of di- $\eta_c(2S)$ & $\Xi_{cc}\bar{\Xi}_{cc}$ channels?
- low-mass structure appears to require broad resonance consistent with predicted $0^{++}(1S)$ at 6191.5 ± 25 MeV.
- Implications for $bb\bar{b}\bar{b}$ tetraquarks

recent venture into exotics with light quarks only

arXiv:2406.05920v1 [hep-ph] 9 Jun 2024

Possible mixing of a diquark-antidiquark with a $p\bar{p}$ hadronic molecule

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
ABSTRACT

We discuss the possibility that the two nearby resonances observed by BESIII partially below the $p\bar{p}$ threshold might be due to mixing between two metastable states with the same $J^{PC} = 0^{-+}$ quantum numbers, but rather different internal structure. One is a $p\bar{p}$ hadronic molecule and the other a bound state of a light-quark diquark and an antidiquark, both with spin 1 and isospin 0, a composite color antitriplet and triplet, respectively. The doubling of resonances, one of which may be interpreted as a hadronic molecule, while the other arises from $q\bar{q}$ annihilation in a state with vacuum quantum numbers may be a more general feature than the specific case considered here.

mixing of diquark-antidiquark with a $p\bar{p}$ H.M. ?

- BESIII: two close resonances in $J/\psi \rightarrow \gamma 3(\pi^+\pi^-)$
 - X(1840): $M = 1842.2 \pm 4.2_{-2.6}^{+7.1}$ MeV, $\Gamma = 83 \pm 14 \pm 11$ MeV, $J^{PC}=0^{-+}$
 - X(1880): $M = 1882.1 \pm 1.7 \pm 0.7$ MeV, $\Gamma = 30.7 \pm 5.5 \pm 2.4$ MeV, $J^{PC}=0^{-+}$
width includes ~ 10 MeV below $p\bar{p}$ threshold if $p\bar{p}$
- postulate: 2nd state a P -wave narrow diquark-antidiquark state, both $S = 1$
- $p\bar{p} \iff \{qq\}_{S=1} - \{\bar{q}\bar{q}\}_{S=1}$ via $q\bar{q}$ annihilation in 3P_0 flavor singlet
vacuum q. numbers
- $M(\{qq\}_{S=1} - \{\bar{q}\bar{q}\}_{S=1}) = 1886$ MeV, (quark model estimate)
- possible analogues:
 - $f_0(980)$: $K\bar{K}$ molecule and mixture of $(u\bar{u} + d\bar{d})/\sqrt{2}$ and $s\bar{s}$ in 3P_0
 - $D_{s0}(2317)$: $c\bar{s}$ in 3P_0 ; expect DK^+ molecule near 2359 MeV threshold
 - $\chi_{c1}(3872)$: $\bar{D}D^*$ with admixture of $c\bar{c}$ in 3P_1

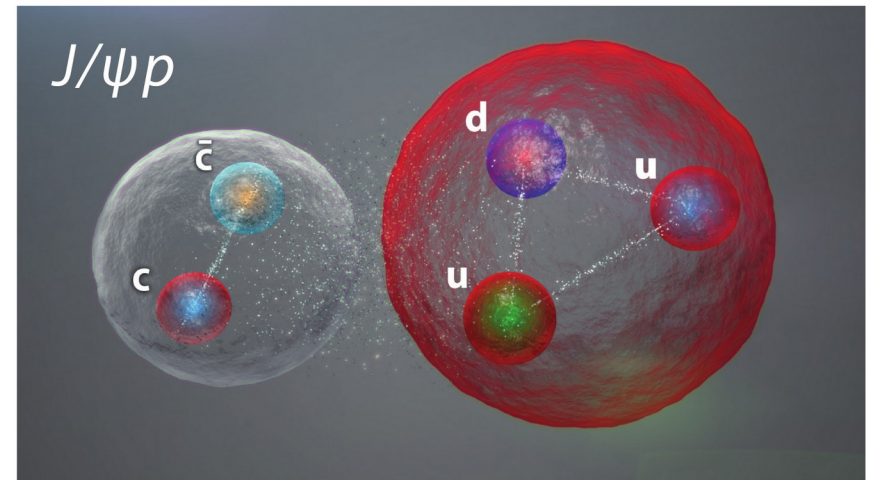
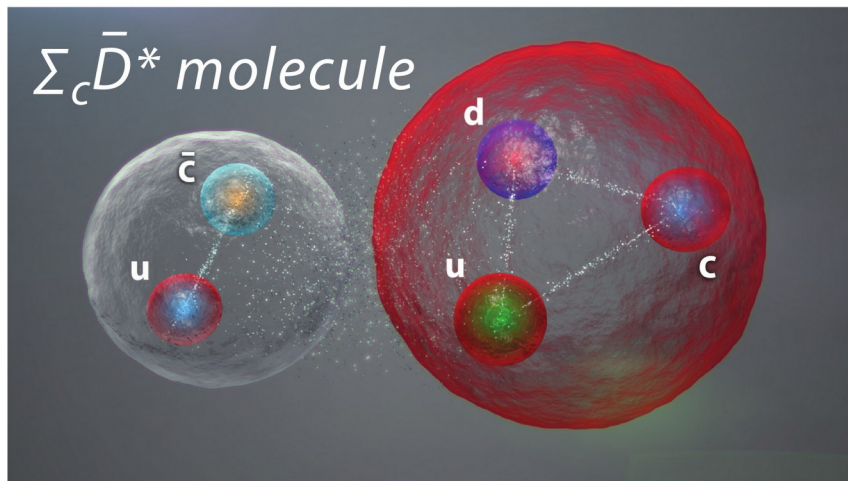
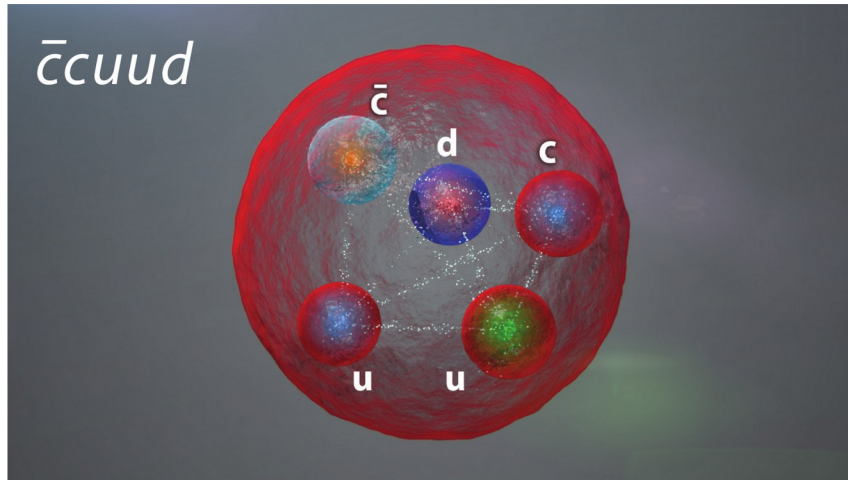
SUMMARY

- narrow $cc\bar{u}\bar{d}$ tetraquark discovered by LHCb
- doubly charmed baryon found exactly where predicted
 $\Xi_{cc}^{++}(ccu) \Rightarrow (bcq), (bbq)$
- stable $bb\bar{u}\bar{d}$ tetraquark: LHCb!
- narrow exotics with $Q\bar{Q}$: “heavy deuterons” / molecules
 $\bar{D}D^*, \bar{D}^*D^*, \bar{B}B^*, \bar{B}^*B^*,$
 $\Sigma_c \bar{D}^*(S = \frac{1}{2}, \frac{3}{2}), \Sigma_c \bar{D}(S = \frac{1}{2}); \quad \gamma p \rightarrow J/\psi p ?$
 $\Xi_c \bar{D}^{(*)}$ seen, expect 3 additional $\Xi_c' \bar{D}^{(*)}$ states
 $\Sigma_c B^*, \Sigma_b \bar{D}^*, \Sigma_b B^*, D^* B^*, \dots$
- $D^+ K^-$ res. $\Leftrightarrow cs\bar{u}\bar{d}$ Tq w. string junction  ; $bs\bar{u}\bar{d} = \bar{B}^0 K^- ?$
- $J/\psi J/\psi$ res. \Leftrightarrow excited $cc\bar{c}\bar{c}$ Tq, probably $2S$, $J/\psi \Upsilon, \Upsilon \Upsilon ?$
- light quark sector: possible mixture of $p\bar{p}$ and $\{qq\}_{S=1} - \{\bar{q}\bar{q}\}_{S=1}$, etc.

both kinds of exotic hadrons exist in Nature
exciting new spectroscopy awaiting discovery

Backup transparencies

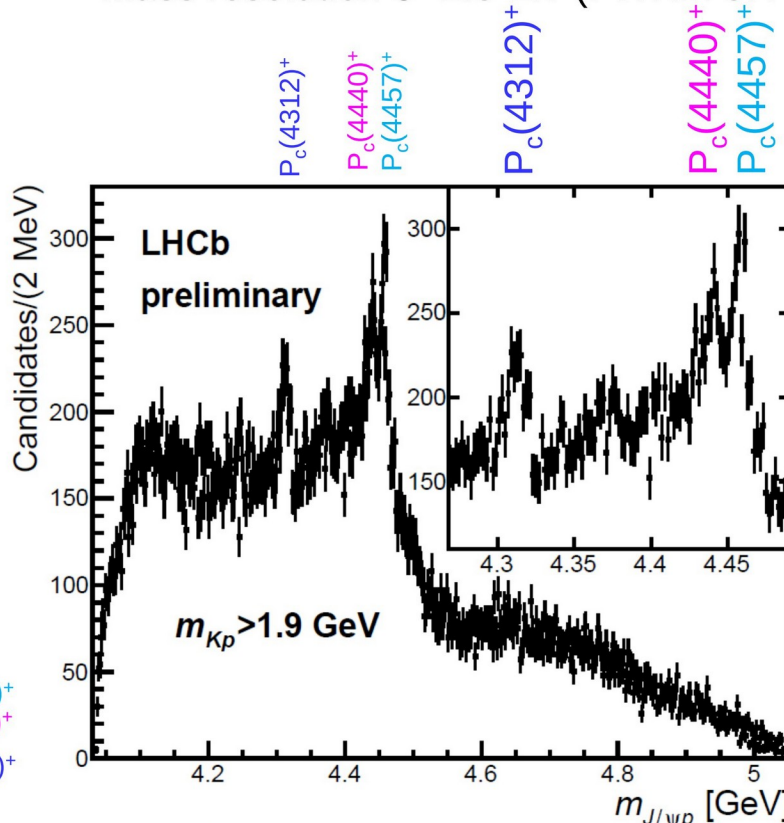
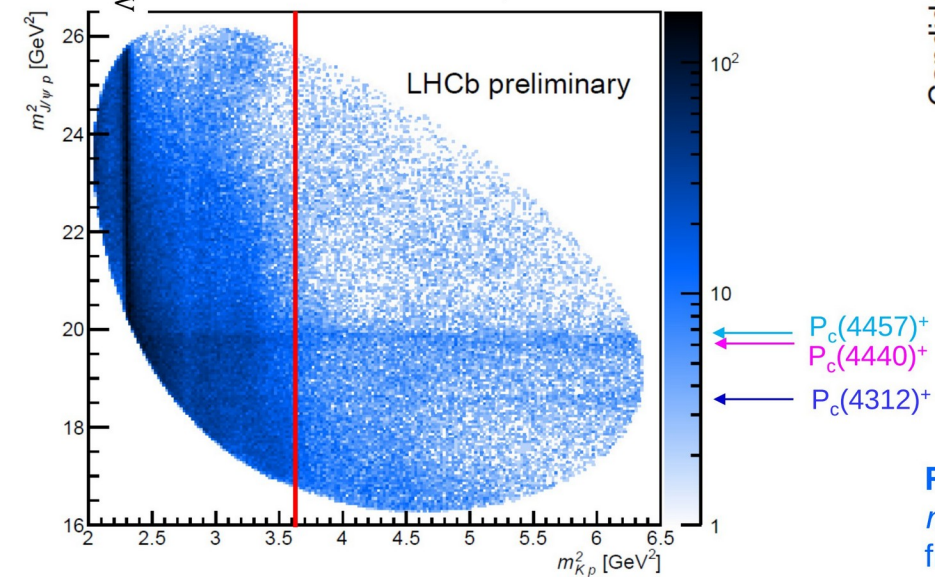
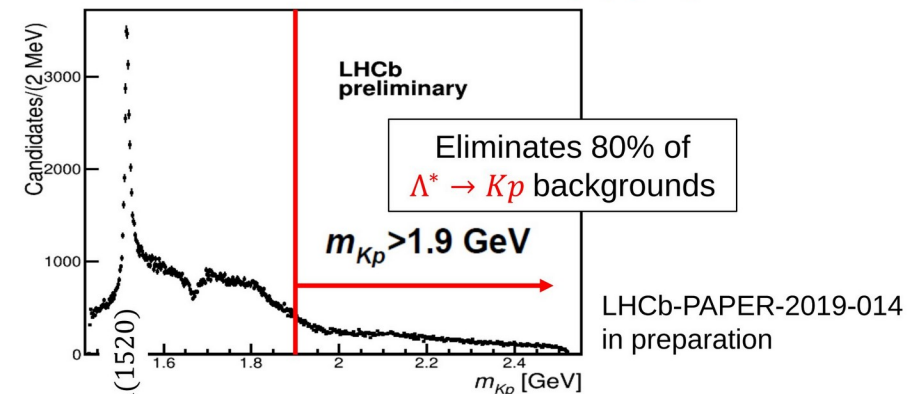
Decay of a tightly bound pentaquark vs. hadronic molecule to $J/\psi p$



$$|\langle \Sigma_c \bar{D}^* | J/\psi p \rangle| \ll |\langle \bar{c}cuud | J/\psi p \rangle|$$

Narrow $P_c^+ \rightarrow J/\psi p$ peaks with Λ^* suppression

Mass resolution $\sigma=2.3\text{-}2.7$ (FWHM 5.4-6.4) MeV



Proper amplitude analysis faces new challenges: must consider $m_{J/\psi p}$ resolution effects, large statistics and sub-percent precision in fit fractions required in the amplitude model – work in progress

State	M [MeV]	Γ [MeV]	(95% CL)	\mathcal{R} [%]
$P_c(4312)^+$	$4311.9 \pm 0.7^{+6.8}_{-0.6}$	$9.8 \pm 2.7^{+3.7}_{-4.5}$	(< 27)	$0.30 \pm 0.07^{+0.34}_{-0.09}$
$P_c(4440)^+$	$4440.3 \pm 1.3^{+4.1}_{-4.7}$	$20.6 \pm 4.9^{+8.7}_{-10.1}$	(< 49)	$1.11 \pm 0.33^{+0.22}_{-0.10}$
$P_c(4457)^+$	$4457.3 \pm 0.6^{+4.1}_{-1.7}$	$6.4 \pm 2.0^{+5.7}_{-1.9}$	(< 20)	$0.53 \pm 0.16^{+0.15}_{-0.13}$

$(c\bar{c}uds)$ molecular pentaquarks

a very clear peak $> 10 \sigma$:

$$P_{\psi_s}^\Lambda(4338) : \quad M = 4338.2 \pm 0.7 \text{ MeV}, \quad \Gamma = 7.0 \pm 1.2 \text{ MeV}$$

and a structure with two peaks split by 13 MeV, @ 3.1σ

$$P_{\psi_s}^\Lambda(4455) : \quad M = 4454.9 \pm 2.7 \text{ MeV}, \quad \Gamma = 7.5 \pm 9.7 \text{ MeV}$$

$$P_{\psi_s}^\Lambda(4468) : \quad M = 4467.8 \pm 3.7 \text{ MeV}, \quad \Gamma = 5.2 \pm 5.3 \text{ MeV}.$$

Several features of $P_{\psi_s}^\Lambda(4338)$ strongly suggestive of a $\Xi_c \bar{D}$ hadronic molecule:

(a) Vicinity to the relevant baryon-meson threshold(s):

$$M[P_{\psi_s}^\Lambda(4338)] \text{ only } 0.8 \text{ MeV above } \Xi_c^+ D^-$$

$$2.9 \text{ MeV above } \Xi_c^0 D^0$$

(b) Spin and parity:

$$\frac{1}{2}^+ \text{ baryon \& } 0^- \text{ meson}$$

$$S\text{-wave molecule} \Rightarrow \frac{1}{2}^-$$

(c) $\Gamma \lll$ phase space:

$$\Gamma[P_{\psi_s}^\Lambda(4338)] = 7.0 \pm 1.2 \text{ MeV}$$

$$\text{vs. } Q\text{-value} = 126 \text{ MeV.}$$

More support (with \ll stats) for molecular interpret.

from earlier LHCb $P_{\psi_s}^\Lambda(4459)$ pentaquark data

A peak in $M_{inv}(J/\psi \Lambda)$ in $\Xi_b^- \rightarrow J/\psi \Lambda K^-$,

$$M = 4458.8 \pm 2.9_{-1.1}^{+4.7} \text{ MeV}, \quad \Gamma = 17.3 \pm 6.5_{-5.7}^{+8.0} \text{ MeV}, \quad @3.1 \sigma.$$

M approx. 20 MeV below the $\Xi_c \bar{D}^*$ threshold.

Remarkably, LHCb has equally good fit w. *a two peak structure*,

with the two peaks split by 13 MeV:

$$P_{\psi_s}^\Lambda(4455) : \quad M = 4454.9 \pm 2.7 \text{ MeV}, \quad \Gamma = 7.5 \pm 9.7 \text{ MeV}$$

$$P_{\psi_s}^\Lambda(4468) : \quad M = 4467.8 \pm 3.7 \text{ MeV}, \quad \Gamma = 5.2 \pm 5.3 \text{ MeV}.$$

highly reminiscent of LHCb $P_\psi^N(4440)^+$ and $P_\psi^N(4457)^+$

caveat:

analogy between $\Sigma_c \bar{D}^{(*)}$ and $\Xi_c \bar{D}^{(*)}$ h.m. goes only so far, as $P_{\psi_s}^\Lambda(4455)$, $P_{\psi_s}^\Lambda(4468)$ not an $SU(3)_F$ rotation $q \rightarrow s$ ($q=u,d$) of $P_\psi^N(4440)^+$, $P_\psi^N(4457)^+$.

Nor $P_{\psi_s}^\Lambda(4338)$ an $SU(3)_F$ rotation of $P_\psi^N(4312)^+$, because P_ψ^N are $\Sigma_c \bar{D}^{(*)}$ h.m.

and under $SU(3)_F$ $q \rightarrow s$ ($q = u, d$) $\Sigma_c \rightarrow \Xi'_c$, $\Sigma_c \not\rightarrow \Xi_c$

$\Delta M \equiv M(\Xi'_c) - M(\Xi_c) \approx 110 \text{ MeV} < m_\pi$, so Ξ'_c stable under s.i.

\Rightarrow in addition to the already observed $\Xi_c \bar{D}^{(*)}$ three h.m.

expect three additional v. narrow $\Xi'_c \bar{D}^{()}$ h.m.*

shifted upwards by $\Delta M \approx 110 \text{ MeV}$ for each J^P

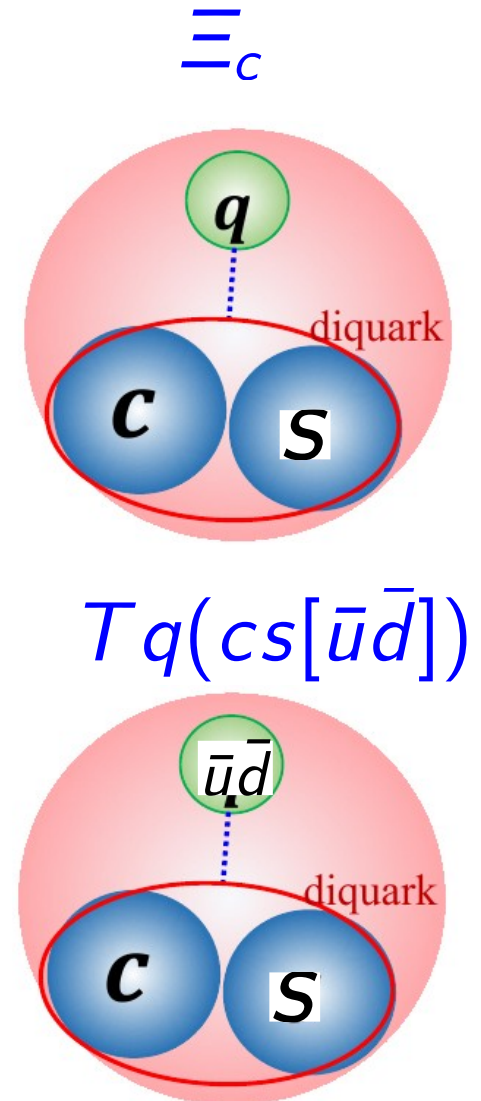
- two BW-s:
 $X_0(2900)$, $J^P = 0^+$ at 2866 ± 7 MeV, $\Gamma_0 = 57 \pm 13$ MeV
 $X_1(2900)$, $J^P = 1^-$ at 2904 ± 7 MeV $\Gamma_1 = 110 \pm 12$ MeV.
- our interpretation:
 $X_0(2900) = cs\bar{u}\bar{d}$ isosinglet compact tetraquark,
mass = 2863 ± 12 MeV, from quark model incl. 2 string junctions
- **the first exotic hadron with open heavy flavor**
- analogous $bs\bar{u}\bar{d}$ Tq predicted at 6213 ± 12 MeV
- $X_1(2900)$: ?
currently $J^P = 1^-$ preferred, but if $J^P = 2^+$,
possibly a D^*K^* molecule, c.f. threshold at 2902 MeV

$\Xi_c(csq)$ baryon vs. $cs[\bar{u}\bar{d}]$ tetraquark

- cs color antitriplet diquark in both
- $3_c^* [cs]$ $S = 0$ interacts with 3_c : q or $[\bar{u}\bar{d}]$
- $\bar{u}\bar{d}$: $S = 0, I = 0$ “good” diquark $[\bar{u}\bar{d}]$ much lighter than $S = 1, I = 1$ ($\bar{u}\bar{d}$), due to strong spin-dep. interaction between light quarks, c.f.

$$\Sigma_b(b(ud)) - \Lambda_b(b[ud]) \approx 194 \text{ MeV}$$

- $J^P = 0^+$
- all parameters from ordinary hadrons



tetraquark interpretation of peak near 6.9 GeV

- GS of $T(cc\bar{c}\bar{c})$ from string junction picture:
 $(cc)_{3_c^*}(\bar{c}\bar{c})_{3_c}$: two spin-1 diquarks coupled in S -wave to $0^{++}(1S)$, $M = 6191.5 \pm 25$ MeV
just below $2J/\psi$ at 6194 MeV and above $2\eta_c$ at 5968 MeV
- $2^{++}(1S)$ at 6429 ± 25 MeV
- $0^{++}(2S)$ at 6871 ± 25 MeV
- $2^{++}(2S)$ at 6967 ± 25 MeV
- peak around 7200 in the right place for $3S$ of $(cc)_{3_c^*}(\bar{c}\bar{c})_{3_c}$
- $\Xi_{cc}\bar{\Xi}_{cc}$ threshold at 7242 MeV: very natural – lightest state created when $(cc)_{3_c^*}(\bar{c}\bar{c})_{3_c}$ string breaks via $\bar{q}q$ production

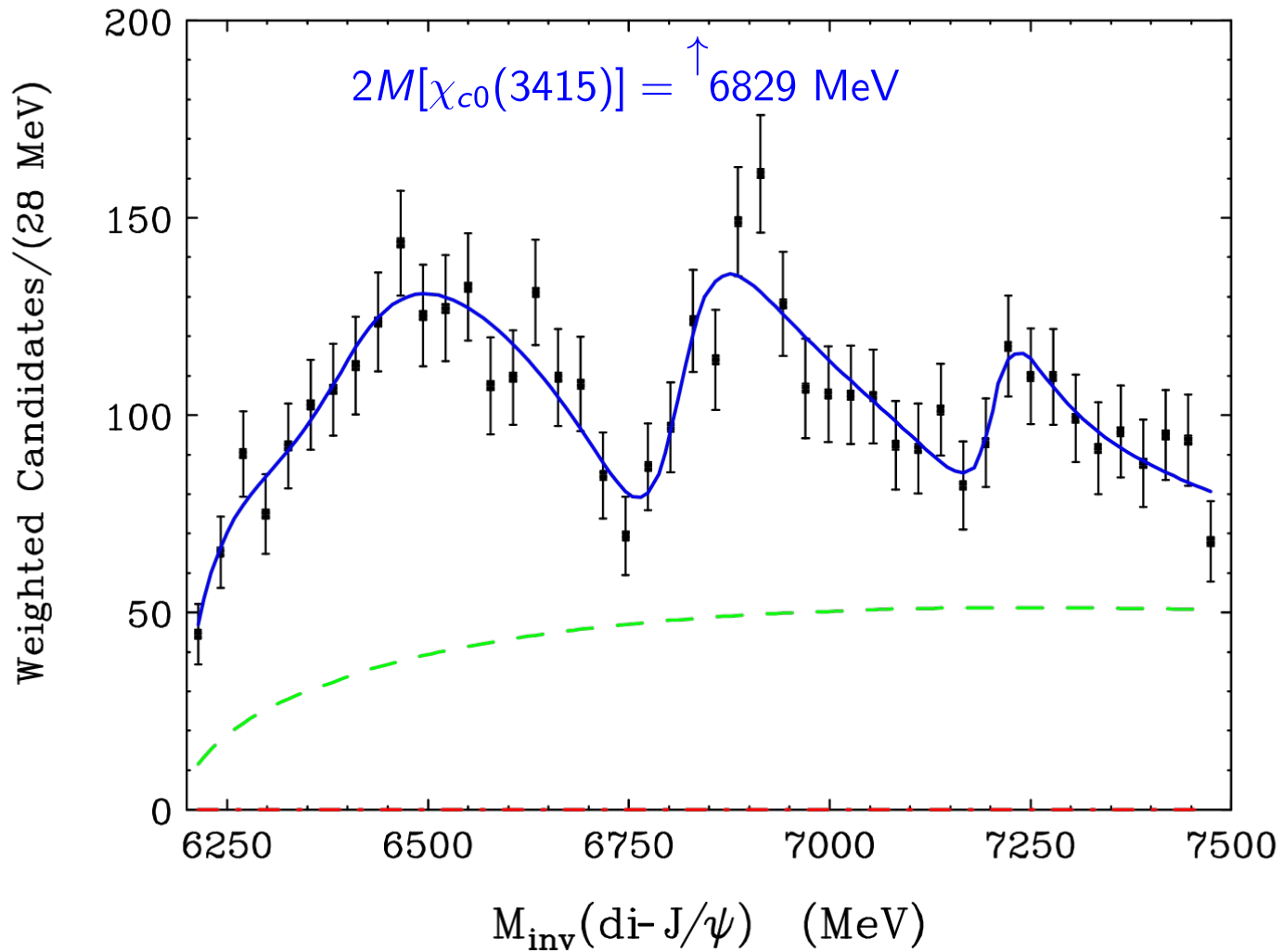


Figure 1: Spectrum of J/ψ pairs reported by the LHCb Experiment [3], together with our best fit to data (blue line), as given in Table I and described in the Appendix. The green dashed line denotes the DPS contribution, subtracted before fitting.

$$(cc)_{3_c^*} (\bar{c}\bar{c})_{3_c}$$

Table IV: Predicted masses of lowest-lying bound states of a color-antitriplet spin-1 cc diquark and a color-triplet spin-1 $\bar{c}\bar{c}$ antidiquark. The $\chi_{c0}\chi_{c0}$ threshold is 6829 MeV.

	$M(1S)$ (MeV)	$M(2S)$ (MeV)
$J^{PC} = 0^{++}$	6192	6871
$J^{PC} = 2^{++}$	6429	6967

$$(bb)_{3_h^*} (\bar{b}\bar{b})_{3_c}$$

Table V: Predicted masses of lowest-lying bound states of a color-antitriplet spin-1 bb diquark and a color-triplet spin-1 $\bar{b}\bar{b}$ antidiquark. The $\chi_{b0}\chi_{b0}$ threshold is 19719 MeV. ←

$\Upsilon(1S)\Upsilon(1S)$ threshold is 18920 MeV

$\Xi_{bb}\Xi_{bb}$ threshold is at 20324 MeV

	$M(1S)$ (MeV)	$M(2S)$ (MeV)
$J^{PC} = 0^{++}$	18826	19434
$J^{PC} = 2^{++}$	18956	19481

$cs\bar{u}\bar{d}$ & $cc\bar{c}\bar{c}$ summary

- narrow D^+K^- LHCb 0^+ resonance at 2866 ± 7 MeV:
likely compact isosinglet $cs\bar{u}\bar{d}$ tetraquark
mass predicted at 2863 ± 12 MeV
from quark model + 2 string junctions
- wider D^+K^- LHCb 1^- resonance at 2904 ± 7 MeV:
tantalizingly close to D^*K^* threshold at 2902 MeV
but inconsistent J^P ?
- structure in LHCb di- J/ψ spectrum around 6.9 and 7.2 GeV
interpreted in terms of $J^{PC} = 0^{++}$ $(cc)-(\bar{c}\bar{c})$ Tq resonances
+ opening of thresholds; dip around 6.75 GeV: S -wave di- χ_{c0}
- main peak around 6.9 GeV likely dominated by $0^{++}(2S)$,
radial exc. of $(cc)-(\bar{c}\bar{c})$ Tq, predicted at 6.871 ± 0.025 GeV