# Hands on Neul at: A Toolbox for Neural Samplers in Lattice Field Theory



#### $N E U L A T$

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October 24, 2024 @ ML4PhysChem

https://github.com/neulat/neulat

#### About me



#### Christopher J. Anders

PostDoc at RIKEN AIP, Tokyo

#### Research Interests

#### Background

- **Deep Learning**
- **Model Understanding**
- Software for MI
- ML in the Sciences

#### Disclaimer: I am not a physicist!

- B.Sc. Computer Science @ TU Berlin (2016)
- **M.Sc.** Computer Science @ TU Berlin (2018)
- PhD Computer Science © TU Berlin (2024)



software framework for machine-learning-based lattice field theory

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	- trivializing maps with flows (Bacchio et al. (2023))

**Faster development of new ideas** 

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Existing examples:

- SchNetPack Deep Neural Networks for Atomistic Systems
- BGFlow Boltzmann Generators (BG) and other sampling methods



There are already great tools available!

Introduction to Normalizing Flows for Lattice Field Theory (Albergo et al., 2021)

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- **Hamiltonian Monte Carlo** 
	- **fthmc:** Field Transformation HMC (Sam Foreman et al.)
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But: We want to create a highly customizable reference implementation.

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	- various MCMC implementations (HMC, Cluster algorithms, etc.)
	- **Normalizing Flow framework** 
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		- **Neural HMC**

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- **Estimation:** 
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	- Sampling in the presence of mode-collapse (Nicoli et al. (2023)).

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#### **Tutorials and Documentation:**

- $\blacksquare$  Step-by-step tutorials
- **Extensive reference**

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- **Modularity and Customizability:** Swiftly incorporate new actions/theories/models/techniques

Action

Actions  $S[U]$  define physical theories  $p(U) \propto e^{-S[U]}$ 



Actions are, e.g.,  $\phi^4$  and  $U(1)$ 



Samplers are anything that can be sampled from



Samplers are, e.g., MCMCs, Flows,  $\mathcal{N}(0, 1)$ 



Samplers require Actions



Estimators are used to estimate observables


Estimators are, e.g., i.i.d or correlated, based on the samples



Estimators require samples from Samplers



Observables, such as Magnetization in  $\phi^4$ , are used by the Estimator



Resulting Statistics are estimations for the Observables

#### **Actions**

Actions are objects and need to be instantiated.

```
1 import torch
2 from neulat.action.phi4 import Phi4Action
3
4 \mid # ndim_features is the number of dimensions in the lattice
5 action = Phi4Action(kappa=0.3, lamb=0.022, ndim_features=2)
```
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```
Action objects can be called to compute action values for configurations.

```
1 \vert \text{config} = \text{torch.random}(8, 8)
```

```
2 | unnormalized_prob = torch.exp(-action(config))
```
### Defining Actions

2

Actions are very simple to implement, for instance  $\phi^4$ :

```
1 from neulat.action.base import Action
3 class Phi4Action(Action):
4 name = 'phi4_action'
5 def __init_(self, kappa, lambd, ndim_feature=2):
 6 \mid \cdot \cdot \cdot \cdot7 def forward(self, config):
8 dims = tuple(range(-1, -self.ndim_feature, -1))
9 | kinetic = (-2 * \text{self.kappa}) * \text{config} * \text{sum}(10 torch.roll(config, 1, dim) for dim in dims)
11 \vert mass_inter = (1 - 2 * \text{self.lambd}) * \text{config} * 212 inter = self.length * config ** 4
13 return (kinetic + mass + inter).sum(dim=dims)
```


At the core of NeuLat are Samplers, which is anything from which can be sampled.

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For instance, the normal distribution is a Sampler in Neulat:

```
1 from neulat.sampler.distribution import Normal
```

```
\overline{3} | normal = Normal(loc=0., scale=1., feature_shape=(8, 8))
```
## Sampling

3

Samplers can be sampled from, and may or may not support probability values.

```
1 samples = normal.sample(sample_shape=8)
2 | logprobs = normal.logprob(samples)
```

```
4 | samples2, logprobs2 = normal.sample_with_logprob((2, 2))
```
### **Sampling**

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```
In NeuLat, we assume configurations of shape (\*sample\_shape, \*feature\_shape).

- $\blacksquare$  feature shape is the shape of the lattice
- $\blacksquare$  sample shape is the number of samples, supporting arbitrary shapes

### Hamiltonian Monte Carlo

A more involved Sampler is the HMC:

```
1 from neulat.sampler.mc.hmc import HMCMarkovChain
2
3 hmc = HMCMarkovChain(
4 action, # action
5 feature_shape=(8, 8), # lattice shape
6 burn_in=5000, # equilibration steps
7 | skip_interval=1, # skipped samples in chain
8 overrelax_interval=50, # steps between sign flips
9 eps=0.05, # step size along trajectory
10 traj_steps=20, # number of steps in trajectory
11 bias=0.0, # bias in initialization
12 )
```
The HMC can be sampled from, as any sampler

1  $\vert$  configs = hmc.sample(sample\_shape=13)

The HMC can be sampled from, as any sampler

```
configs = hmc.sample(sample\_shape=13)
```
However, HMC does not implement logprob and by extension sample with logprog, as no normalized probabilities are available

```
1 \mid # both cause exceptions:
2 \mid # \text{logprobs} = \text{hmc}.\text{logprob}(\text{sample\_shape}=13)\frac{3}{4} \neq configs2, logprobs2 = hmc.sample_with_logprob(13)
```
One can also iterate over HMCs to sample

```
1 configs = []2 for n, config in zip(range(25), hmc):3 configs.append(config)
4 print(f'Sampled config number {n}.')
5
6 \mid # this gives a list of configs, combine them:
7 configs = torch.cat(configs)
```
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```
But be careful, HMCs are infinite iterators.

# Normalizing Flows

Normalizing flows require a base distribution, and a transform.

```
1 from neulat.sampler.flow import Flow, SequentialTransform
2
3 \mid flow = Flow(
4 base_distribution=Normal(feature_shape=(8, 8)),
5 transform=SequentialTransform([]) # identity for demo
6 )
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# Normalizing Flows

Normalizing flows require a base distribution, and a transform.

```
1 | from neulat.sampler.flow import Flow, SequentialTransform
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3 \mid f \cdot \overline{b} = F \cdot \overline{b}4 base_distribution=Normal(feature_shape=(8, 8)),
5 transform=SequentialTransform([]) # identity for demo
6 )
```
Normalizing flows are (i.i.d.) Samplers supporting logprobs.

```
1 configs, logprobs = flow.sample_with_logprob(8)
```
### Normalizing Flows: Base Distributions

The base distribution can be any sampler that supports logprobs.

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<sup>4</sup> )

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Commonly, simple distributions such as  $\mathcal{N}(0, 1)$  are used.

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```
1 \mid f \cdot \overline{f} = F \cdot \overline{f}2 base_distribution=Normal(feature_shape=(8, 8)),
3 transform=SequentialTransform([]) # identity for demo
```
Flows themselves support logprobs, and can thus be base distributions.

```
1 \quad \text{flow2} = \text{Flow(}2 base_distribution=flow,
3 transform=SequentialTransform([]) # identity for demo
4 )
```
Transforms are invertible PyTorch modules, and require a forward and a inverse.

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```
E.g., implementation for transform f(\mathsf{x}) = -\mathsf{x}, f^{-1}(\mathsf{x}) = -\mathsf{x}
```

```
1 from sampler.flow.base import Transform, withlogdet
2
3 class FlipSign(Transform):
4 @withlogdet
5 def forward(self, input):
6 return -input, 1.
7 @withlogdet
8 def inverse(self, input):
9 return -input, 1.
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The second return value is the *log absolute jacobian determinant* of the transform.

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```
The decorator @withlogdet makes sure the logdet is accumulated between transforms.

A useful transform is the SequentialTransform, which is used to apply transforms sequentially:

```
1 from sampler.flow.base import SequentialTransform
2
3 | flip_a_bunch = SequentialTransform([4 FlipSign(),
5 FlipSign(),
6 FlipSign(),
7 \mid \mid \mid \mid
```
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5 FlipSign(),
6 FlipSign(),
7 ])
```
For common Coupling Flows, there is however a more convenient way.

## Coupling Flows

Coupling flows like NICE consist of two parts, a partitioner, and a net\_factory

```
1 from neulat.sampler.flow.coupling import NICE
2
3 coupling = NICE(
4 partitioner=partitioner,
5 net_factory=net_factory
\, 6 \,
```
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The partitioner *partitions* (or masks) the input into *active* and *passive* components.

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The net factory is a function that constructs the *conditioner*, e.g., a neural network that acts on the partitioned input.

### Coupling Flows: Partitioners

A very simple partitioner is the AltFlatPartitioner, which stands for alternating flattened partitioner

```
1 | partitioner = AltFlatPartitioner(feature_shape=(2, 2)),
2 \text{ input} = \text{torch. tensor}([\lbrack 1., 2.], \lbrack 3., 4. \rbrack]3 active, passive = partitioner(input)
4 active += 105 output = partitioner (active, passive)
```
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```
This will generate an output of 
$$
\begin{pmatrix} 11 & 2 \\ 13 & 4 \end{pmatrix}
$$

# Coupling Flows: Flipping Partitioners

Partitioners usually flip the active and pasive elements.

Such a partitioner can be created by calling .flip():

```
1 | flipped = partitioner.flip()
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3 active, passive = flipped(input)
4 active += 15 output = flipped(active, passive)
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```
This will generate an output of  $\begin{pmatrix} 1 & 12 \ 3 & 14 \end{pmatrix}$ 

$$
\begin{matrix}12\\14\end{matrix}
$$

### Coupling Flows: Net Factory (Conditioner)

The net factory define the conditioner  $\Theta$  that transforms the passive input:

$$
\mathbf{x}_{\text{active}}^{l+1} = h(\mathbf{x}_{\text{active}}^l, \Theta(\mathbf{x}_{\text{passive}}^l)
$$
(1)

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$$
(1)

```
1 from functools import partial
2 from neulat.sampler.flow.coupling.affine import NICE, MLP
3
4 net_factor = partial(
5 MLP,
6 n_blocks=3,
7 latent_size=1024,
8 activation=torch.nn.Tanh,
9 bias=False,
10 )
```
# Coupling Flows: Defining Couplings

The coupling Transform itself is mostly only concerned with implementing the coupling function h. E.g. in NICE:  $h(a, b) = a + b$ 

```
1 class NICE(Coupling):
2 Cwithlogdet
3 @partitioned
4 def forward(self, active, passive):
5 return active + self.net(passive), 1.
7 Withlogdet
8 @partitioned
9 def inverse(self, active, passive):
10 \vert return active - self.net(passive), 1.
```
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```
Recall: @withlogdet makes sure the log abs jacobian det is propagated.

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10 \vert return active - self.net(passive), 1.
```
New: @partitioned automates the partitioning/masking in subsequent couplings!

## Coupling Flows: Completing the Flow

Putting all the previous parts together, we can create a flow in the following way:

```
1 \mid flow = Flow(
2 base_distribution=Normal(0.0, 1.0, feature_shape=(8, 8)),
3 transform=6 * NICE(
4 partitioner=AltFlatPartitioner(feature_shape=(8, 8)),
5 net_factory=partial(MLP, n_blocks=3, latent_size=1024,
6 activation=torch.nn.Tanh, bias=False)
7
```
# Coupling Flows: Completing the Flow

Putting all the previous parts together, we can create a flow in the following way:

```
1 \mid f \cdot \overline{u} = F \cdot \overline{u}2 base_distribution=Normal(0.0, 1.0, feature_shape=(8, 8)),
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4 partitioner=AltFlatPartitioner(feature_shape=(8, 8)),
5 net_factory=partial(MLP, n_blocks=3, latent_size=1024,
6 activation=torch.nn.Tanh, bias=False)
7
```
Notice the transform=6  $*$  NICE. This creates a sequential transform of 6 Couplings, with alternating masking/partitioning!

# Coupling Flows: Traning

Training of the flow with ReverseKL is straight forward:

```
1 from neulat.loss import ReverseKLLoss
2
3 optim = torch.optim.Adam(flow.transform.parameters(), 1r=5e-4)
4 | loss_fn = ReverseKLLoss()
5 for \sin range(1000):
6 configs, log\_probs = flow.sumple\_with\_logprob(10)7 loss = loss_fn(action(configs), log_probs) # loss contains `mean` and `std`
8 optim.zero_grad()
9 loss.mean.backward() # we train only using the loss `mean`
10 optim.step()
```
#### Estimating Observables from i.i.d. Samples

Observables themselves are classes in NeuLat. In order to estimate them, we additionally need an Estimator, and configurations. For instance:

```
1 from neulat.observable.base import AbsMagnetization, Magnetization
2 from neulat.estimator.base import IidEstimator
3
4 observables = [AbsMagnetization(), Magnetization(), action]
5 iid estimator = IidEstimator(observables)
6 \vert configs = flow.sample(1000)
7 flow_statistics = iid_estimator.named_evaluate(configs)
```
The dict flow statistics will contain one entry per observable, e.g.:

 $\{$ 'absmag': Statistics(mean=0.6408, std=0.0473), 'mag': ...}

#### Estimating Observables from Correlated Samples

Estimation of Observables from correlated samples (e.g., from HMC) requires the use of the appropriate estimator:

```
1 from neulat.estimator.base import CorrelatedEstimator
2
3 correlated_estimator = CorrelatedEstimator(observables)
4 \vert configs = hmc.sample(1000)
5 \lnmc_statistics = correlated_estimator.named_evaluate(configs)
```
The dict hmc statistics will instead contain correlated statistics objects,

```
{'absmag': CorrelatedStatistics(mean=32.82628, std=1.4674,
tau int=0.5909, tau int err=0.3162), ...}
```
To obtain an unbiased estimator, Nicoli et. al proposed to use Importance Sampling. This additionally requires the logprobs of the flow, as well as the specific action:

```
1 from neulat.estimator.base import ImportanceSamplingEstimator
2
3 flow_configs, flow_logprobs = flow.sample_with_logprob(1000)
4 iw_estimator = ImportanceSamplingEstimator(observables, action)
5 \int flow_iw_stats = iw_estimator.evaluate(flow_configs, flow_logprobs)
```
The dict flow iw statistics will contain the same Statistics object the IidEstimator returned:

 $\{$ 'absmag': Statistics(mean=2.6021, std=0.4674, ... $\}$ 



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- **NOUR FEATURE HERE!**

We want NeuLat to be a community effort! Please reach out to us!

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NeuLat will be available soon at

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Thank you for your attention!