

# Exploring the large $N_c$ limit with one quark flavour

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# Study SUSY with $N_f = 1$ QCD

- Simulate SUSY without the need to simulate SUSY



previous work

Corrigan & Ramond, 1979

hep-th/0309252      hep-th/0403071

hep-th/0603045      hep-th/0609187

hep-lat/0810.0161

# Study SUSY with $N_f = 1$ QCD

- Simulate SUSY without need to simulate SUSY
  - Study spectrum and compare to EFT

$$\frac{M_{PS}}{M_S} = 1 - \frac{22}{9N_c} - \frac{4}{9}\beta + \mathcal{O}(1/N_c^2)$$

hep-th/0309252

- Equivalence

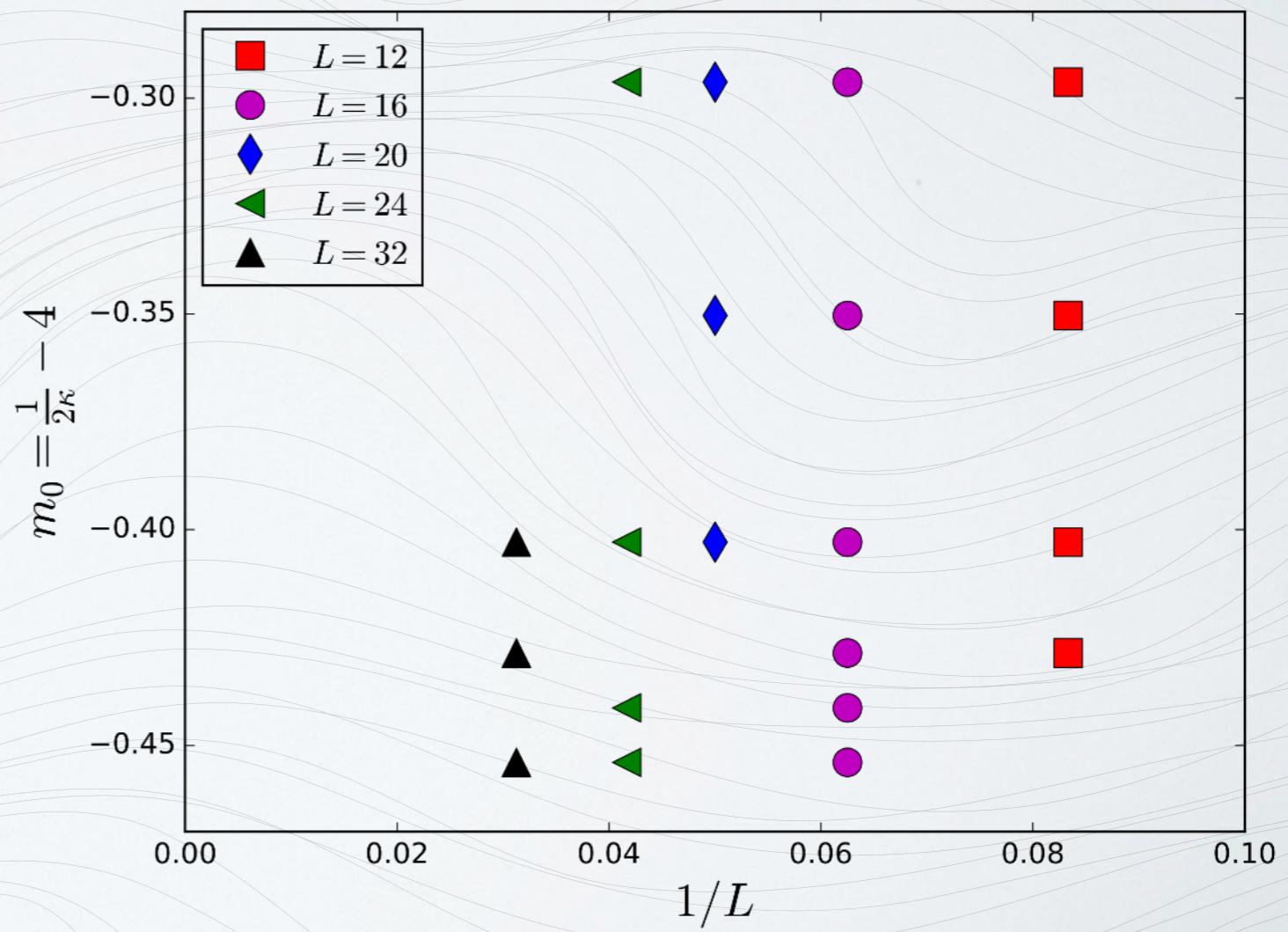
$$\frac{M_{PS}}{M_S} = 1 - \frac{2}{N_c} + \dots$$

hep-th/0508107

- @ Lattice: Compute masses and check the ratio

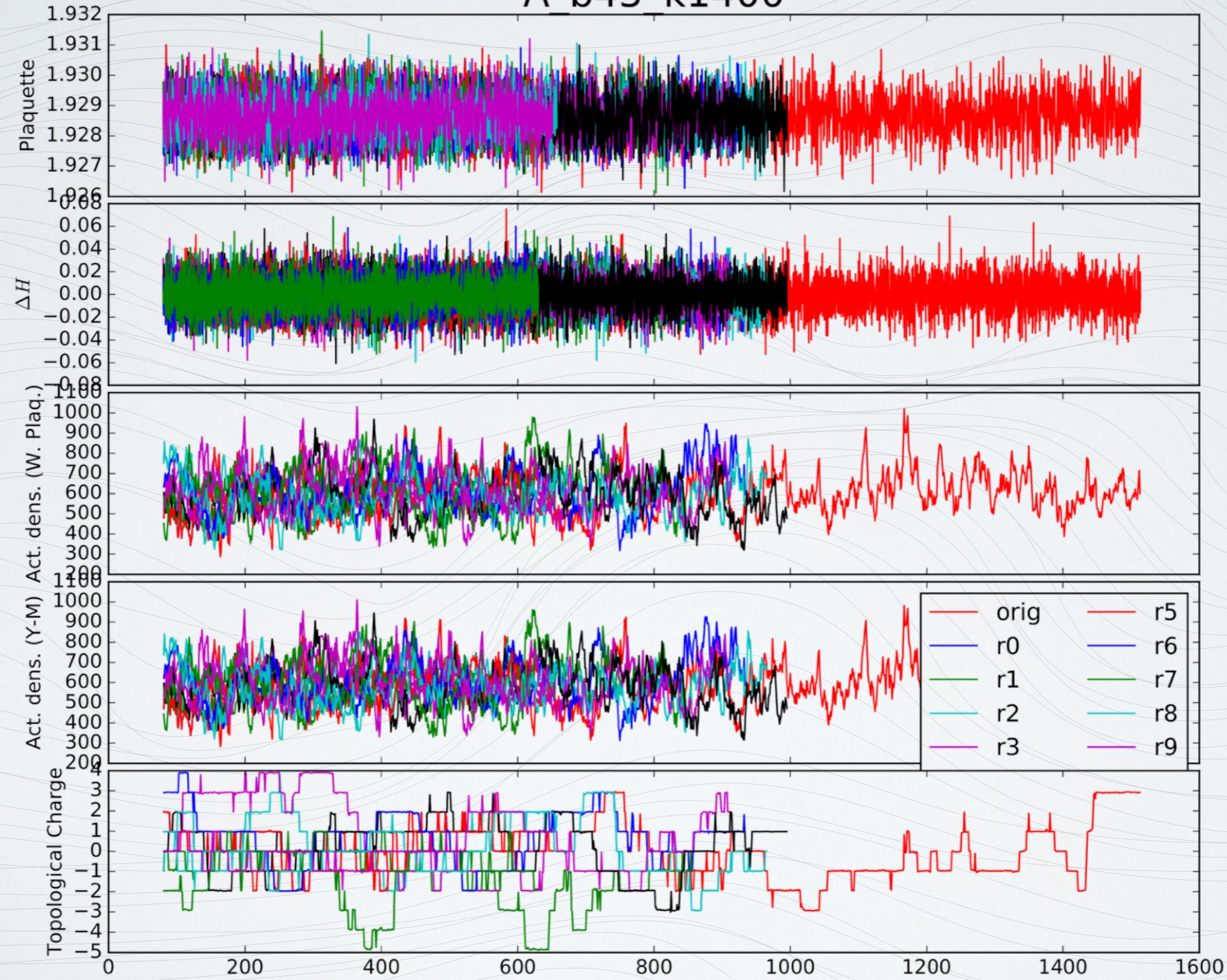
# Lattice Setup

- Our setup
  - Gauge: Symanzik improved gauge action ( $\beta = 4.5$ )
  - Fermion:  $\mathcal{O}(a)$  improved Wilson fermions ( $c_{sw} = 1$ )
  - 5 × Volumes
  - 6 × Masses
  - $a \sim 0.06 \text{ fm}$
- One Flavour
  - Use RHMC
  - Monitor eigenvalues
  - $\det M > 0 ?$

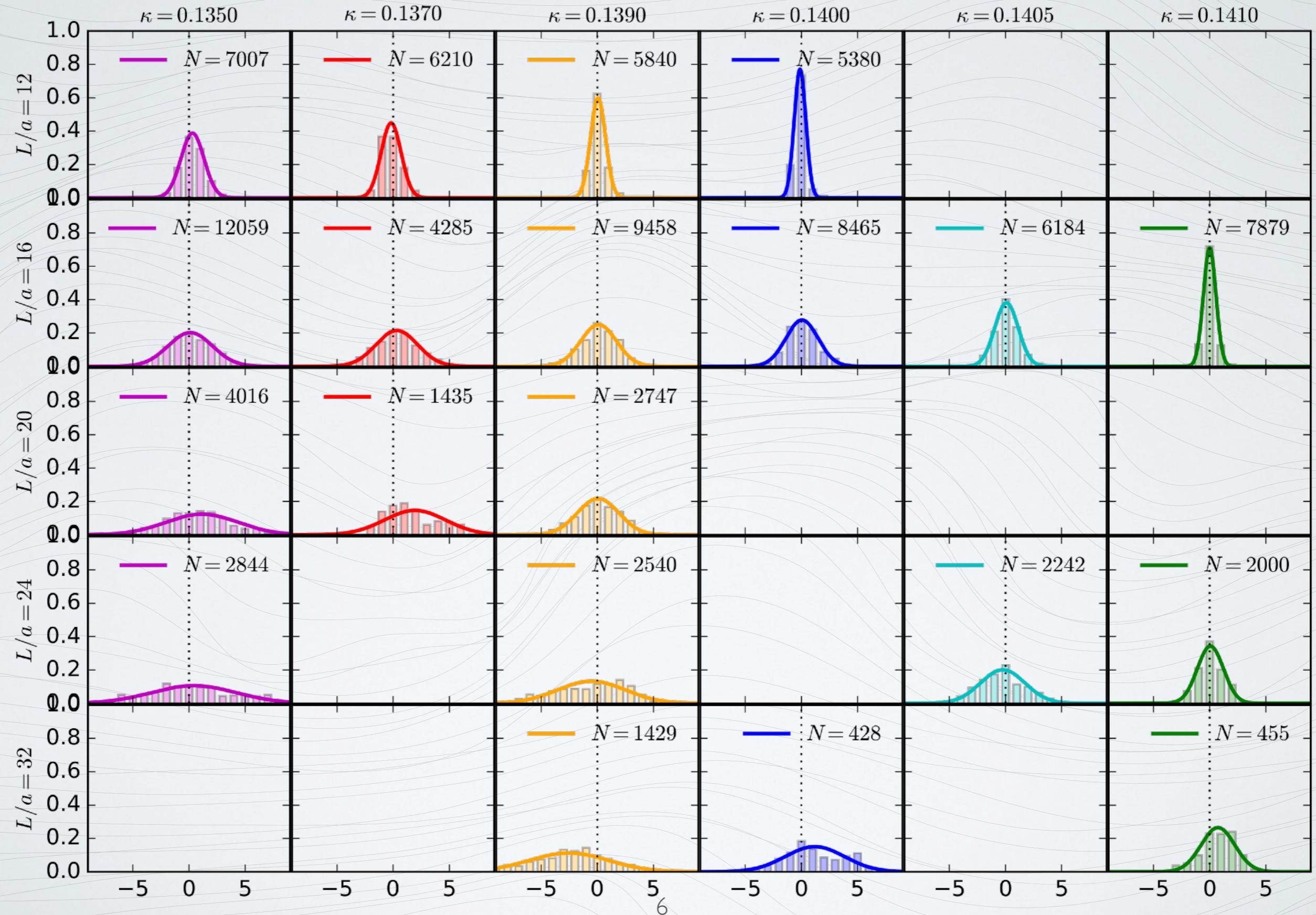


# Typical run

A b45 k1400



# Topological Charge



# Comment on Eigenvalues

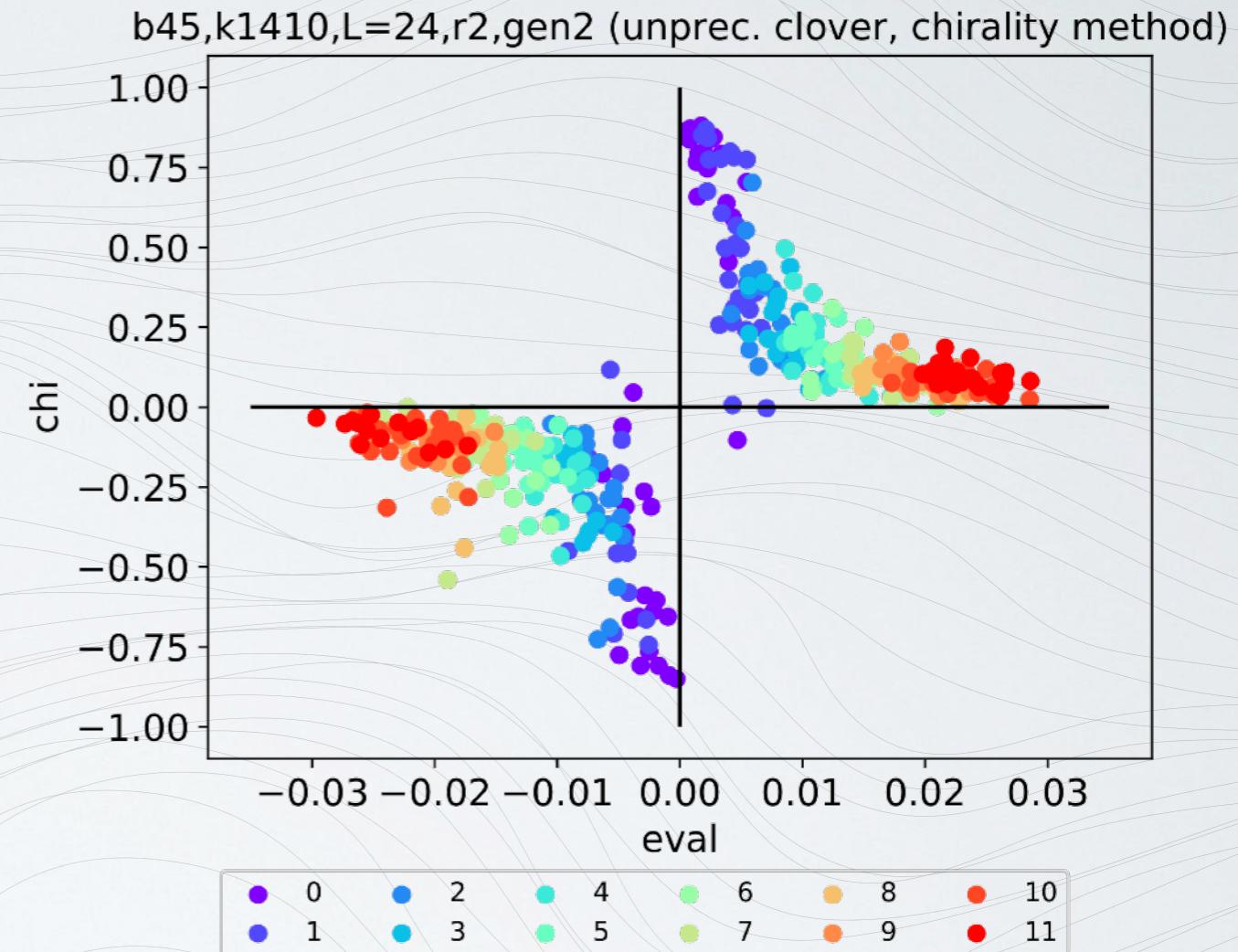
- One Flavour simulation

- Wilson fermions
- $\det(M) < 0$  possible
- Monitor eigenvalues
- Tracking method

2003.13359

- Check eigenvalues

- $L/a = 16$ :  $\det(M) > 0$  for all config
- $L/a = 24$ :  $\det(M) < 0$  for about  $\lesssim 1\%$  config



# Spectrum

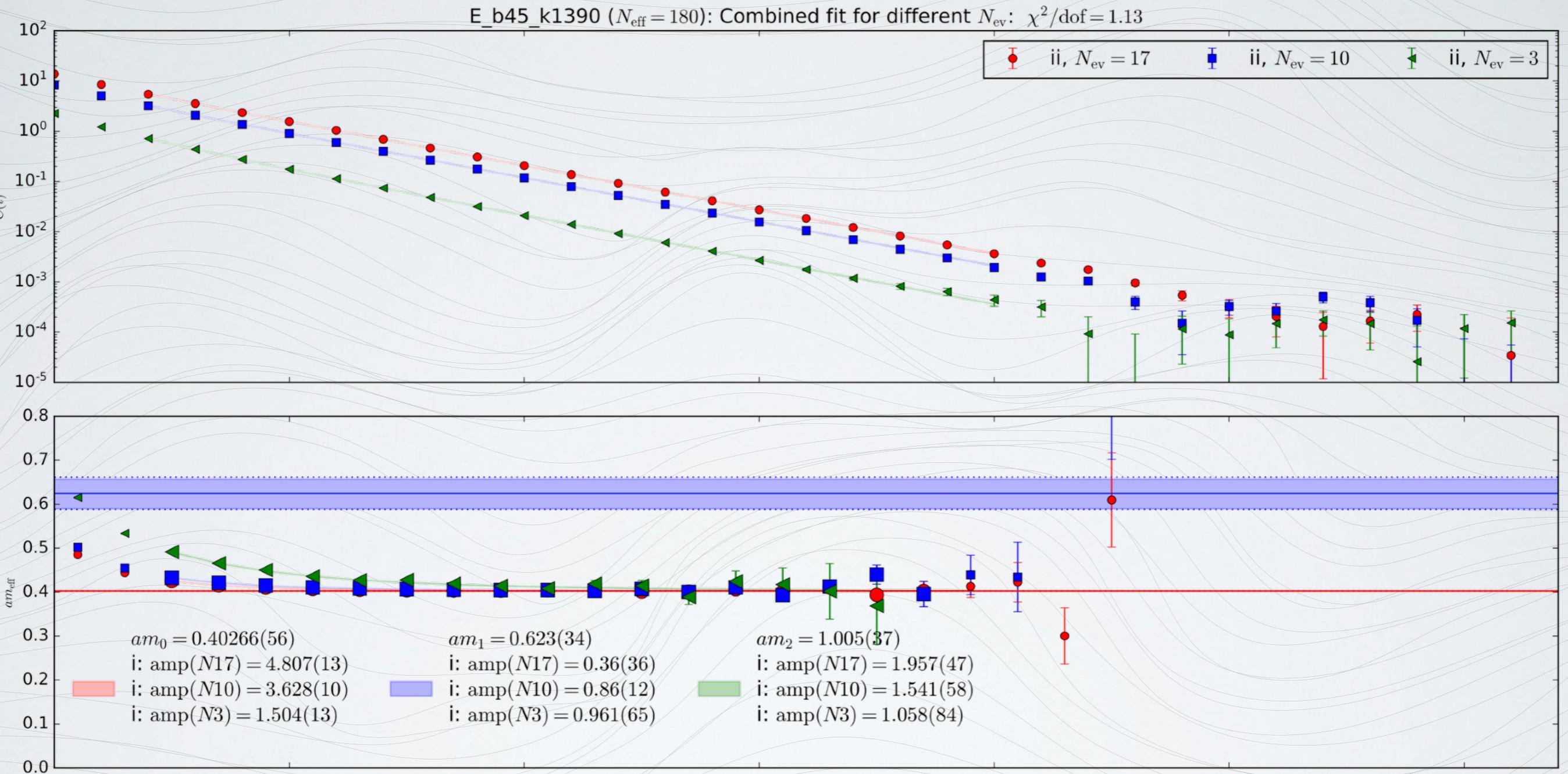
- Compute the spectrum

- Ground state + excited states

$$C_{ij}(t) = \sum_n \langle 0 | \hat{O}_i | n \rangle \langle n | \hat{O}_j^\dagger | 0 \rangle e^{-t m_n}$$

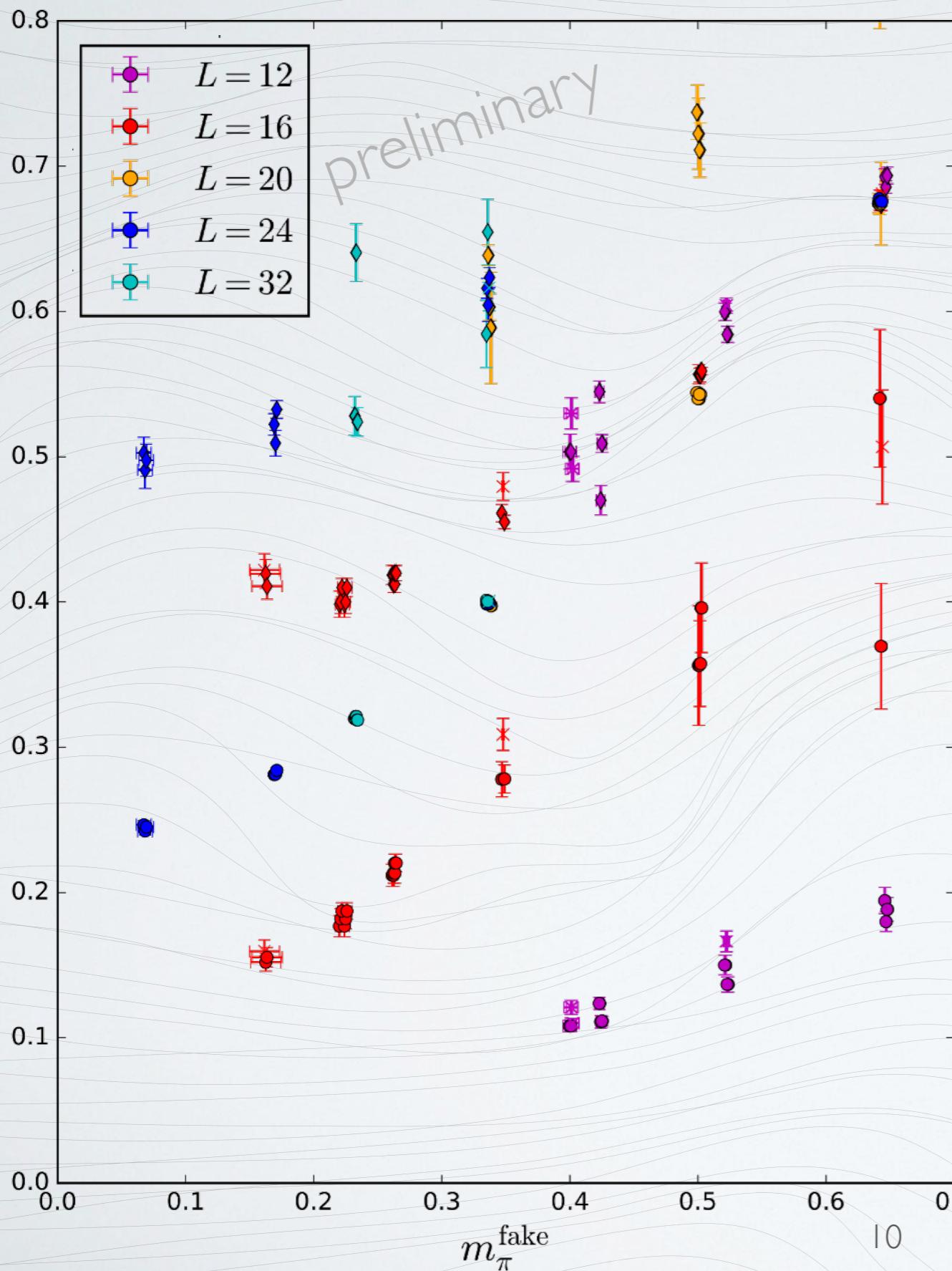
- Operators: scalar (**S**), glue (**G**), vector (**V**), pseudo-scalar (**P**)
- LapH method
  - Disconnected diagram included :)
  - Multiple levels of smearing

# Fitting the Correlators



- Simultaneous fit to different levels of smearing

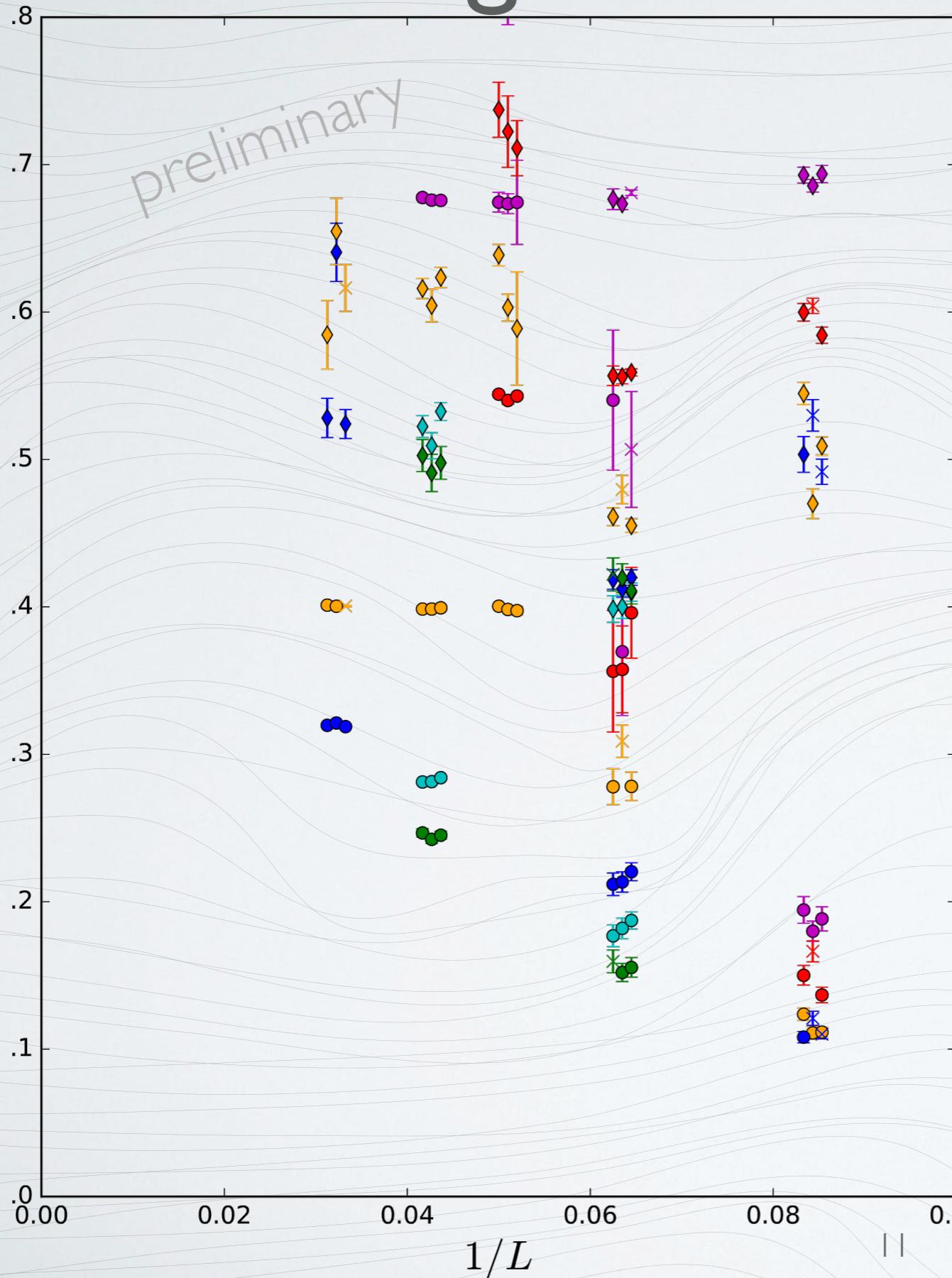
# Making sense of the spectrum



- Vector mass
- Two lowest lying states
- $m_{\pi}^{fake}$ : Connected pion corr.

state	$\bar{q}$	$\Gamma$	$q$	glue ball
vol. dep			<span style="color:red;">X</span>	<span style="color:red;">X</span>
mass dep.		<span style="color:green;">✓</span>	<span style="color:red;">(X)</span>	

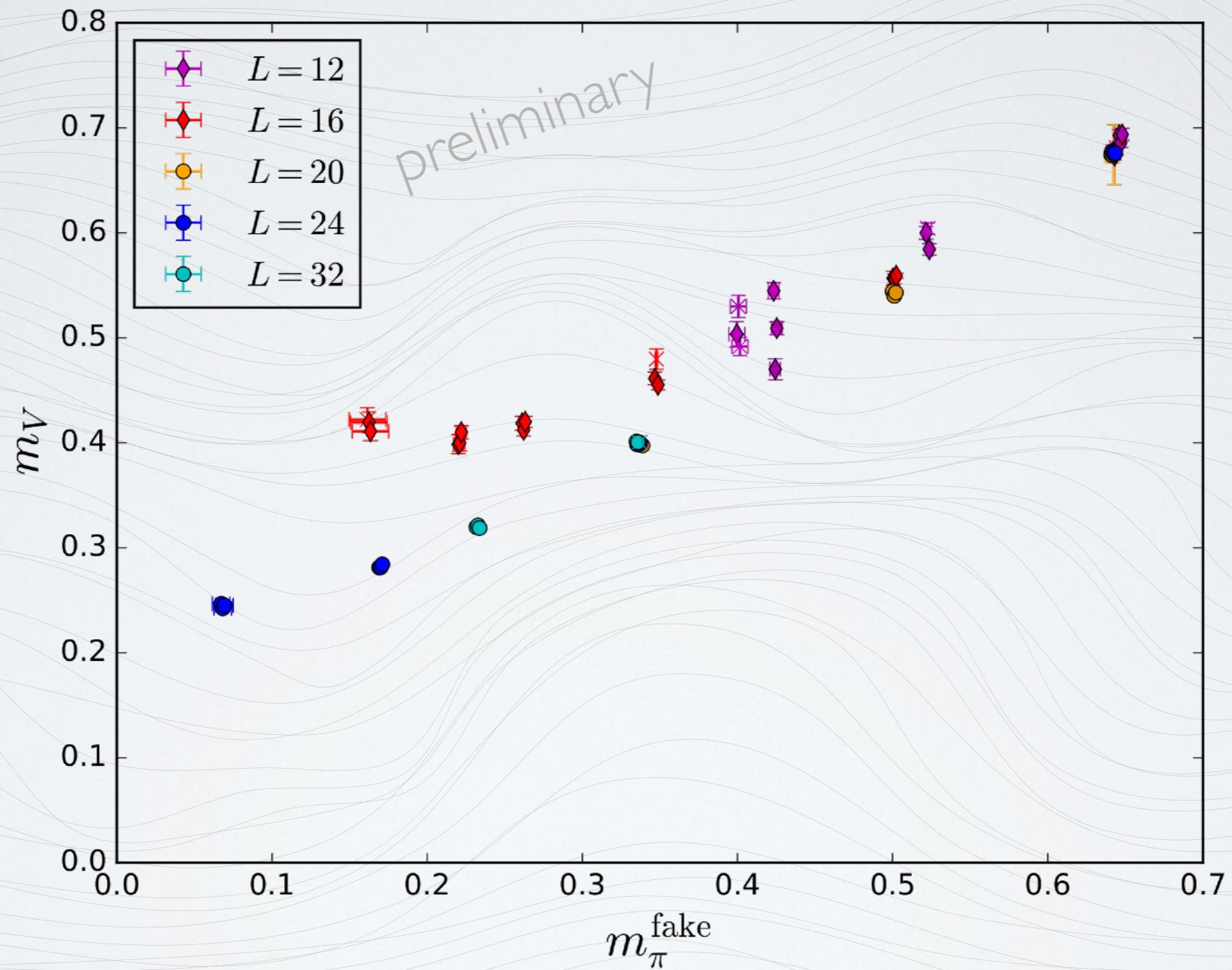
# Making sense of the spectrum



- Vector mass
- Two lowest lying states
- Volume dependence
- Different colour  $\leftrightarrow$  masses

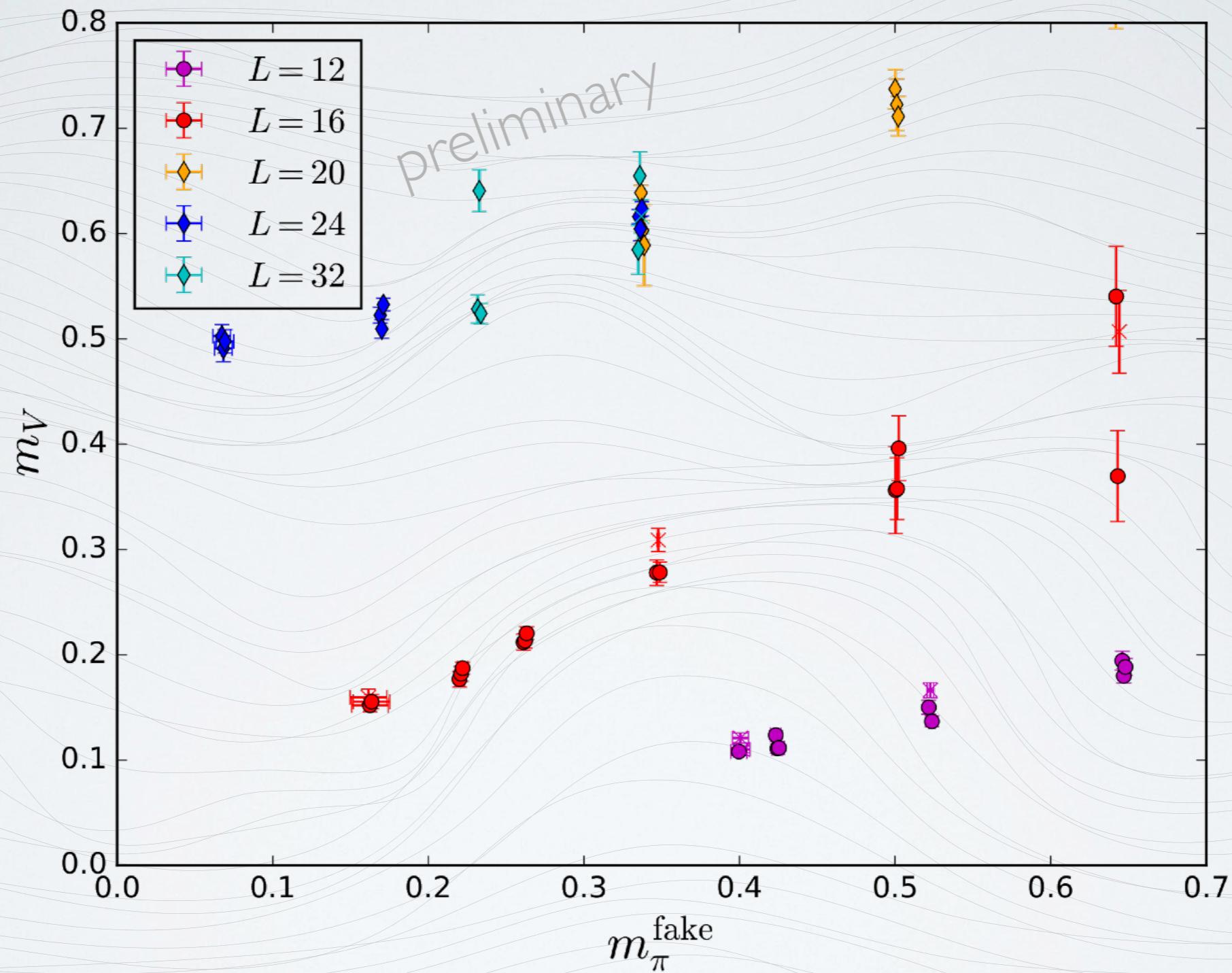
state	$\bar{q} \Gamma q$	glue ball
vol. dep.	X	X
mass dep.	✓	(X)

# Results - Vector



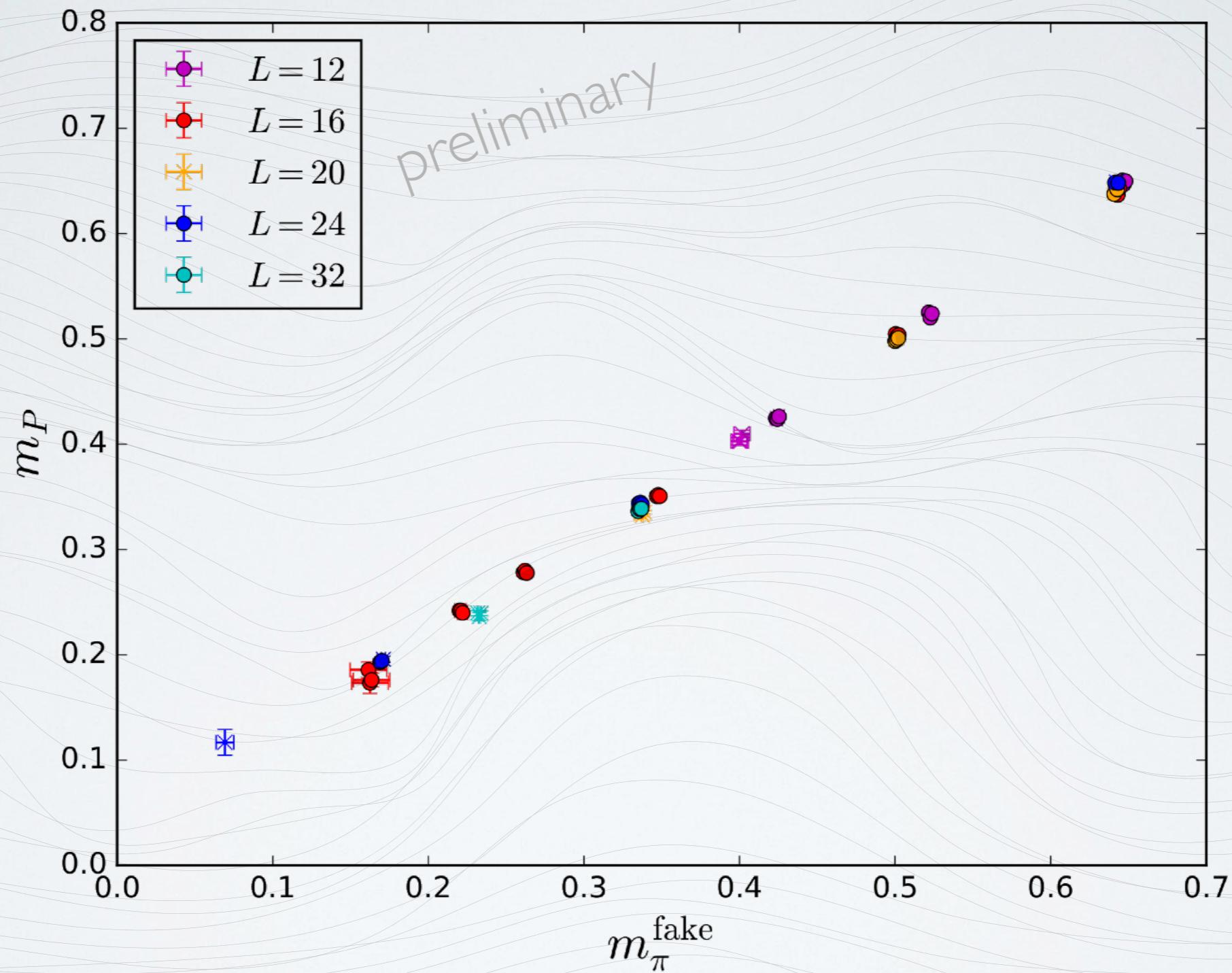
$\bar{q}\Gamma q$  state - clear mass dependence

# Results - Vector



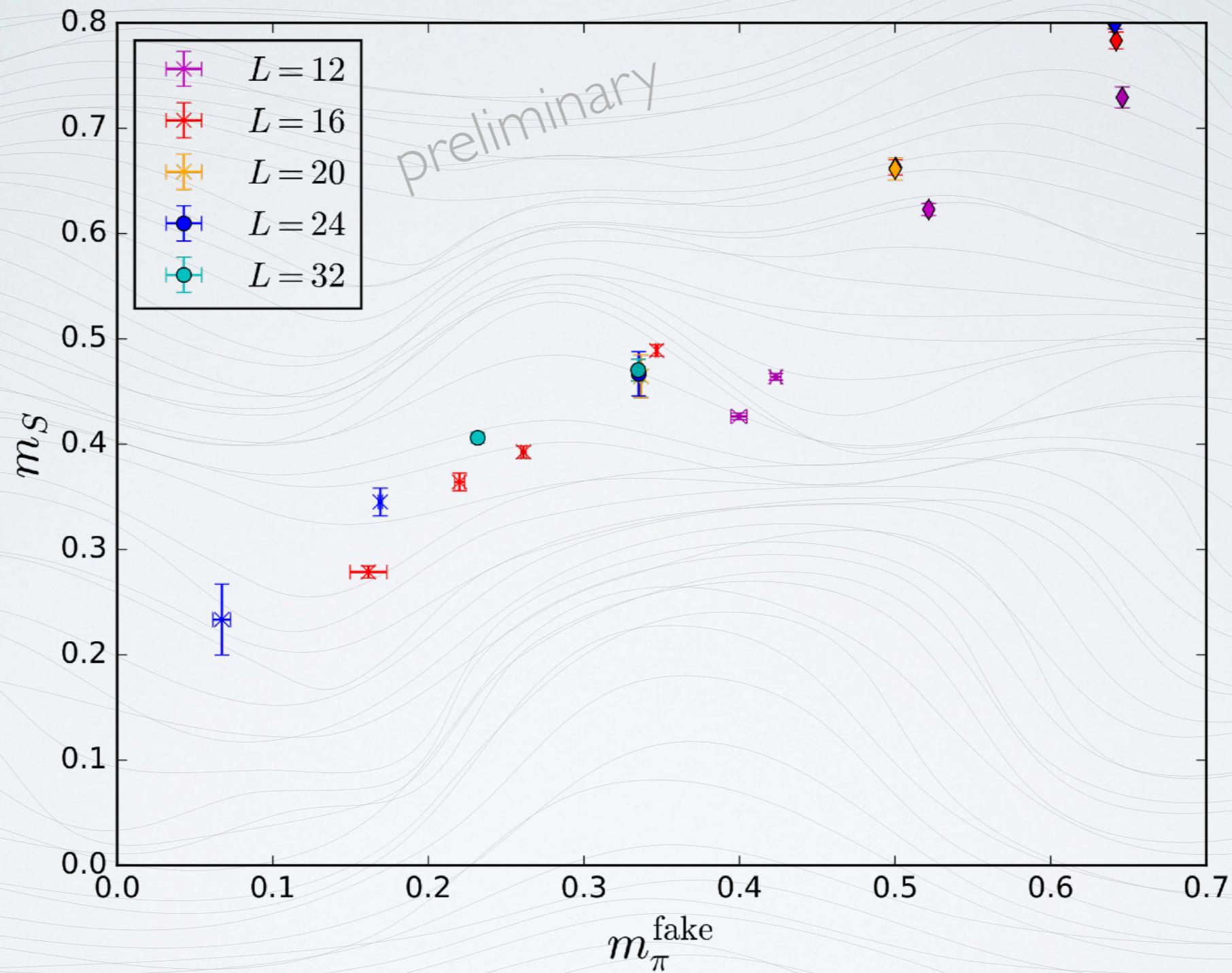
toleron state - volume dependent

# Results - Pseudo-scalar



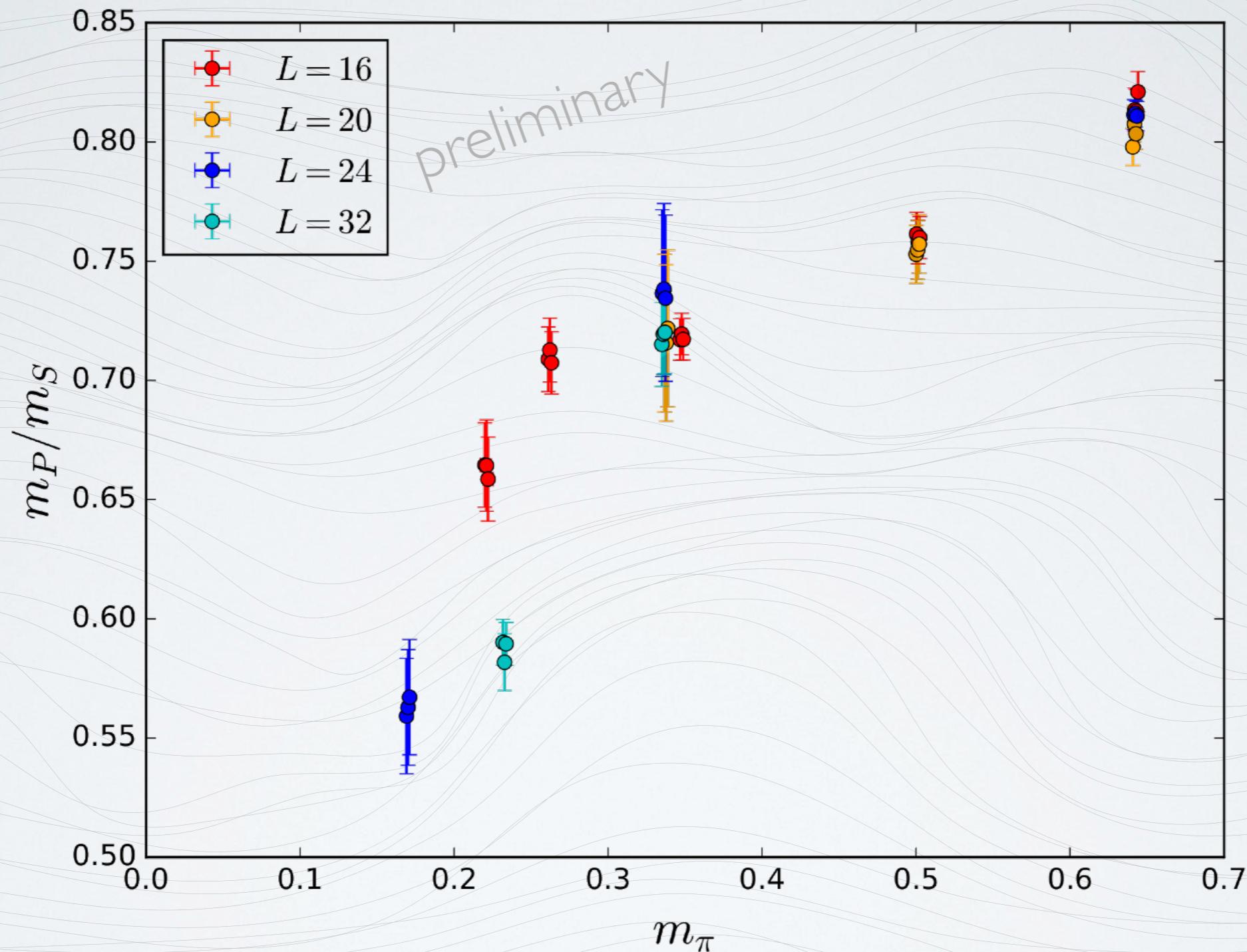
$\bar{q}\Gamma q$  state - clear mass dependence

# Results - Scalar



$\bar{q}\Gamma q$  state - clear mass dependence

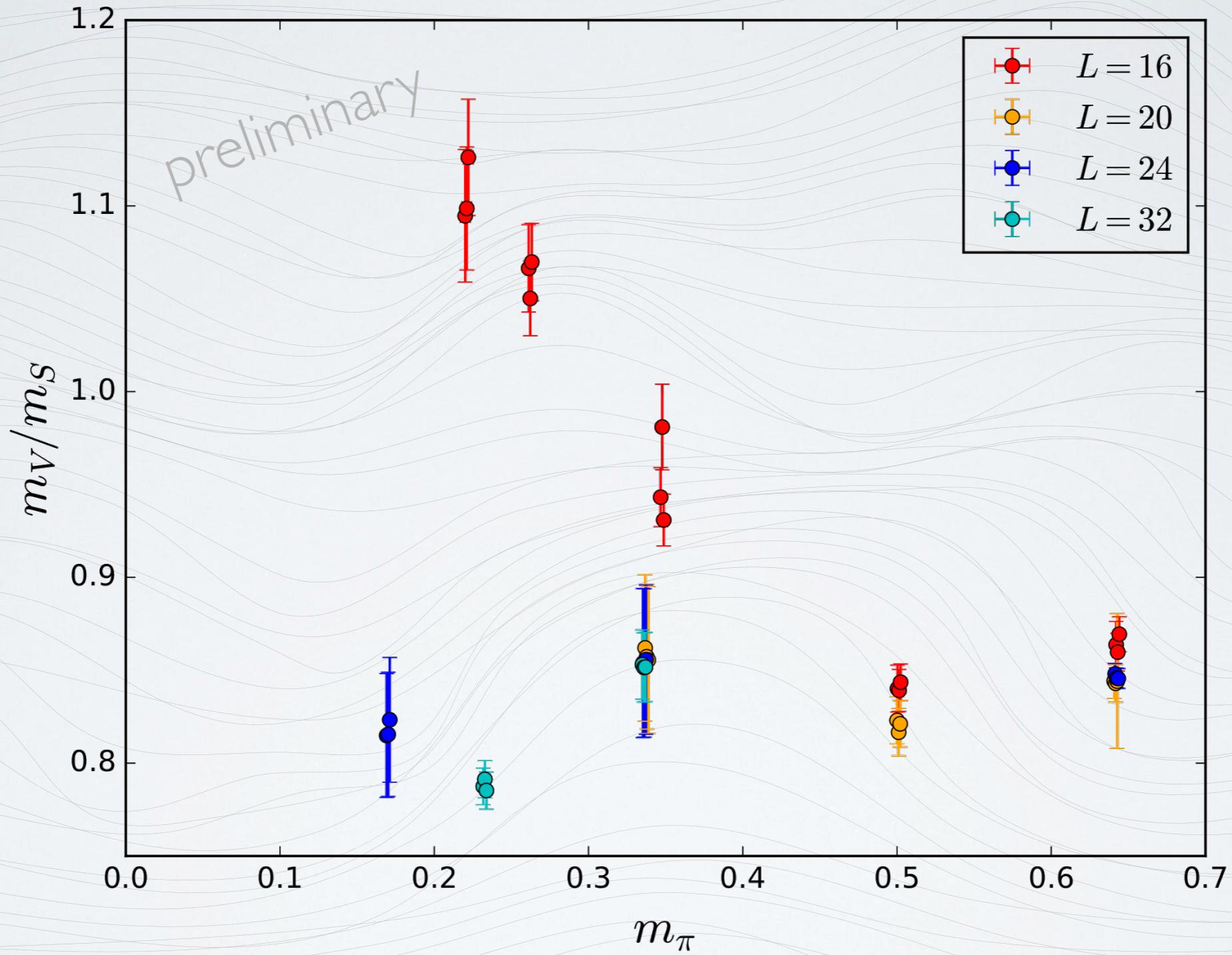
# Build ratio - P / S



Comparison with prediction:  $\frac{M_{PS}}{M_S} = 0.410(32)(15)$

hep-lat/0810.0161

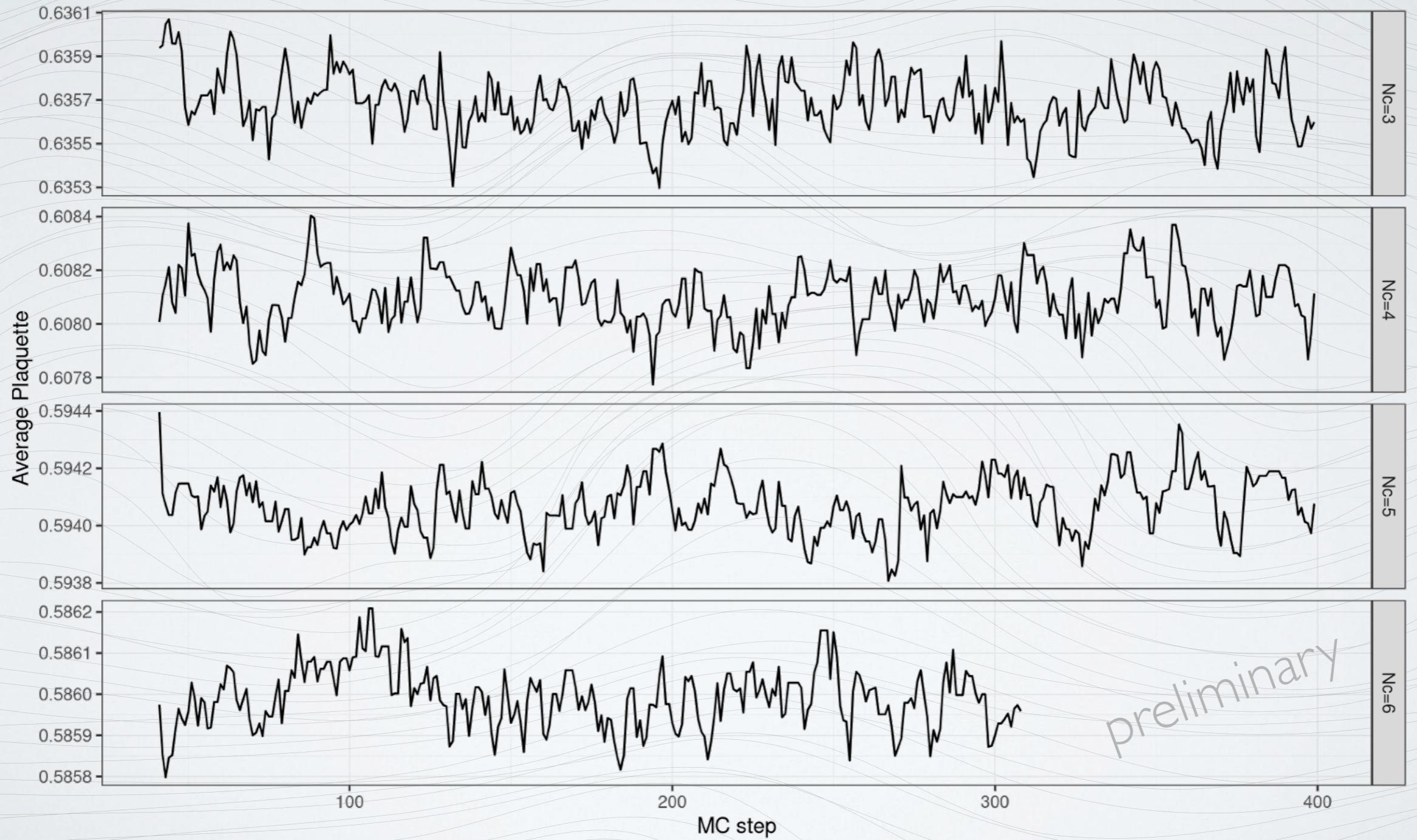
# Build ratio - V / S



# Future

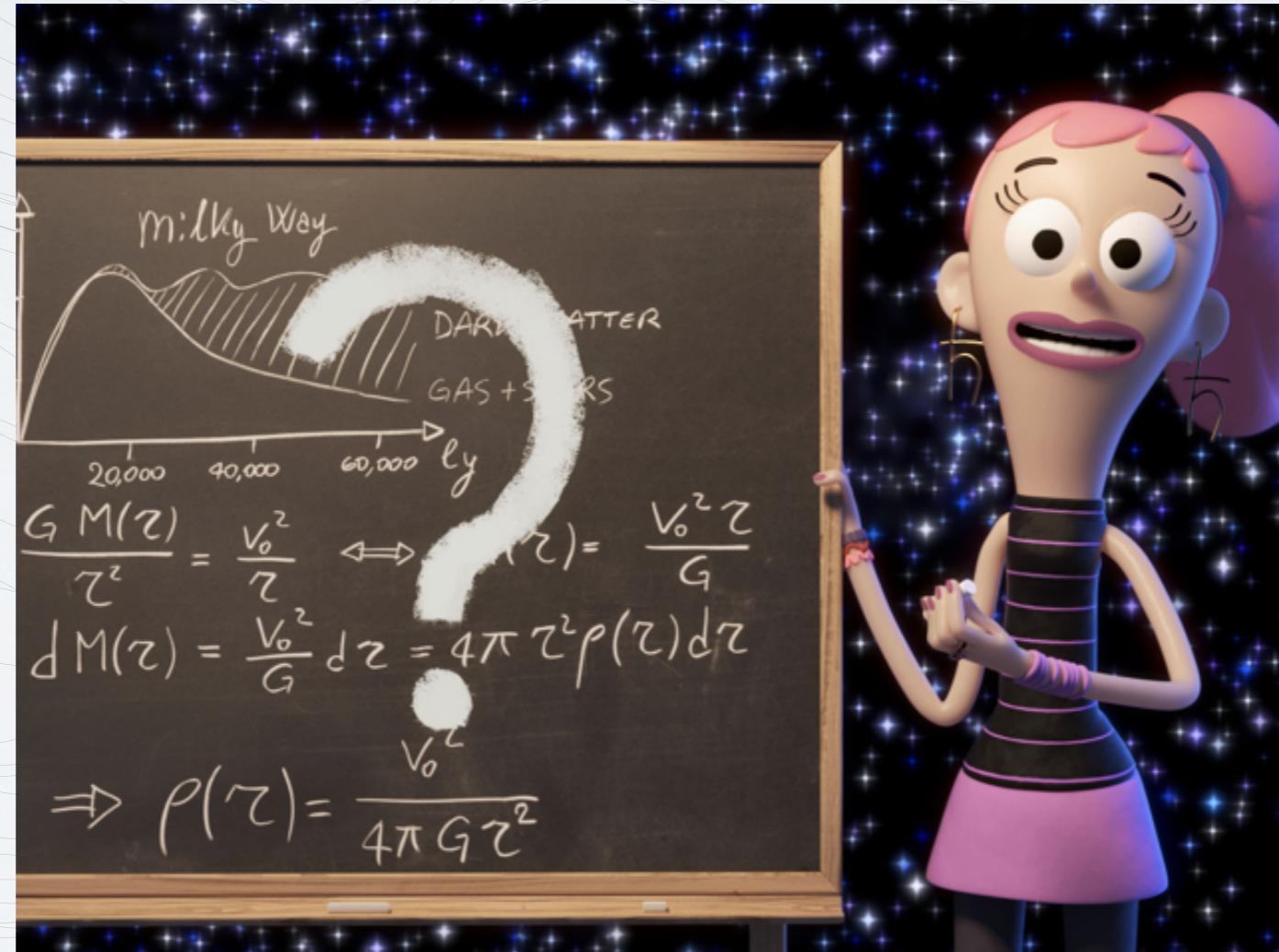
- Increase  $N_c$  - first for Pure Gauge - Using GRID

hep-lat/1512.03487



# Questions?

Thank you for your attention!



Quantum Kate (orig. Kvante Karina): CP3 Outreach <http://www.kvantebanditter.dk/en>