

B-meson semileptonic decays with highly improved staggered quarks

Andrew Lytle

University of Illinois @ Urbana-Champaign

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Bonn, Germany

FNAL-MILC allhisq working group

Carleton DeTar

Elvira Gámiz

Steve Gottlieb

William Jay

Aida El-Khadra

Andreas Kronfeld

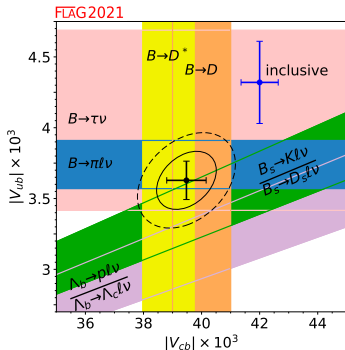
Jim Simone

Alejandro Vaquero

Motivation

- Semileptonic decays are a rich source of information for determining CKM matrix elements.
- Relatively simple decay processes – measured in accelerator experiments, require theoretical input from lattice QCD to extract fundamental parameters.
- Desire precise measurements of $|V_{xb}|$ from multiple decay processes to test the consistency of the Standard Model.

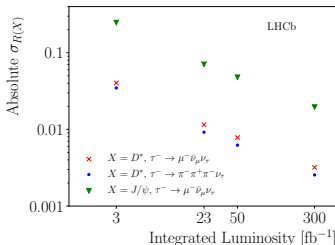
Stress-testing the CKM paradigm



- Inclusive/exclusive discrepancies for $|V_{ub}|$ and $|V_{cb}|$
- Also discrepancies from SM expectations in $R(D, D^*, J/\psi, K^*, \dots)$ see e.g. Snowmass 2205.15373
- \rightarrow Want high accuracy SM predictions for sl decays

Experimental outlook - $|V_{cb}|$ and V_{ub}

- Belle II
 - ▶ $\delta|V_{cb}| \approx 2\% \rightarrow 1.4\%$ by ~ 2025 .
 - ▶ $\delta|V_{ub}| \approx 2\% \rightarrow 1.2\%$ by ~ 2025 .
- Increasing precision of measured R -ratios:



- New channels LHCb 2012.05143, 2001.03225:

$$|V_{cb}| = 42.3(8)_{\text{stat}}(9)_{\text{syst}}(12)_{\text{ext}} \times 10^{-3} \quad \text{LHCb } B_s \rightarrow D_s^{(*)}$$

$$|V_{cb}| = 38.3(3)_{\text{stat}}(7)_{\text{syst}}(6)_{\text{lqcd}} \times 10^{-3} \quad \text{Belle total } B \rightarrow D^*$$

Outline

1. Intro & Motivation.
2. Computational framework.
3. Status and preliminary results.
 - ▶ Two-point and three-point correlators.
 - ▶ Form factor results.
 - ▶ Renormalization.
4. Summary & Outlook.

Heavy quarks

Treatment of c and especially b quarks challenging in lattice simulation due to lattice artifacts which grow as $(am_h)^n$

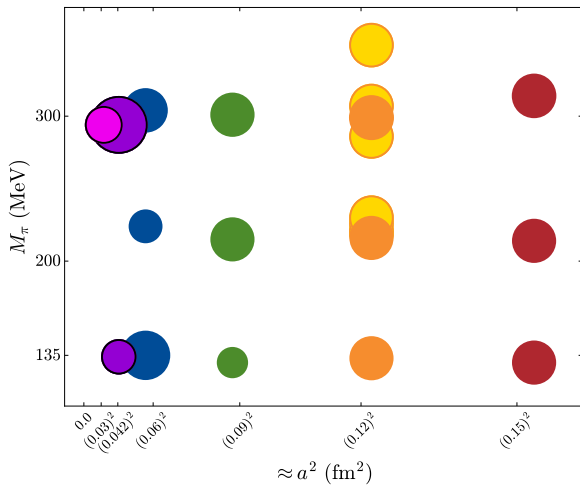
- May use an effective theory framework to handle the b quark.
 - ▶ Fermilab method, RHQ, OK, NRQCD
 - ▶ Pros: Solves problem w/ am_h artifacts.
 - ▶ Cons: Requires matching, can still have ap artifacts.
- Also possible to use relativistic fermion provided a is sufficiently small $am_c \ll 1$, $am_b < 1$.
 - ▶ Use improved actions e.g. $\mathcal{O}(a^2) \rightarrow \mathcal{O}(\alpha_s a^2)$
 - ▶ Pros: Absolutely normalised current, straightforward continuum extrap.
 - ▶ Cons: Numerically expensive, extrapolate $m_h \rightarrow m_b$.

allhisq simulations

- Here we simulate *all* quarks with the HISQ action.
- Unified treatment for wide range of $B_{(s)}$ (and $D_{(s)}$) to pseudoscalar transitions:
 - ▶ $B_{(s)} \rightarrow D_{(s)}$
 - ▶ $B_{(s)} \rightarrow K$
 - ▶ $B \rightarrow \pi$
- Ensembles with (HISQ) sea quarks down to physical at each lattice spacing.

See Will Jay's talk on $D_{(s)} \rightarrow$ light transitions in this session.

- HISQ fermion action.
 - ▶ Discretization errors begin at $\mathcal{O}(\alpha_s a^2)$.
 - ▶ Designed for simulating heavy quarks (m_c and higher at current lattice spacings).
- Symanzik-improved gauge action, takes into account $\mathcal{O}(N_f \alpha_s a^2)$ effects of HISQ quarks in sea. [0812.0503]
- Multiple lattice spacings down to ~ 0.042 (now 0.03) fm.
- Effects of u/d , s , and c quarks in the sea.
- Multiple light-quark input parameters down to physical pion mass.
 - ▶ Chiral fits.
 - ▶ Reduce statistical errors.



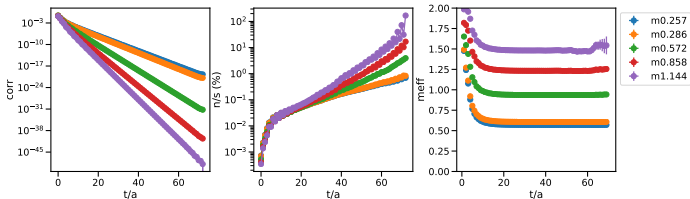
- Use a heavy valence mass h as a proxy for the b quark.
- Work at a range of m_h , with $am_c < am_h \lesssim 1$ on each ensemble. On sufficiently fine ensembles, m_h is near to m_b (e.g. m_b at $am_h \approx 0.65$ on $a = 0.03$ fm).
- Map out physical dependence on m_h , remove discretisation effects $\sim (am_h)^{2n}$ using information from several ensembles. Extrapolate results $a^2 \rightarrow 0, m_h \rightarrow m_b$.

Preliminary results

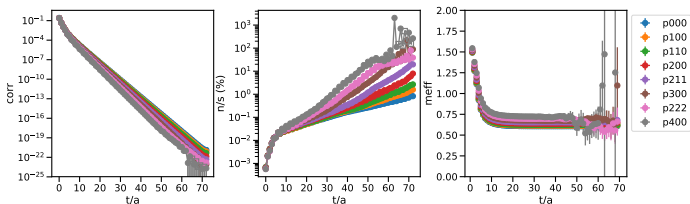
Two point functions

Consider $B_{(s)} \rightarrow D_{(s)}$ decays for $a = 0.06$ fm, $m_l/m_s = 0.1$.

- Compute $H_{(s)}$ mesons at a range of am_h values:

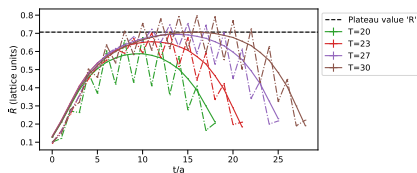
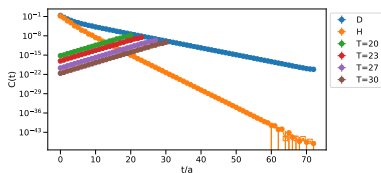


- $D_{(s)}$ mesons for a range of momenta:



Three point functions

- Generate three-point functions for scalar, vector, and tensor current insertions, $\langle D_{(s)}(T) J(t) H_{(s)}^\dagger(0) \rangle$.
- Fit simultaneously with two-point functions to extract the matrix elements of interest $\rightarrow \langle D_{(s)} | J | H_{(s)} \rangle$



- We use scalar (S), and vector (V^0, V^i) current insertions to extract the form factors f_0 and f_+ .

Extracting form factors

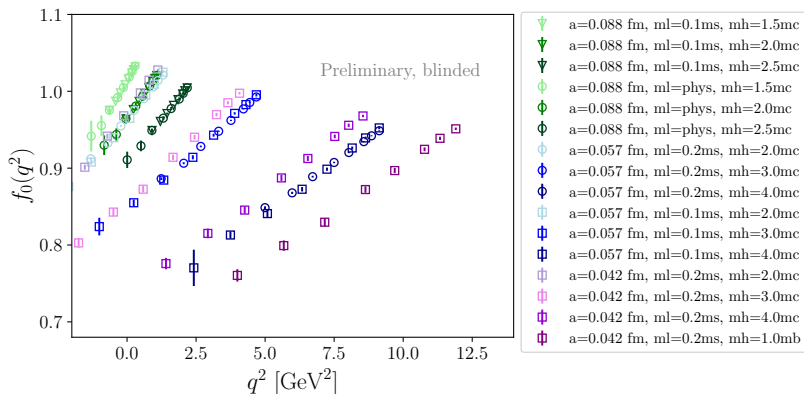
$$f_0(q^2) = \frac{m_h - m_\ell}{M_H^2 - M_L^2} \langle L|S|H \rangle$$

$$f_{\parallel}(q^2) = Z_{V^0} \frac{\langle L|V^0|H \rangle}{\sqrt{2M_H}}$$

$$f_{\perp}(q^2) = Z_{V^i} \frac{\langle L|V^i|H \rangle}{\sqrt{2M_H}} \frac{1}{p_L^i},$$

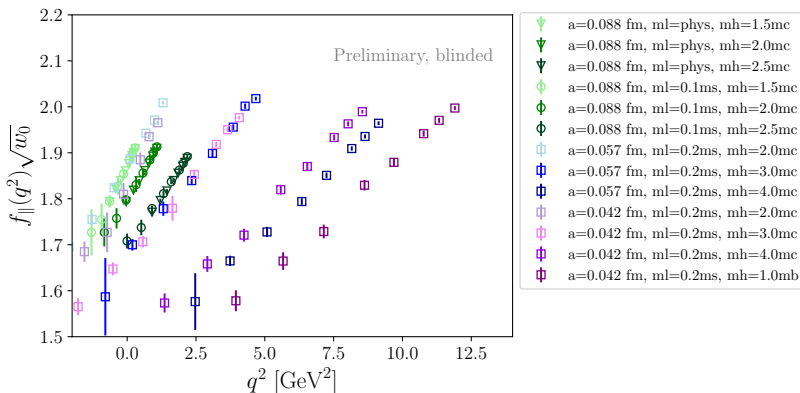
$$f_+ = \frac{1}{\sqrt{2M_H}} (f_{\parallel} + (M_H - E_L)f_{\perp}).$$

$B_s \rightarrow D_s: f_0(q^2)$



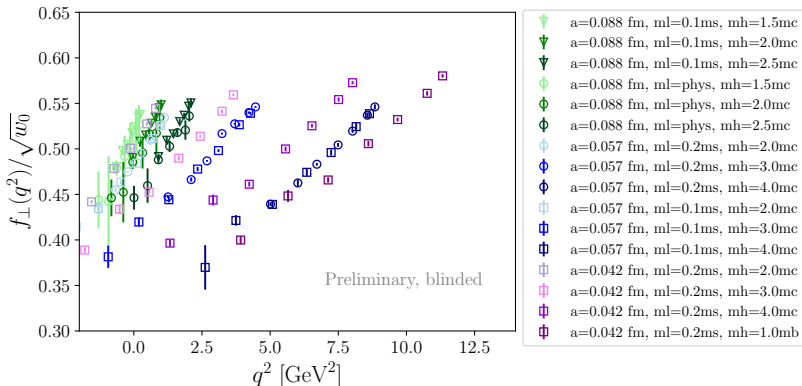
- Good precision out to $p = 400$
- Rightmost points on figure have $m_h = m_b$

$B_s \rightarrow D_s: f_{\parallel}(q^2)$



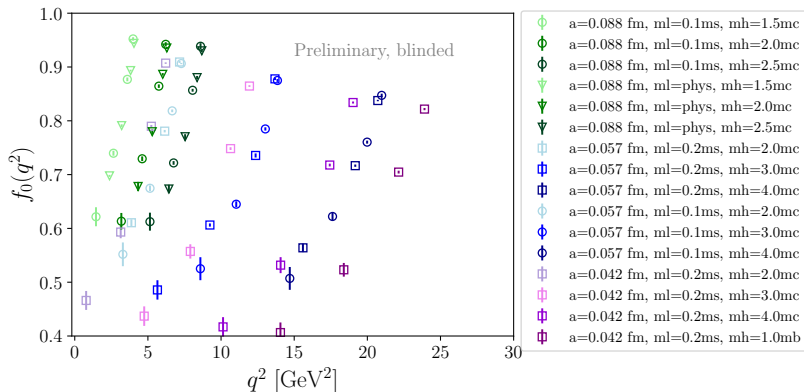
- Good precision out to $p = 400$
- Rightmost points on figure have $m_h = m_b$

$B_s \rightarrow D_s: f_{\perp}(q^2)$



- Good precision out to $p = 400$
- Rightmost points on figure have $m_h = m_b$

$B_s \rightarrow K: f_0(q^2)$



- Good precision out to $p = 300$
- Rightmost points on figure have $m_h = m_b$
- Mild sea quark mass dependence

Normalization of vector currents

We renormalize the vector current by applying the partially conserved vector current (PCVC) relation directly to extracted matrix elements:

$$\partial_\mu V_\mu^{\text{cons}} = (m_h - m_l)S$$

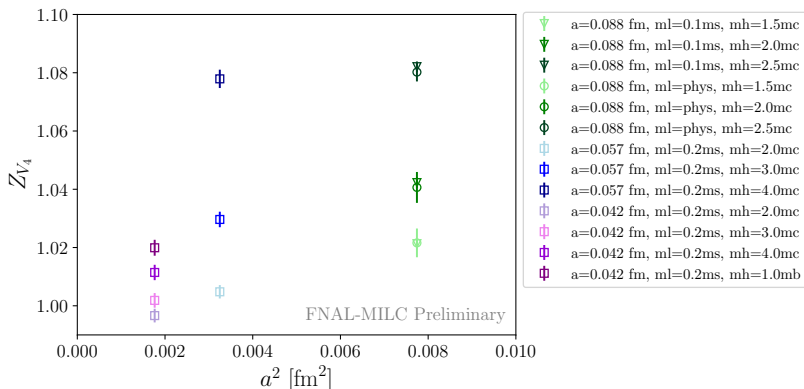
Applied to our lattice matrix elements,

$$Z_{V^0}(M_H - E_L)\langle L|V^0|H\rangle + Z_{V^i}\mathbf{q} \cdot \langle L|\mathbf{V}|H\rangle = (m_h - m_l)\langle L|S|H\rangle,$$

where V^0 is local and V^i is a one-link current.

Renormalization - Z_{V_4}

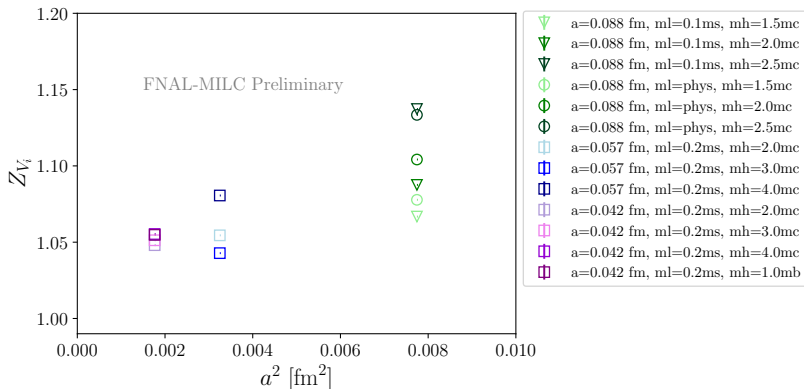
- Z_{V_4} determined from zero-momentum vector and scalar correlators.
- $Z_{V_0}(M_H - E_L)\langle L|V^0|H\rangle = (m_h - m_l)\langle L|S|H\rangle$



- Z-factors tend towards 1 as $a \rightarrow 0$, $am \rightarrow 0$.

Renormalization - Z_{V_i}

- Z_{V_i} determined from non-zero momentum correlators.
- Here use $\mathbf{p} = (3, 0, 0)$ data (need to fit/optimize).

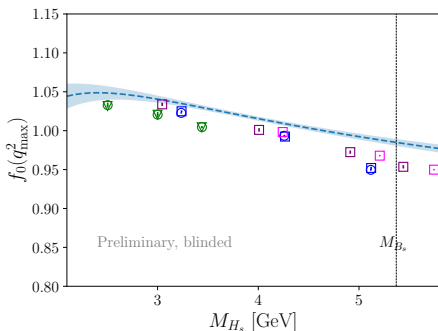


- Z-factors tend towards 1 as $a \rightarrow 0$, $am \rightarrow 0$.

$B_s \rightarrow D_s$ - a simple $f_0(q_{\max}^2)$ fit

Basic fit parameterizing M_H dependence and heavy quark discretization. Chiral variation ignored.

$$f_0(q_{\max}^2)[M_H, am_h] = \sum_{ij} c_{ij} \left(\frac{1}{M_H} \right)^i (am_h)^{2j}$$



Good precision obtained ($\sim 0.5\%$) at M_{B_s} .

Summary & Outlook

- Unified treatment for range of semileptonic decays.
- HISQ action used for *all* quarks.
- Good statistical precision (percent-level) achieved.
- Small discretization effects.
- Will permit *interpolation* in both m_l and m_h .

Thank you!

