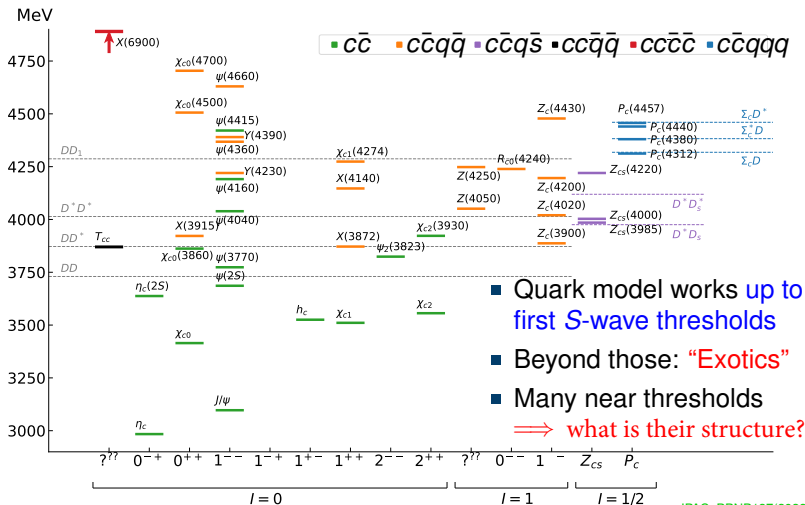


# THE LHCb PENTAQUARKS AS HADRONIC MOLECULES

June 25, 2024 | Christoph Hanhart | IAS Forschungszentrum Jülich



# SETTING THE STAGE



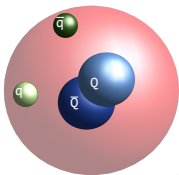
- Quark model works up to first S-wave thresholds
- Beyond those: “Exotics”
- Many near thresholds  $\implies$  what is their structure?

JPAC, PPNP127(2022)103981

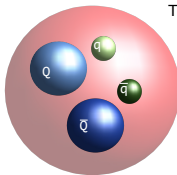


# THE NAME OF THE GAME:

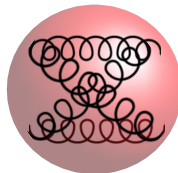
HADRO-  
QUARKONIUM



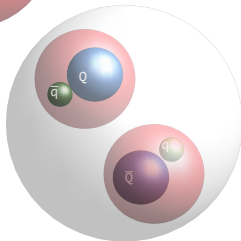
TETRAQUARK



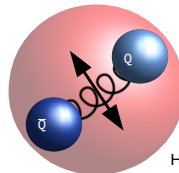
GLUEBALL



HADRONIC  
MOLECULE



HYBRID



Picture by Soeren Lange

How can one disentangle the different structures?



# HADRONIC MOLECULES

review article: Guo et al., Rev. Mod. Phys. 90(2018)015004

- are few-hadron states, **bound by the strong force**
- **do exist**: light nuclei.  
e.g. **deuteron as  $pn$  & hypertriton as  $\Lambda d$  bound state**
- are located typically **close to relevant continuum threshold**;  
e.g., for  $E_B = m_1 + m_2 - M$  ( $\gamma = \sqrt{2\mu E_B}$ ;  $\mu = m_1 m_2 / (m_1 + m_2)$ )
  - $E_B^{\text{deuteron}} = 2.22 \text{ MeV}$  ( $\gamma = 40 \text{ MeV}$ )
  - $E_B^{\text{hypertriton}} = (0.13 \pm 0.05) \text{ MeV}$  (to  $\Lambda d$ ) ( $\gamma = 26 \text{ MeV}$ )
- **can be identified in observables (Weinberg compositeness)**:

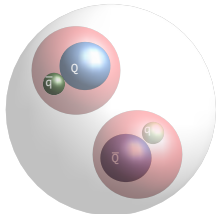
$$\frac{g_{\text{eff}}^2}{4\pi} = \frac{4M^2\gamma}{\mu}(1 - \lambda^2) \rightarrow a = -2 \left( \frac{1 - \lambda^2}{2 - \lambda^2} \right) \frac{1}{\gamma}; \quad r = - \left( \frac{\lambda^2}{1 - \lambda^2} \right) \frac{1}{\gamma}$$

$(1 - \lambda^2)$ =probability for molecular component in wave function

Corrections are  $\mathcal{O}(\gamma R)$

Range corrections: Song, Dai, Oset (2022); Li, Guo, Pang, Wu (2022); Kinugawa, Hyodo (2022)

Are there mesonic molecules?





# OUTLINE FOR THE REST OF THE TALK

Discussion on the imprint of molecular structures in observables

General: **Strong coupling to continuum channel as unique signature**

Using three examples:

- Example 1: Exploratory study for  $Y(4230)$

⇒ Do we need the  $Y(4330)$ ?

L. von Detten et al., PRD109(2024)116002

- Example 2: Heavy meson effective field theory for  $Z_b$  states

⇒ Towards a **systematic approach to doubly heavy molecules**

Q. Wang et al., PRD98(2018)074023

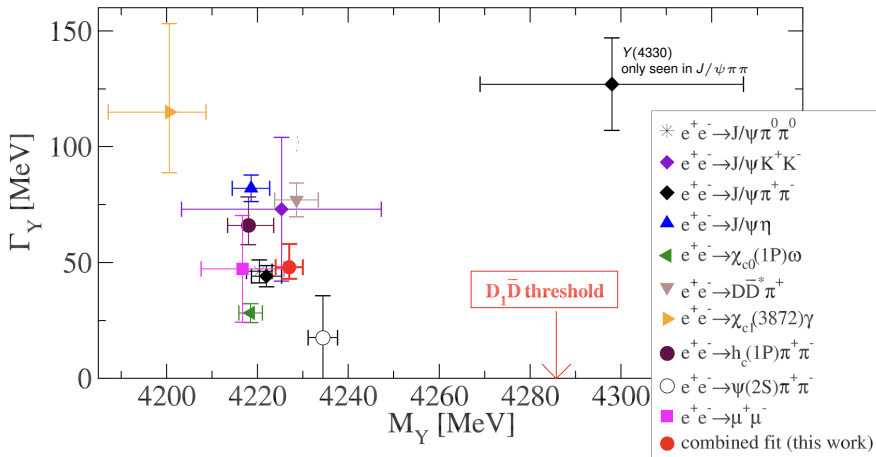
- Example 3: HMEFT for  $P_c$  pentaquarks

⇒ **Molecular signatures** in yet unmeasured cross sections

M. L. Du et al., PRL 124 (2020) 7, 072001; M. L. Du et al., JHEP 08 (2021) 157



# EXAMPLE 1: $Y(4230)$ AS $D_1\bar{D}$ MOLECULE

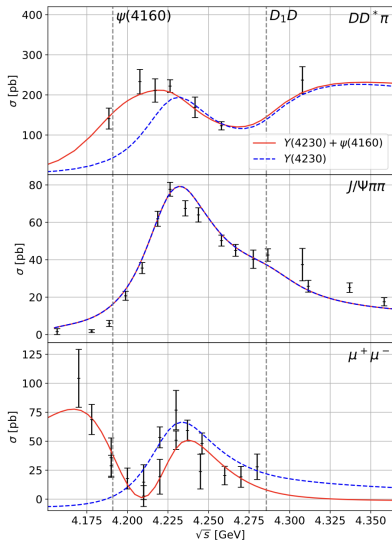


- Inclusion of  $D_1\bar{D}$  intermediate states ( $g_{YD_1D}$  large for molecule)
- Inclusion of charmonium  $\psi(4160)$  ( $M_{\psi(4160)} = 4191$  MeV)

L. von Detten, V. Baru, CH, Q. Wang, D. Winney, Q. Zhao; PRD109(2024)116002



# IMPACT OF $\psi(4160)$



Well established  $\bar{c}c$  state

Parameters from RPP2023:

2023 update of R. L. Workman *et al.* [PDG], PTEP2022 (2022)083C01

$$m_{\psi(4160)} = (4191 \pm 5) \text{ MeV}$$

$$\Gamma_{\psi(4160)} = (70 \pm 10) \text{ MeV}$$

Experimental extractions:

$$D^0 D^{*-} \pi^+ : \Gamma_{\gamma} = (77 \pm 6.3 \pm 6.8) \text{ MeV}$$

BESIII, PRL130(2023) 121901

$$J/\psi \pi^+ \pi^- : \Gamma_{\gamma} = (41.8 \pm 2.9 \pm 2.7) \text{ MeV}$$

BESIII, PRD106(2022)072001

in both cases  $\psi(4160)$  omitted

$$\mu^+ \mu^- : \Gamma_{\gamma} = (47.2 \pm 22.8 \pm 10.5) \text{ MeV}$$

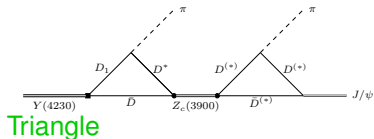
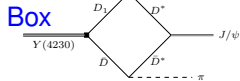
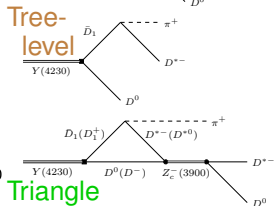
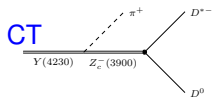
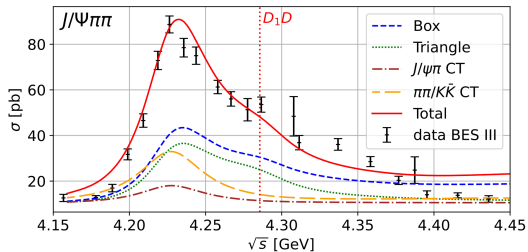
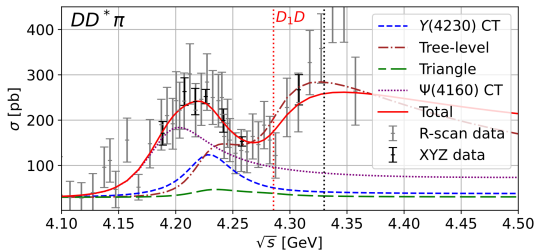
BESIII, PRD102(2020)112009

with  $\psi(4160)$  included





# ROLE OF $D_1\bar{D}$ CUT



# HOW TO GO BEYOND ...

- The formalism presented is 'diagnostic' — especially,
  - it does **not allow** for conclusions on the binding force
  - it allows one **only to study individual states**.

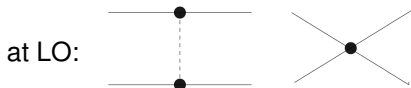
To go beyond that we **need to include more dynamics**

- **ChPT for heavy-heavy molecules**
  - **Most general potential consistent with symmetries**
  - Organised by **power counting & resummed**

S. Weinberg, PLB251(1990)288

Analogous to two nucleon system

Epelbaum et al., RMP81(2009)1773



$1-\pi$  exchange connects  
 $S$  to  $D$  waves

**Coupled channels needed!**

$1-\pi$  exchange only well defined together with contact terms!

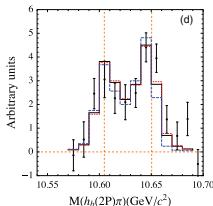
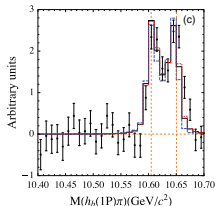
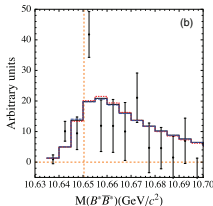
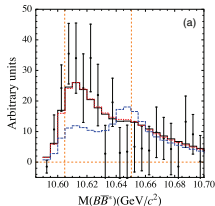
V. Baru et al., PRD91(2015)034002



# EXAMPLE 2: HMCHPT FOR $Z_b$ STATES

Results for  $Z_b$  spectra: 2 counter terms

Q. Wang et al., PRD98(2018)074023



Three different fits:

Black solid:

Constant contact terms only

Red dotted:

Constant contact terms

+  $1-\pi$ -exch. in  $S$ -wave

Blue dashed:

Constant contact terms

+ full  $1-\pi$ -exch.

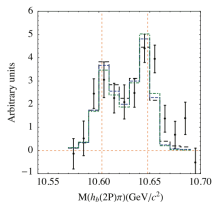
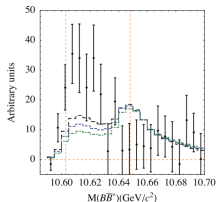
- The data call for a decoupling of  $B\bar{B}^*$  and  $B^*\bar{B}^*$  channels
- $1-\pi$ -exchange provides a strong transition between these



# WHAT'S WRONG?

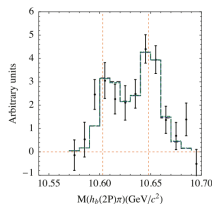
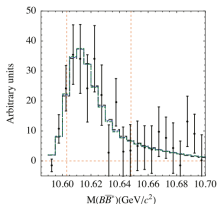
At  $B^* \bar{B}^*$ -threshold  $B^* \bar{B}$  momentum  $\sim 500$  MeV

$\implies$  No suppression of  $S(B^* \bar{B}^*) - D(B^* \bar{B})$  transition



- Strong  $B^* \bar{B}^* \rightarrow B^* \bar{B}$
- strong  $\Lambda$  dependence  
 black:  $\Lambda = 800$  MeV  
 blue:  $\Lambda = 1000$  MeV  
 green:  $\Lambda = 1200$  MeV

Promote  $S - D$  contact term to leading order:



- Fit improves significantly
- $\Lambda$  dependence gone
- $Z'_b \rightarrow B^* \bar{B}$  very small
- NLO  $S - S$  CT small

Why  $Z'_b \nrightarrow B^* \bar{B}$  not understood



# EXAMPLE 3: PENTAQUARKS

Predicted in phenomenological analysis

J. J. Wu, R. Molina, E. Oset and B. S. Zou, PRL 105(2010), 232001

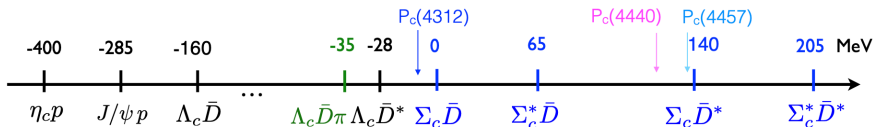
Various pion less EFT studies

Nieves, Oset, Geng, Valderrama, ....

We here apply formalism from above

M. L. Du et al., PRL 124 (2020) 7, 072001

Potentially relevant thresholds:



Systematic study of pertinent channels — Idea:

- Formation of states in  $\Sigma_c^{(*)} \bar{D}^{(*)}$  channels (elastic channels)
- Aim at fitting experimental data for  $\Lambda_b \rightarrow K p J/\psi$
- Predictions for  $\Lambda_b \rightarrow K \Sigma_c^{(*)} \bar{D}^{(*)}$  and  $\Lambda_b \rightarrow K \eta_c p$
- Is there room for  $\Lambda_b \rightarrow K \Lambda_c \bar{D}^{(*)}$ ?



# FORMALISM

$$V_{\text{LO}}^{\text{eff}} = \text{[Contact Term]} + \text{[OPE]} + \text{[Imaginary part]}$$

HQSS: 2 S-S wave LECs at  $O(Q^0)$   
 1 S-D wave LEC at  $O(Q^2)$

Long range: OPE

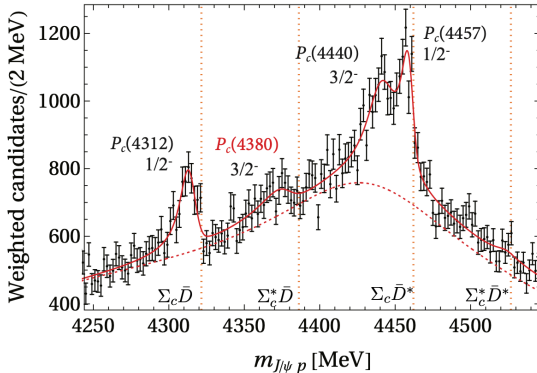
Imaginary part from inelastic channels

Total number of parameters **without/with** the  $\Lambda_c \bar{D}^{(*)}$  channels

- elastic channels:**  $\Sigma_c^{(*)}$  has  $j_{\text{light}} = 1$ ;  $D^{(*)}$  has  $j_{\text{light}} = 1/2$   
 $\implies$  **2 counter terms** with  $j_{\text{light}} = 1/2$  &  $j_{\text{light}} = 3/2$ , respectively
- $J/\psi p$  and  $\eta_c p$ : transitions in S and D wave  
 $\implies$  2 parameters for  $\Sigma_c^{(*)} \bar{D}^{(*)} \rightarrow p(J/\psi/\eta_c)$
- $\Lambda_c^{(*)}$  has  $j_{\text{light}} = 0$ ;  $D^{(*)}$  has  $j_{\text{light}} = 1/2$   
 $\implies$  **1** parameter for  $\Lambda_c \bar{D}^{(*)} \rightarrow \Sigma_c^{(*)} \bar{D}^{(*)}$
- 1 (2)** parameters for the promoted  $S - D$  counter terms  
 $\implies$  **5 parameters (7 parameters)** control the scattering,  
but the 2 first are most important
- .... and 7 parameters to control the production



# RESULTS



- Data described well ( $\chi^2/dof \approx 1$ )
- Without OPE **two good fits** (different order of the  $\Sigma \bar{D}^*$  states)
- With OPE **unique fit**
- Observe indications for **narrow  $P_c(4380)$**

⇒ Fit provides **1  $\Sigma_c \bar{D}$ , 1  $\Sigma_c^* \bar{D}$ , 2  $\Sigma_c \bar{D}^*$**  and **3  $\Sigma_c^* \bar{D}^*$**  molecules

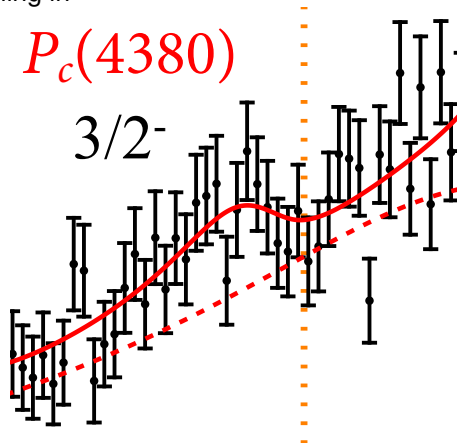
⇒ basically **2 parameters fixed by fitting 3 states**

⇒ Not all show up in the data (**importance of production vector?**)



# PENTAQUARKS

Zooming in



Fit with spin symmetry un-avoidably gives this additional state

Source coupling of  $\Sigma_c^* D$  channel different from 0 by  $1.7 \sigma$

Its confirmation would provide strong support for the molecular picture!

The amount of spin symmetry violation is specific to the structure

M. Cleven et al., PRD92(2015)014005

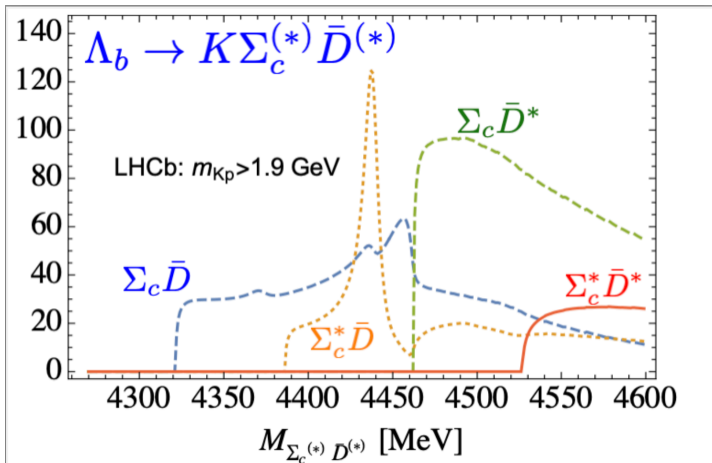




# SIGNATURES IN ELASTIC CHANNELS

Typical spectrum

Du et al., JHEP 08 (2021) 157



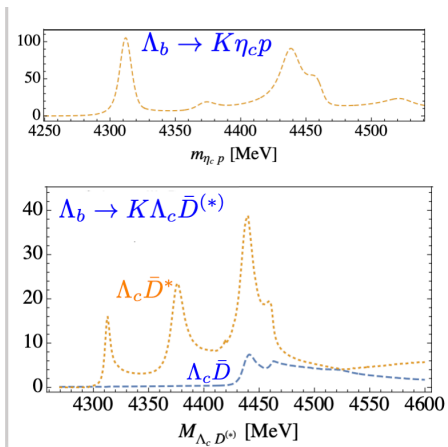
strong threshold enhancement - unavoidable for hadronic molecules



# SIGNATURES IN INELASTIC CHANNELS

Du et al., JHEP 08 (2021) 157

- For  $\Sigma_c^{(*)} \bar{D}^{(*)} \rightarrow \Lambda_c \bar{D}^{(*)}$  OPE + two add. para. (S-S and S-D)



- $\eta_c p$  channel similar to  $J/\psi p$  (spin symmetry!)
- $\Lambda_c \bar{D}^{(*)}$  final states **not constrained yet**
- Shown: **Some typical spectrum**
- Data even compatible with very weak signal
- $(\Lambda_c \bar{D} \rightarrow \Sigma_c \bar{D})_{S\text{-wave}} = 0$   
 $(\Lambda_c \bar{D} \rightarrow \Sigma_c^* \bar{D})_{DS\text{-wave}} = 0$



# SUMMARY AND PERSPECTIVES

- These are exciting times in (heavy meson) spectroscopy
- The recent and future data have the potential to allow us to identify the prominent components in XYZ states

## to-do for experiment

- **Continue** great performance! Especially needed:
  - data for **different quantum numbers** and
  - data for **line shapes**

## to-do for theory

- Provide more predictions for the **different scenarios**
- Go beyond most simple approaches  
e.g. study **interplay of regular quarkonia with exotics**
  - potentially significant mixing

Kalashnikova et al., PRD80(2009)074004; Takizawa et al., PTEP(2013)093D01; Ortega et al., JPG 40(2013)065107;  
Coito et al., EPJC73(2013)2351; Cincioglu et al., EPJC76(2016)576

- negligible mixing

van Beveren et al., PLB641(2006)265; Hammer et al., EPJA52(2016)330, C.H. et al., PRD106(2022)114003

Thanks a lot for your attention

