



Exotic multi-quark states and baryon spectroscopy workshop

25–27 Jun 2024

Universitätsclub Bonn, the University of
Bonn

η and η' photoproduction on nucleons

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for A2 and Mainz-Tuzla-Zagreb Collaborations



JOHANNES GUTENBERG
UNIVERSITÄT MAINZ

Outline

- **Motivation**
- **Experimental data sets**
- **EtaMAID**
- **Regge phenomenology for high energy region**
- **Selected results**
- **Summary**

Motivation

1. Baryon spectroscopy
2. Search for missing resonances
3. Search for exotic states
4. Reaction mechanism

Data sets



- $d\sigma/d\Omega$, A2MAMI-17: $E_\gamma=0.71-1.57$ GeV [PRL 118 (2017) 212001]
- $d\sigma/d\Omega$, CBELSA/TAPS-09: $E_\gamma=0.87-2.55$ GeV [PRC 80 (2009) 055202]
- $d\sigma/d\Omega$, CLAS-09: $E_\gamma=1.46-3.7$ GeV [PRC 80 (2009) 045213]
- T, F A2MAMI-14: $E_\gamma=0.71-1.4$ GeV [PRL 113 (2013) 102001]
- T CBELSA/TAPS-
- Σ , CLAS-17: $E_\gamma=1.07-1.84$ GeV [PLB 771 (2017) 213]
- Σ , GRAAL-07: $E_\gamma=0.71-1.5$ GeV [EPJA 33 (2007) 169]
- E, CLAS-16: $E_\gamma=0.71-2.15$ GeV [PLB 755 (2016) 64]

- $d\sigma/dt$, DESY-70 $E_\gamma=4, 6$ GeV [PLB 33 (1970) 236]
- $d\sigma/dt$, WLS-71 $E_\gamma=4, 8$ GeV [PLB 37 (1971) 326]
- $d\sigma/dt$, Σ , Daresbury-76 $E_\gamma=2.5, 3$ GeV [PLB 61 (1976) 479]
- $d\sigma/dt$, CEA-68 $E_\gamma=4$ GeV [PRL 21 (1968) 1205]
- T, Daresbury-80 $E_\gamma=4$ GeV [NP B185 (1981) 269]
- Σ , GlueX-17 $E_\gamma=8.7$ GeV [PRC 95 (2017) 042201R]

Data sets



- $d\sigma/d\Omega$, A2MAMI: $E_\gamma=1.45-1.57$ GeV [PRL 118 (2017) 212001]
- $d\sigma/d\Omega$, CBELSA/TAPS-09: $E_\gamma=1.53-2.48$ GeV [PRC 80 (2009) 055202]
- $d\sigma/d\Omega$, CLAS-09: $E_\gamma=1.51-3.43$ GeV [PRC 80 (2009) 045213]
- Σ , CLAS-17: $E_\gamma=1.46-1.84$ GeV [PLB 771 (2017) 213]
- Σ , GRAAL-15: $E_\gamma=1.46-1.48$ GeV [EPJA 51 (2015) 77]



- $d\sigma/d\Omega$, A2MAMI-14: $E_\gamma=0.72-1.40$ GeV [RRC 90 (2014) 015205]
- $d\sigma/d\Omega$, CBELSA/TAPS-11: $E_\gamma=0.74-2.06$ GeV [EPJA 47 (2011) 89]
- $d\sigma/d\Omega_{1/2,3/2}$ A2MAMI-17: $E_\gamma=0.72-1.40$ GeV [RRC 95 (2017) 055201]
- Σ , GRAAL-08: $E_\gamma=0.74-1.44$ GeV [PRC 78 (2008) 015203]
- E , A2MAMI-17: $E_\gamma=0.72-1.40$ GeV [RRC 95 (2017) 055201]



- $d\sigma/d\Omega$, CBELSA/TAPS-11: $E_\gamma=1.53-2.45$ GeV [EPJA 47 (2011) 11]

<https://maid.kph.uni-mainz.de>

MAID

Photo- and Electroproduction of Pions, Eta, Etaprime and Kaons on the Nucleon

Institut für Kernphysik, Universität Mainz

Mainz, Germany

MAID2007	unitary isobar model for $(e,e'\pi)$
DMT2001	dynamical model for $(e,e'\pi)$
KAON-MAID	isobar model for $(e,e'K)$
ETA-MAID	EtaMAID2000 isobar model for $(e,e'\eta)$ EtaMAID2018 isobar model for (γ,η) and (γ,η') ^{NEW}
Chiral MAID	chiral perturbation theory approach for $(e,e'\pi)$
2-PION-MAID	isobar model for $(\gamma,\pi\pi)$
archive	MAID2000 DMT2001original EtaMAID2003 ETAprime2003



[update info](#) **NEW**

An Isobar Model for Eta and Etaprime Photoproduction on the Nucleon

Victor Kashevarov and Lothar Tiator

Reference:

[L. Tiator, M. Gorchtein, V.L. Kashevarov, K. Nikonov, M. Ostrick \(Mainz\),
M. Hadzimehmedovic, R. Omerovic, H. Osmanovic, J. Stahov \(Tuzla\),
and A. Svarc \(Zagreb\), arXiv:1807.04525,
Eur. Phys. J. A \(2018\) 54: 210](#)

-
- [Electromagnetic Multipoles \(\$E_{l\pm}\$, \$M_{l\pm}\$ \)](#)
 - [CGLN and Helicity Amplitudes \(\$F_1, \dots, F_4\$, \$H_1, \dots, H_4\$ \)](#)
 - [Observables \(with beam, target and recoil polarization\)](#)
 - [Total Cross Sections](#)

Now MAID is part of research program of

MTZ Collaboration

Mainz: M. Gorchteyn, V. L. Kashevarov, M. Ostrick, L. Tiator
Tuzla: M. Hadžimehmedović, R. Omerović, H. Osmanović, J. Stahov
Zagreb: Alfred Švarc

Publication of MTZ Collaboration for MAID project:

Eta and Etaprime Photoproduction on the Nucleon with the Isobar Model EtaMAID2018.
Eur.Phys.J.A 54 (2018) 12, 210

Single-energy partial-wave analysis for π^0 n photoproduction with fixed-t analyticity.
Phys.Rev.C 104 (2021) 3, 034605

Single-energy partial wave analysis for π^0 photoproduction on the proton with fixed-t analyticity imposed.
Phys.Rev.C 100 (2019) 5, 055203

Role of angle-dependent phase rotations of reaction amplitudes in η photoproduction on protons
Phys.Rev.C 98 (2018) 4, 045206

Fixed-t analyticity as a constraint in single-energy partial-wave analyses of meson
Photoproduction reactions
Phys.Rev.C 97 (2018) 1, 015207

Other PWA groups analyzing (γ, η) and (γ, η') data

BnGa: Bonn-Gatchina group:

A.V. Anisovich, E. Klempt, V.A. Nikonov, A.V. Sarantsev, and U. Thoma.

Multi-channel K-matrix model and N/D dispersion approach.

Predictions up to $W=2500$ MeV for 3 channels:

$p(\gamma, \eta) p$, $n(\gamma, \eta) n$, and $p(\gamma, \eta') p$

JüBo: Jülich-Bonn group:

D. Rönchen, M. Döring, H. Haberzettl, J. Haidenbauer, U.-G. Meißner, and K. Nakayama.

Covariant multi-channel dynamical model.

Predictions up to $W=2380$ MeV for 1 channel: $p(\gamma, \eta) p$

KSU: Kent State University group:

B.C. Hunt and D.M. Manley.

Multi-channel K-matrix model.

Predictions for 2 channels: $p(\gamma, \eta) p$ up to $W=1990$ MeV,

$n(\gamma, \eta) n$ up to $W=1870$ MeV

Details of model

All the most well-known models (MAID, SAID, BnGa, JüBo etc.) are applicable for data analysis and predictions only in the resonance energy region ($W < 2.5$ GeV).

There are several models for higher energies (JPAC and various Regge models). However, all of them are applicable for energies ($W > 2.5$ GeV), for scattering angles only to forward or backward, and for specific reaction channels.

The last version of EtaMAID2018 allows data analysis for energies up to $W = 6$ GeV, at any scattering angles, and for 4 reaction channels:

1. $\gamma p \rightarrow \eta p$
2. $\gamma n \rightarrow \eta n$
3. $\gamma p \rightarrow \eta' p$
4. $\gamma n \rightarrow \eta' n$

Details of model

1. EtaMAID 2018 is an isobar model.
2. 22 nucleon resonances, parameterized with Breit-Wigner shapes.
3. The model includes Born terms in s and u channels.
Contribution is small because of coupling constant < 0.1 .
It is very important for pion photoproduction with coupling constant ~ 14 .
4. Meson exchange in t channel with damping factors (DF).
Dominates at high energy ($W > 2.5$ GeV)
5. Fit parameters:
 - Background: only DF parameters.
 - Resonances: mass M , total width Γ , branching ratios $\beta(\eta N)$ and $\beta(\eta' N)$,
photon helicity amplitudes $pA_{1/2}$, $nA_{1/2}$,
damping parameters for ηN ($\eta' N$) and gN vertices: X and Xg

Details of model: resonances

Breit-Wigner ansatz for s-channel resonance excitations:

$$\mathcal{M}_{\ell\pm}(W) = \bar{\mathcal{M}}_{\ell\pm} f_{\gamma N}(W) \frac{M_R \Gamma_{\text{tot}}(W)}{M_R^2 - W^2 - i M_R \Gamma_{\text{tot}}(W)} f_{\pi N}(W) C_{\pi N}$$

$$f_{\pi N}(W) = \zeta_{\pi N} \left[\frac{1}{(2J+1)\pi} \frac{k}{q} \frac{M_N}{W} \frac{\Gamma_{\pi N}(W)}{\Gamma_{\text{tot}}(W)^2} \right]^{1/2}$$

$$f_{\gamma N}(W) = \left(\frac{k}{k_R} \right)^2 \left(\frac{X^2 + k_R^2}{X^2 + k^2} \right)^2$$

isospin factor:

$$C_{\eta N} = C_{\eta' N} = -1$$

$$C_{\pi N} = \begin{cases} -1/\sqrt{3} & : I = 1/2 \\ \sqrt{3}/2 & : I = 3/2 \end{cases}$$

relative phase of individual resonance:

$$\zeta_{\pi N} = 1, \zeta_{\eta N} = \pm 1, \zeta_{\eta' N} = \pm 1$$

Details of model: list of resonances

Resonances included in the fit

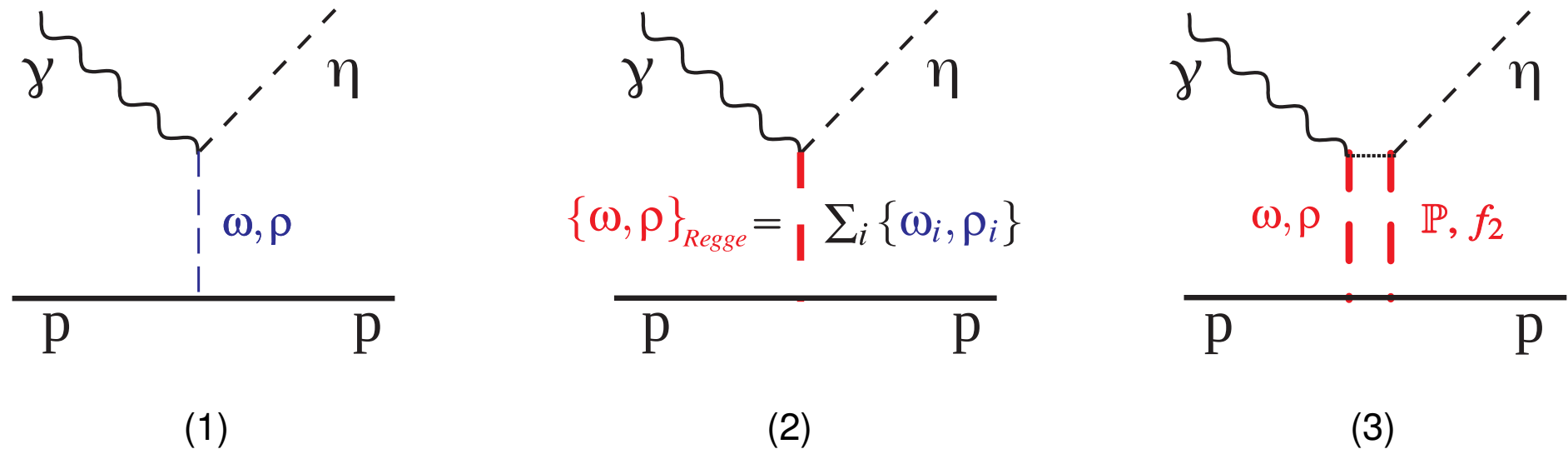
1. $P_{11}(1440)$ ***** MAID 2007
2. $D_{13}(1520)$ ***** MAID 2007
3. $S_{11}(1535)$ ***** MAID 2007
4. $S_{11}(1650)$ ***** MAID 2007
5. $D_{15}(1675)$ ***** MAID 2007
6. $F_{15}(1680)$ ***** MAID 2007
7. $D_{13}(1700)$ ***
8. $P_{11}(1710)$ *****
9. $P_{13}(1720)$ ***** MAID 2007
10. $F_{15}(1860)$ **
11. $D_{13}(1875)$ ****
12. $P_{11}(1880)$ **
13. $S_{11}(1895)$ *****
14. $P_{13}(1900)$ ***
15. $F_{17}(1990)$ **
16. $F_{15}(2000)$ **
17. $D_{15}(2060)$ **
18. $P_{11}(2100)$ **
19. $D_{13}(2120)$ **
20. $G_{17}(2190)$ *****
21. $G_{19}(2250)$ *****
22. $H_{19}(2220)$ *****

Resonances not included in the fit (PDG overall rating: two stars and more)

1. $D_{15}(2570)$ **
2. $H_{111}(2600)$ ***
3. $I_{113}(2700)$ **

Details of model: background

t -channel contribution to η photoproduction from single poles (1),
Regge amplitudes (2), and Regge cuts (3).



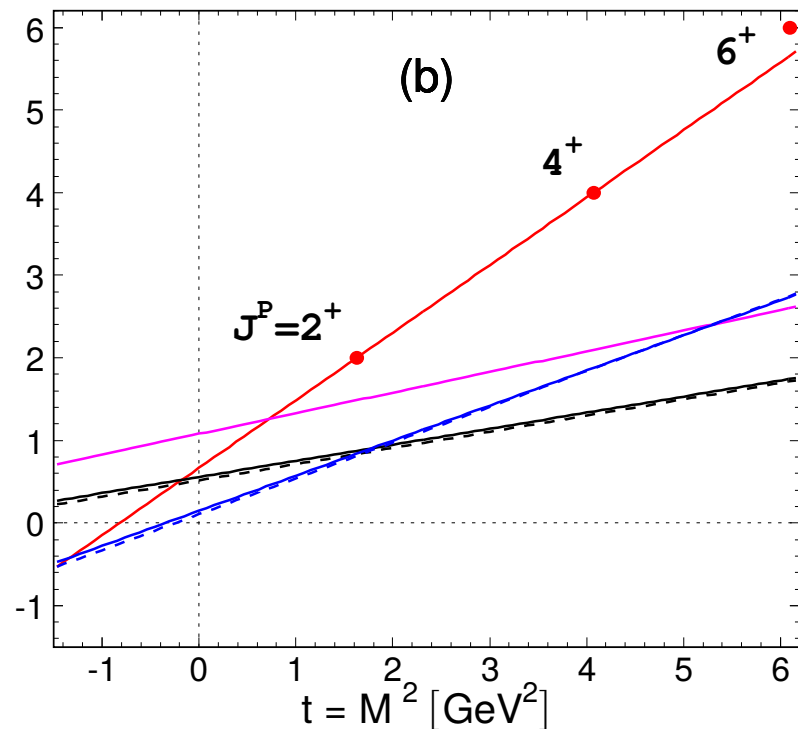
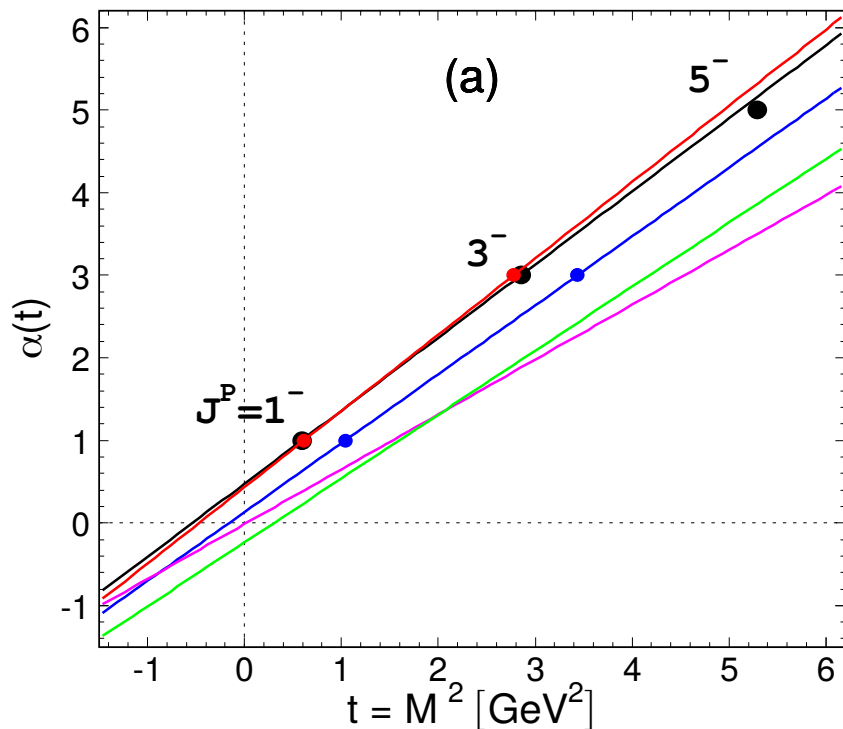
V. L. Kashevarov, M. Ostrick, L. Tiator, Phys. Rev. C **96** (2017) 045207

Regge phenomenology

Chew-Frautchi plots with Regge trajectories

(a) ρ (black), ω (red), φ (blue), b_1, h_1 (green), ρ_2, ω_2 (magenta)

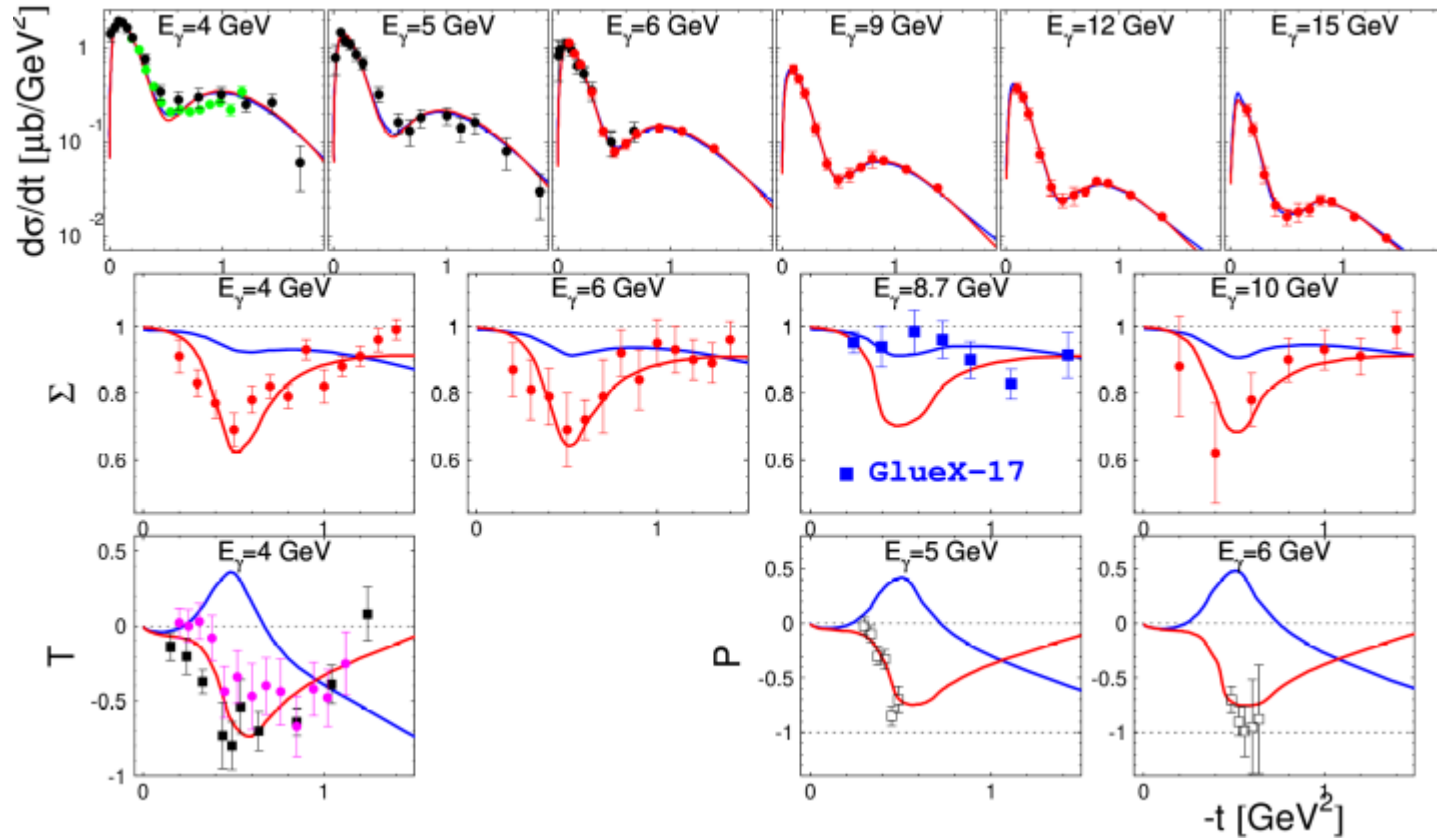
(b) P (magenta), f_2 (red), $\rho P, \omega P$ (black solid and dashed) and $\rho f_2, \omega f_2$ (blue solid and dashed)



Prediction for ρ_2 and ω_2 from relativized quark model: S. Godfrey, N. Isgur, PRD 32 (1985) 189.

Results for high energies

V. L. Kashevarov, M. Ostrick, L. Tiator , Phys. Rev. C **96** (2017) 045207



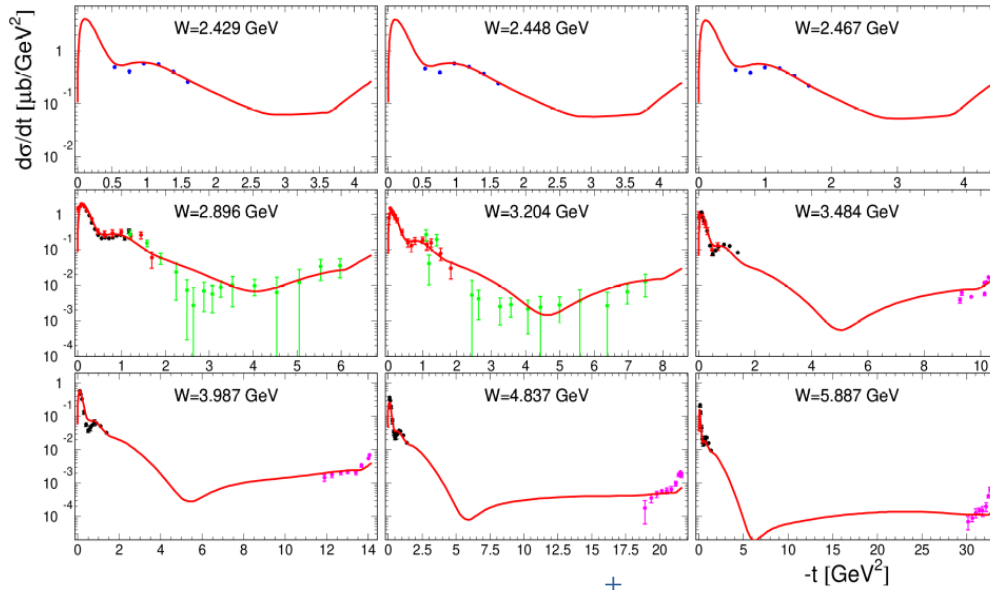
Red lines: our fit result to all data

Blue lines: fit to $d\sigma/dt$ and GlueX-17 data.

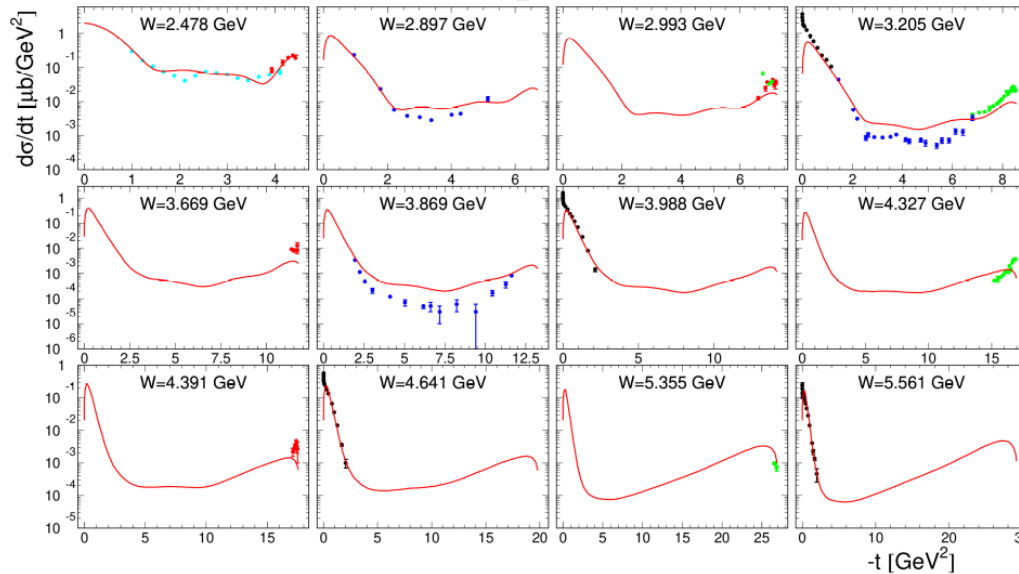
DATA: $d\sigma/dt$ and Σ : SLAC-71 (red), DESY-68 (black discs), DESY-73 (Nucl.Phys. B51) (green)
 T : Daresbury-72 (magenta), DESY-73 (PL B46) (black full squares),
 P : CEA-73 (black open squares).

Details of model: background

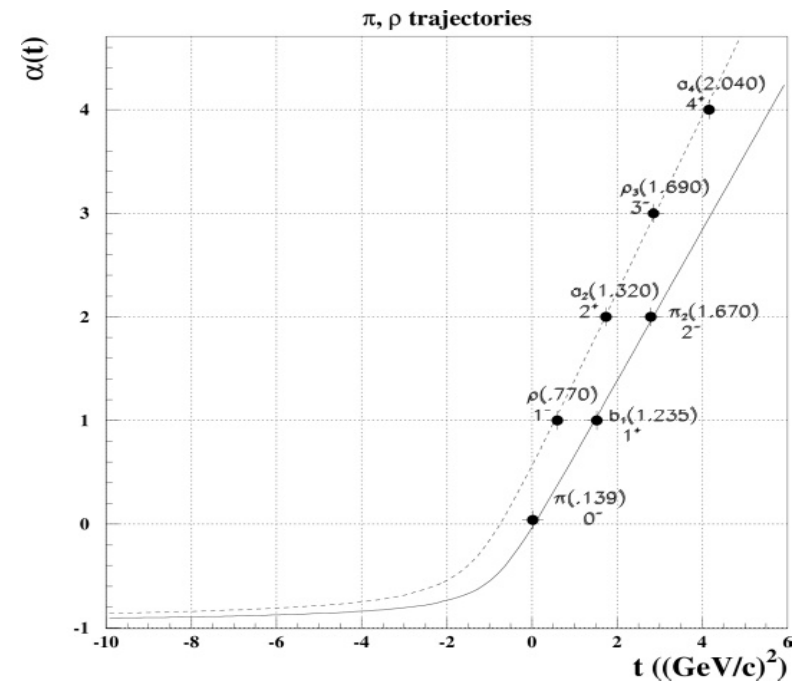
$$\gamma p \rightarrow \pi^0 p$$



$$\gamma p \rightarrow \pi^+ n$$



Saturation of Regge trajectories.
Example for ρ and π reggeons.

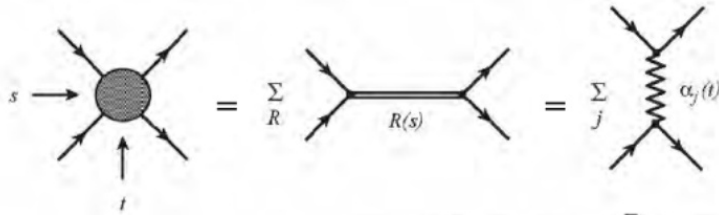


Details of model: duality

from **quark-hadron duality** it is known:

sum over all s-channel resonances is equivalent to sum over all t-channel resonances

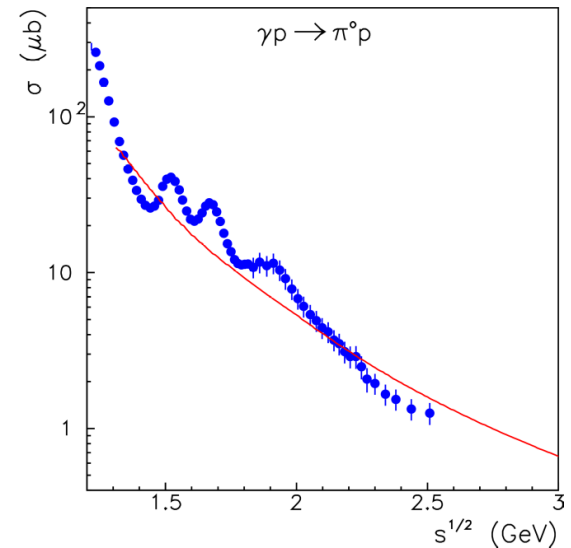
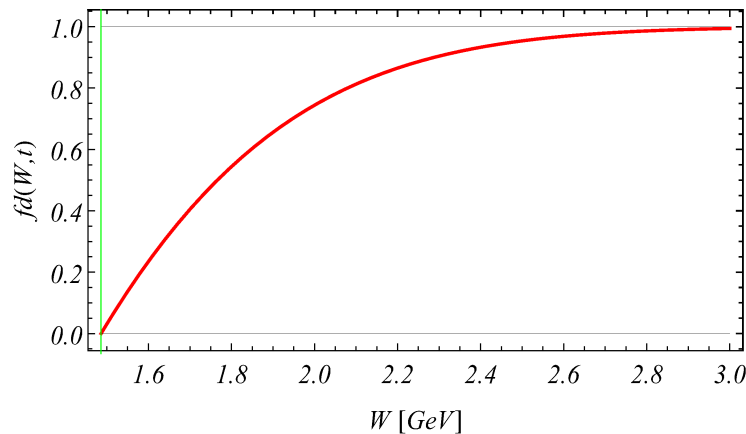
therefore: keeping both leads to double counting



$$M = \sum_{i=1}^{\infty} M_s^{Res_i} = \sum_{i=1}^{\infty} M_t^{Res_i} = \sum_{i=1}^N M_s^{Res_i} + \left[\sum_{i=1}^{\infty} M_t^{Res_i} - \sum_{i=1}^N M_s^{Res_i} \right]$$

$$\approx \sum_{i=1}^N M_s^{Res_i} + M^{Regge} \cdot F_d(W) \quad \text{: our approach}$$

$$f_d(W) = 1 - e^{-\frac{W-W_{thr}}{\Lambda}}$$

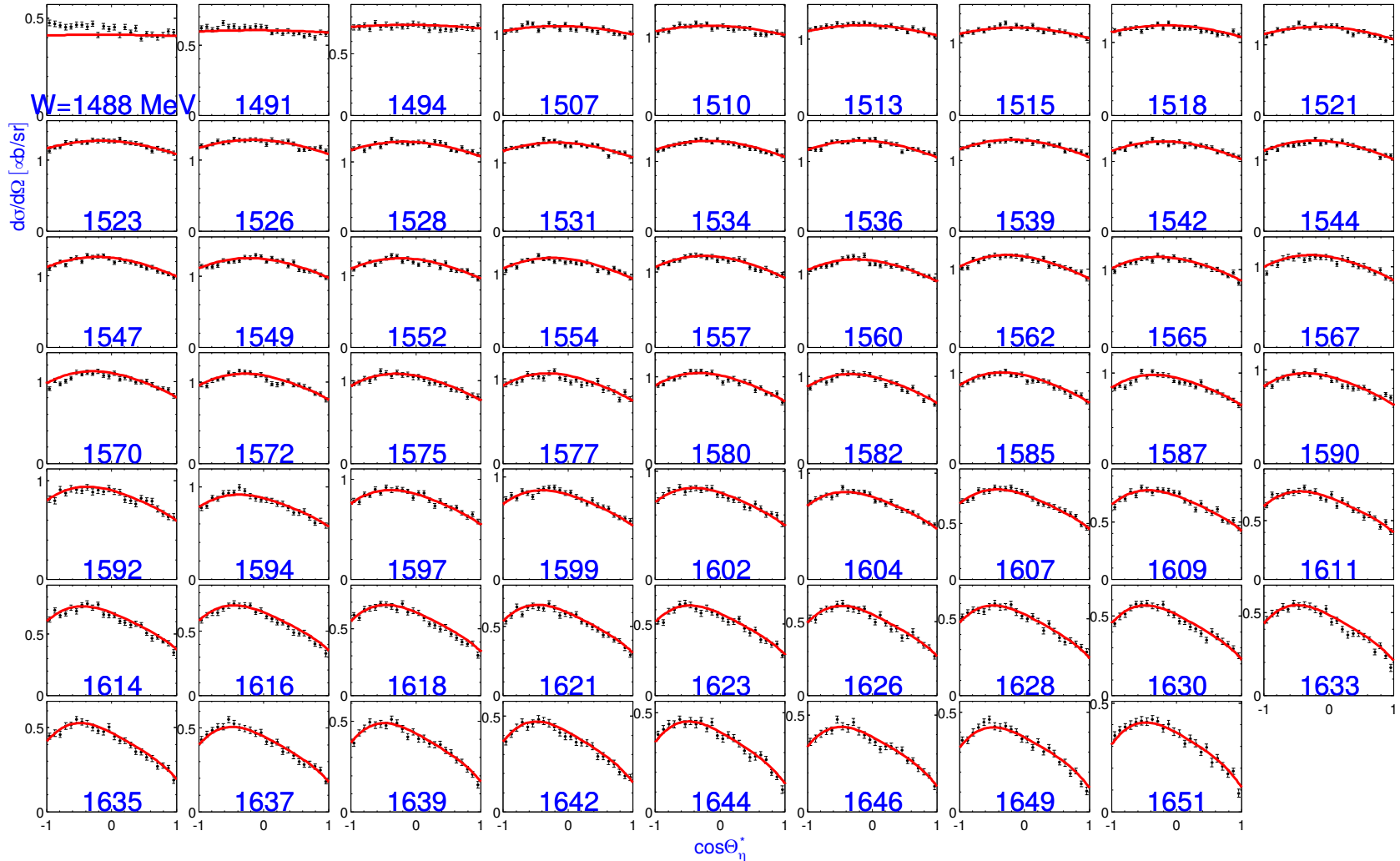


A.~Sibirtsev, J.~Haidenbauer,
S.~Krewald, U.~G.~Meissner,
and A.~W.~Thomas, EPJA {bf 41}, 71
(2000)

Selected results

$d\sigma/d\Omega$ for $\gamma p \rightarrow \eta p$. $W = 1488 - 1651$ MeV, 24 angular bins

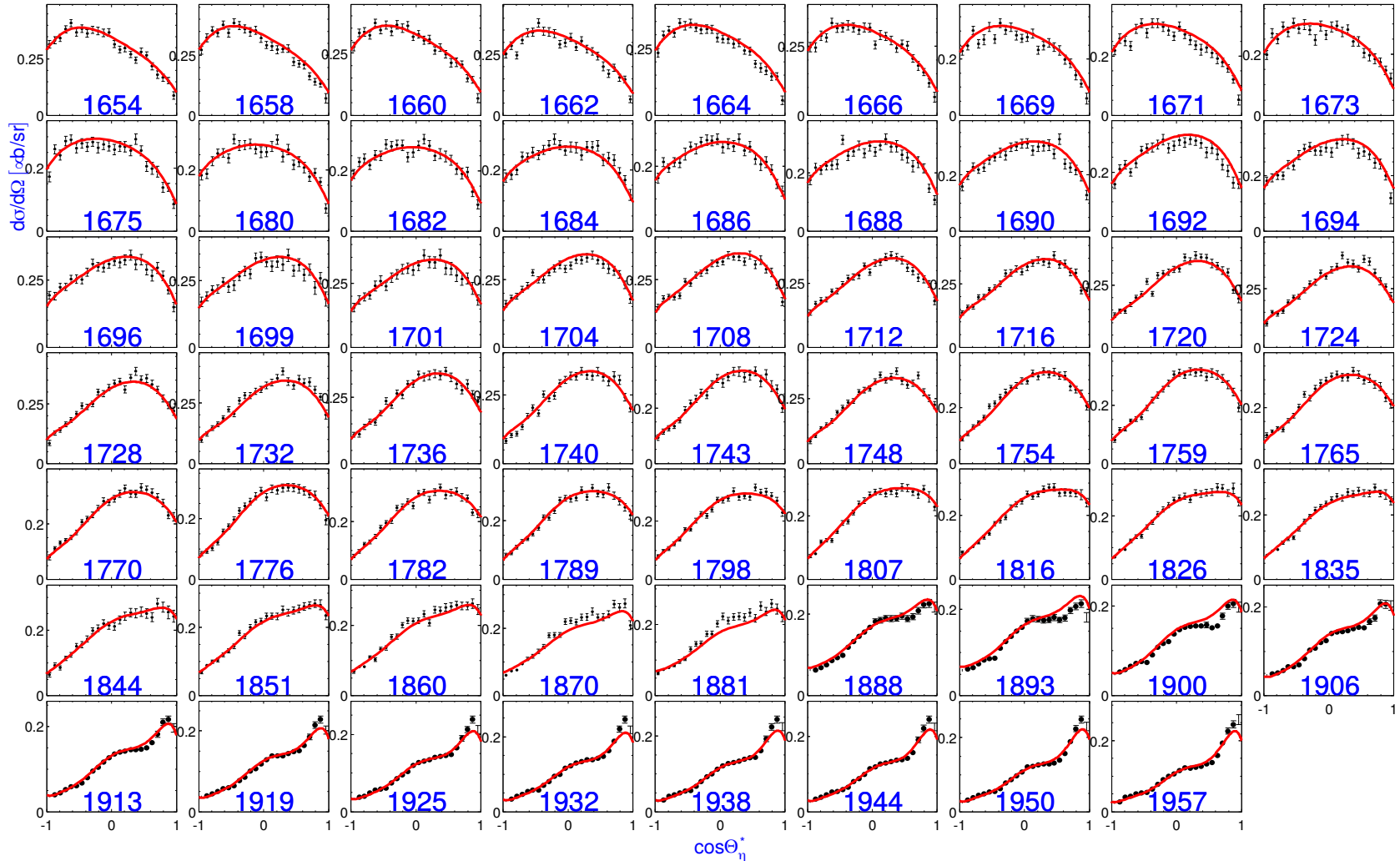
Data: A2MAMI-17, Red line - full solution.

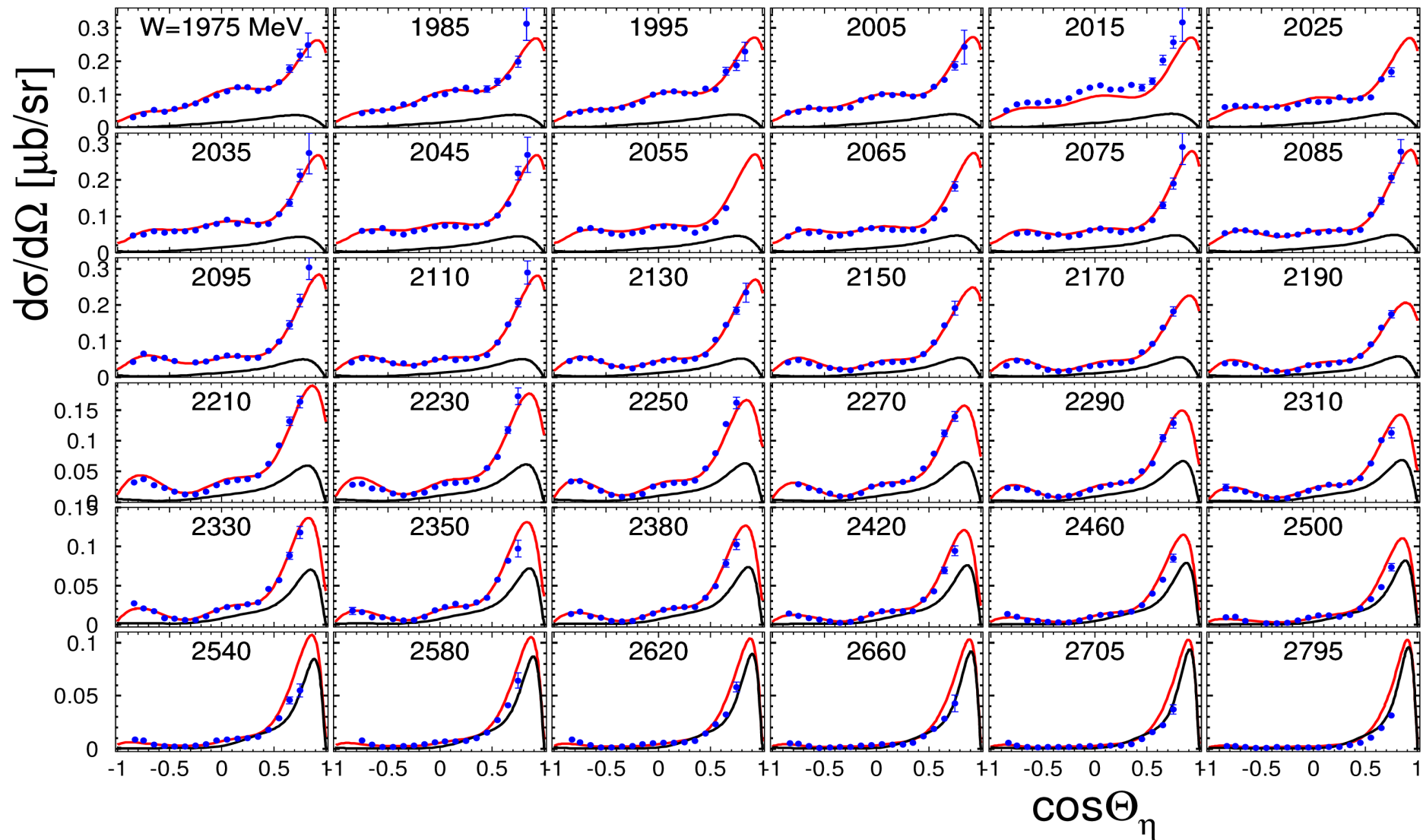


Selected results

$d\sigma/d\Omega$ for $\gamma p \rightarrow \eta p$. $W = 1654 - 1957$ MeV, 24 angular bins

Data: A2MAMI-17, Red line - full solution.



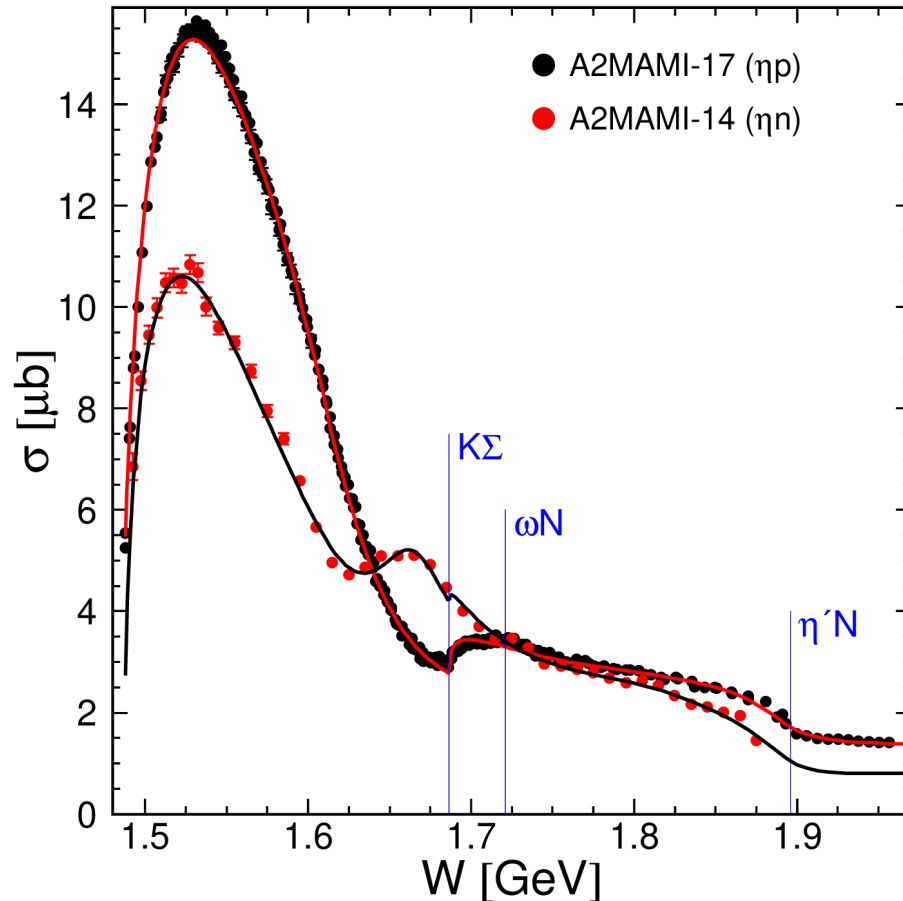
$\gamma p \rightarrow \eta p$ Selected results: $d\sigma/d\Omega$ 

$$\chi^2 = 2265/634 \approx 3.57$$

Data: CLAS-09

Lines: red – full solution; solid black – Regge+Born; dashed – Regge; dotted – Born terms

Selected results: total cross sections



Lines: full solution for γp (red) and γn (black) channels.

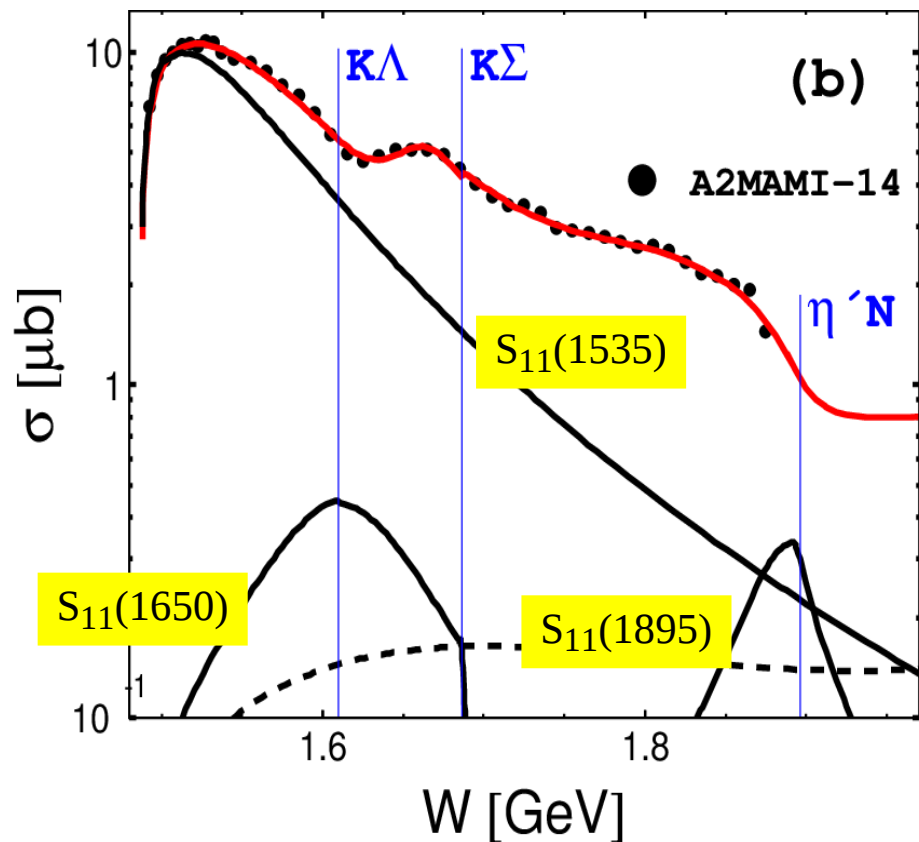
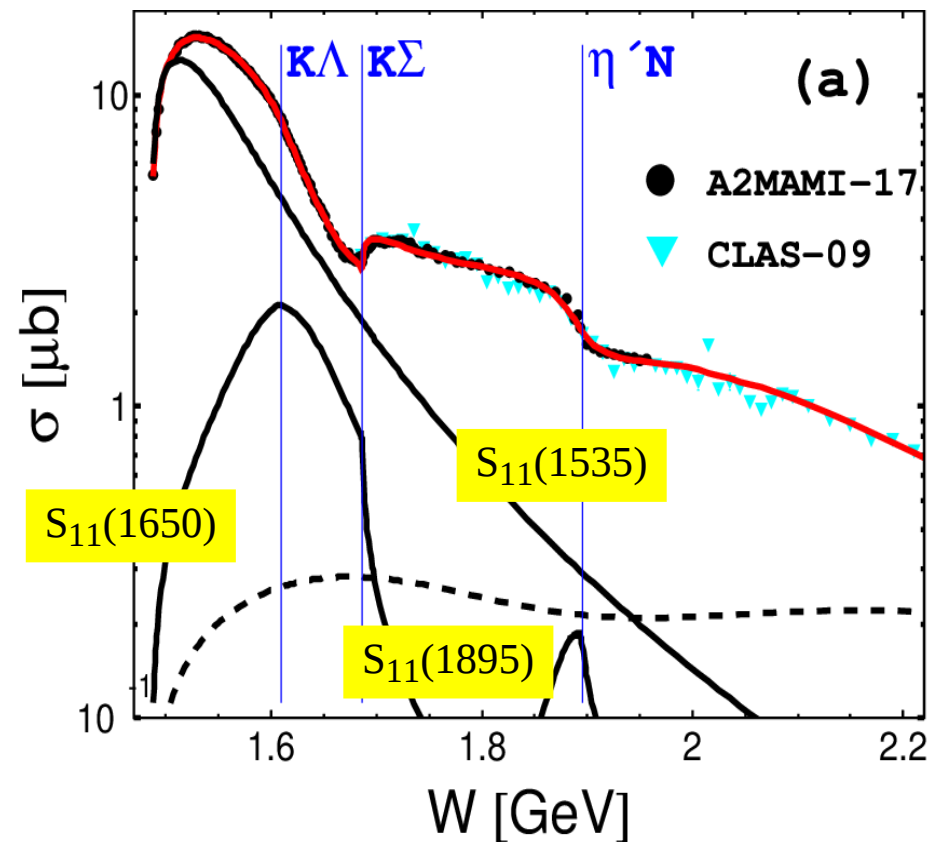
$$\gamma p \rightarrow \eta p: \chi^2 = 238.6/125 \approx 1.91;$$

$$\gamma n \rightarrow \eta n: \chi^2 = 120.6/44 \approx 2.74;$$

$$\gamma p \rightarrow \eta' p: \chi^2 = 9.46/12 \approx 0.79 \text{ (A2MAMI)}$$

$$\gamma n \rightarrow \eta' n: \chi^2 = 10.9/17 \approx 0.64$$

Selected results: partial contribution of resonances

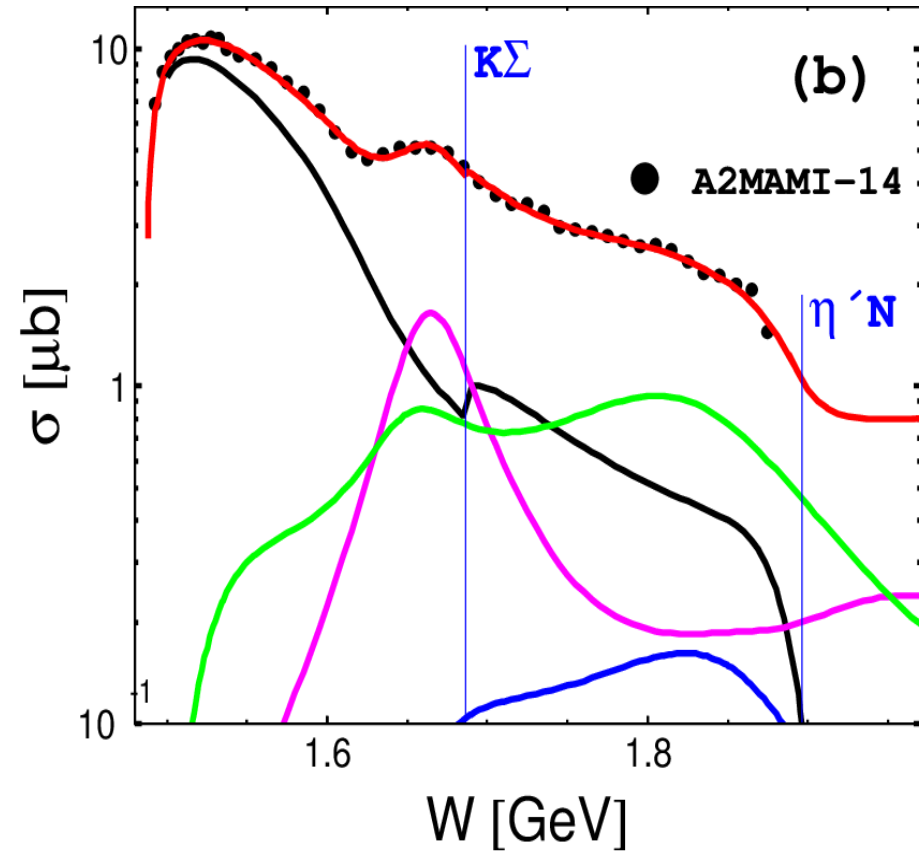
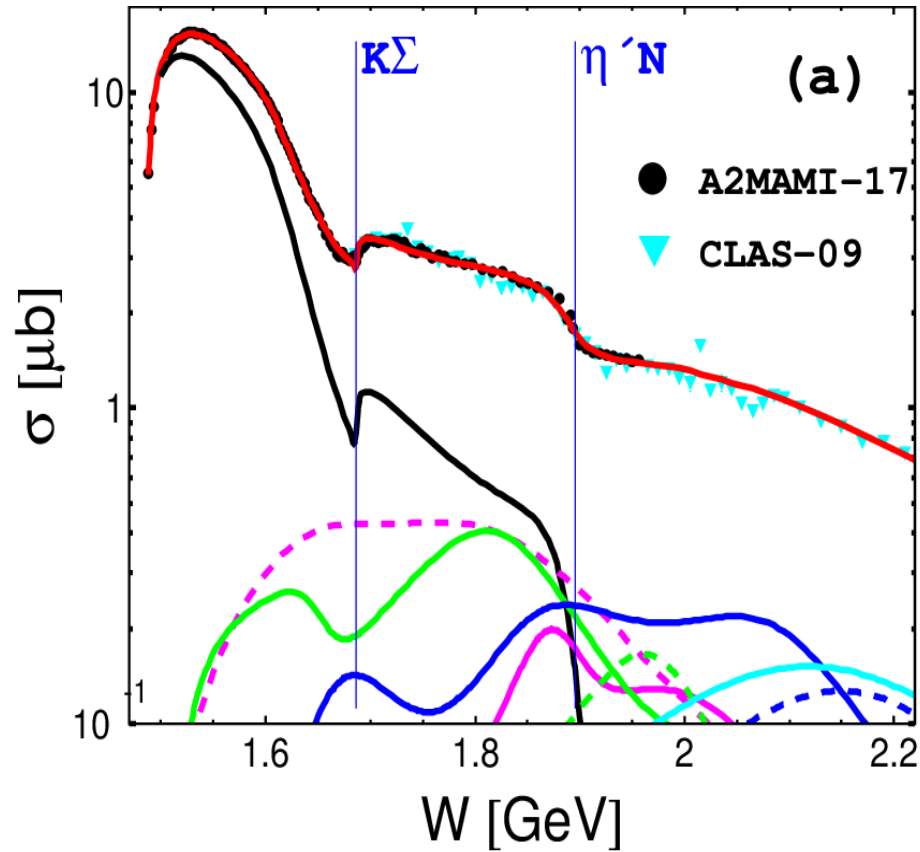


Black dashed line – Regge + Bonn contribution

Selected results: partial waves contribution (no bgr)

$\gamma p \rightarrow \eta p$

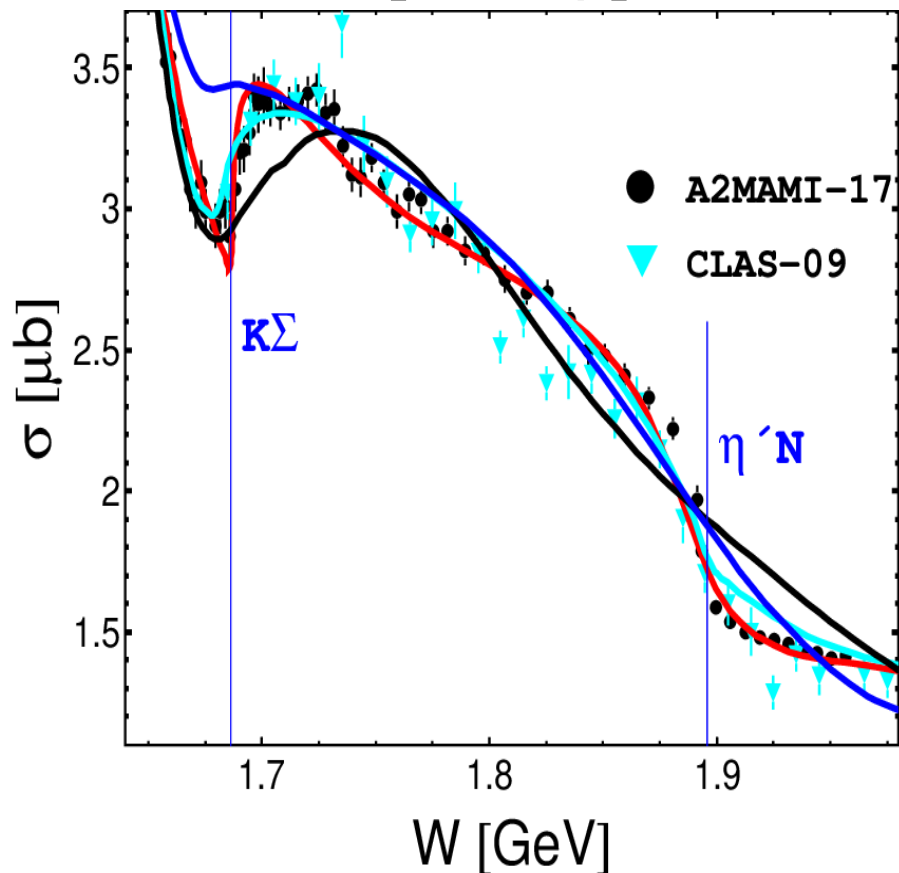
$\gamma n \rightarrow \eta n$



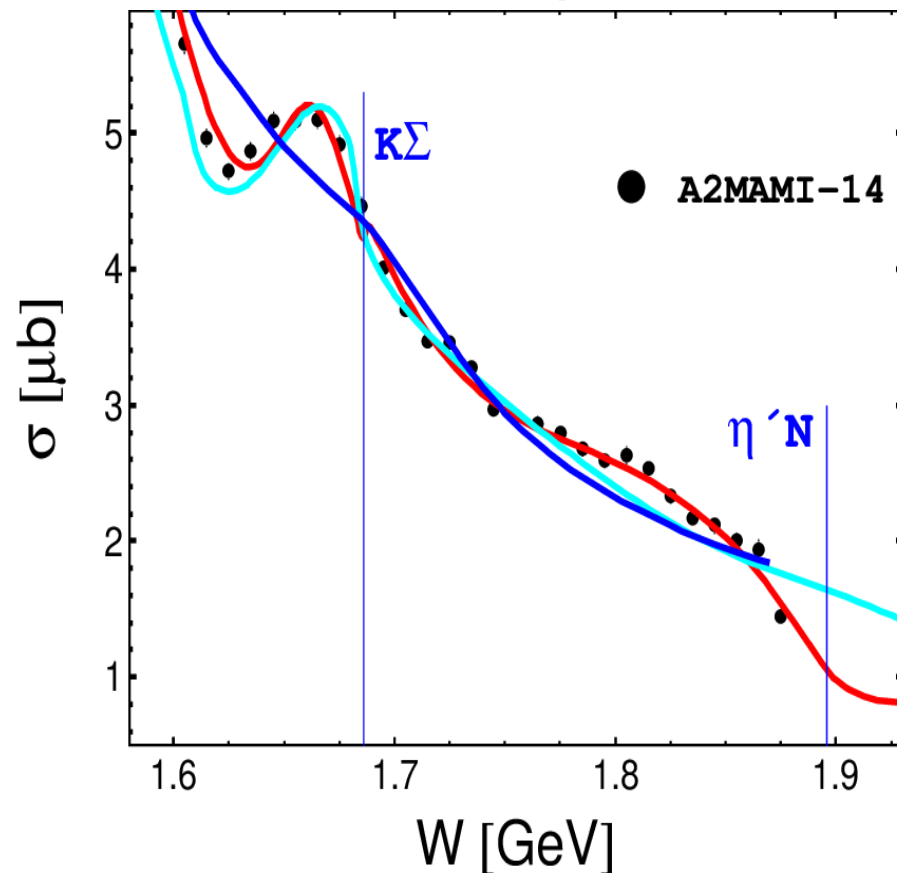
S_{11} – black solid;
 P_{11} – magenta solid; P_{13} – magenta dashed
 D_{13} – green solid; D_{15} – green dashed
 F_{15} – blue solid; F_{17} – blue dashed
 G_{17} – cyan solid

Comparison with other new PWA

$\gamma p \rightarrow \eta p$



$\gamma n \rightarrow \eta n$



Red line: EtaMAID2018

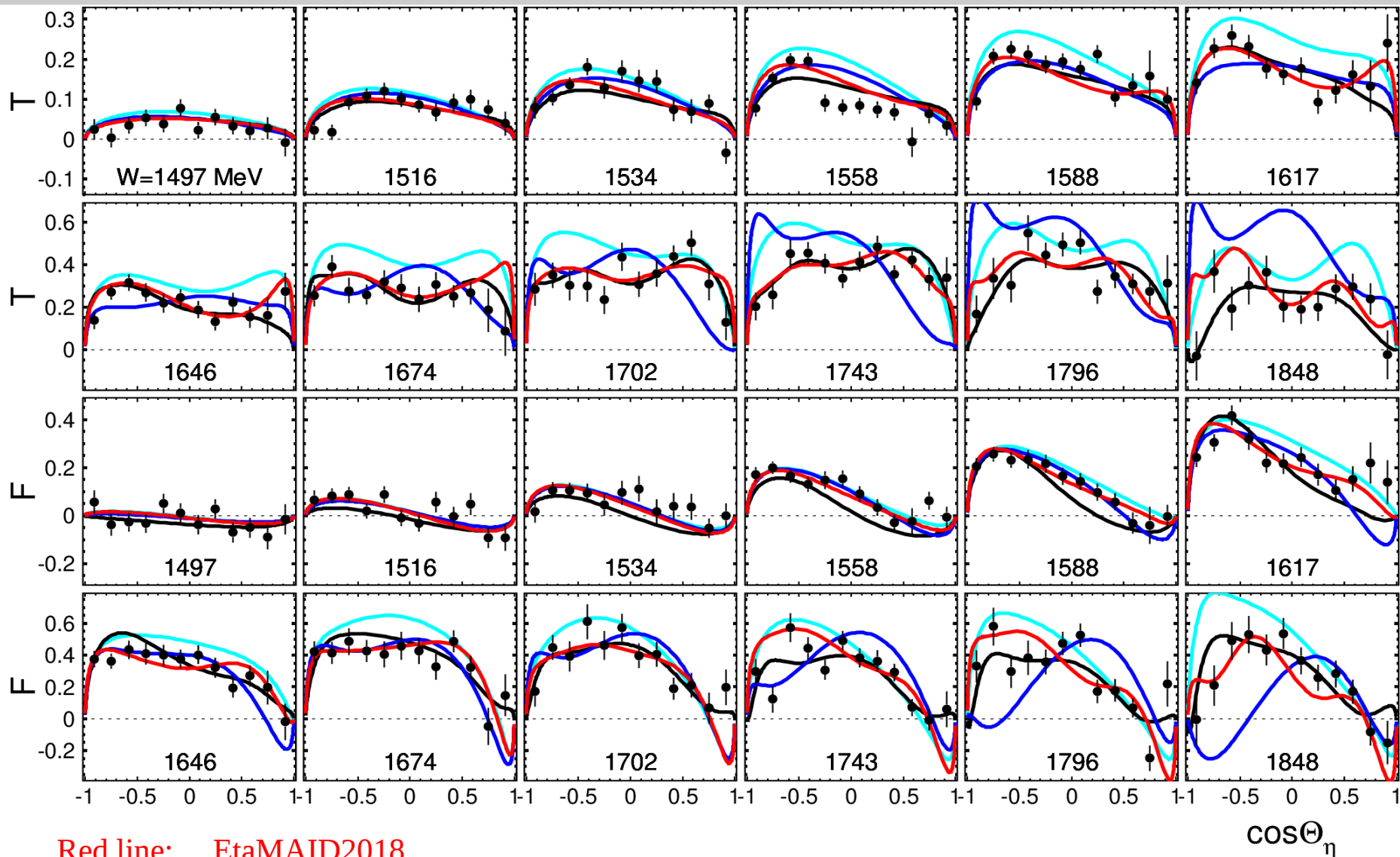
Cyan line: BnGa

Blue line: KSU

Black line: JüBo

$\gamma p \rightarrow \eta p$

Polarization observables T and F



Red line: EtaMAID2018

Cyan line: BnGa

Blue line: KSU

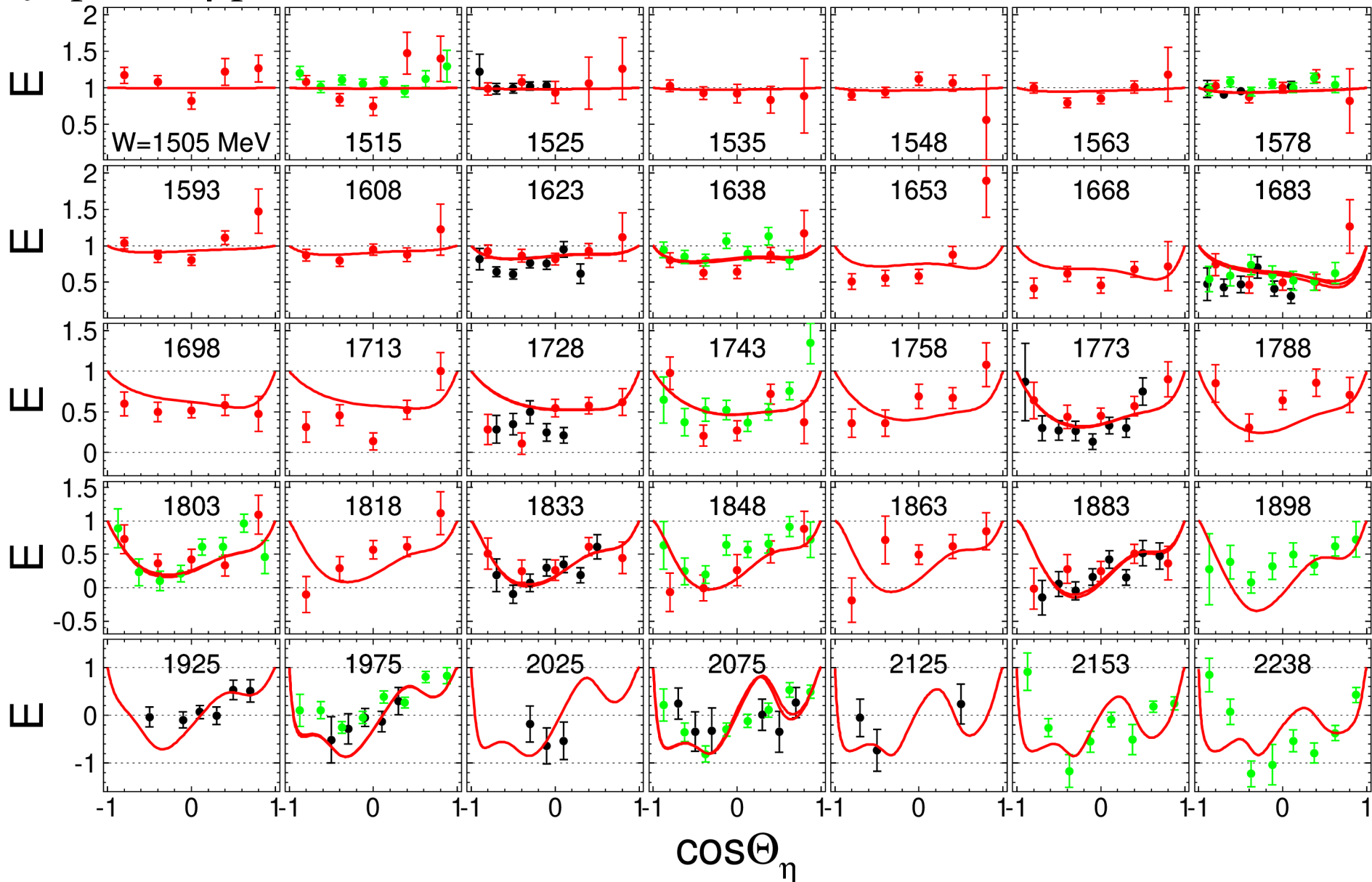
Black line: JüBo

Data: A2MAMI-14

 $T: \chi^2 = 255.3/144 \approx 1.77; \quad F: \chi^2 = 253.3/144 \approx 1.76$

$\gamma p \rightarrow \eta p$

Polarization observables: E



Data: black – CLAS-16;

red – A2MAMI-17;

green – CBELSA/TAPS

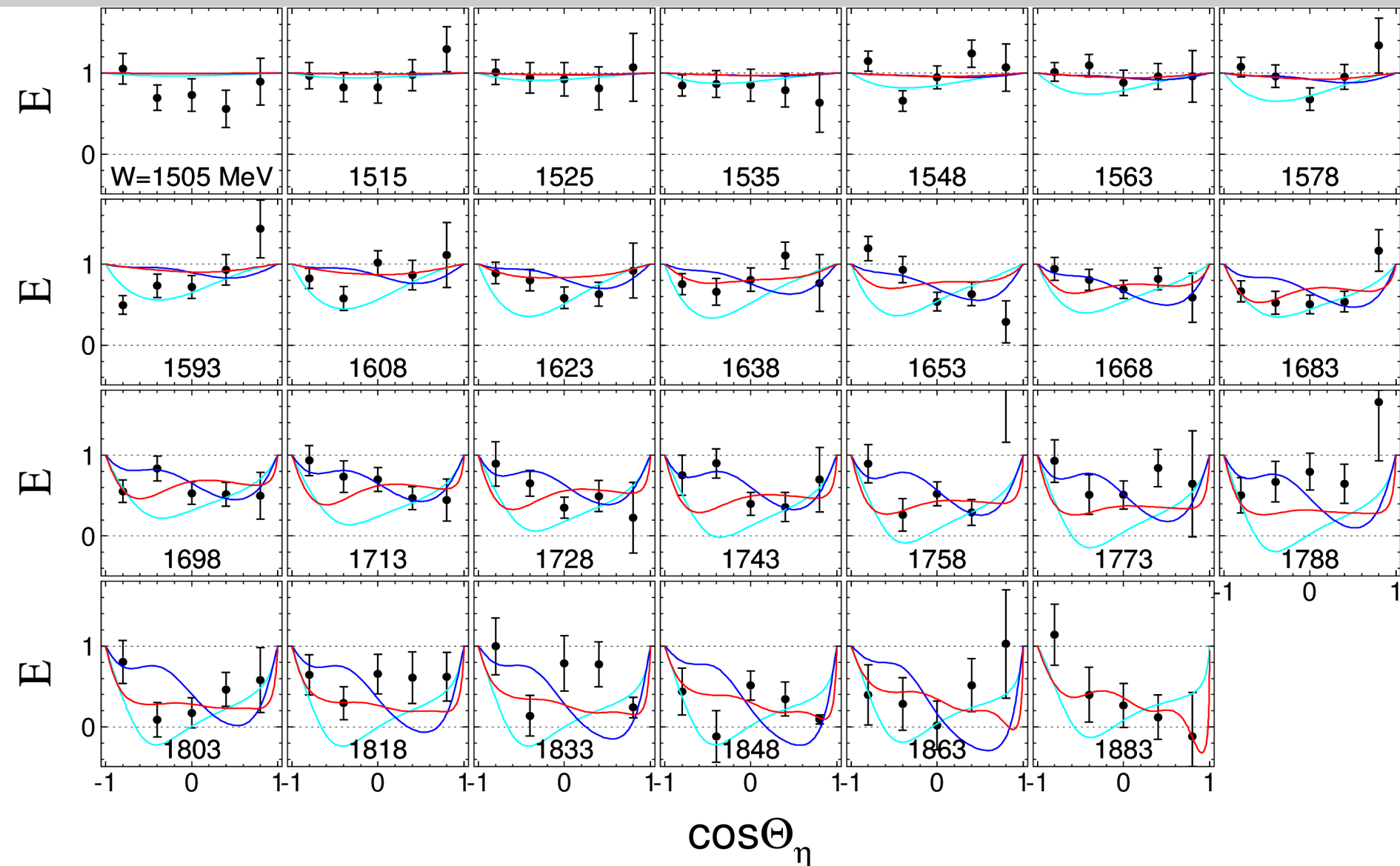
$$\chi^2 = 170.6/73 \approx 2.34$$

$$\chi^2 = 272.3/135 \approx 2.02$$

$$\chi^2 = 395.5/93 \approx 4.25$$

$\gamma n \rightarrow \eta n$

Helicity beam asymmetry E



Red line: EtaMAID2018

Cyan line: BnGa

Blue line: KSU

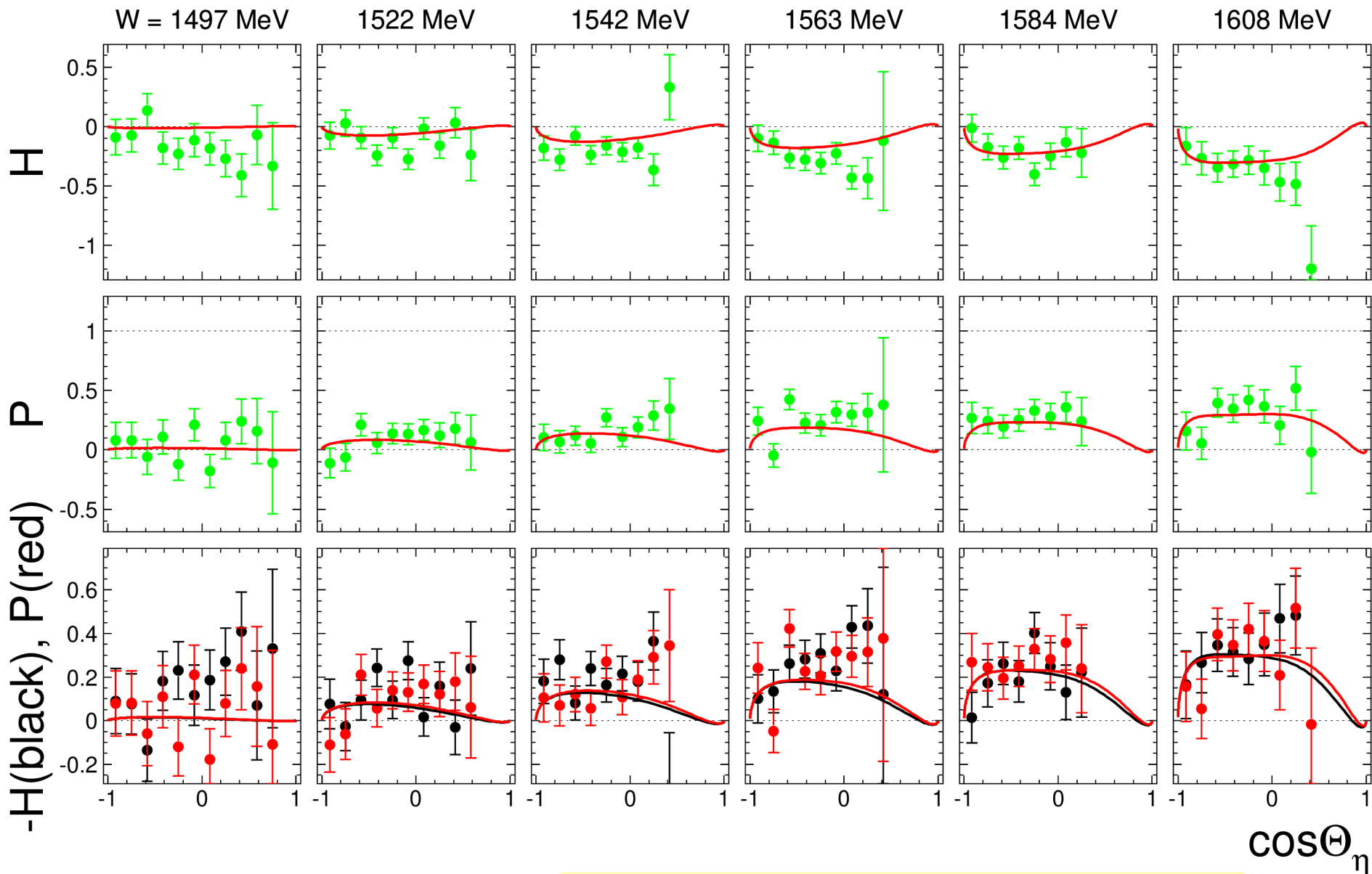
 $\chi^2 = 349.8/135 \approx 2.59$

Data: A2MAMI-17



Polarization observables: H and P

P \approx -H ?



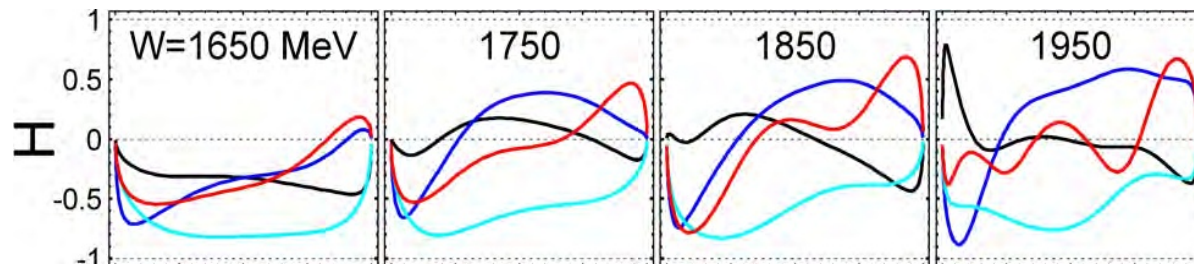
Data: CBELSA/TAPS
 Lines: full solution

H: $\chi^2 = 81.08/56 \approx 1.45$; P: $\chi^2 = 57.07/56 \approx 1.02$

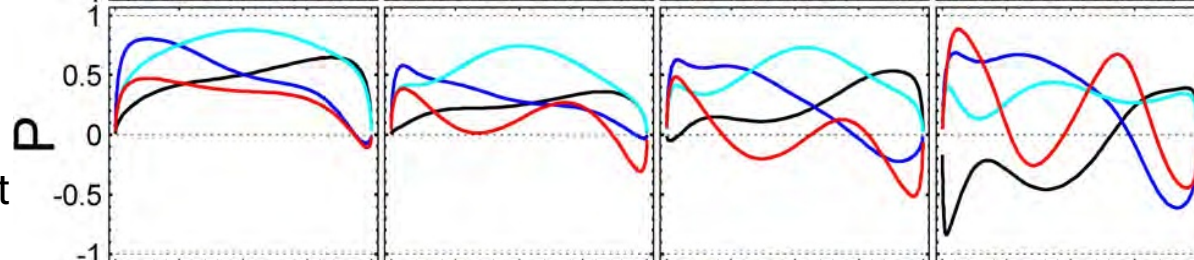
predictions for unmeasured polarization observables

— EtaMAID — BnGa — JüBo — KSU

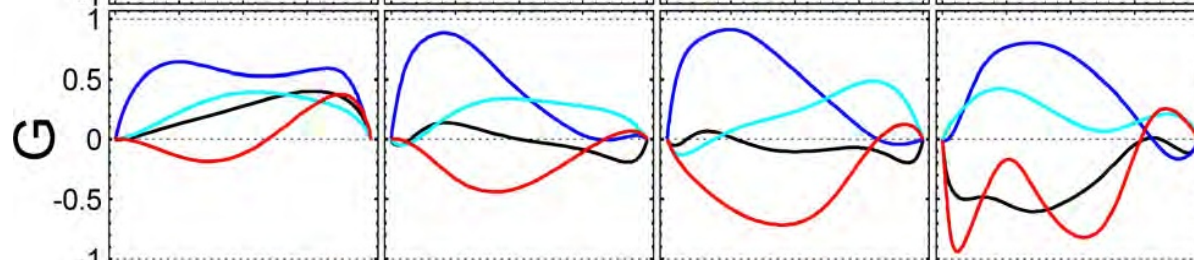
beam-target H



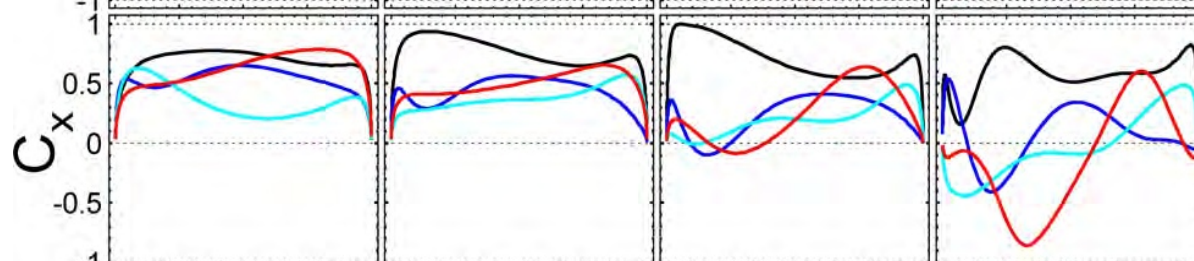
recoil pol. P
equivalent to beam-target



beam-target G



beam-recoil C_x^x
very hard



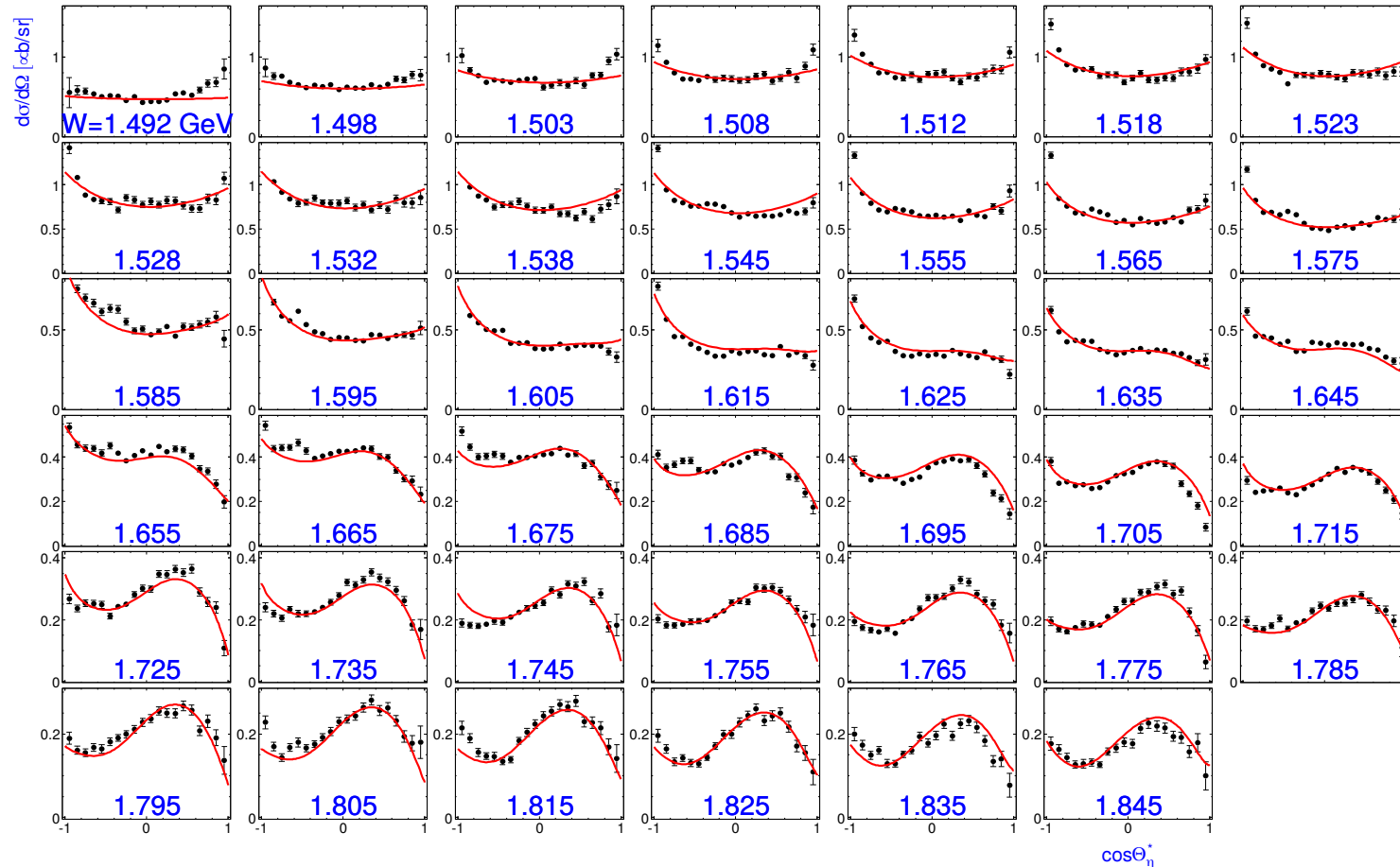
$\cos\Theta_n$

Selected results

$d\sigma/d\Omega$ for $\gamma n \rightarrow \eta n$

Data: A2MAMI-14 (black)

Red line - full solution.

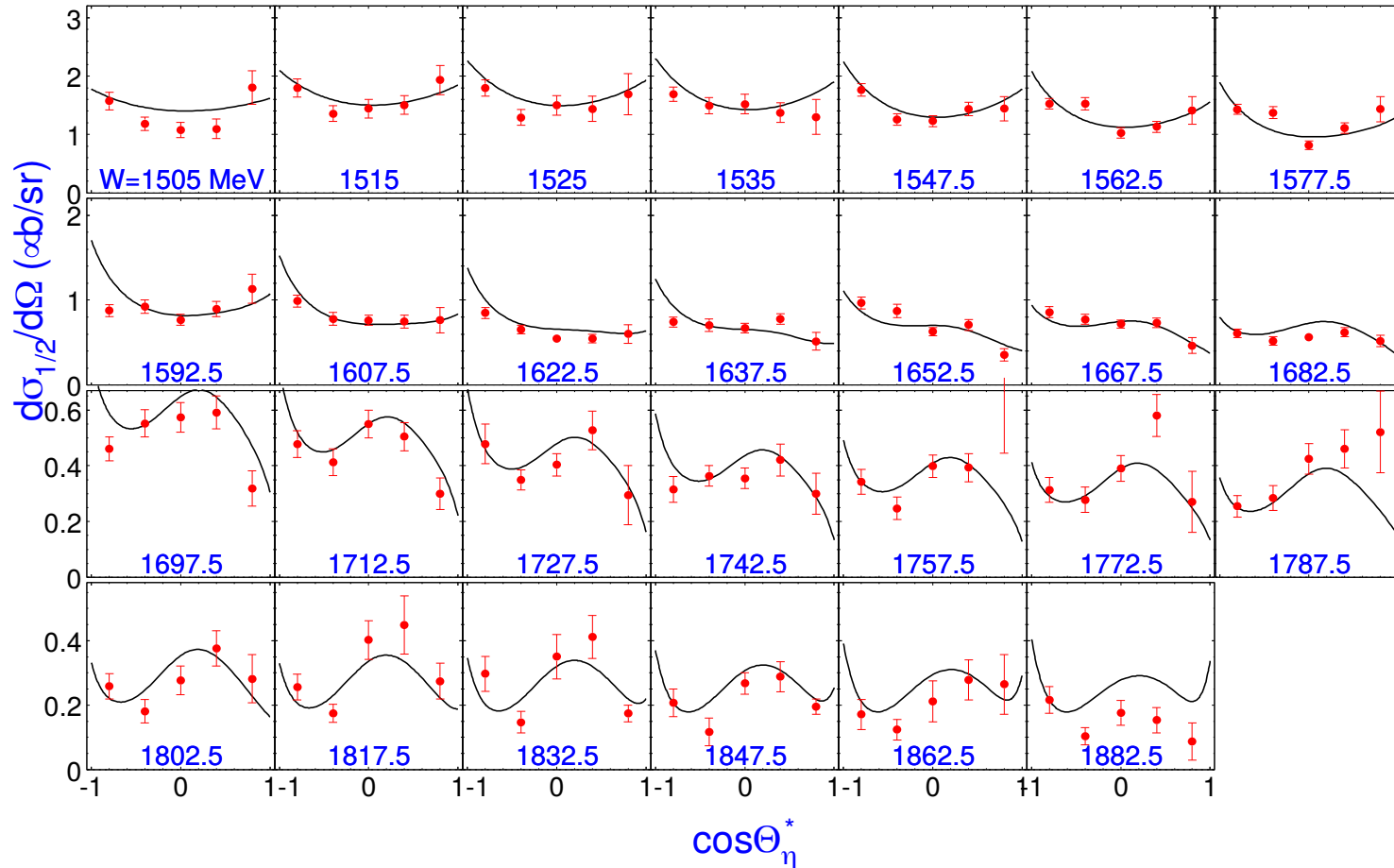


Selected results

$d\sigma/d\Omega_{1/2}$ for $\gamma n \rightarrow \eta n$

Data: A2MAMI-17 (black)

Red line - full solution.

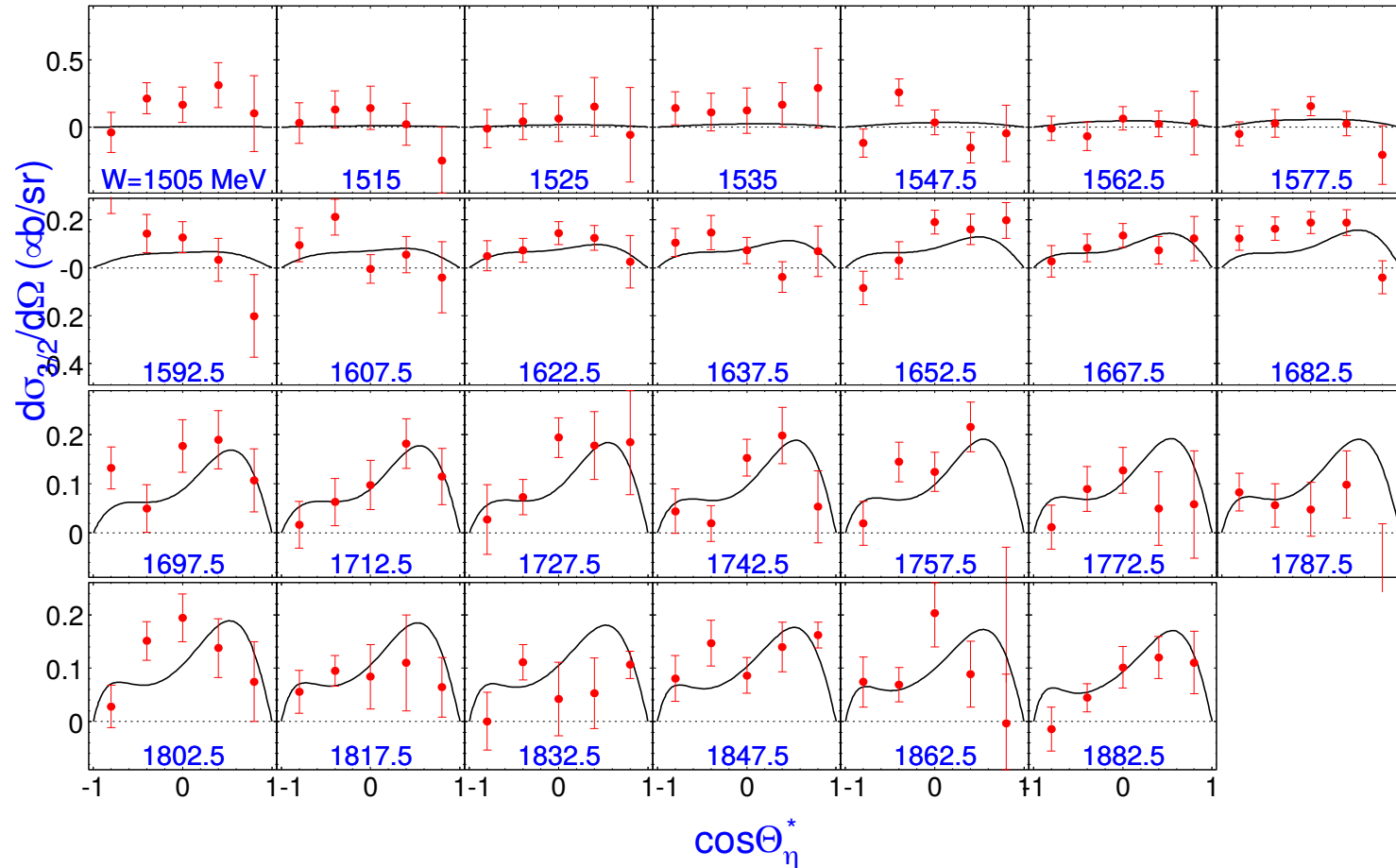


Selected results

$d\sigma/d\Omega_{3/2}$ for $\gamma n \rightarrow \eta n$

Data: A2MAMI-17 (black)

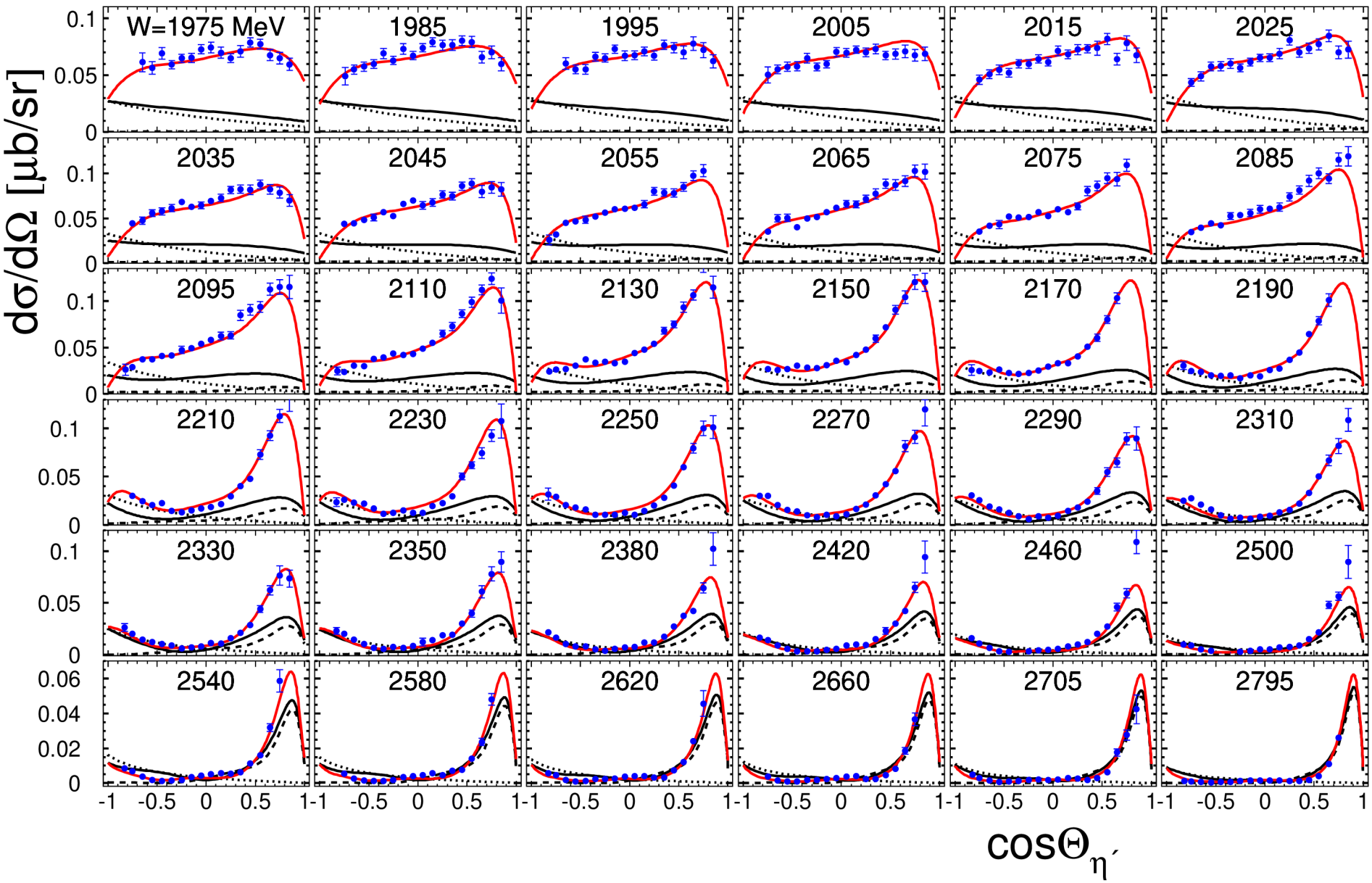
Red line - full solution.





Differential cross sections

$\chi^2 = 2145.6/639 \approx 3.36$



Data: CLAS-09

Lines: red – full solution;

solid black – Regge+Born;

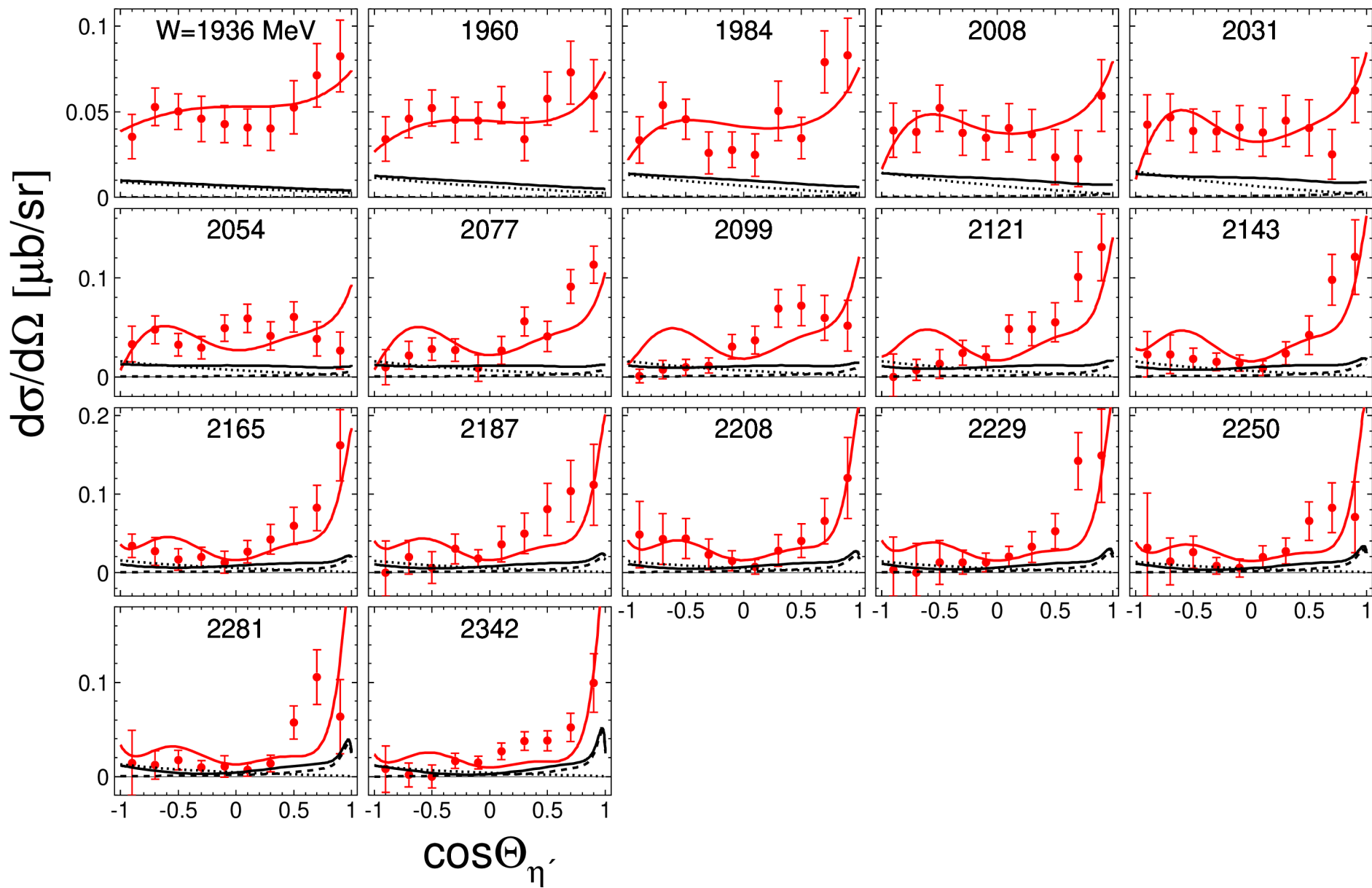
dashed – Regge ;

dotted – Born terms



Differential cross sections

$\chi^2 = 279.9/170 \approx 1.64$



Data: CBELSA/TAPS-11

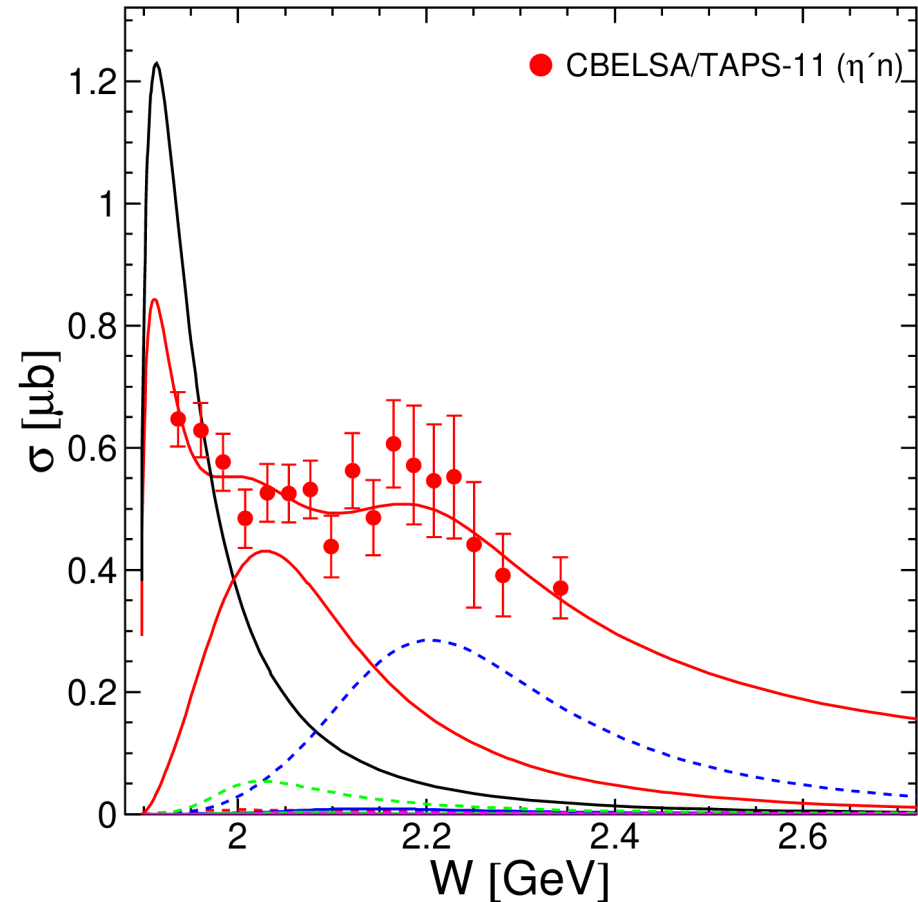
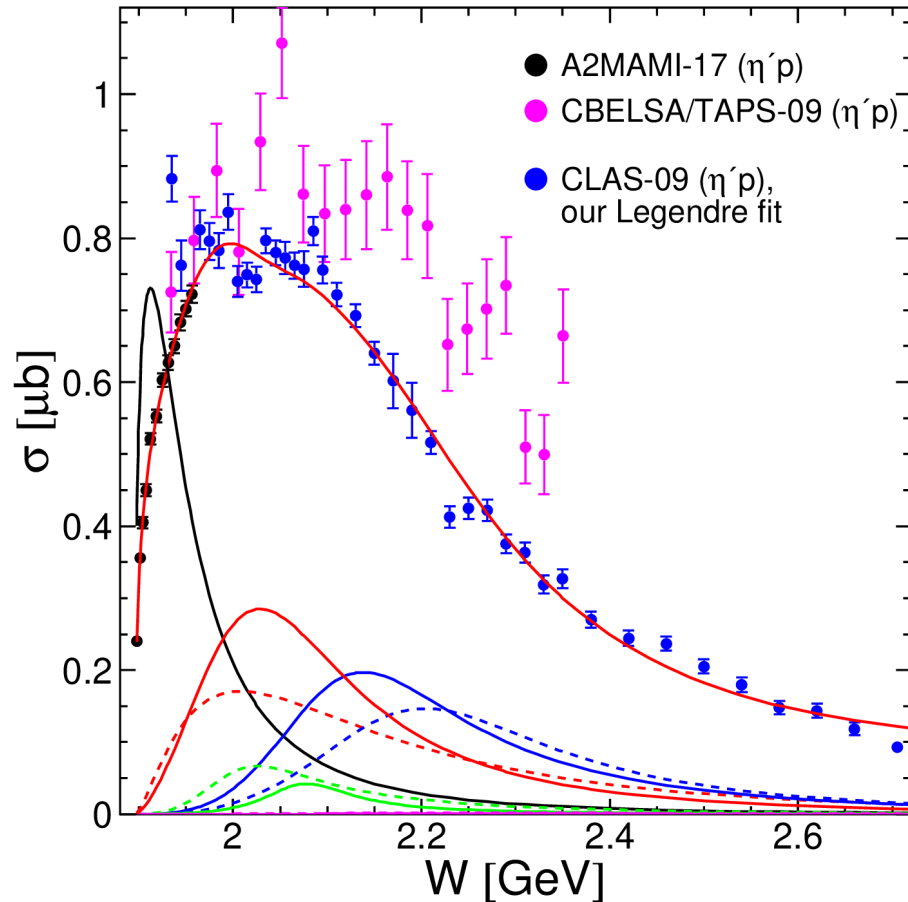
Lines: red – full solution;

solid black – Regge+Born;

dashed – Regge ;

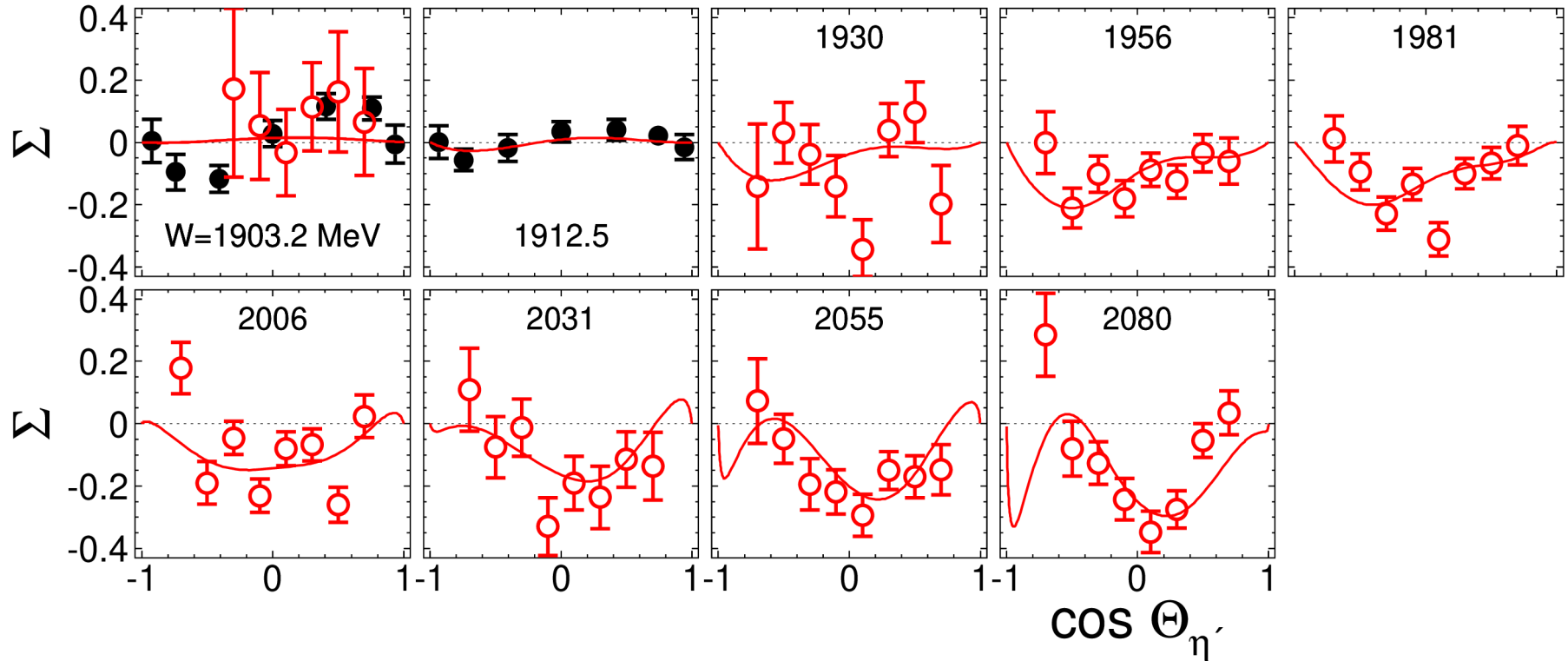
dotted – Born terms 35

Fit results: partial contribution of resonances



S11 – black solid;
 P11 – red solid;
 D13 – green solid;
 F15 – blue solid;
 G17 – magenta solid;

P13 – red dashed
 D15 – green dashed
 F17 – blue dashed
 G19 – magenta dashed



Data: black – GRAAL-15;

$$\chi^2 = 27.89/14 \approx 1.99$$

red – CLAS-17

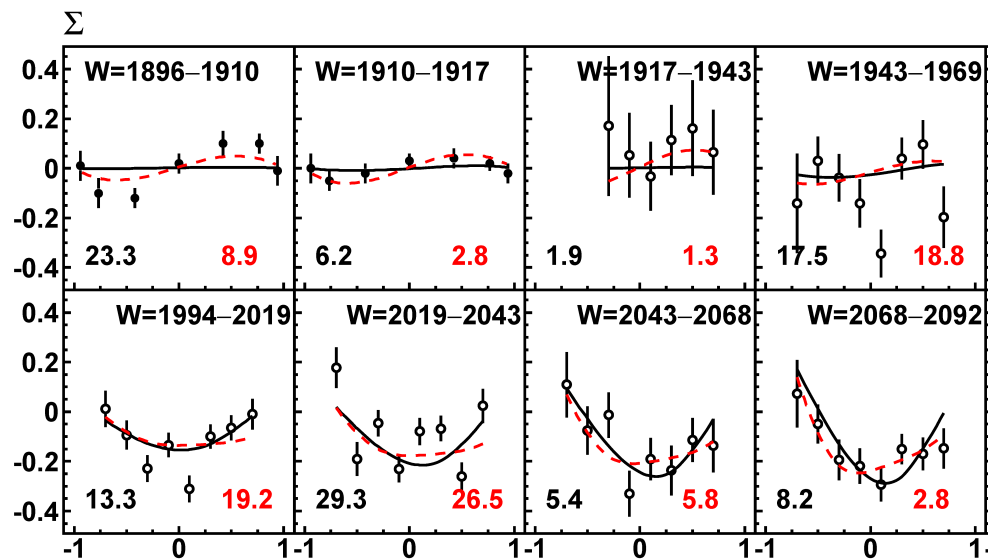
$$\chi^2 = 118.1/62 \approx 1.90$$

Narrow resonance in η' photoproduction?

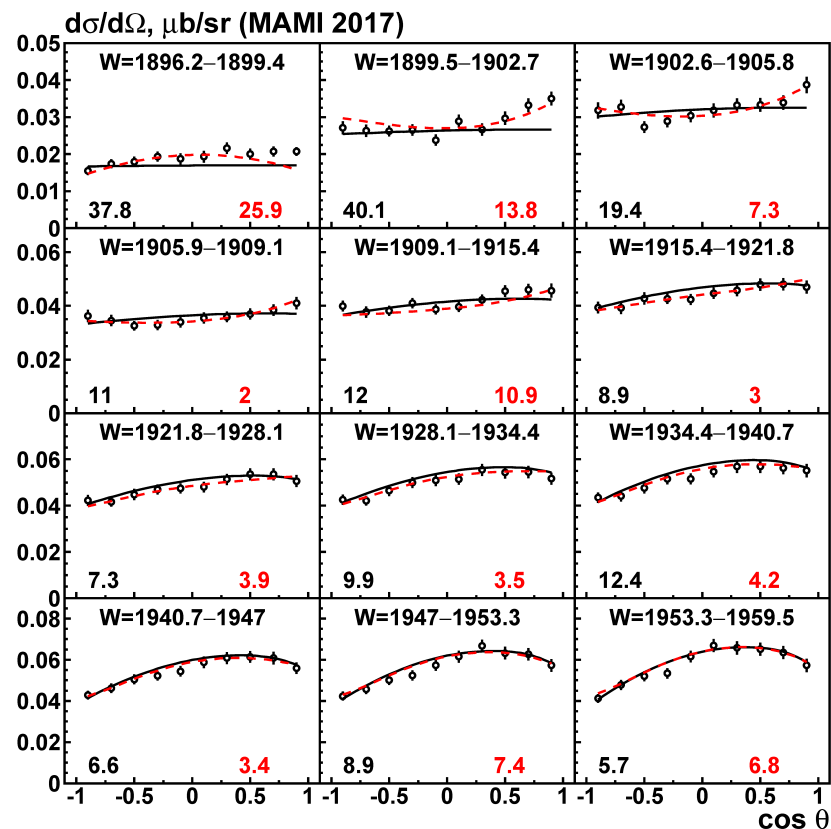
Anisovich, Burkert, Dugger, Klempt, Nikonov, Ritchie, Sarantsev, Thoma, arXiv:1803.06814 (2018)

———— BnGa-2017 solution without narrow resonance

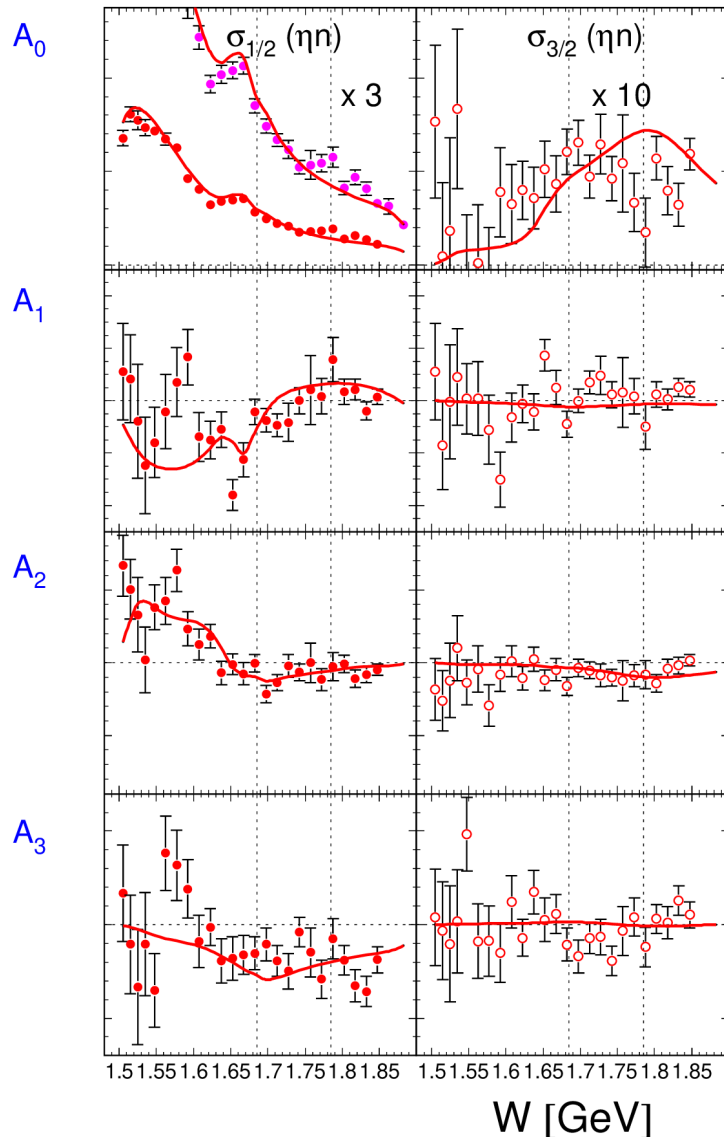
----- BnGa2018 solution with a narrow D_{13} : $M_R = 1900 \pm 1$ MeV, $\Gamma < 3$ MeV



beam asymmetry Σ :
 black disks: GRAAL-2015
 red circles: CLAS-2017



diff. cross sect. $d\sigma/d\Omega$:
 A2MAMI-2017



Partial wave content of Legendre coefficients, $l_{max} = 3$

$$A_0 = SS + PP + SD + DD + PF + FF$$

$$A_1 = SP + PD + SF + DF$$

$$A_2 = PP + SD + DD + PF + FF$$

$$A_3 = PD + SF + DF$$

$$A_4 = DD + PF + FF$$

$$A_5 = DF$$

$$A_6 = FF$$

Data: A2MAMI-17;
Red lines: full solution

Summary and conclusions

1. New version of EtaMAID for η and η' photoproduction on protons and neutrons is finished and available on the MAID webpage.
2. The well-known duality problem is addressed in a new approach with a damping factor removing most of Regge background in the resonance region.
3. Unitarization was done by adding a phase for each resonance as free parameter.
4. New EtaMAID2018 describes all data very well and explains most of them:
 - cusp in eta total cross section, in connection with steep rise of the η' total cross section from its threshold, is explained by a strong coupling of $N(1895)1/2^-$ to both channels;
 - narrow bump in (ηn) and dip in (ηp) channels have different origin: the first is a result of interference of a few resonances, and the second is a threshold effect due to opening $K\Sigma$ decay channel of $N(1650)1/2^-$ resonance;
 - angular dependence of Σ asymmetry for $\gamma p \rightarrow \eta p$ at $W > 2$ GeV is explained by an interference of $N(2120)3/2^-$ and $N(2060)5/2^-$ resonances.
5. The near threshold behavior of Σ for $\gamma p \rightarrow \eta' p$ is still an open question.
6. Possible narrow resonance with $M=1726$ MeV observed both in $\gamma p \rightarrow \eta p$ and $\gamma n \rightarrow \eta n$ reaction channels for $\sigma_{1/2}$ needs further investigation.
7. Next step: adding πN , ωN , $K \Lambda$, $K \Sigma$ channels and electroproduction.

Selected results

M.Polyakov



Large violation of the flavour SU(3) symmetry in η MAID2018 isobar model
(the neutron anomaly case)

1,2

1,3

		M_R (MeV) Γ	M_R (MeV) lg	$lg_{\pi N}$	$lg_{\eta N}$	$lg_{K\Lambda}$	$lg_{K\Sigma}$
N	1535, $\frac{1}{2}^-$	1521.7	174.7	0.45	0.62	N/A N/A	
N	1650, $\frac{1}{2}^-$	1626.3	132.5	0.36	0.28	0.20	1.21
N	1710, $\frac{1}{2}^+$	1669.5	63.2	0.10	0.22	0.52	0