

# FIMPs imprint on Cosmology as Non Cold Dark Matter

Laura Lopez Honorez



mainly inspired by JCAP 03 (2022) 03, 041  
in collaboration with Q. Decant, J. Heisig, D. Hooper.

LLP Bethe Forum Bonn  
13-17/11/23 - Bonn

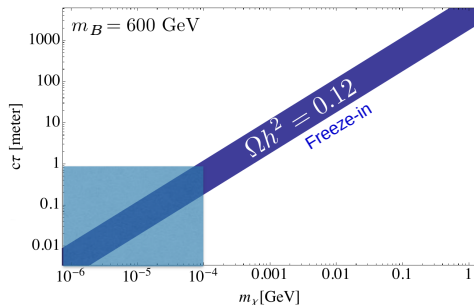
# Why FIMPs & Non-Cold DM in a LLP workshop?

# Exemplary case of Freeze-in: LLPs and NCDM

e.g. [Hall'09, Co'15, Hessler'16, d'Eramo'17, Heeck'17, Boulebane'17, Brooijmans'18, Garny'18, Calibbi'18, No'19, Belanger'18, Decant'22, Becker'23, etc.]

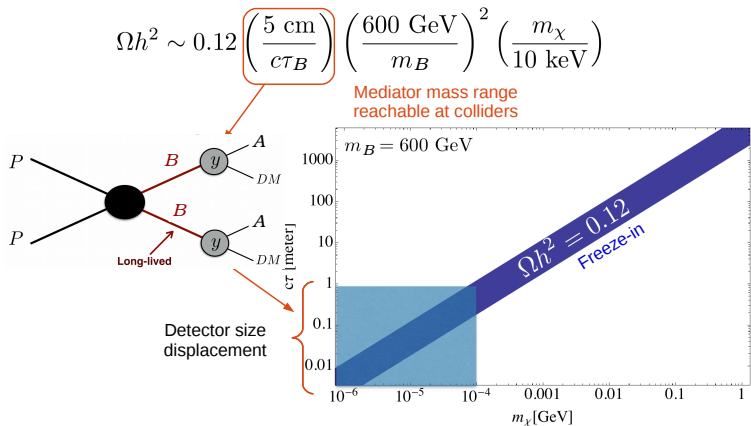
$$\Omega h^2 \sim 0.12 \left( \frac{5 \text{ cm}}{c\tau_B} \right) \left( \frac{600 \text{ GeV}}{m_B} \right)^2 \left( \frac{m_\chi}{10 \text{ keV}} \right)$$

Mediator mass range  
reachable at colliders



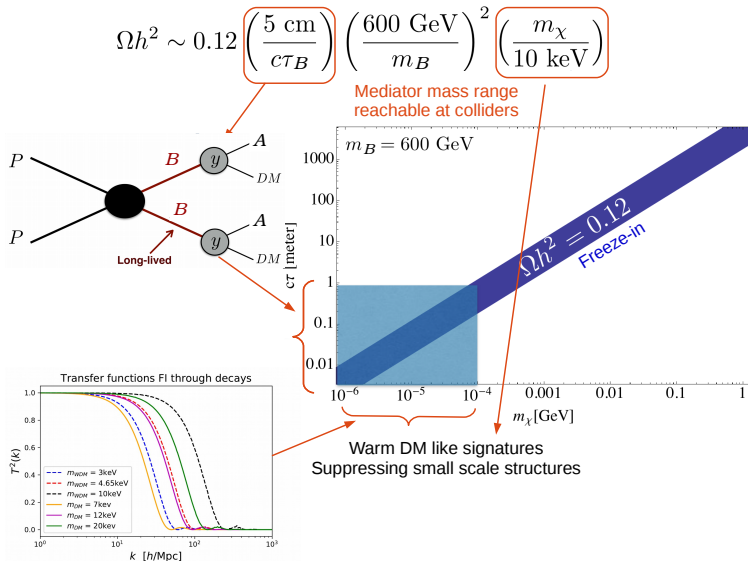
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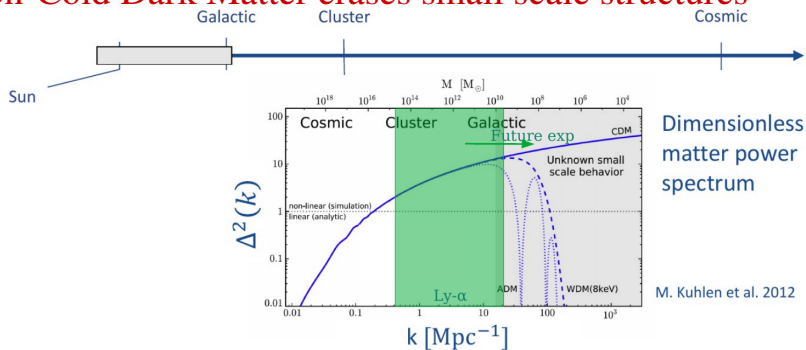
# Exemplary case of Freeze-in: LLPs and NCDM

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# Non-Cold Dark Matter??

# Non-Cold Dark Matter erases small scale structures

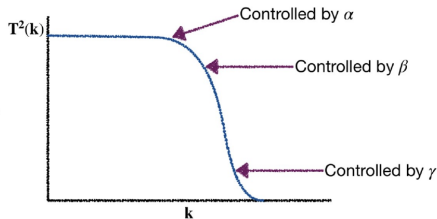


- WDM **free-streaming** from overdense to underdense regions  
 $\rightsquigarrow$  Smooth out inhomogeneities for  $\lambda \lesssim \lambda_{FS} \sim \int v/adt$
- Effects  $P(k)$  and  $T(k)$  generalized to **Non-Cold DM** see e.g. [Bode'00, Viel'05, Murgia'17], including non-thermal DM from freeze-in, superWIMP or e.g. DM from PBH evap.

# Non-Cold Dark Matter erases small scale structures

$$T^2(k) = \frac{P(k)_{\text{nCDM}}}{P(k)_{\text{CDM}}} = [1 + (\alpha k)^\beta]^{2\gamma}$$

[Murgia'17]

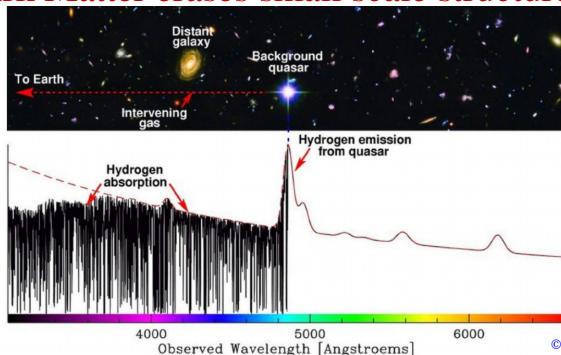


[Courtesy DC Hooper]

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© M. Murphy

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- Effects  $P(k)$  and  $T(k)$  generalized to **Non-Cold DM** see e.g. [Bode'00, Viel'05, Murgia'17], including non-thermal DM from freeze-in, superWIMP or e.g. DM from PBH evap.
- Tested against **Lyman- $\alpha$** : absorption lines along line of sights to distant quasars probe smallest structures  $\rightsquigarrow m_{\text{WDM}}^{\text{thermal}} > 1.9\text{-}5.3 \text{ keV}$   
 see e.g. [Viel'05, Yeche'17, Palanque-Delabrouille'19, Garzilli'19]

# NCDM: (un-)usual suspects production in the early universe

# NCDM: thermal WIMP vs non-thermal FIMP

Cosmology

$$\frac{df_{\chi}(t, p)}{dt} = \mathcal{C}[f_{\chi}]$$

Particle Physics

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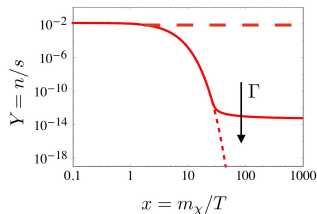
Particle Physics

Weak coupling  
to SM

$$\Gamma_{\chi \leftrightarrow \text{SM}} > H$$

"Thermal DM" (incl. WIMP)

$$f_{\chi}(t, p) = f_{\chi}(t, p)^{fD, BE}$$



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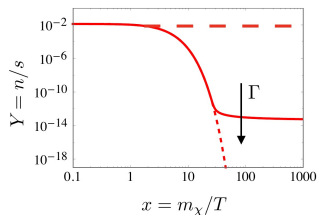
$$\Gamma_{\chi \leftrightarrow \text{SM}} > H$$

Feeble coupling  
to SM

$$\Gamma_{\chi \leftrightarrow \text{SM}} < H$$

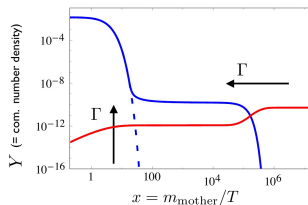
"Thermal DM" (incl. WIMP)

$$f_{\chi}(t, p) = f_{\chi}(t, p)^{f^{D, BE}}$$



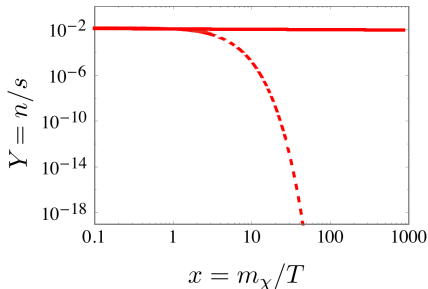
"Non-Thermal" FIMP

$$f_{\chi}(t, p) \neq f_{\chi}(t, p)^{f^{D, BE}}$$



# Thermal DM from relativistic freeze-out (WDM)

$$\frac{df_\chi}{dt} = C_{\chi\chi\leftrightarrow AA'}[f_\chi] \quad \rightsquigarrow \quad n_\chi \propto \frac{g_{*,S}^0}{g_{*,S}(T_D)}$$

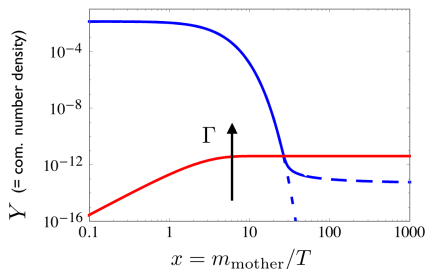


- DM **annihilation** driven freeze-out
- DM is weakly coupled:  $\lambda_\chi \sim g_{EW}$   
 $\rightsquigarrow$   $\chi$  chem. & kin. equilibrium
- DM decouples while relativistic:  
 $x_D = m_B/T_D$  and  $x_D < 3$
- $\Omega_\chi h^2 = 0.12 \frac{g_\chi^{(n)} m_\chi}{6 \text{ eV}} \frac{g_{*,S}^0}{g_{*,S}(T_D)}$

# Non-thermal DM from Freeze-in

see also [McDonald '02; Covi'02; Choi'05; Asaka'06; Frère'06; Petraki'08; Hall'09; etc]

$$\frac{df_\chi}{dt} = C_{B \rightarrow \chi A} [f_\chi] \quad \rightsquigarrow \quad n_\chi \propto \Gamma_{B \rightarrow \chi} M_p / m_B^2 = R_\Gamma$$



- Freeze-in from  $B$  decays
- $B$  in chem. & kin. equilibrium
- $\Omega_\chi h^2 = 0.12 \rightsquigarrow \lambda_\chi \lesssim 10^{-8}$   
i.e.  $\chi$  decoupled
- $x = m_B/T$  and  $x_{\text{FI}} \sim 3$
- $\Omega_\chi h^2 \propto m_\chi R_\Gamma$

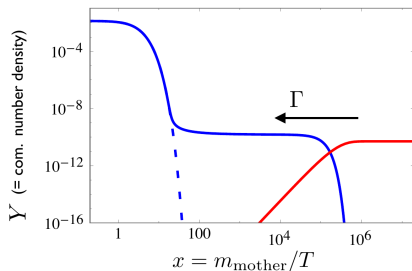
**Careful:** late decay (SW), production via scattering, early matter dominated era ( $T_R$  small), non renormalisable operators and thermal corrections for ultra-relativistic DM not taken into account.

Zero  $\chi$  initial abundance assumed.

# Non thermal DM from superWIMP

see also [Covi '99 ;Feng '03]

$$\frac{df_\chi}{dt} = C_{B \rightarrow \chi A} [f_\chi] \quad (\text{for } x > x_{\text{FO}}) \quad \rightsquigarrow \quad n_\chi = n_B(x_{\text{FO}})$$

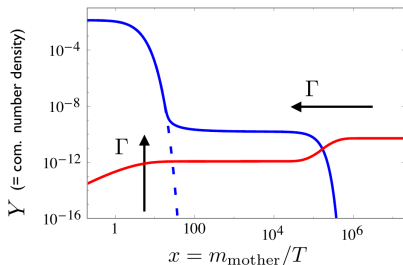


- superWIMP from late  $B$  decays
- $B$  chem. decoupled at  $x = x_{\text{FO}}$  &  $\chi$  decoupled
- $x = \frac{m_B}{T}$  and  $x_{\text{SW}} \sim R_\Gamma^{-1/2} > x_{\text{FO}}$
- $\Omega_\chi h^2 = m_\chi/m_B \times \Omega_B h^2|_{\text{FO}}$   
if  $B \rightarrow A_{\text{SM}} A'_{\text{SM}}$  not open



# FIMPs from FI & superWIMP

**Careful:** both SW and FI contributions are always present for production via  $B$  decays!!



- $\chi$  decoupled
- $\chi$  population slowly builds up from  $B$  before and after FO.
- $\Omega_\chi h^2 = \Omega_\chi h^2|_{\text{FI}} + \Omega_\chi h^2|_{\text{SW}}$

Substantial FI and SW contributions may arise from the very same process  $B \rightarrow A\chi$  but FI and SW take place at very different times:  $x_{\text{FI}} < x_{\text{SW}}$

# Free streaming Velocity Rule of Thumb

# Can we translate WDM bound to FIMP?

see also [ Kamada'19, Baumholzer'19, Ballesteros'20, d'Eramo'20 ]

Naive estimate for “similar velocity distributions” :

$$\langle v_\chi \rangle|_{t_0}^{\text{NCDM}} \geq \langle v_\chi \rangle|_{t_0}^{\text{WDM lim}}$$

$$\text{with } \langle v_\chi \rangle|_{t_0} = \frac{\langle p_\chi \rangle}{m_\chi} \Big|_{t_0} = \frac{\langle p_\chi \rangle}{T} \Big|_{t_{\text{prod}}} \times \left( \frac{g_{*S}(t_0)}{g_{*S}(t_{\text{prod}})} \right)^{1/3} \times \frac{T_0}{m_\chi}$$

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- WDM:  $\Omega_\chi h^2 = 0.12 \rightsquigarrow g_{*,S}(T_D) \simeq 10^3 \times \frac{m_\chi}{\text{keV}}$   
 $\Rightarrow \langle v_\chi \rangle|_{t_0}^{\text{WDM}} \propto m_{\text{WDM}}^{-4/3}$

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 $\Rightarrow \langle v_\chi \rangle|_{t_0}^{\text{FI}} \propto m_\chi^{-1}$

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 $\Rightarrow \langle v_\chi \rangle|_{t_0}^{\text{SW}} \propto m_\chi^{-1} \times R_\Gamma^{-1/2}$

$$m_\chi \gtrsim (m_{\text{WDM}}^{\text{lim}})^{4/3} \begin{cases} \#_{\text{FI}} & \text{for FI,} \\ \#_{\text{SW}} \times (R_\Gamma)^{-1/2} & \text{for SW,} \end{cases}$$

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$$m_\chi \gtrsim \begin{cases} 16 \text{ keV} & \text{for FI,} \\ 0.38 \text{ GeV} \times \sqrt{10^{-4}/R_\Gamma} & \text{for SW,} \end{cases} \text{ for } m_{\text{WDM}}^{\text{Ly}-\alpha} > 5.3 \text{ keV}$$



# Velocity Distributions: Impact on overdensities

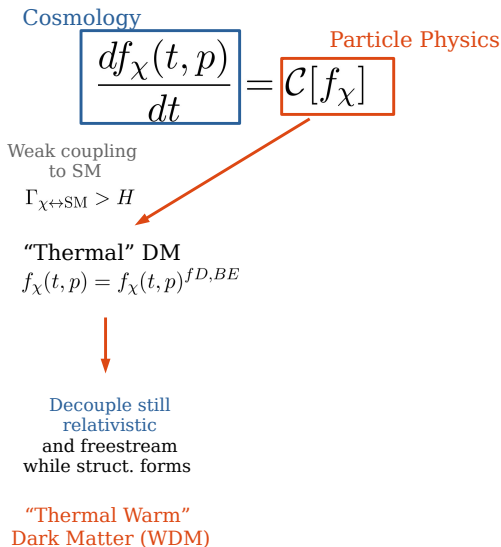
# WDM vs FIMP distributions

Cosmology

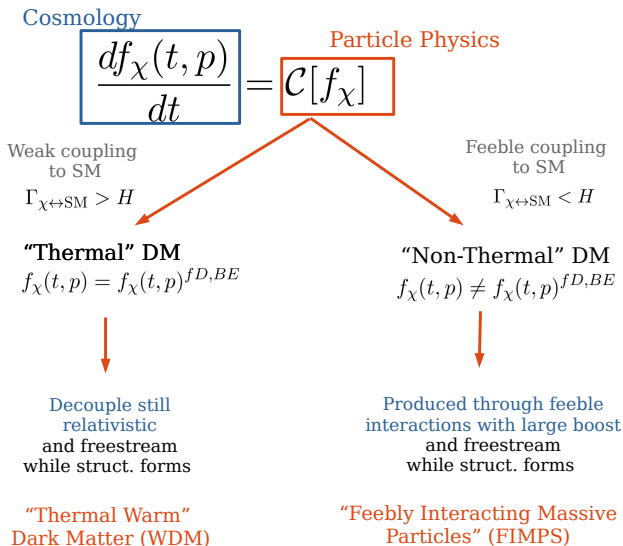
$$\frac{df_{\chi}(t, p)}{dt} = \mathcal{C}[f_{\chi}]$$

Particle Physics

# WDM vs FIMP distributions

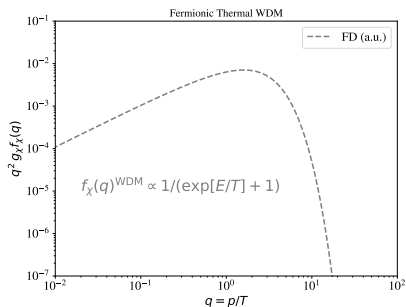


# WDM vs FIMP distributions



# Thermal WDM: exponential cut in $P(k)$ at small scales

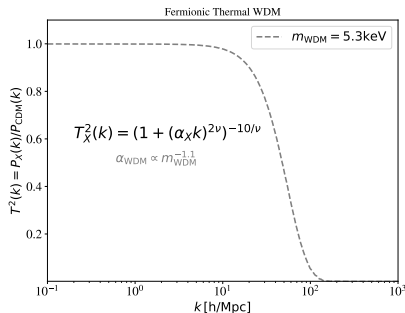
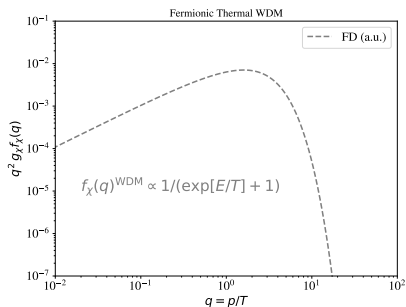
see also [Bode'00,Viel'05]



- Thermal WDM is in kinetic equilibrium thanks to fast elastic scatterings with thermal plasma:  $\frac{d}{dt}f_{\chi} = C_{el}[f_{\chi}] \rightsquigarrow f_{\chi} \propto f_{\chi}^{eq}(q)$

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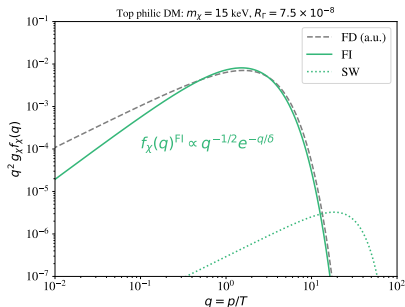


- Thermal WDM is in kinetic equilibrium thanks to fast elastic scatterings with thermal plasma:  $\frac{d}{dt} f_{\chi} = C_{el}[f_{\chi}] \rightsquigarrow f_{\chi} \propto f_{\chi}^{eq}(q)$
- Evolve  $f_{\chi}$  up to 1st order pert. (w/ Boltzmann code):

Free-streaming scale:  $\alpha_{WDM} \sim 0.045 \left( \frac{m_{WDM}}{\text{keV}} \right)^{-1.11} \text{ Mpc}/h$

# “Pure” FI & SW: WDM-like

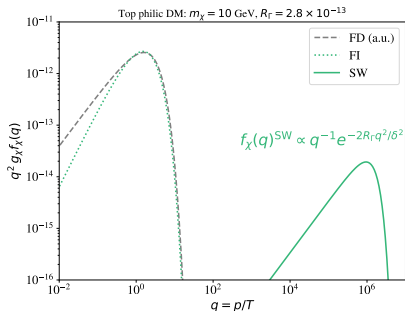
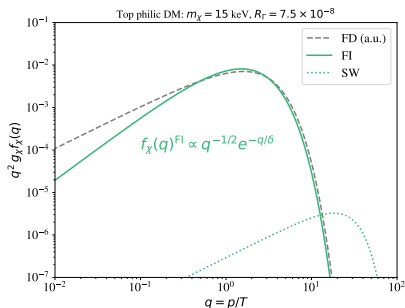
see also [Petraiki'16, Heck'17, Boulebane'17, Kamada'19, Baumholzer'19, Ballesteros'20, d'Eramo'20]



- Contrarily to “usual” WDM, FIMPs are non-thermally produced.  
Distribution  $f_\chi \propto q_\star^{-\alpha} \exp(-q_\star^\beta)$  with  $\alpha = \frac{1}{2}, 1$  and  $\beta = 1, 2$  for FI, SW.

# “Pure” FI & SW: WDM-like

see also [Petraiki'16,Heeck'17, Boulebane'17, Kamada'19, Baumholzer'19, Ballesteros'20, d'Eramo'20]

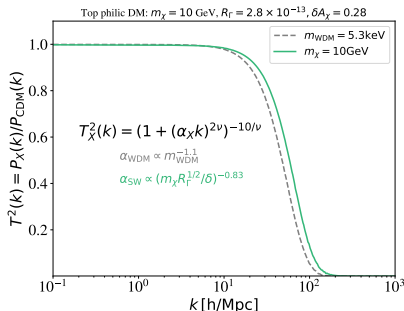
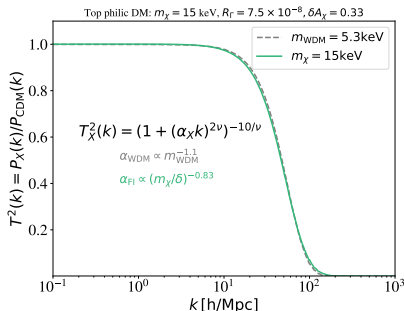


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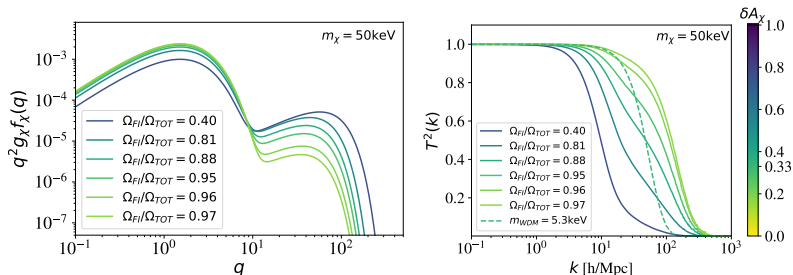


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- Modified CLASS:** Pure FI/SW transfer functions similar to thermal WDM.  $\rightsquigarrow$  Lower mass bound from Lyman- $\alpha$  ( $m_B \ll m_A$ ,  $T_{\text{prod}} > T_{\text{EW}}$ ):

$$m_\chi \gtrsim \begin{cases} 15 \text{ keV} & \text{for FI,} \\ 0.38 \text{ GeV} \times \sqrt{10^{-4}/R_f} & \text{for SW,} \end{cases} \text{ for } m_{\text{WDM}}^{\text{Ly}-\alpha} > 5.3 \text{ keV}$$

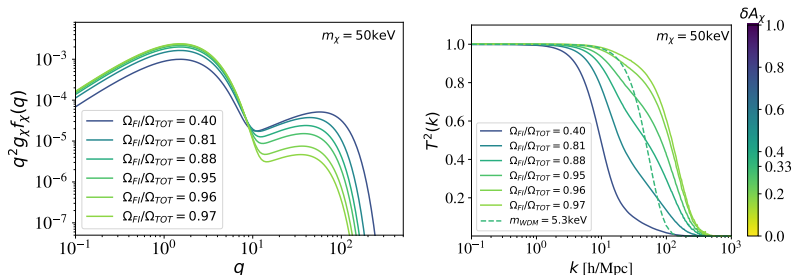
[Decant, Heisig, Hooper, LLH'21]

# Mixed FI & SW: significant deviations from WDM



- Mixed FI-SM  $q^2 f_\chi$  is **multimodal**  $\rightsquigarrow T^2(k) = P_{\text{FIMP}}(k)/P_{\text{CDM}}(k)$  can **significantly deviate** from e.g. WDM,  $\alpha, \beta, \gamma$  param. or CDM+WDM

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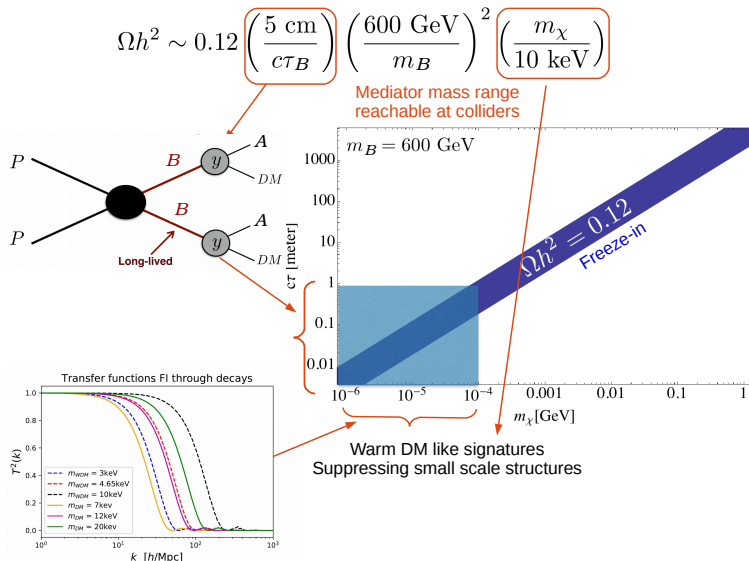


- Mixed FI-SM  $q^2 f_\chi$  is **multimodal**  $\rightsquigarrow T^2(k) = P_{\text{FIMP}}(k)/P_{\text{CDM}}(k)$  can **significantly deviate** from e.g. WDM,  $\alpha, \beta, \gamma$  param. or CDM+WDM
- We use the **area criterion** [Murgia'17] measuring the relative  $P_{1D}(k)$  deviation over  $0.5h/\text{Mpc} < k < 20h/\text{Mpc}$ :  $\delta A_\chi < \delta A_{\text{WDM}}^{\text{Ly}-\alpha} = 0.33$  for  $m_{\text{WDM}}^{\text{Ly}-\alpha} > 5.3 \text{ keV}$   
see also [Schneider'16] and e.g. [D'Eramo'20, Egana-Ugrinovic'21]

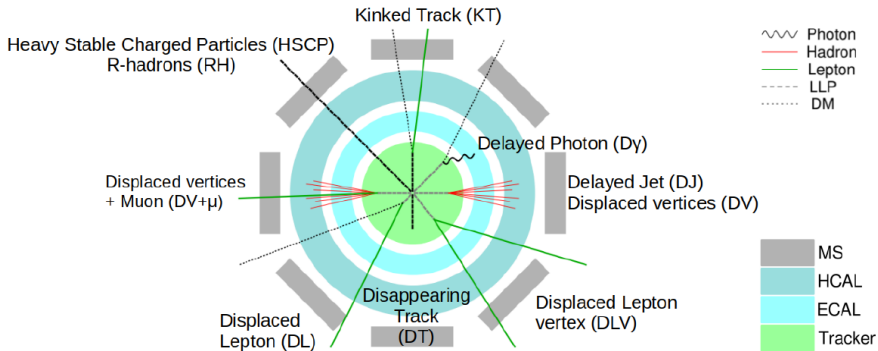
# NCDM FIMPs: Complementarity with LLP searches

# FIMPs: LLPs and NCDM

e.g. [Hall'09, Co'15, Hessler'16, d'Eramo'17, Heeck'17, Boulebane'17, Brooijmans'18, Garny'18, Calibbi'18, No'19, Belanger 18, etc]

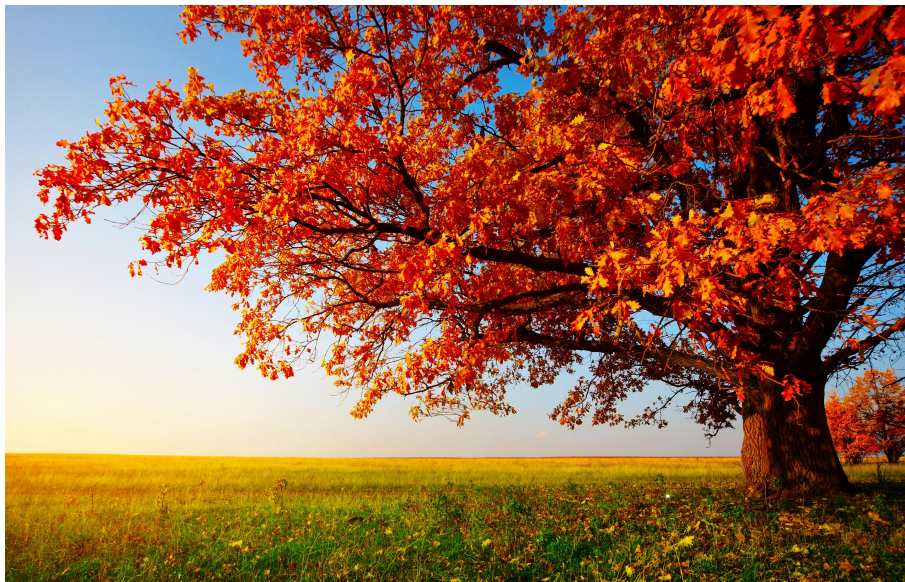


# Collider searches for LLP's



[Calibbi,d'Eramo,Junius,LLH '21]

# Illustrative frameworks



# Illustrative frameworks





## Illustrative framework: minimal FIMP models

Dark matter  $\chi$  coupled to dark  $B$  and SM  $A$  through Yukawa-like interactions

$$\mathcal{L} \subset \lambda_\chi \chi A_{SM} B$$

- Dark sector ( $Z_2$  odd):  $m_B > m_\chi$
- $B$  is  $SU(3) \times SU(2) \times U(1)$  charged
  - fast  $B^\dagger B \leftrightarrow$  SM SM through gauge interactions at early time
  - $B$  is produced at colliders today

# Illustrative framework: minimal FIMP models

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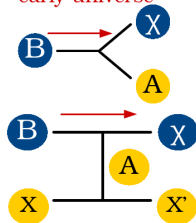
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  - $B$  is produced at colliders today
- Minimal scenarios:

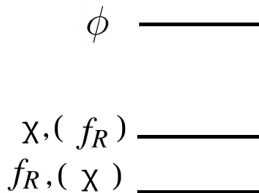
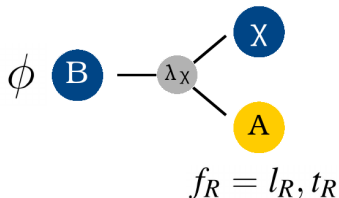
$A_{SM}$	Spin DM	Spin B	Interaction	Label
$\psi_{SM}$	0	1/2	$\bar{\psi}_{SM} \Psi_B \phi$	$\mathcal{F}_{\psi_{SM} \phi}$
	1/2	0	$\bar{\psi}_{SM} \chi \Phi_B$	$\mathcal{S}_{\psi_{SM} \chi}$
$F^{\mu\nu}$	1/2	1/2	$\bar{\Psi}_B \sigma_{\mu\nu} \chi F^{\mu\nu}$	$\mathcal{F}_{F\chi}$
$H$	0	0	$H^\dagger \Phi_B \phi$	$\mathcal{S}_{H\phi}$
	1/2	1/2	$\bar{\Psi}_B \chi H$	$\mathcal{F}_{H\chi}$

[Calibbi, D'Eramo, Junius, LLH, Mariotti 21]

Production in the early universe



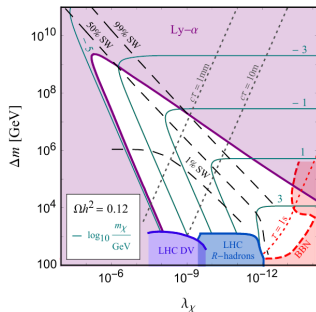
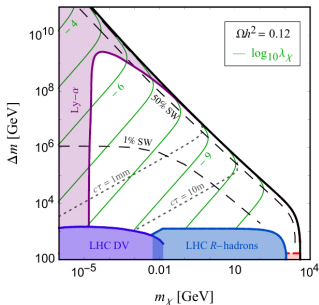
# Top philic DM



$$\mathcal{L} \subset \mathcal{L}_K - \frac{m_\chi}{2} \bar{\chi}\chi - m_\phi \phi^\dagger \phi - \lambda_\chi \phi \bar{\chi} f_R + h.c.$$

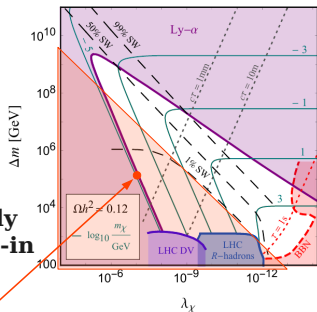
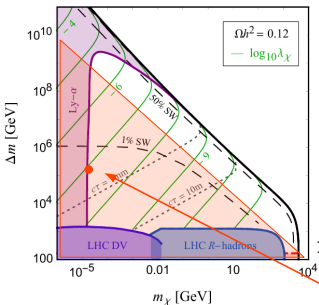
- SM + 1 charged/colored dark scalar  $\phi$  + 1 Majorana dark fermions  $\chi$  ( $Z_2$  symmetry for DM stability) and  $f_R = t_R$
- Sommerfeld and BSF taken into account to account for SW [Harz& Petraki'18]
- $\Omega_\chi h^2|_{\text{FI}}$  driven by  $\phi \rightarrow t\chi$  gets an extra 15-25% contribution from scatterings from  $t\phi \rightarrow g\chi$  and  $g\phi \rightarrow t\chi$ .

# Exemplary case of top-philic DM

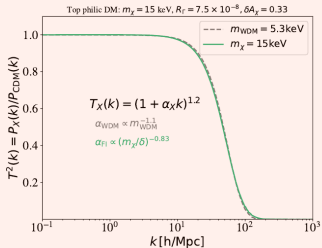
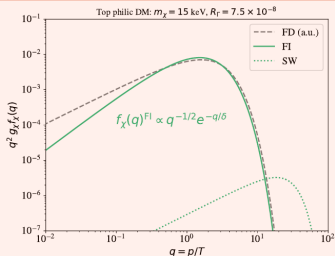


$$\mathcal{L} \subset \mathcal{L}_K - \frac{m_\chi}{2} \bar{\chi}\chi - m_\phi \phi^\dagger \phi - \lambda_\chi \phi \bar{\chi} t_R + h.c.$$

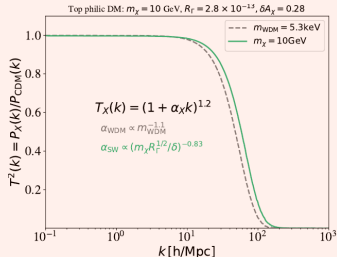
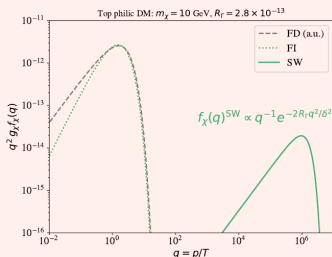
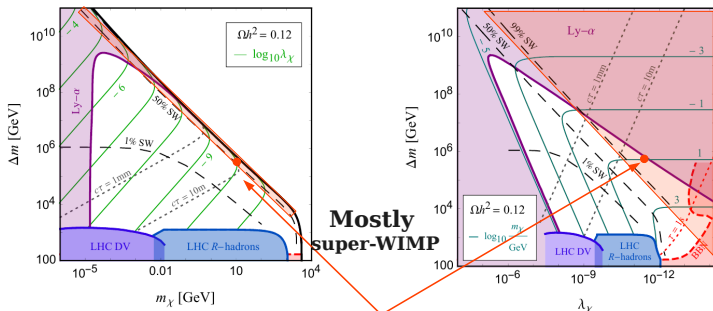
# Exemplary case of top-philic DM



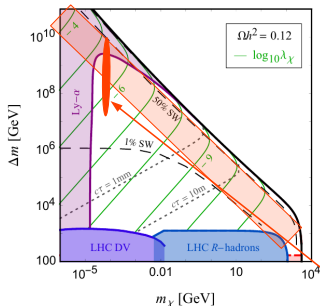
Mostly freeze-in



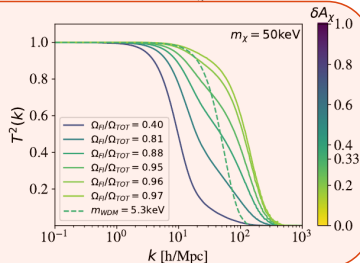
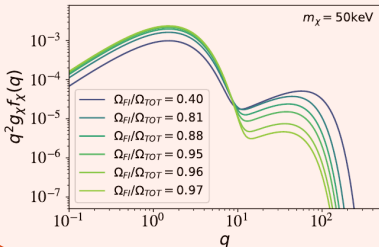
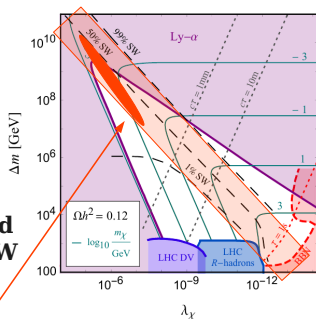
## Exemplary case of top-philic DM



## Exemplary case of top-philic DM



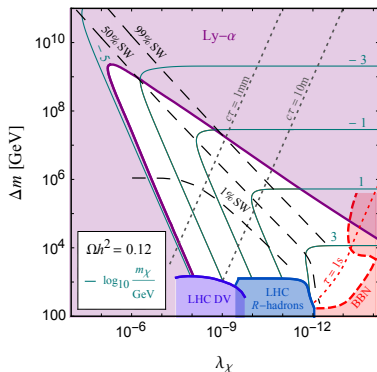
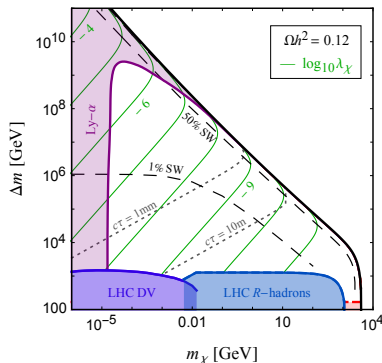
Mixed FI-SW



# Exemplary case of top-philic DM

see also e.g. [Hall'09; Co'15; Hessler'16; d'Eramo'17; Buchmueller'17; Brooijmans'18; Belanger'18; No'19; Garmy'18; Calibbi'18,21; etc]

$$\mathcal{L} \subset \mathcal{L}_K - \frac{m_\chi}{2} \bar{\chi}\chi - m_\phi \phi^\dagger \phi - \lambda_\chi \phi \bar{\chi} t_R + h.c.$$



- Topphilic DM: Parameter space **cornered by particle** (DV + R-hadron searches at LHC - for top-philic) and **cosmology** (Lyman- $\alpha$ , BBN) probes.
- **Lyman- $\alpha$  constraints play a key role** and excludes DM over a large range of  $\lambda_\chi$ , complementary to BBN for  $m_\chi \sim$  few 100 GeV.



## Take home message

Even if dark matter would be (not even) **very feebly interacting** with the SM it can leave **distinctive cosmology signature in the form of NCDM**.

NCDM can be **free-steaming** (focus of today's talk) and/or experiencing collisional damping and give rise to suppressed structure formation at small scales.

- **NCDM is not necessarily thermal WDM** and can have a **mass much larger than few keV**.
- **Multiple NCDM production mechanisms** can give rise to the same/similar features in Cosmology observations. Lyman- $\alpha$  forest data can probe a large parts of the DM parameter space.
- **Complementary observations** are necessary to pin point the DM nature.

To do extra:

- **Modified cosmology** can change prospects for LLP signatures (low  $T_R$ , etc) it will also change Ly- $\alpha$  constraints.
- Future radio telescopes (**21cm Cosmology**) might put stringent constraints on NCDM and distinguish between NCDM scenarios (might depend on  $T_{vir}^{min}$  [Giri'22])

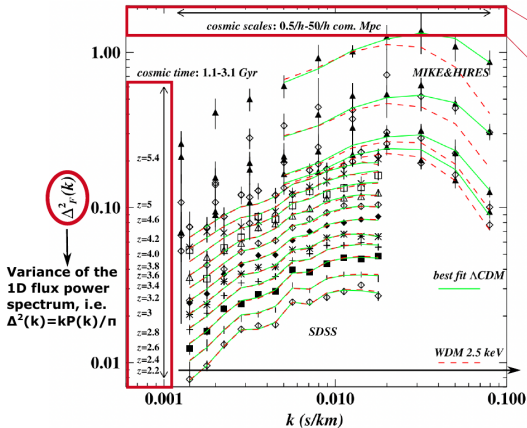
Thank you the invitation  
and for your attention!!

# Backup

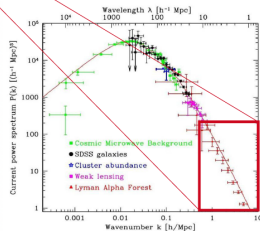
# Lyman- $\alpha$ forest

Absorption lines produced by the inhomogeneous IGM along different line of sights to distant quasars: a fraction of photons is absorbed at the Lyman- $\alpha$  wave-length (corresponding to  $\lambda_\alpha \sim 121$  nm), resulting in a depletion of the observed spectrum at a given frequency ( $\lambda_{abs} < \lambda_\alpha$ ).

- Allows us to trace neutral hydrogen clouds, i.e. smallest structures
- Provides a tracer of the matter power spectrum at high redshifts ( $2 < z < 6$ ) and small scales ( $0.5 h/\text{Mpc} < k < 20 h/\text{Mpc}$ ).
- IGM modelling requires nonlinear evolution: this needs N-body hydrodynamical simulations. Computational expensive and only available for few benchmark models.



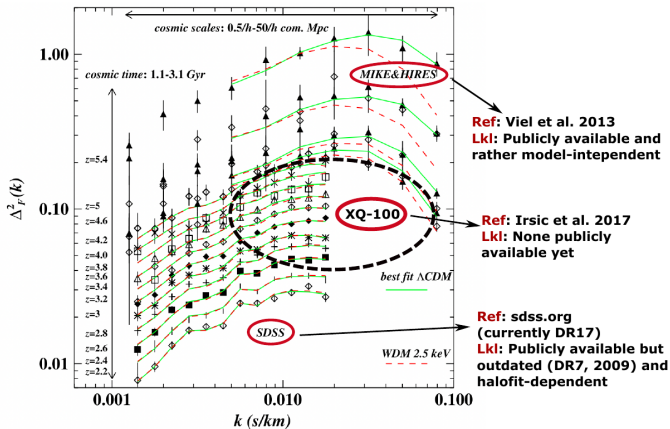
Adapted from Tegmark et al. 2004



- The higher the  $z$  of the source,
- 1) the more absorption one gets,
  - 2) the lower the mean transmission is,
  - 3) the more the density fluctuations amplify,
  - 4) the larger the amplitude of the spectrum

Adapted from Viel et al. 2013

4/25



Adapted from Viel et al. 2013

5/25

Matteo Lucca

## Area criterium [Schneider 2016, Murgia, Merle, Viel, Totzauer, Schneider 2017]

- Consider ratio of 1D power spectra, computed with CLASS

$$r(k) = \frac{P_{1D}^X(k)}{P_{1D}^{\text{CDM}}(k)} \quad \text{with} \quad P_{1D}^X(k) = \int_k^\infty dk' k' P_X(k'),$$

- Compute area under the curve

$$A_X = \int_{k_{\min}}^{k_{\max}} dk' r(k')$$

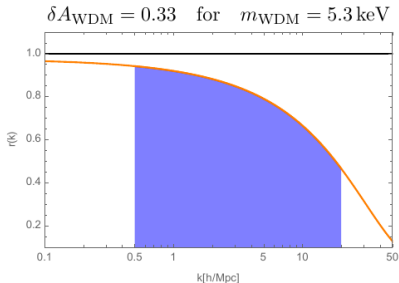
and

$$\delta A_X = \frac{A_{\text{CDM}} - A_X}{A_{\text{CDM}}}$$

- For freeze-in ( $\delta = 1$ ):

$$m_{\text{FI}} > 15.3 \text{ keV}$$

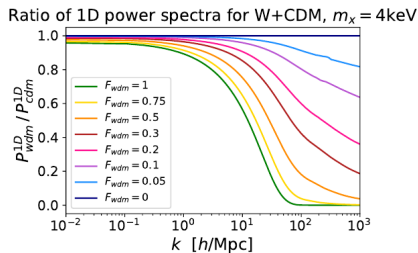
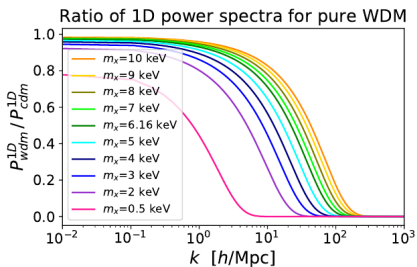
- Suitable for mixed scenario



[see also D'Eramo, Lenoci, 2020; Egana-Ugrinovic, Essig, Gift, LoVerde 2021]

# C+WDM mixed scenarios

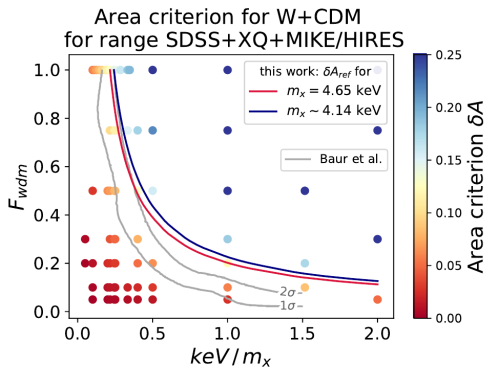
preliminary results from Eva Punter master thesis at ULB, 2022, see also [Murgia'17]





# C+WDM mixed scenarios

preliminary results from Eva Punter master thesis at ULB, 2022, see also [Murgia'17]



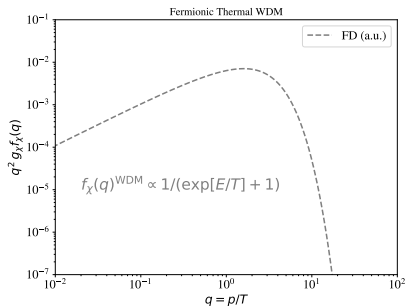
(b)

Figure 5.2: The area difference  $\delta A$  for W+CDM is shown for different WDM masses  $m_x$  and fractions  $F_{\text{wdm}}$ . The range of  $k$  over which is integrated is (a)  $[0.001 - 0.02] \text{ s km}^{-1}$  or  $[0.046 - 0.92] \text{ h Mpc}^{-1}$ , and (b)  $[0.001 - 0.08] \text{ s km}^{-1}$  or  $[0.046 - 3.68] \text{ h Mpc}^{-1}$ . The blue and red solid lines represent the reference values  $\delta A_{\text{ref}}$  for a different  $m_x$  throughout the

The area criterium put **conservative constraints** on mixed W+CDM scenario.  
We can expect similar conclusions for FI+SW scenarios.

# Thermal WDM: exponential cut in $P(k)$ at small scales

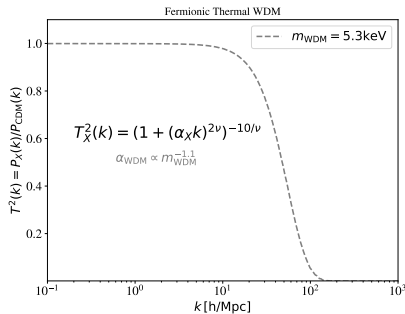
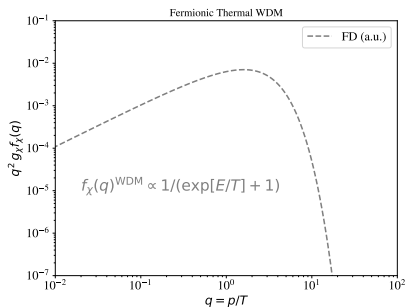
see also [Bode'00,Viel'05]



- Thermal WDM is in kinetic equilibrium thanks to fast elastic scatterings with thermal plasma:  $\frac{d}{dt}f_{\chi} = C_{el}[f_{\chi}] \rightsquigarrow f_{\chi} \propto f_{\chi}^{eq}(q)$

# Thermal WDM: exponential cut in $P(k)$ at small scales

see also [Bode'00,Viel'05]



- Thermal WDM is in kinetic equilibrium thanks to fast elastic scatterings with thermal plasma:  $\frac{d}{dt}f_\chi = C_{el}[f_\chi] \rightsquigarrow f_\chi \propto f_\chi^{eq}(q)$
- Evolve  $f_\chi$  up to 1st order pert. (w/ Boltzmann code as e.g. CLASS):  
Transfer function  $T(k) = (1 + (\alpha_{WDM}k)^{2\nu})^{-5/\nu}$  with  $\nu = 1.12$  [Viel'05]

Free-streaming scale:  $\alpha_{WDM} \sim 0.045 \left(\frac{m_{WDM}}{\text{keV}}\right)^{-1.11} \text{Mpc}/h$

# DM cosmo probes

see [2203.06380]

*Snowmass2021 Theory Frontier: Astrophysical and Cosmological Probes of Dark Matter*

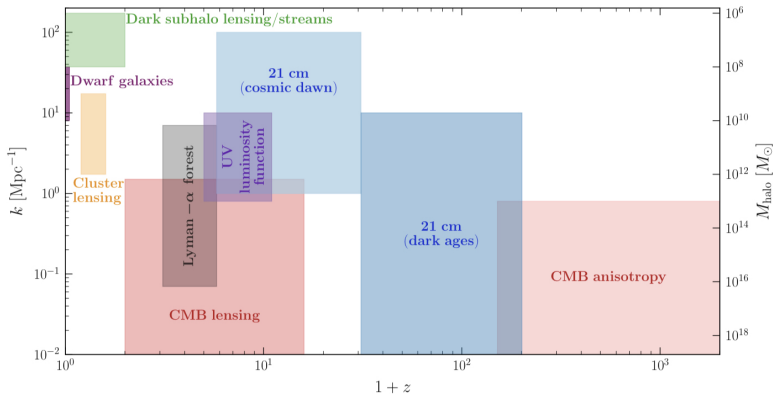
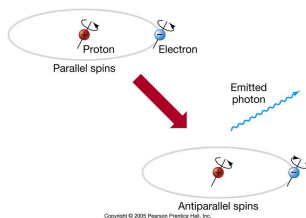


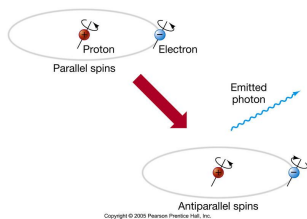
Figure 3: Schematic representation of the coverage of current and future probes of dark matter physics across various ranges of redshift  $z$  (i.e., eras that observable photons or signals primarily originate from), wave number  $k$ , and the corresponding halo mass  $M_{\text{halo}}$ . The ranges of individual probes are approximate. Note that some of the listed probes

# 21 cm Cosmology

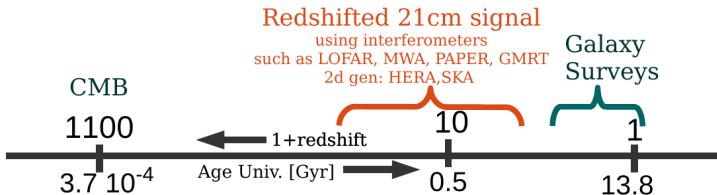


- Transitions between the two ground state energy levels of neutral hydrogen HI  
↔ 21 cm photon ( $\nu_0 = 1420$  MHz)

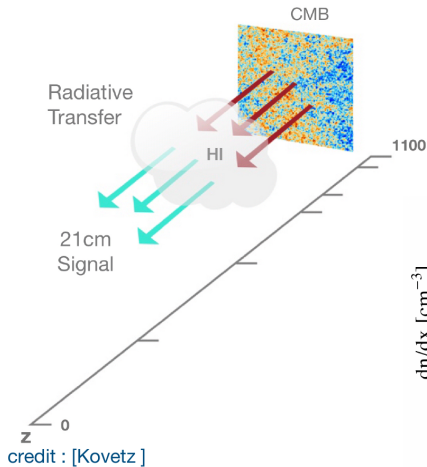
# 21 cm Cosmology



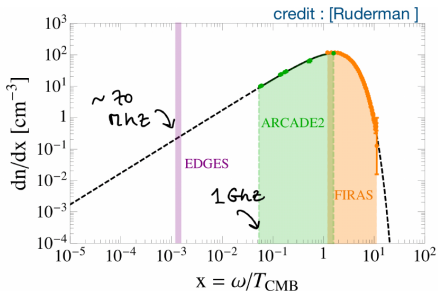
- Transitions between the two ground state energy levels of neutral hydrogen HI  
     $\rightsquigarrow$  21 cm photon ( $\nu_0 = 1420$  MHz)
- 21 cm photon from HI clouds during **dark ages & EoR** redshifted to  $\nu \sim 100$  MHz  
     $\rightsquigarrow$  **new cosmology probe**



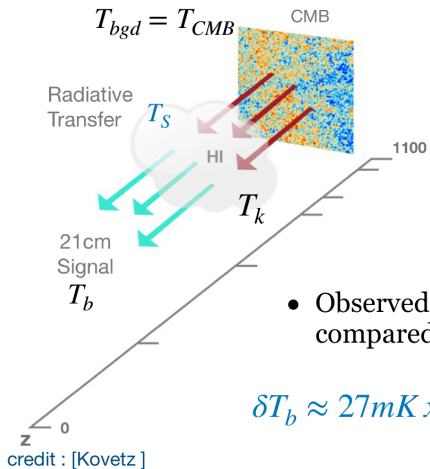
# 21 cm in practice



- 21cm signal observed as CMB spectral distortions



# 21 cm in practice



- 21cm signal observed as CMB spectral distortions

- The spin temperature (= excitation  $T$  of HI) characterises the relative occupancy of HI ground state

$$n_1/n_0 = 3 \exp(-h\nu_0/k_B T_S)$$

- Observed brightness of a patch of HI compared to CMB at  $\nu = \nu_0/(1+z)$

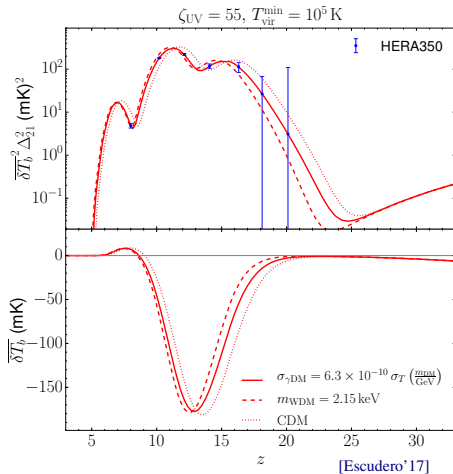
$$\delta T_b \approx 27 \text{mK} x_{HI} (1 + \delta) \sqrt{\frac{1+z}{10}} \left( 1 - \frac{T_{CMB}}{T_S} \right)$$



# Delayed 21cm features for Non-CDM

see also [Sitwell'13, Escudero'18, Schneider'18, Safarzadeh'18, Lidz'18, LLH'18, Muñoz'20, Schneider'22, Giri'22, etc]

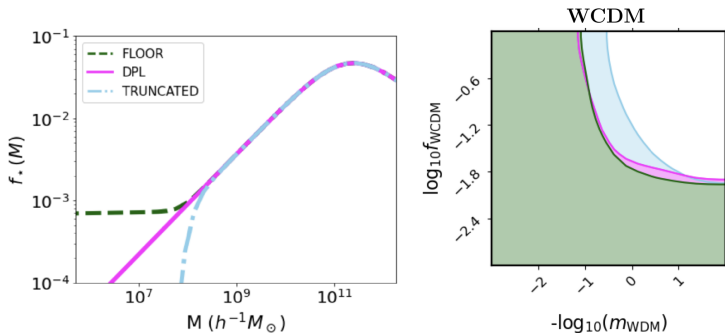
Halo suppression can lead to **delayed astro processes** giving rise to **reionization or 21cm features**. Stronger delay for WDM than IDM.



# Forecast SKA constraints on WDM+CDM

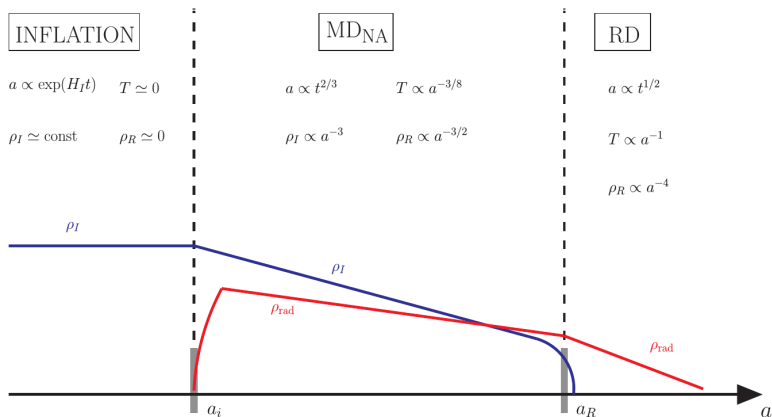
see also [Munoz'19,Hibbard'22, Giri'22, etc]

[Giri'22] (MCMC analysis): For low minimum virial mass ( $T_{vir}^{min} < 10^4$  K) and in the case that minihaloes are populated with stars, **stringent constraints** can be obtained on e.g. 100% WDM: up to  $m_{WDM} < 15$  keV.



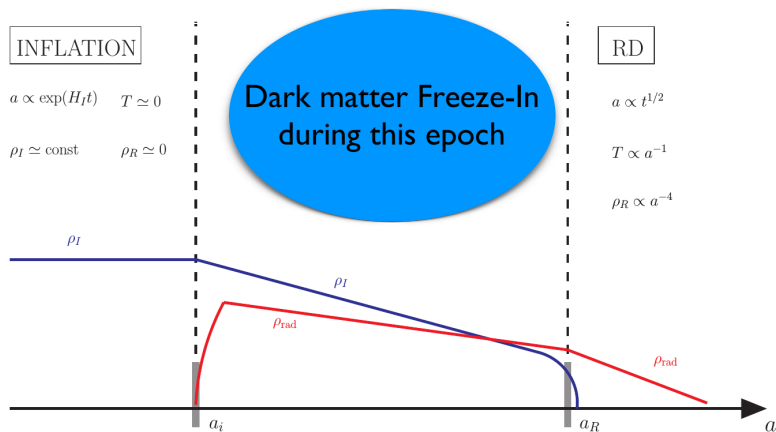
For  $T_{vir}^{min} \sim 10^4$  K it will be difficult to distinguish between an inefficient source models and a universe filled with NCDM.

# Freeze-in in early Matter Dominated era



For FI in **early Matter Dominated era (MD)**, the relic density depends on the reheating temperature  $T_{RH}$  [Co'15].

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## Minimal Frameworks: 3 extra parameters $m_\chi, m_B, \lambda_\chi$

Dark matter  $\chi$  coupled to dark  $B$  and SM  $A$  through Yukawa-like interactions

$$\mathcal{L} \subset \lambda_\chi \chi A_{SM} B$$

- Dark sector ( $Z_2$  odd):  $m_B > m_\chi$
- $B$  is  $SU(3) \times SU(2) \times U(1)$  charged
  - fast  $B^\dagger B \leftrightarrow$  SM SM through gauge interactions at early time
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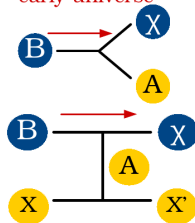
$$\mathcal{L} \subset \lambda_\chi \chi A_{SM} B$$

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- $B$  is  $SU(3) \times SU(2) \times U(1)$  charged
  - fast  $B^\dagger B \leftrightarrow$  SM SM through gauge interactions at early time
  - $B$  is produced at colliders today
- Minimal scenarios:

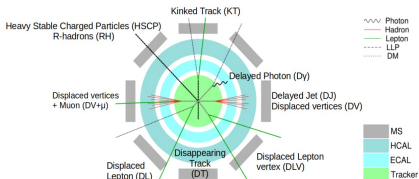
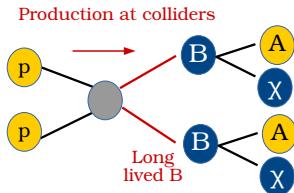
$A_{SM}$	Spin DM	Spin B	Interaction	Label
$\psi_{SM}$	0	1/2	$\bar{\psi}_{SM} \Psi_B \phi$	$\mathcal{F}_{\psi_{SM} \phi}$
	1/2	0	$\bar{\psi}_{SM} \chi \Phi_B$	$\mathcal{S}_{\psi_{SM} \chi}$
$F^{\mu\nu}$	1/2	1/2	$\bar{\Psi}_B \sigma_{\mu\nu} \chi F^{\mu\nu}$	$\mathcal{F}_{F\chi}$
$H$	0	0	$H^\dagger \Phi_B \phi$	$\mathcal{S}_{H\phi}$
	1/2	1/2	$\bar{\Psi}_B \chi H$	$\mathcal{F}_{H\chi}$

[Calibbi, D'Eramo, Junius, LLH, Mariotti 21]

Production in the early universe



# Model dependent signatures



← Displaced B decay → Stable B →

Label	DV + MET	DJ + MET	DJ + $\mu$	DL	DLV	$D\gamma$	DT	RH	HSCP	KT
$\mathcal{F}_{l\phi} \& \mathcal{S}_{l\chi}$				✓					✓	✓
$\mathcal{F}_{\tau\phi} \& \mathcal{S}_{\tau\chi}$	✓	✓		✓					✓	✓
$\mathcal{F}_{q\phi} \& \mathcal{S}_{q\chi}$	✓	✓						✓		
$\mathcal{F}_{l\phi} \& \mathcal{S}_{l\chi}$	✓	✓	✓	✓				✓		
$\mathcal{F}_{G\chi}$	✓	✓						✓		
$\mathcal{F}_{W\chi}$	✓	✓	✓	✓	✓	✓	✓			✓
$\mathcal{S}_{H\phi} \& \mathcal{F}_{H\chi}$	✓	✓	✓	✓	✓	✓	✓			✓

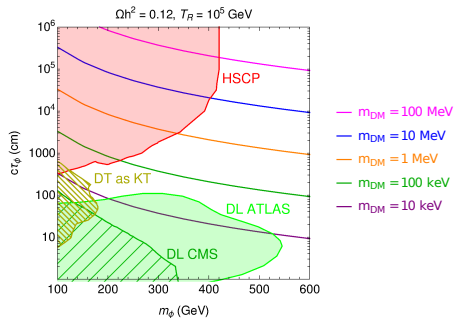
[Calibbi, D'Eramo, Junius, LLH, Mariotti '21]



# Leptophilic DM: Collider vs NCDM Constraints

see also e.g. [Hall'09, Belanger 18, etc]

$$\mathcal{L} \subset \mathcal{L}_K - \frac{m_\chi}{2} \bar{\chi}\chi - m_\phi \phi^\dagger \phi - \lambda_\chi \phi \bar{\chi} l_R + h.c.$$



$$\text{DM FI via } B \text{ decays: } c_{\mathcal{T}B} \simeq 3.3 \times 10^6 \text{ cm} \left( \frac{m_\chi}{10 \text{ GeV}} \right) \left( \frac{1 \text{ TeV}}{m_B} \right)^2.$$

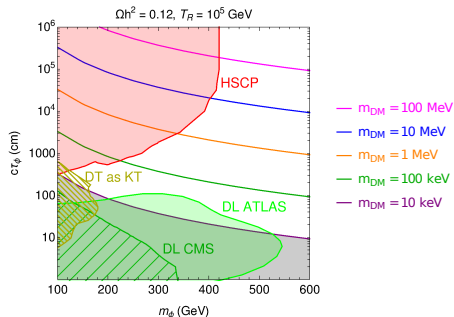
$\Rightarrow B$  decays usually beyond detector size ( $\sim 10 \text{ m}$ )  
unless DM saturates the Lyman- $\alpha$  constraints



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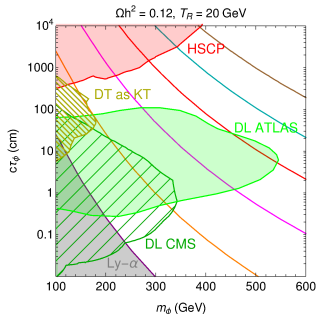
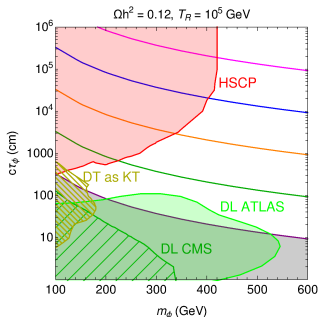
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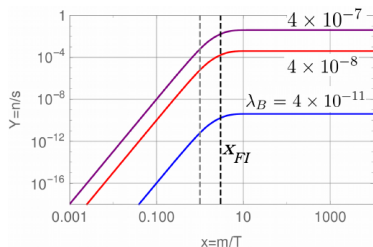
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Dislaced events at colliders might point to freeze-in with **modified early universe cosmology** diluting DM (e.g. EMDE with low  $T_R$ . see Calibbi'21, also Arias'20)

# Reheating after FI and smaller $c\tau_B$

Freeze-in DM production ( $m_{DM}=10$  GeV and  $m_B=1$  TeV)

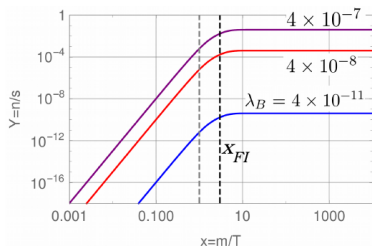
in Radiation Dominated (RD) era



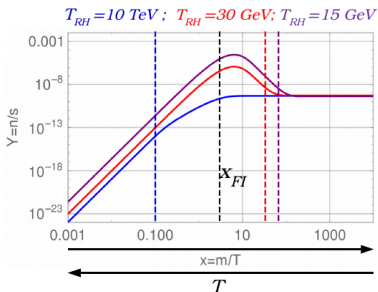
# Reheating after FI and smaller $c\tau_B$

Freeze-in DM production ( $m_{DM}=10$  GeV and  $m_B=1$  TeV)

in Radiation Dominated (RD) era



in RD vs MD era



DM yield is diluted due to extra entropy production from inflaton decay:

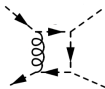
$$Y_X(T_{FI})/Y_X^\infty \propto (T_{FI}/T_{RH})^5,$$

↪ **The lower  $T_{RH}$** , the longer is the dilution and the lower is  $Y_X^\infty$  compared to  $Y_X(T_{FI})$ , the higher is  $\lambda_B$  to account for DM abundance and **the lower is  $c\tau_B$** .

# Effects impacting the relic abundance

$$\Omega_\chi h^2 \propto \frac{1}{\langle \sigma_{\text{eff}} v \rangle}$$

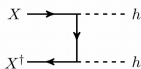
## Higher order corrections



$$\sigma_{\text{eff}} v_{\text{rel}} = \sigma^{\text{NLO}} v_{\text{rel}}$$

can lead to corrections of around 20% to the DM abundance

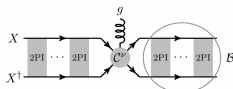
## Born level annihilation



$$\sigma_{\text{eff}} v_{\text{rel}} = \sigma^{\text{tree}} v_{\text{rel}}$$

usual DM codes include *only* born level calculation

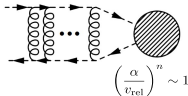
## Bound state formation



$$\langle \sigma_{\text{eff}} v_{\text{rel}} \rangle = \langle \sigma_{\text{ann}} v_{\text{rel}} \rangle + \langle \sigma_{\text{BSF}} v_{\text{rel}} \rangle_{\text{eff}}$$

bound state formation and subsequent decay open up a new effective DM annihilation channel

## Sommerfeld enhancement



$$\sigma_{\text{eff}} v_{\text{rel}} = \sigma^{\text{tree}} v_{\text{rel}} \times S_0$$



Julia Harz

Bound state formation in colored coannihilation scenarios of dark matter

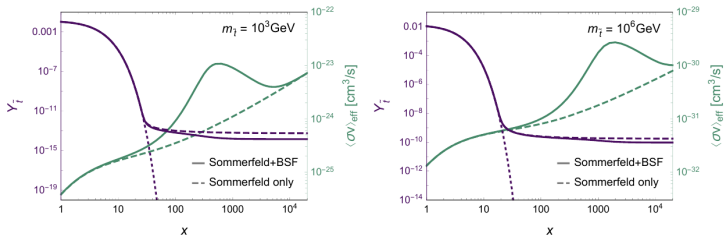


Technische Universität München

## Non perturbative effects on mediator annihilation/Freeze-out due to massless gauge boson (g) exchange

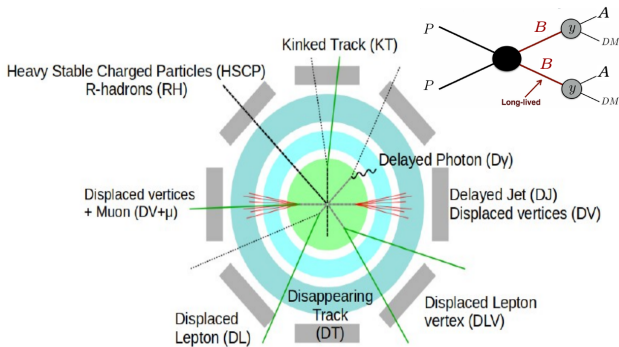
$$\langle \sigma_{\tilde{t}\tilde{t}^*} v \rangle_{\text{eff}} = \langle \sigma_{\tilde{t}\tilde{t}^* \rightarrow g g} v \rangle \times S_{\text{Som}} + \langle \sigma_{\tilde{t}\tilde{t}^* \rightarrow q \bar{q}} v \rangle + \langle \sigma_{\tilde{t}\tilde{t}^* \rightarrow B g} v \rangle \times \frac{\Gamma_{B,\text{dec}}}{\Gamma_{B,\text{ion}} + \Gamma_{B,\text{dec}}}$$

We took into accounts the Sommerfeld enhancement factor and the thermally averaged bound state formation cross-section ( $\Gamma_{B,\text{ion}}$  is the respective ionization rate  $Bg \rightarrow \tilde{t}\tilde{t}^*$  while  $\Gamma_{B,\text{dec}}$  its decay rate,  $B \rightarrow gg$ ) following [Harz, Petraki'18]. Annihilation into q is p-wave suppressed.



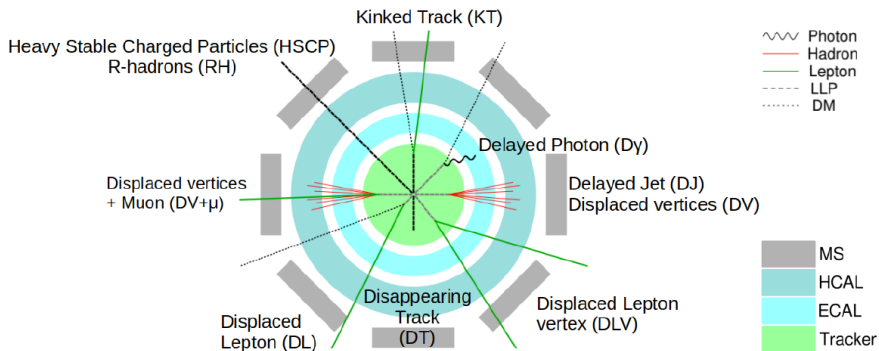
**Prolonged Freeze-out due to late time enhancement of mediator annihilation**

# LLP signatures are framework dependent



- FIMP= feebly interacting massive particle, i.e.  $\lambda_\chi \ll 1$
- $\lambda_\chi \ll 1$  and  $\Delta m/m < 1 \rightsquigarrow$  possibly  $c\tau_B \gtrsim$  collider detector size.
- $B$  long lived particle (LLP), heavy stable particle and displaced events

# Collider searches

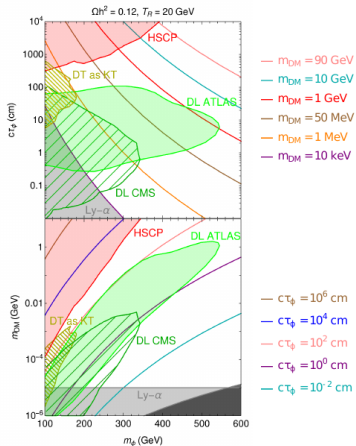
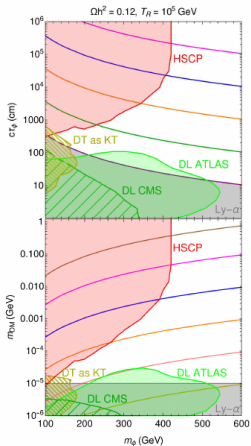




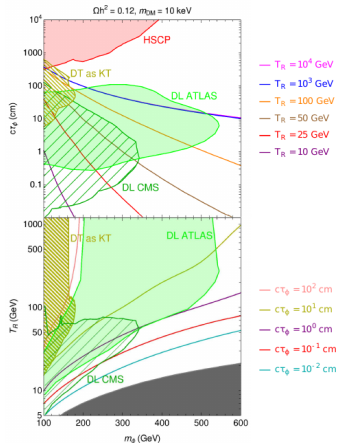
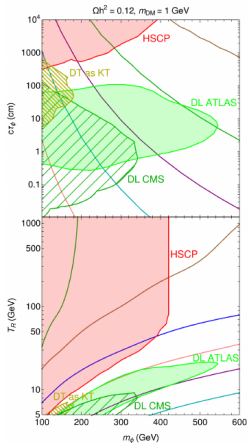
# Collider searches

Signature	Exp. & Ref.	$\mathcal{L}$	Maximal sensitivity	Label
R-hadrons Heavy stable charged particle	CMS [48] ATLAS [49]	12.9 fb <sup>-1</sup> 36.1 fb <sup>-1</sup>	$c\tau \gtrsim 10$ m	RH HSCP
Disappearing tracks	ATLAS [50] CMS [51, 52]	36.1 fb <sup>-1</sup> 140 fb <sup>-1</sup>	$c\tau \approx 30$ cm $c\tau \approx 60$ cm	DT
Displaced leptons	CMS [53] CMS [54] ATLAS [55]	19.7 fb <sup>-1</sup> † 2.6 fb <sup>-1</sup> 139 fb <sup>-1</sup>	$c\tau \approx 2$ cm $c\tau \approx 5$ cm	DL
Displaced vertices + MET	ATLAS [56]	32.8 fb <sup>-1</sup>	$c\tau \approx 3$ cm	DV+MET
Delayed jets + MET	CMS [57]	137 fb <sup>-1</sup>	$c\tau \approx 1 - 3$ m	DJ+MET
Displaced vertices + $\mu$	ATLAS [58]	136 fb <sup>-1</sup>	$c\tau \approx 3$ cm	DV+ $\mu$
Displaced dilepton vertices	ATLAS [59]	32.8 fb <sup>-1</sup>	$c\tau \approx 1 - 3$ cm	DLV
Delayed photons	CMS [60]	77.4 fb <sup>-1</sup>	$c\tau \approx 1$ m	D $\gamma$

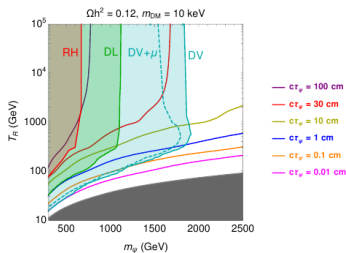
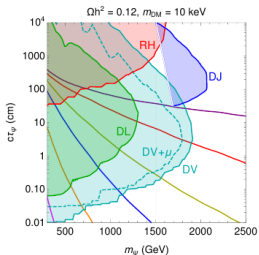
# Leptophilic DM



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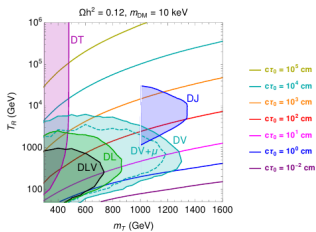
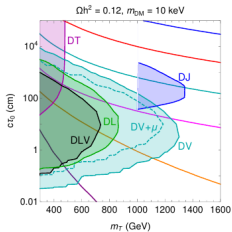
# Topphilic DM



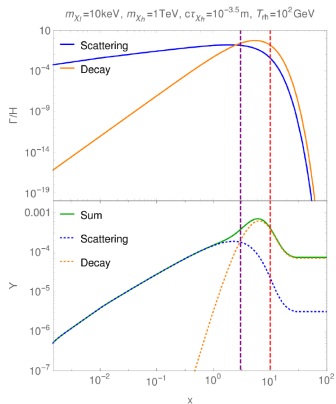
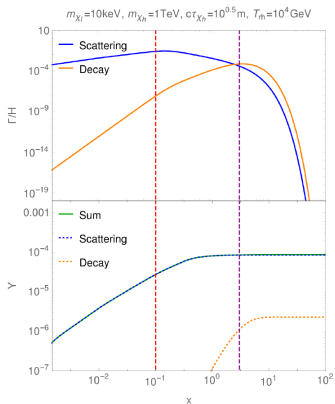
# Singlet-Triplet DM

$$\mathcal{L}_{BSM} = -\frac{m_S}{2}\bar{\chi}_S\chi_S - \frac{m_T}{2}Tr[\bar{\chi}_T\chi_T] + \frac{1}{2}Tr[\bar{\chi}_T i \not{D}\mu\chi_T] \\ + \frac{\kappa}{\Lambda}(W_{\mu\nu}^a\bar{\chi}_S\sigma^{\mu\nu}\chi_T^a + \text{h.c.}),$$

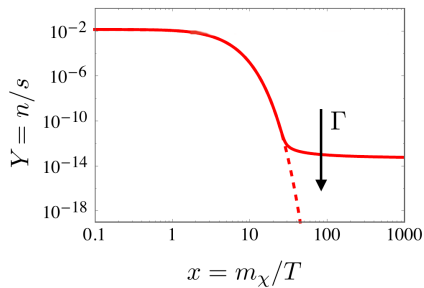
$$\chi_S = \chi_l^0, \quad \chi_T = \begin{pmatrix} \chi_h^0/\sqrt{2} & \chi^+ \\ \chi^- & -\chi_h^0/\sqrt{2} \end{pmatrix}$$



# Singlet-Triplet DM



# Thermal DM from non-relativistic Freeze-out (WIMP)



- DM annihilation driven freeze-out
- $\chi$  chem. & kin. equilibrium
- $\Omega_\chi \propto 1/\langle\sigma v\rangle_{\chi\chi}$
- $\Omega_\chi h^2 = 0.12$   
 $\rightsquigarrow \langle\sigma v\rangle_{\chi\chi} = 3 \times 10^{-26} \text{ cm}^3/\text{s}$
- $x = m_\chi/T$  and  $x_{\text{FO}} \sim 25$

Carefull,

- coannihilations, velocity suppressed  $\langle\sigma v\rangle$ , potential large contributions from higher order processes, etc, not taken into account in this simple picture.
- WIMP still free-stream after kinetic decoupling: for e.g. 100 GeV DM with  $T_{\text{KD}} \sim 30$  MeV, you expect  $M_{\text{fs}} \sim 10^{-6} M_\odot$ .

bla



This is really the end