

Study of charm and beauty in QGP from unquenched lattice QCD

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HOTQCD collaboration

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Correlators and SPFs

The spectral function

Lattice correlators

Outlook

Correlators and spectral functions

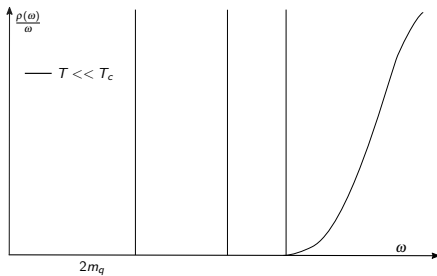
- Heavy $q\bar{q}$: a thermometer of QGP in heavy ion collisions
- The spectral functions $\rho_H(\omega)$ contains information about the in-medium hadron properties

$$\sum_{\vec{x}} \langle \bar{\psi} \Gamma_H \psi(\tau, \vec{x}) (\bar{\psi} \Gamma_H \psi(0, \vec{0}))^\dagger \rangle \equiv G_H(\tau) = \int_0^\infty \frac{\omega}{\pi} \rho_H(\omega) \frac{\cosh(\omega(\tau - \frac{1}{2T}))}{\sinh(\frac{\omega}{2T})}$$

Strategy:

- $G_H(\tau)$ on the lattice
- Extract spectral function
- Estimate in-medium hadronic properties
- In addition transport coefficients, like heavy quark diffusion coefficients, are encoded in the vector meson spectral function

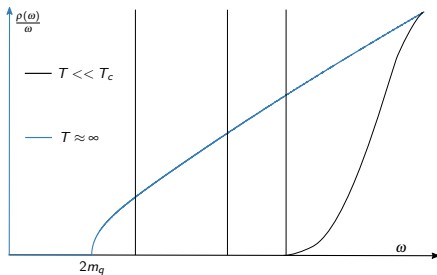
The spectral function



Ref. [H. Sandmeyer's thesis]

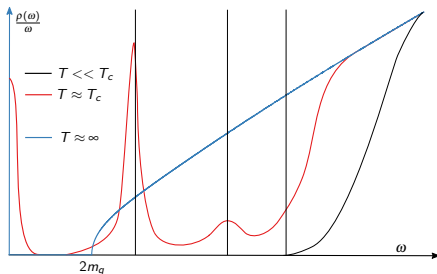
The spectral function

- At infinite temperature there cannot be bound states



Ref. [H. Sandmeyer's thesis]

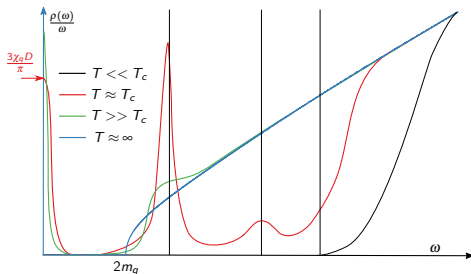
The spectral function



- At infinite temperature there cannot be bound states
- Melting of states visualizes in **shrinking and broadening of bound peaks**

Ref. [H. Sandmeyer's thesis]

The spectral function



- At infinite temperature there cannot be bound states
- Melting of states visualizes in **shrinking and broadening of bound peaks**
- **Heavy quark diffusion constant** can be read off in vector channel

$$D = \frac{\pi}{3\chi_q} \lim_{\omega \rightarrow 0} \sum_{i=1}^3 \frac{\rho_V(\omega, T)}{\omega}$$

Extraction of spectral function is ill-posed problem → large lattices needed. Ref. [H. Sandmeyer's thesis]

SPF's contribution to correlators

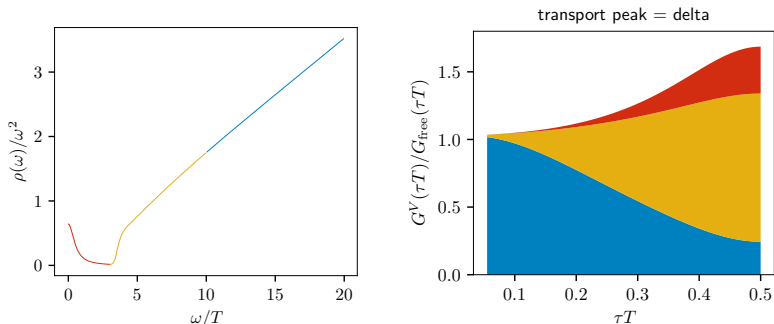
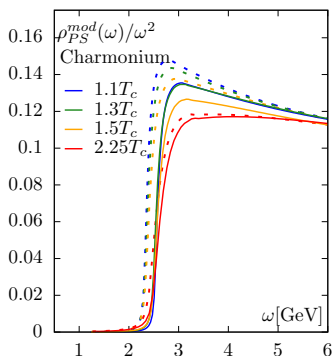
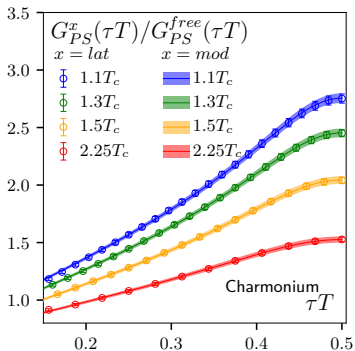


Figure: Visualization of which parts of the spectral function contribute to the correlator at different τT . Ref. [H. Sandmeyer's thesis]

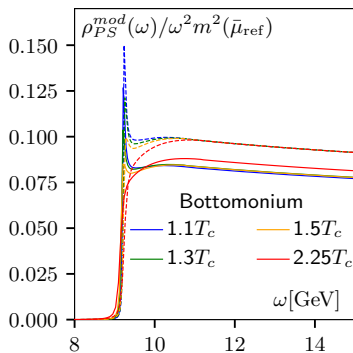
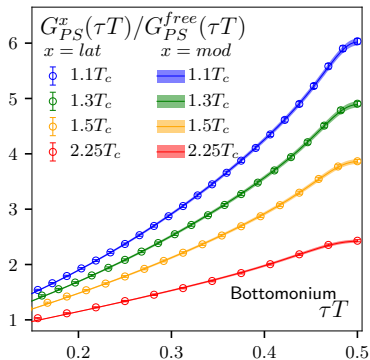
Spectral reconstruction (Quenched)

$$\rho_{PS}^{pert}(\omega) = A^{match} \rho_{PS}^{VAC}(\omega) + \rho_{PS}^{THERM}(\omega)$$

$$\rho_{PS}^{mod}(\omega) = A \rho_{PS}^{pert}(\omega - B)$$

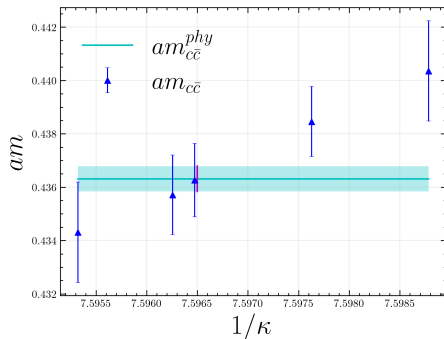


Spectral reconstruction (Quenched)



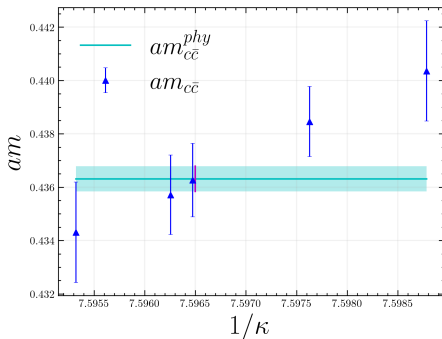
Ref. [JHEP 11 (2017) 206, A. Lorenz's thesis]

Mass tuning on mixed action (Full QCD)



- Mixed action approach (Wilson Clover fermions on HISQ configurations)
- Tadpole improved tree-level, $c_{SW} = \frac{1}{u_0^3}$, $u_0 = (tr[U_{\mu\nu}])^{\frac{1}{4}}$
- Quark mass tuning
- Tune spectrum to experimental values

Mass tuning on mixed action (Full QCD)



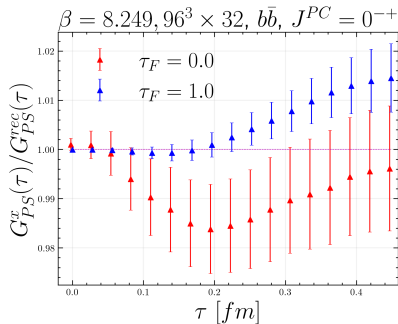
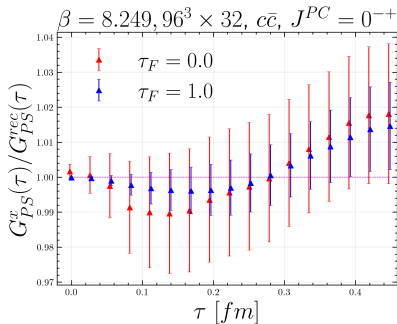
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- HISQ lattices from HotQCD (arXiv:2110.11659) ($m_l = m_s/5$); $64^3 \times 64$, $96^3 \times 32$, new temperatures at $96^3 \times 56$ and $96^3 \times 28$
- Gradient flow (renormalizes the operators, removes cut-off and mixed action effects and improves signal-to-noise ratio)

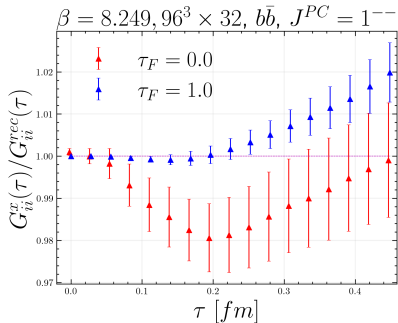
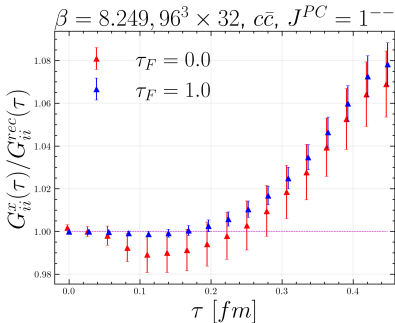
Full QCD (HOTQCD PRELIMINARY)

$N_f=2+1$ HISQ, $a^{-1} = 7$ GeV, $m_l = m_s/5$

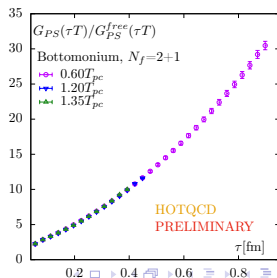
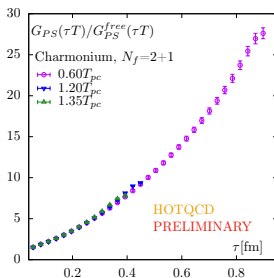
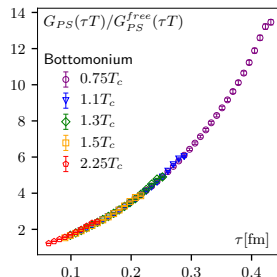
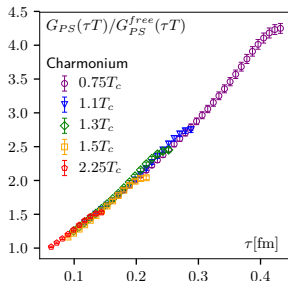
$$G_H^{rec}(\tau, T, T') = \int_0^\infty \frac{\omega}{\pi} \rho_H(\omega, T') \frac{\cosh(\omega(\tau - \frac{1}{2T}))}{\sinh(\frac{\omega}{2T})}$$



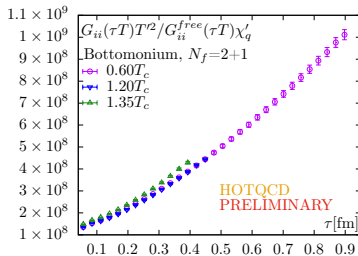
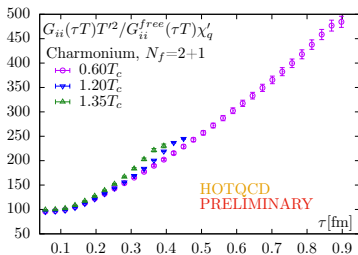
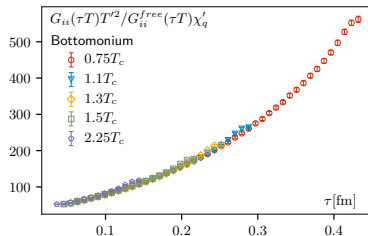
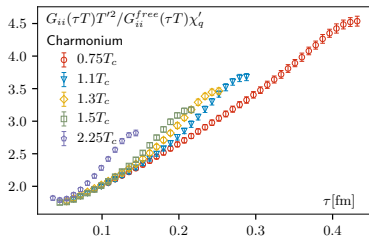
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Correlators: Quenched VS Unquenched



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Outlook

- Extend the studies on spectral and transport properties from quenched to dynamical QCD
- Study light quark mass effects by comparing $m_l = m_s/5$ and $m_l = m_s/27$
- Study cut-off effects and perform continuum extrapolation
- Improve on perturbative and non-perturbative spectral function models
- Spectral reconstruction based on spectral function model fits and other reconstruction methods
- Estimate in-medium hadronic and transport properties (Kubo relation)

Thank you for your attention !