

Floccinaucinihilipilification

by

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collaborators: Joe Davighi, Ben Gripaios, Joe
Tooby-Smith, Scott Melville

“The act of deciding something is worthless”

Standard Model $\times U(1)$

Semi-simple extensions

During the **2000s**

We wanted to be the Grand Architects



RPV mSUGRA

PHYSICAL REVIEW D

covering particles, fields, gravitation, and cosmology

Highlights Recent Accepted Collections Authors Referees Search Pre

R -parity violating minimal supergravity model

B. C. Allanach, A. Dedes, and H. K. Dreiner

Phys. Rev. D **69**, 115002 – Published 2 June 2004; Erratum [Phys. Rev. D **72**, 079902 \(2005\)](#)



During the 2020s

Happy with **any** beyond SM roof



Gauge Rank++

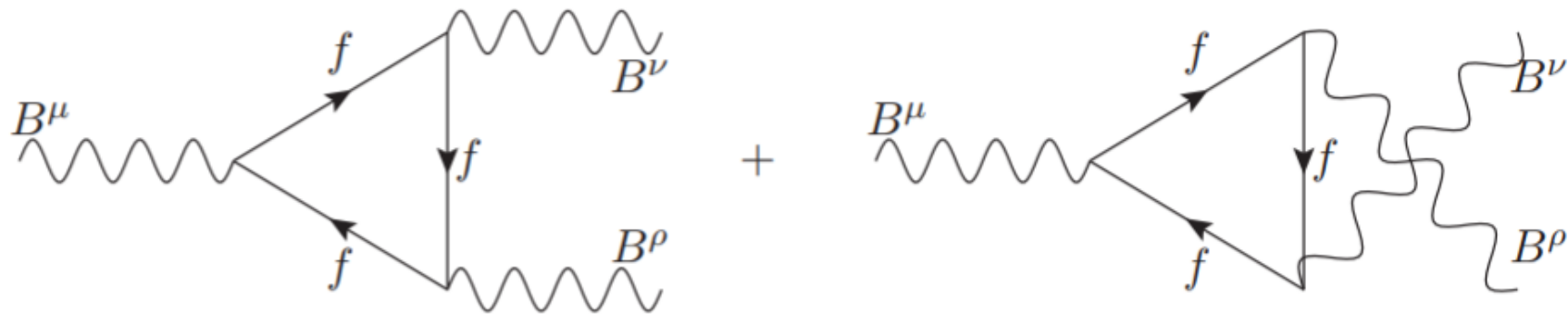
~~$U(1)_X$~~ Z' can explain $b \rightarrow s\mu^+\mu^-$
and/or fermion mass problem

family dependent charges

Z' couplings depend on these

So they change Z' phenomenology

SM: Local Anomalies



$$A \equiv \sum_{LH f_i} Y_i^3 - \sum_{RH f_i} Y_i^3$$

+two RH $B \rightarrow g/G/W$.

$$Y^3 : \quad 0 = \sum_{j=1}^3 \left(6Y_{Q_j}^3 + 3Y_{U_j}^3 + 3Y_{D_j}^3 + 2Y_{L_j}^3 + Y_{E_j}^3 \right),$$

$$3^2 Y : \quad 0 = \sum_{j=1}^3 \left(2Y_{Q_j} + Y_{U_j} + Y_{D_j} \right),$$

$$2^2 Y : \quad 0 = \sum_{j=1}^3 \left(3Y_{Q_j} + Y_{L_j} \right),$$

$$\text{grav}^2 Y : \quad 0 = \sum_{j=1}^3 \left(6Y_{Q_j} + 3Y_{U_j} + 3Y_{D_j} + 2Y_{L_j} + Y_{E_j} \right).$$

Extra $U(1)$

3 RH ν : N_i

Field labels denote the extra $U(1)$ charge

18 Charges

Anomaly cancellations conditions

$$3^2 X : 0 = \sum_{j=1}^3 (2Q_j + U_j + D_j),$$

$$2^2 X : 0 = \sum_{j=1}^3 (3Q_j + L_j),$$

$$Y^2 X : 0 = \sum_{j=1}^3 (Q_j + 8U_j + 2D_j + 3L_j + 6E_j),$$

$$\text{grav}^2 X : 0 = \sum_{j=1}^3 (6Q_j + 3U_j + 3D_j + 2L_j + E_j + N_j),$$

$$YX^2 : 0 = \sum_{j=1}^3 (Q_j^2 - 2U_j^2 + D_j^2 - L_j^2 + E_j^2),$$

$$X^3 : 0 = \sum_{j=1}^3 (6Q_j^3 + 3U_j^3 + 3D_j^3 + 2L_j^3 + E_j^3 + N_j^3).$$

Diophantus

Solutions over \mathbb{Z}^{18}

Can absorb overall real factor in

$$-g \sum_{\psi} Q_{\psi} \bar{\psi} X_{\mu} \gamma^{\mu} \psi$$

Charges are **commensurate**

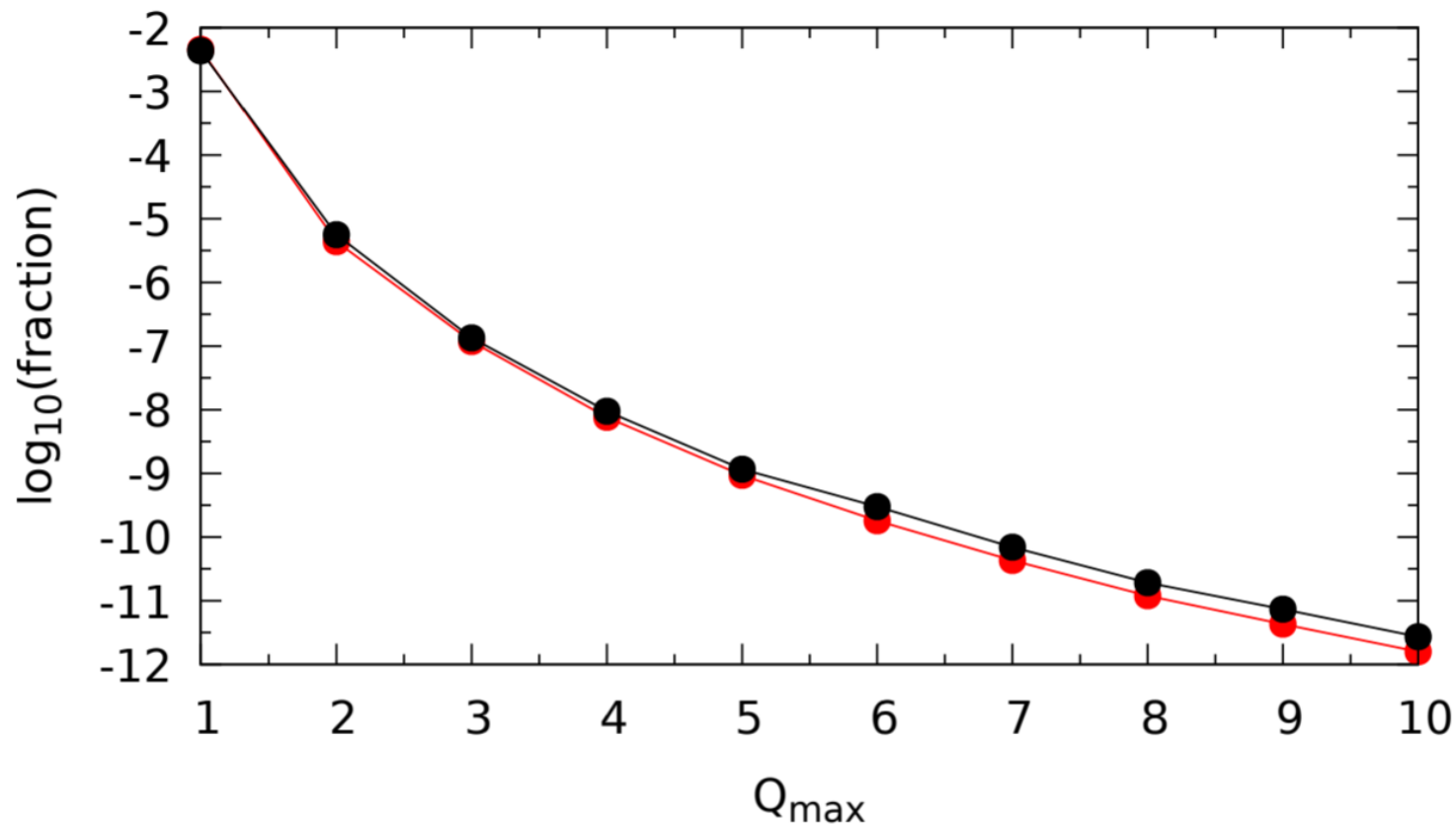
For generic equations: number theory
can solve one cubic in 3D

Anomaly-free Atlas

Charges between $-Q_{max}$ and $Q_{max} = 10$: numerical scan (~~$21^{18} \sim 10^{24}$~~): BCA, Davighi, Melville, 1812.04602.

An **Anomaly-Free Atlas** is available for public use:

<http://doi.org/10.5281/zenodo.1478085>



18 charges and 6 ACCs: sparser away from $\mathbf{0}$. Want analytic understanding.

Examples

	Q_1	Q_2	Q_3	U_1	U_2	U_3	D_1	D_2	D_3	L_1	L_2	L_3	E_1	E_2	E_3	N_1	N_2	N_3
A	0	0	1	0	0	-4	0	0	-2	0	0	-3	0	0	6	0	0	0
B	1	1	1	-1	-1	-1	-1	-1	-1	-3	-3	-3	3	3	3	3	3	3
C	-1	0	1	-1	0	1	-1	0	1	-1	0	1	-1	0	1	0	0	0

A is TFHM (BCA, Davighi, arXiv:1809.01158)

B is $B - L$, vector-like

C has inter-family cancellation

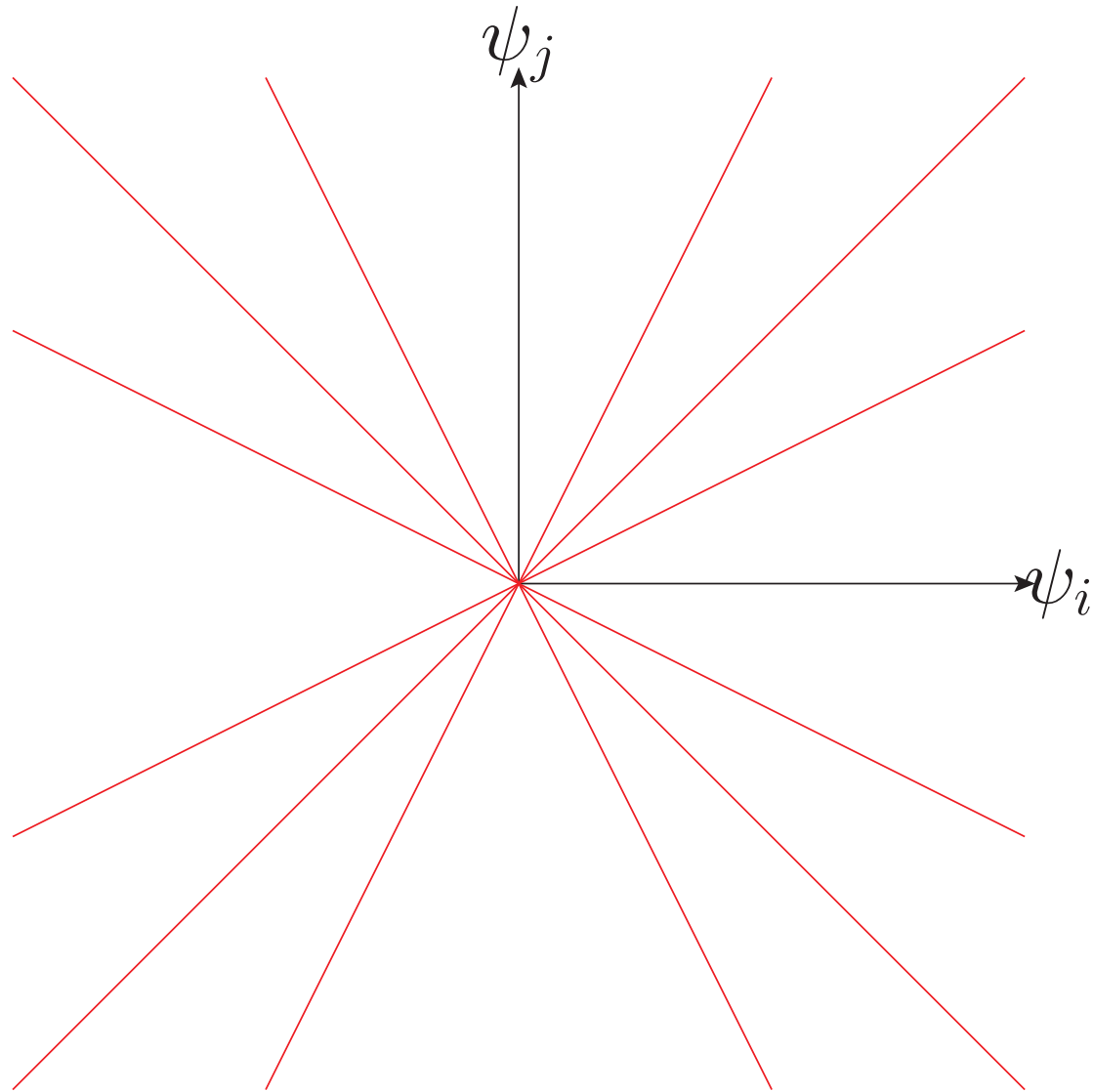
Analytic Solution: any Q_{max}

g re-scaling symmetry of charges ψ_i
leads to an equivalence class

So solutions in \mathbb{Z}^{18} equivalent to \mathbb{Q}^{18}

\mathbb{Q}^{18} is a field: can define **geometry** on
it

Projective space $P\mathbb{Q}^{17}$



Preliminaries

4 linear ACCS: $P\mathbb{Q}^{17} \rightarrow P\mathbb{Q}^{13}$.

Then, find intersection of quadratic

$$0 = \sum_{j=1}^3 (Q_j^2 - 2U_j^2 + D_j^2 - L_j^2 + E_j^2)$$

and cubic surface

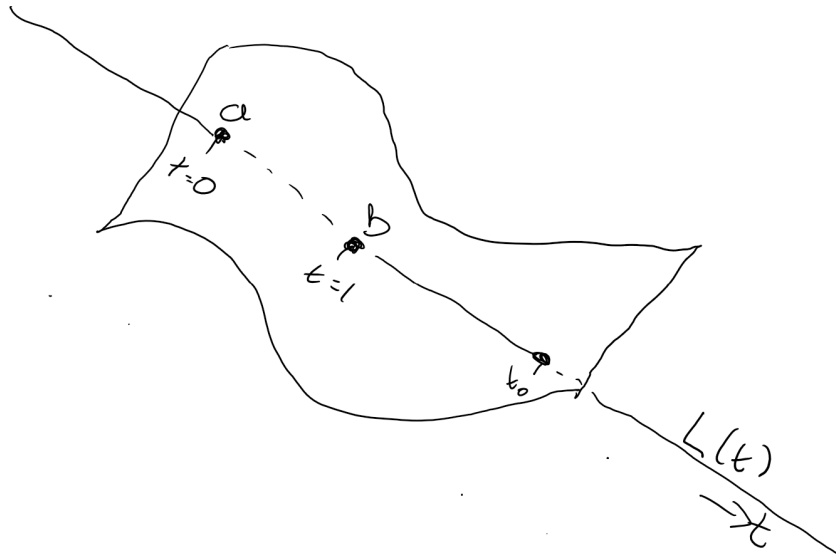
$$0 = \sum_{j=1}^3 (6Q_j^3 + 3U_j^3 + 3D_j^3 + 2L_j^3 + E_j^3 + N_j^3)$$

The Method of Chords¹

Rational cubic $c(\psi_i) = 0$.

$$L(t) = a + t(b - a).$$

$$c(L(t)) = kt(t - 1)(t - t_0); \quad k, t_0 \in \mathbb{Q}$$



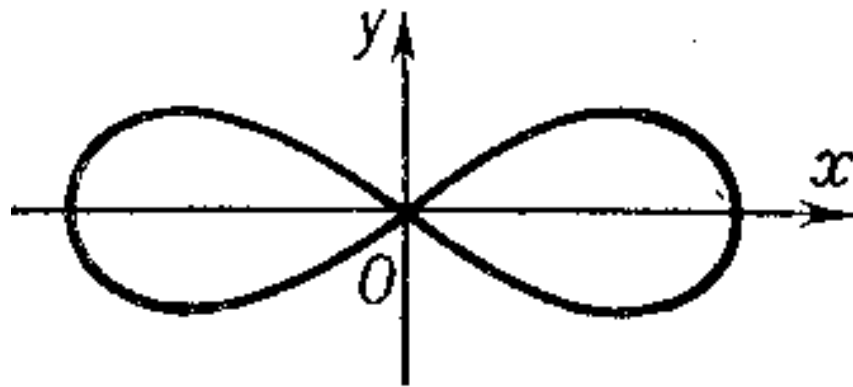
Important caveat:
 $c(L(t)) = 0$
irrespective of t .

¹Newton, Fermat, C17

Double Points

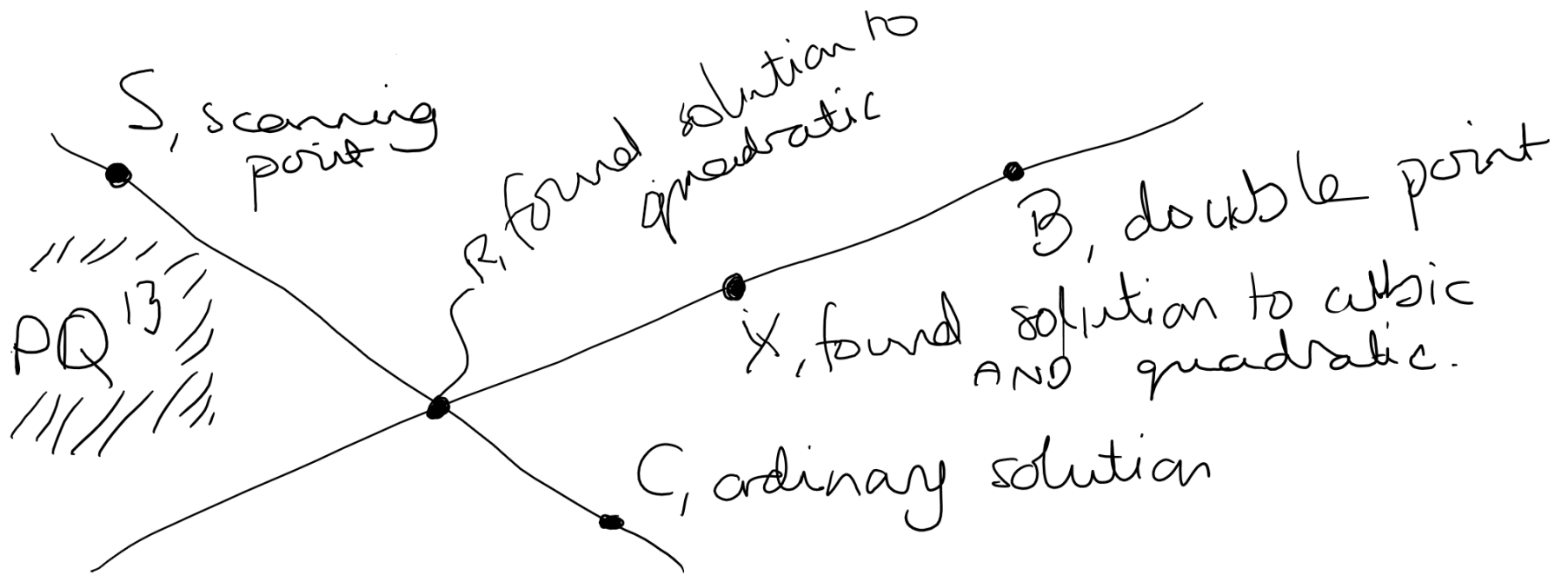
Solutions of multiplicity two. Partial derivatives vanish there, eg origin

$$(x^2 + y^2 + a^2)^2 - 4a^2x^2 - a^4 = 0$$



B is *double point* of quadratic **and** cubic

Method



- Every solution to quadratic R lies on *some* line SC
- B is double point of quadratic $\Rightarrow RB$ in quadratic
- Scan S (parameters) to find *all* R , extend line to find *all* X .

The Nitty-Gritty

$$\begin{aligned}
 Q_1 &= \Gamma - \Sigma + \Lambda S_{Q_1}, \\
 Q_2 &= \Gamma + \Lambda S_{Q_2}, \\
 Q_3 &= \Gamma + \Sigma + \Lambda S_{Q_3}, \\
 U_1 &= -\Gamma - \Sigma + \Lambda S_{U_1}, \\
 U_2 &= -\Gamma + \Lambda S_{U_2}, \\
 U_3 &= -\Gamma + \Sigma + \Lambda S_{U_3}, \\
 D_1 &= -\Gamma - \Sigma + \Lambda S_{D_1}, \\
 D_2 &= -\Gamma + \Lambda S_{D_2}, \\
 D_3 &= -\Gamma + \Sigma + \Lambda S_{D_3}, \\
 L_1 &= -3\Gamma - \Sigma + \Lambda S_{L_1}, \\
 L_2 &= -3\Gamma + \Lambda S_{L_2}, \\
 L_3 &= -3\Gamma + \Sigma + \Lambda S_{L_3}, \\
 E_1 &= 3\Gamma - \Sigma + \Lambda S_{E_1}, \\
 E_2 &= 3\Gamma + \Lambda S_{E_2}, \\
 E_3 &= 3\Gamma + \Sigma + \Lambda S_{E_3}, \\
 N_1 &= 3\Gamma + \Lambda S_{N_1}, \\
 N_2 &= 3\Gamma + \Lambda S_{N_2}, \\
 N_3 &= 3\Gamma + \Lambda S_{N_3},
 \end{aligned}$$

$$\begin{aligned}
 \Gamma &= c(R, R, R) + r\delta_{c(B,R,R),0}\delta_{c(R,R,R),0}, \\
 \Sigma &= (-3c(B, R, R) + t\delta_{c(B,R,R),0}\delta_{c(R,R,R),0}) \\
 &\quad (q(S, S) + a\delta_{q(S,S),0}\delta_{q(C,S),0}), \\
 \Lambda &= (-3c(B, R, R) + t\delta_{c(B,R,R),0}\delta_{c(R,R,R),0}) \\
 &\quad (-2q(C, S) + b\delta_{q(S,S),0}\delta_{q(C,S),0}).
 \end{aligned}$$

$$\begin{aligned}
 q(P, P') &:= \sum_{i=1}^3 (Q_i Q_i' - 2U_i U_i' + D_i D_i' \\
 &\quad - L_i L_i' + E_i E_i'), \\
 c(P, P', P'') &:= \sum_{i=1}^3 (6Q_i Q_i' Q_i'' + 3U_i U_i' U_i'' + 3D_i D_i' D_i'' \\
 &\quad + 2L_i L_i' L_i'' + E_i E_i' E_i'' + N_i N_i' N_i''). \quad (3)
 \end{aligned}$$

$$R = q(S, S)C - 2q(C, S)S + \delta_{q(S,S),0}\delta_{q(C,S),0}(aC + bS),$$

$$S_{Q_3} = \frac{1}{2} \left[-2S_{Q_1} - 2S_{Q_2} + \sum_{i=1}^3 (S_{D_i} + S_{N_i}) \right],$$

$$S_{U_3} = - \left[S_{U_1} + S_{U_2} + \sum_{i=1}^3 (2S_{D_i} + S_{N_i}) \right],$$

$$S_{L_3} = -\frac{1}{2} \left[2S_{L_1} + 2S_{L_2} + 3 \sum_{i=1}^3 (S_{D_i} + S_{N_i}) \right],$$

$$S_{E_3} = -S_{E_1} - S_{E_2} + \sum_{i=1}^3 (3S_{D_i} + 2S_{N_i}).$$

Solution Space

Is a projective *variety*

Over-parameterisation in terms of 18 integers

$$S_{Q_1}, S_{Q_2}, S_{U_1}, S_{U_2}, S_{D_1}, S_{D_2}, S_{D_3}, S_{L_1}, S_{L_2}, S_{E_1}, S_{E_2}, \\ S_{N_1}, S_{N_2}, S_{N_3}, a, b, r, t \in \mathbb{Q}$$

It is at most **11-D**: $S \cdot C = S \cdot B = 0$.

BCA, Gripaios, Tooby-Smith 2104.14555

Check

An inverse ($S = T, a = 0, b = 1, r = 0, t = 1$), was checked against all 21 549 920 Anomaly-free Atlas solns.

BCA, Gripaios, Tooby-Smith 2104.14555

Semi-simple extensions

We allow *non-abelian* $\bigoplus_i \mathfrak{g}_i$

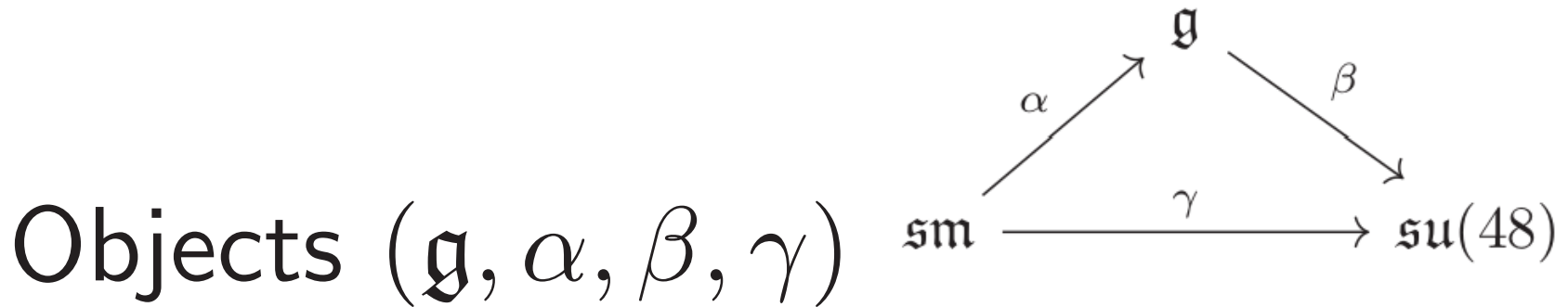
48 fermionic states of $\text{SM} + 3\nu_R$:
unitary rep to preserve kinetic terms

Largest algebra $\mathfrak{su}(48)$ is anomalous

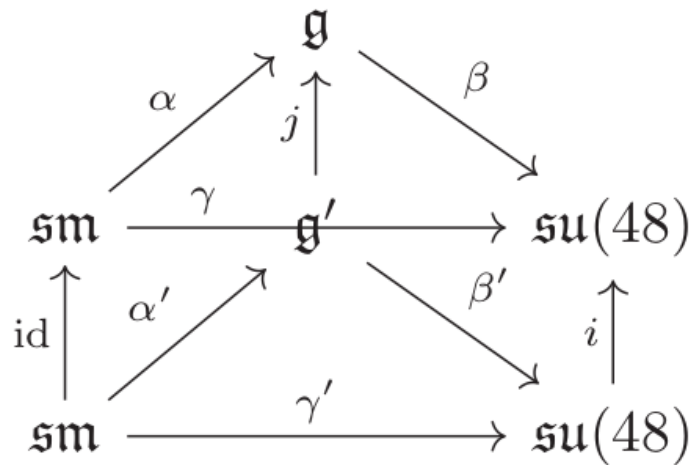
Look for anomaly-free \mathfrak{g} such that
 $\mathfrak{su}(48) \supset \mathfrak{g} \supset \mathfrak{su}(3) \oplus \mathfrak{su}(2) \oplus \mathfrak{u}(1)_Y$

Automorphic \mathfrak{g} are equivalent

Embeddings



Map (j, i) from
 $(\mathfrak{g}', \alpha', \beta', \gamma')$ \rightarrow $(\mathfrak{g}, \alpha, \beta, \gamma)$:



Goal

Find all inequivalent diagrams. Cartan subalgebras \mathfrak{h}_{SM} , \mathfrak{h} , \mathfrak{h}_{48} :

$$\begin{array}{ccc}
 & \mathfrak{g} & \\
 \nearrow \kappa & & \searrow \beta \\
 \mathfrak{su}(3) \oplus \mathfrak{su}(2) & \xrightarrow{\rho} & \mathfrak{su}(48)
 \end{array}
 \qquad
 \begin{array}{ccc}
 & \mathfrak{h} & \\
 \nearrow \tilde{\kappa} & & \searrow \beta| \\
 \mathfrak{u}(1) & \xrightarrow{\tilde{\rho}} & \mathfrak{h}_{48}
 \end{array}$$

(j, i) is an equivalence if j is an isomorphism. A diagram is maximal (minimal) if only maps out of (into) it are equivalences.

Computer Program

Evaluate all embeddings β : keep only anomaly-free ones. Then find all embeddings κ using theory of maximal embeddings. Then find all κ and β s.t. \exists a ρ matching embedding of SM, check if compatible $\tilde{\kappa}, \tilde{\rho}$ exist.

Use projection matrices instead of embeddings and LieART2.0.

Results

342 possibilities BCA, Gripaos, Tooby-Smith
2104.14555

Examples: $so(10) \oplus su(2) : (\mathbf{16}, \mathbf{3})$

$su(12) \oplus su(2) \oplus su(2):$
 $(\overline{\mathbf{12}}, \mathbf{2}, \mathbf{1}) \oplus (\mathbf{12}, \mathbf{1}, \mathbf{2})$

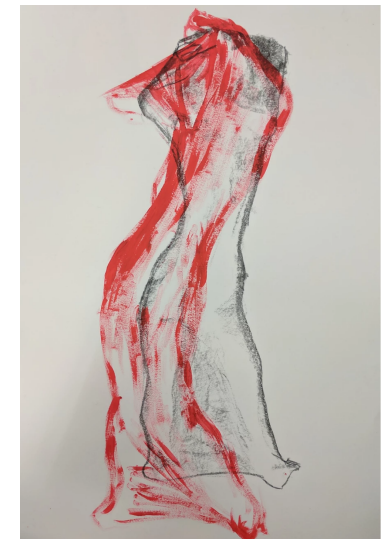
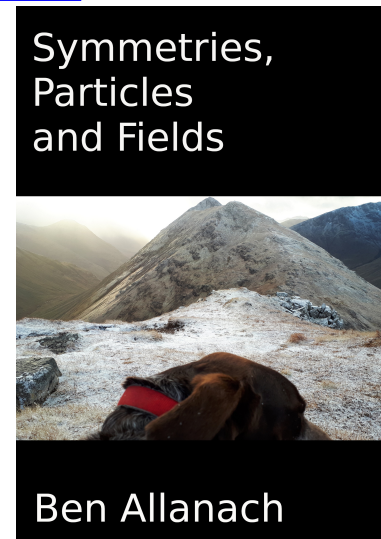
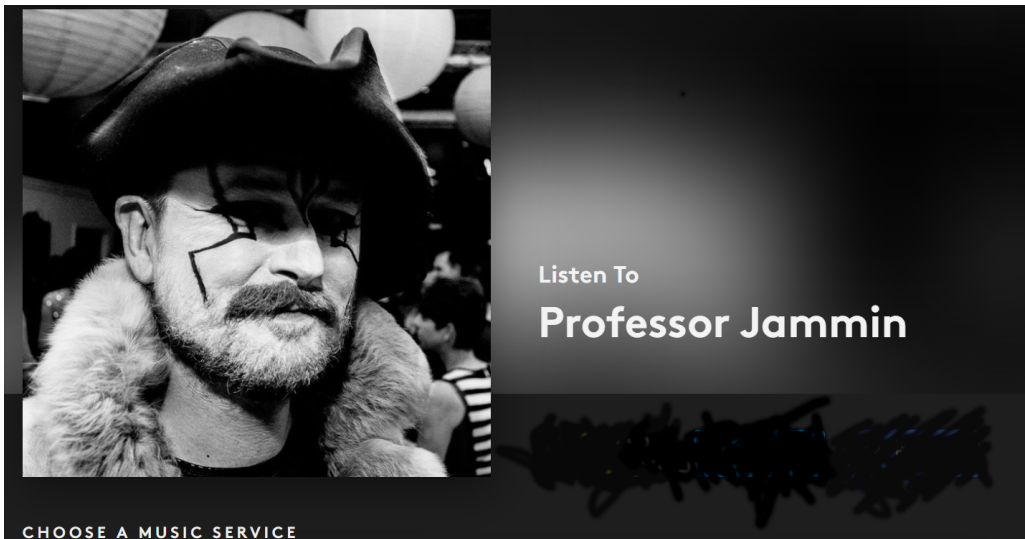
$su(4) \oplus sp(6) \oplus sp(6):$
 $(\overline{\mathbf{4}}, \mathbf{6}, \mathbf{1}) \oplus (\mathbf{4}, \mathbf{1}, \mathbf{6})$ - Electroweak flavour
unification, Davighi, Tooby-Smith, 2201.07245

Happy birthday Herbi!

All anomaly-free $SM \times U(1)$ extensions
and semi-simple extensions

Davighi, Tooby-Smith 2206.11271

Plug for my [music](#), [lectures \(18€\)](#) and [Quantum Selves art](#):



One family anomaly cancellation

If the hypercharges are quantised but otherwise free, the gauge ACC implies the gravitational ACC².

Deforming to $SU(3) \times SU(2) \times \mathbb{R}_Y$, and allowing the hypercharges Y of the chiral fermionic fields to float, the combination of gauge ACC and gravitational ACC implies that the hypercharges must be commensurate³.

²Lohitsiri and Tong, [arXiv:1907.00514](https://arxiv.org/abs/1907.00514)

³Weinberg, *The Quantum Theory of Fields (1995)*, Cambridge University Press

Caveat?

Anomalies can be cancelled by a Wess-Zumino term, a higher dimension \mathcal{L} operator of topological origin. These can eg be obtained by integrating out heavy states.

Generic ones are hard to generate whilst making the relevant heavy states heavy from $u(1)$ spontaneous breakdown.

Other Constraints

Consider perturbativity:

$$\frac{d \ln g}{d \ln \mu} = \frac{g^2 \sum_{i \in \chi_{UV}} z_i^2}{24\pi^2} < 1$$

$$\Leftrightarrow g < \frac{2\pi\sqrt{6}}{\sqrt{\sum_{i \in \chi_{UV}} z_i^2}}.$$

Q_{\max}	Solutions	Symmetry	Quadratics	Cubics	Time/sec
1	38	16	144	38	0.0
2	358	48	31439	2829	0.0
3	4116	154	1571716	69421	0.1
4	24552	338	34761022	932736	0.6
5	111152	796	442549238	7993169	6.8
6	435305	1218	3813718154	49541883	56
7	1358388	2332	24616693253	241368652	312
8	3612734	3514	127878976089	978792750	1559
9	9587085	5648	558403872034	3432486128	6584
10	21546920	7540	2117256832910	10687426240	24748

Inequivalent solutions with 3 RH ν

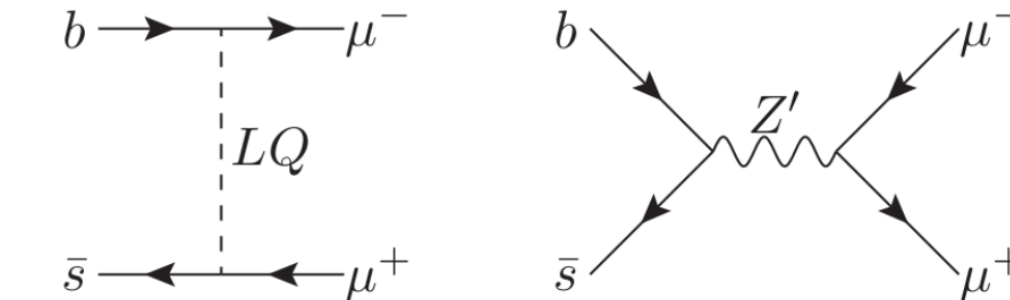
Q	Q	Q	ν	ν	ν	e	e	e	u	u	u	L	L	L	d	d	d
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	-1	0	1	-1	0	1
0	0	0	0	0	0	-1	0	1	0	0	0	-1	0	1	0	0	0
0	0	0	0	0	0	-1	0	1	-1	0	1	0	0	0	-1	0	1
-1	0	1	0	0	0	0	0	0	0	0	0	-1	0	1	0	0	0
-1	0	1	0	0	0	0	0	0	-1	0	1	0	0	0	-1	0	1
-1	0	1	0	0	0	-1	0	1	-1	0	1	0	0	0	0	0	0
-1	0	1	0	0	0	-1	0	1	-1	0	1	-1	0	1	-1	0	1

eg: $Q_{max} = 1$, $N_i = 0$. Charges within a species are listed in *increasing order*.

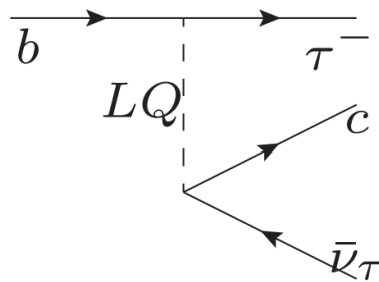
Philosophy and Organisation

There are hundreds of specific models. Many of them reduce to the same important features at the TeV-scale, so we shall take a **bottom up** approach and trust LHCb data more than detailed theoretical assumptions.

Neutral current:



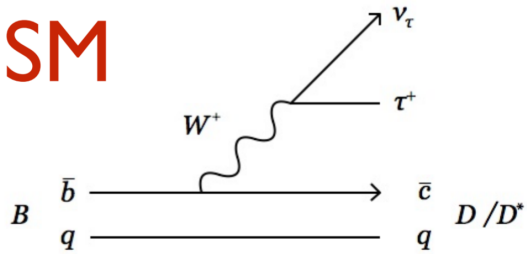
Charged current:



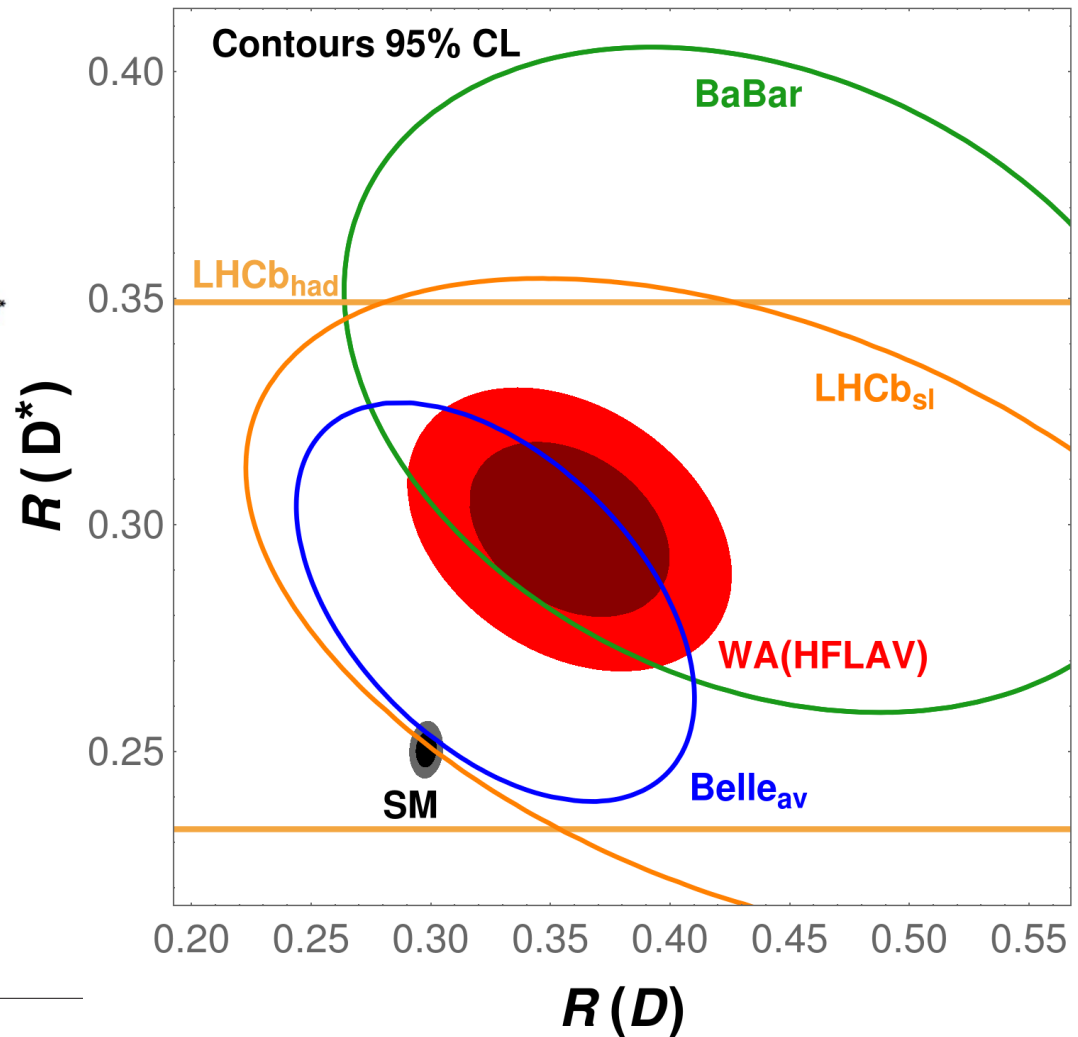
Vector/scalar option for leptoquark (LQ)

$$R_{D^{(*)}} = BR(B^- \rightarrow D^{(*)}\tau\nu) / BR(B^- \rightarrow D^{(*)}\mu\nu)^4$$

SM



SM: 3.1σ

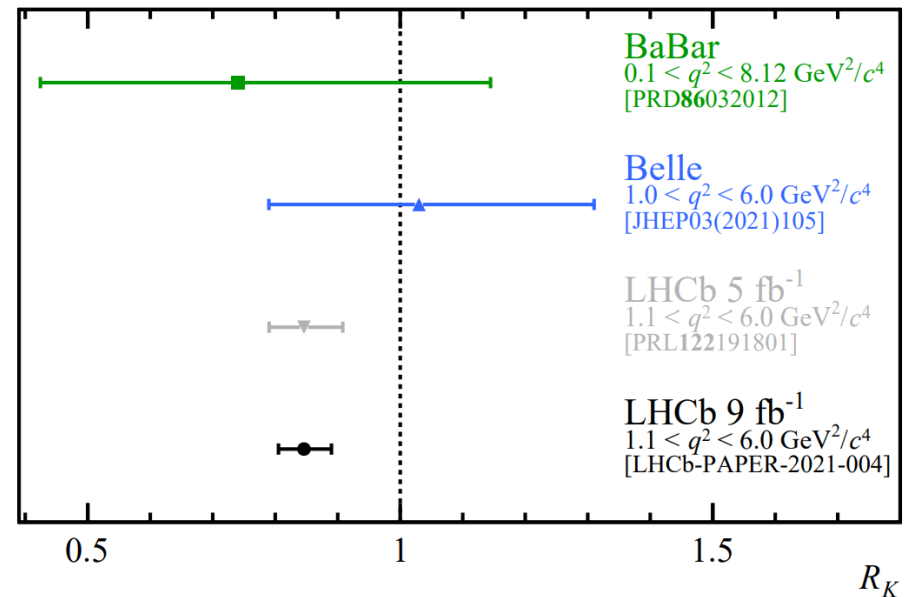
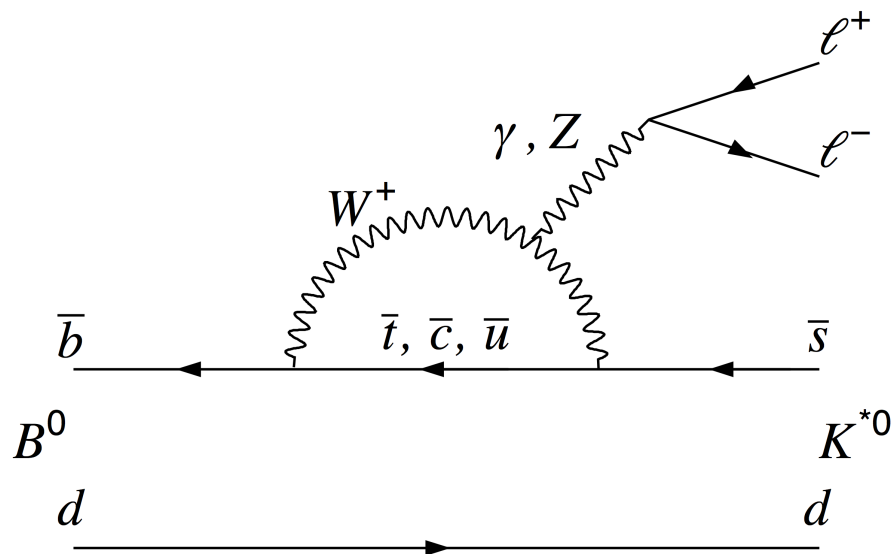


⁴Kind courtesy of M Jung

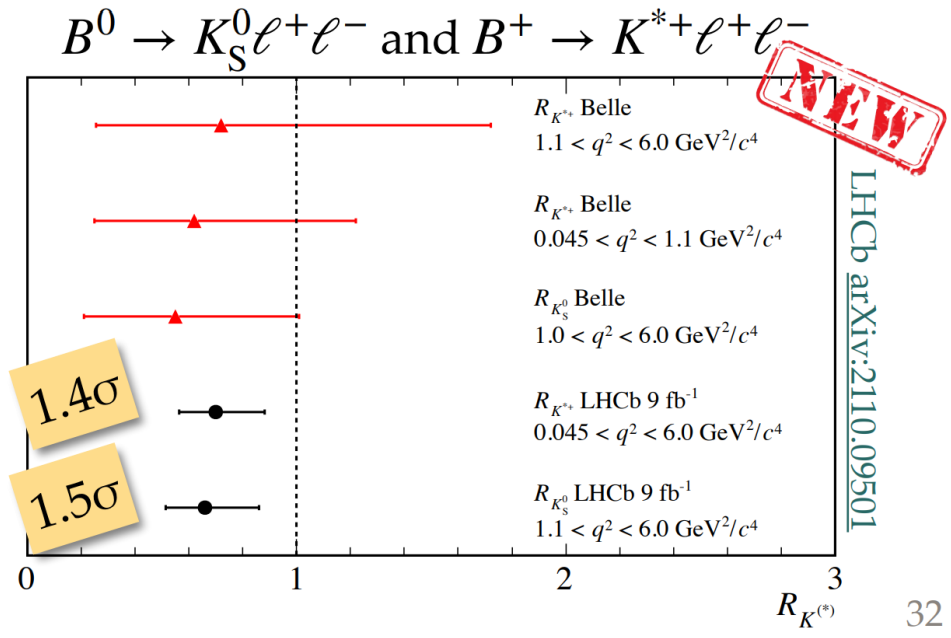
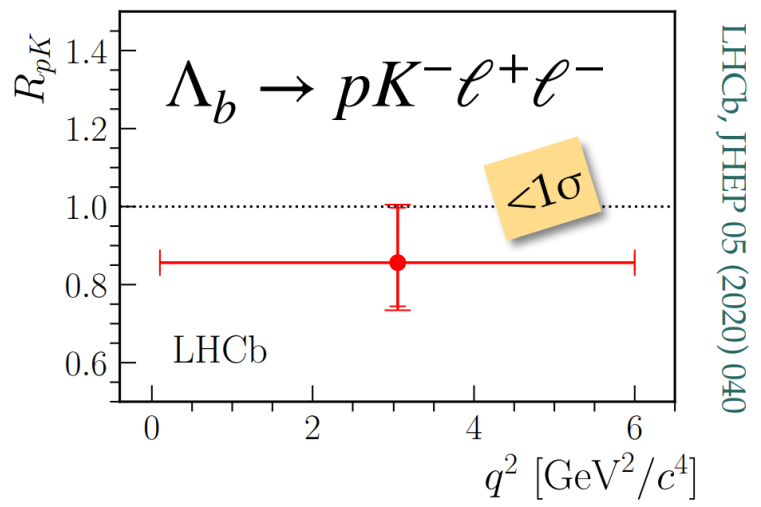
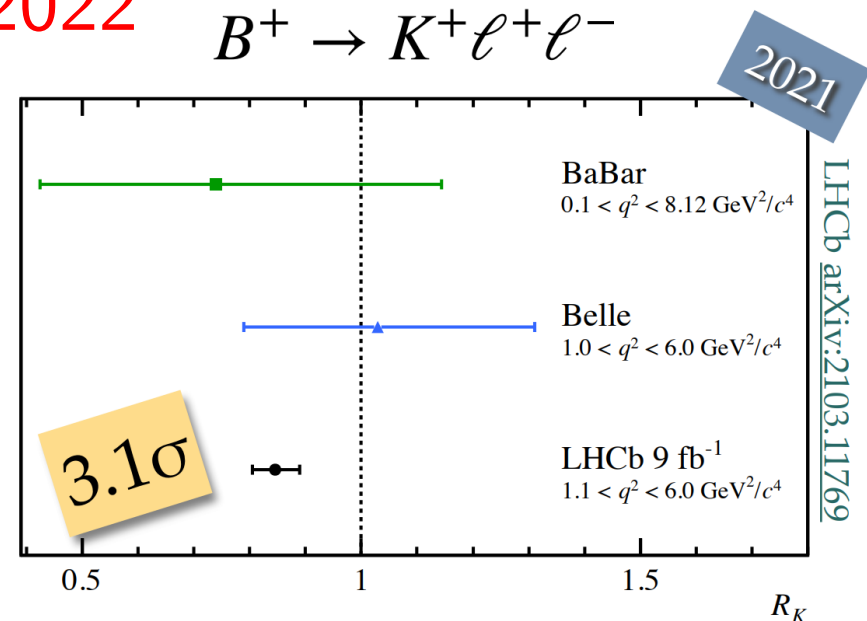
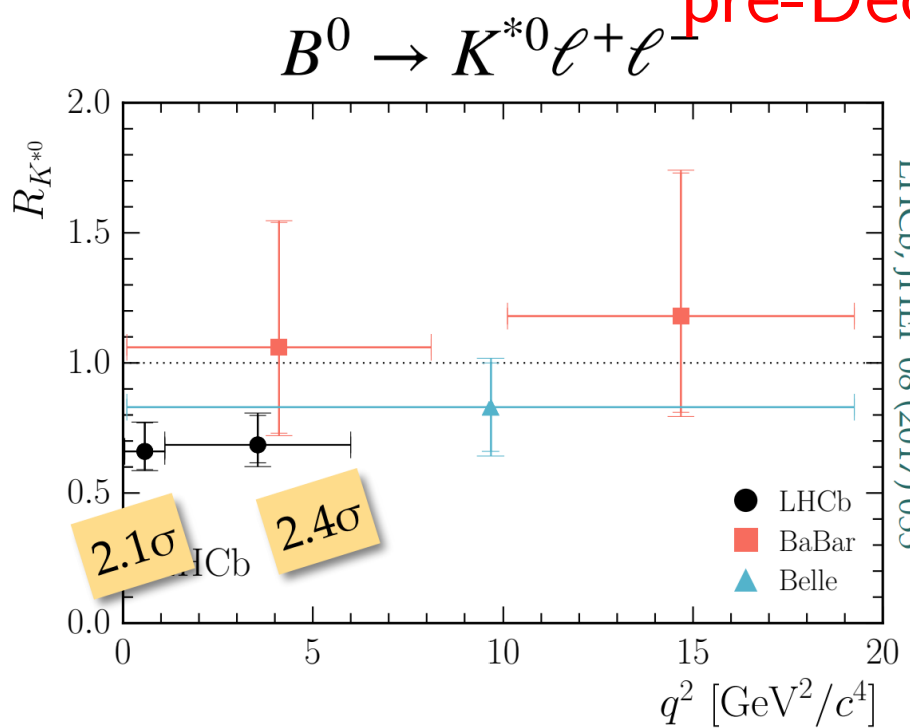
$R_K^{(*)}$ in Standard Model

$$R_K = \frac{BR(B \rightarrow K \mu^+ \mu^-)}{BR(B \rightarrow K e^+ e^-)}, \quad R_{K^*} = \frac{BR(B \rightarrow K^* \mu^+ \mu^-)}{BR(B \rightarrow K^* e^+ e^-)}.$$

These are **rare decays** (each $BR \sim \mathcal{O}(10^{-7})$) because they are absent at tree level in SM+EW+CKM

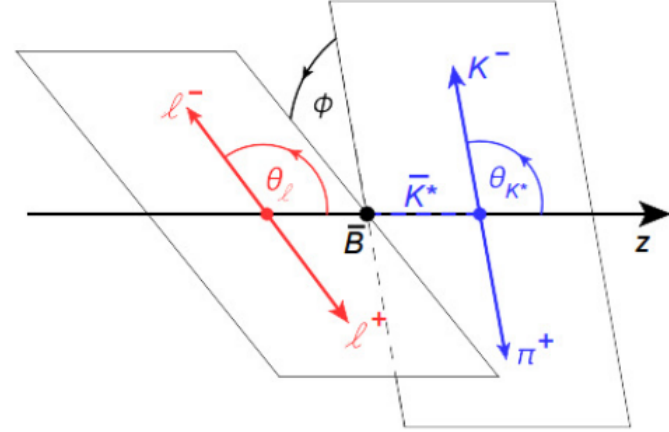
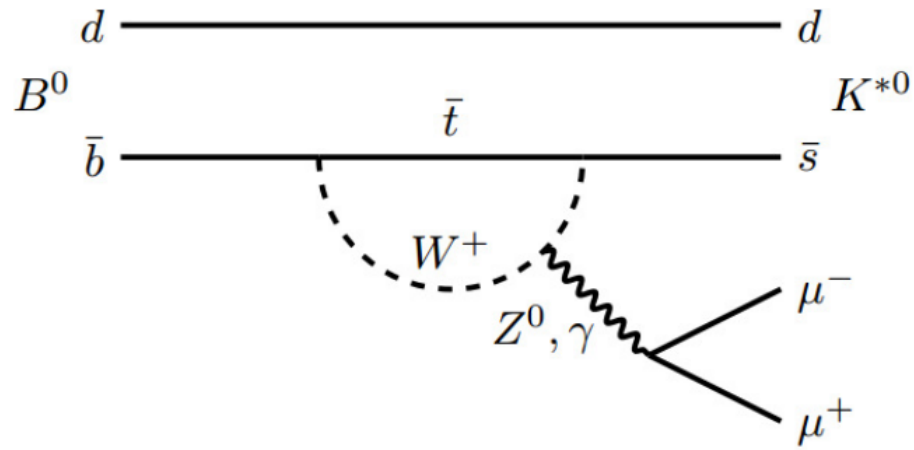


pre-Dec 2022



Stolen from Capdevila et al, *Flavour Anomaly Workshop '21*

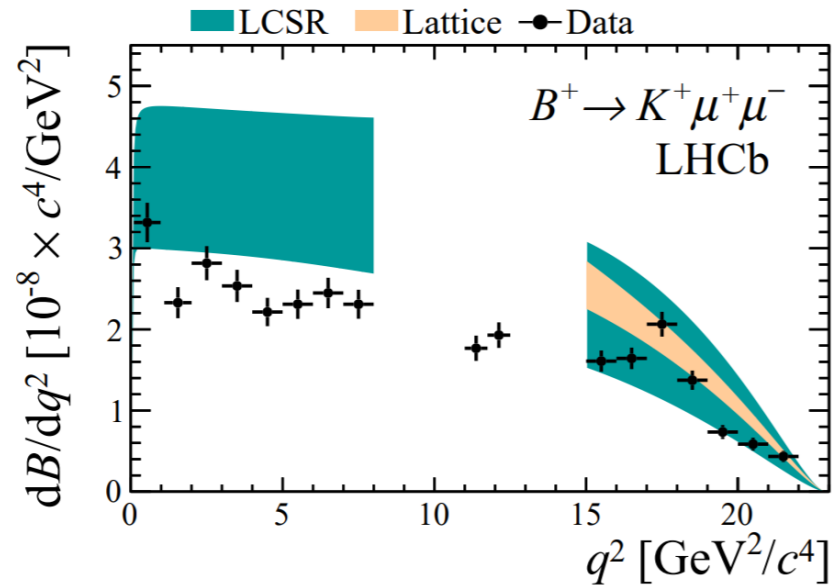
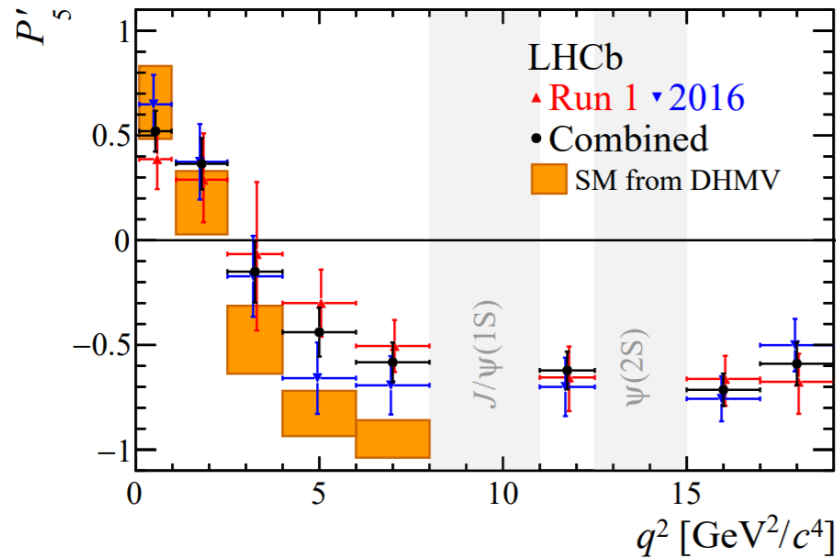
$$B^0 \rightarrow K^{*0} (\rightarrow K^+ \pi^-) \mu^+ \mu^-$$



Decay fully described by three helicity angles $\vec{\Omega} = (\theta_\ell, \theta_K, \phi)$ and $q^2 = m_{\mu\mu}^2$

$$\begin{aligned} \frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} &= \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ &\quad - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi \\ &\quad + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi \\ &\quad + \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \\ &\quad \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right] \end{aligned}$$

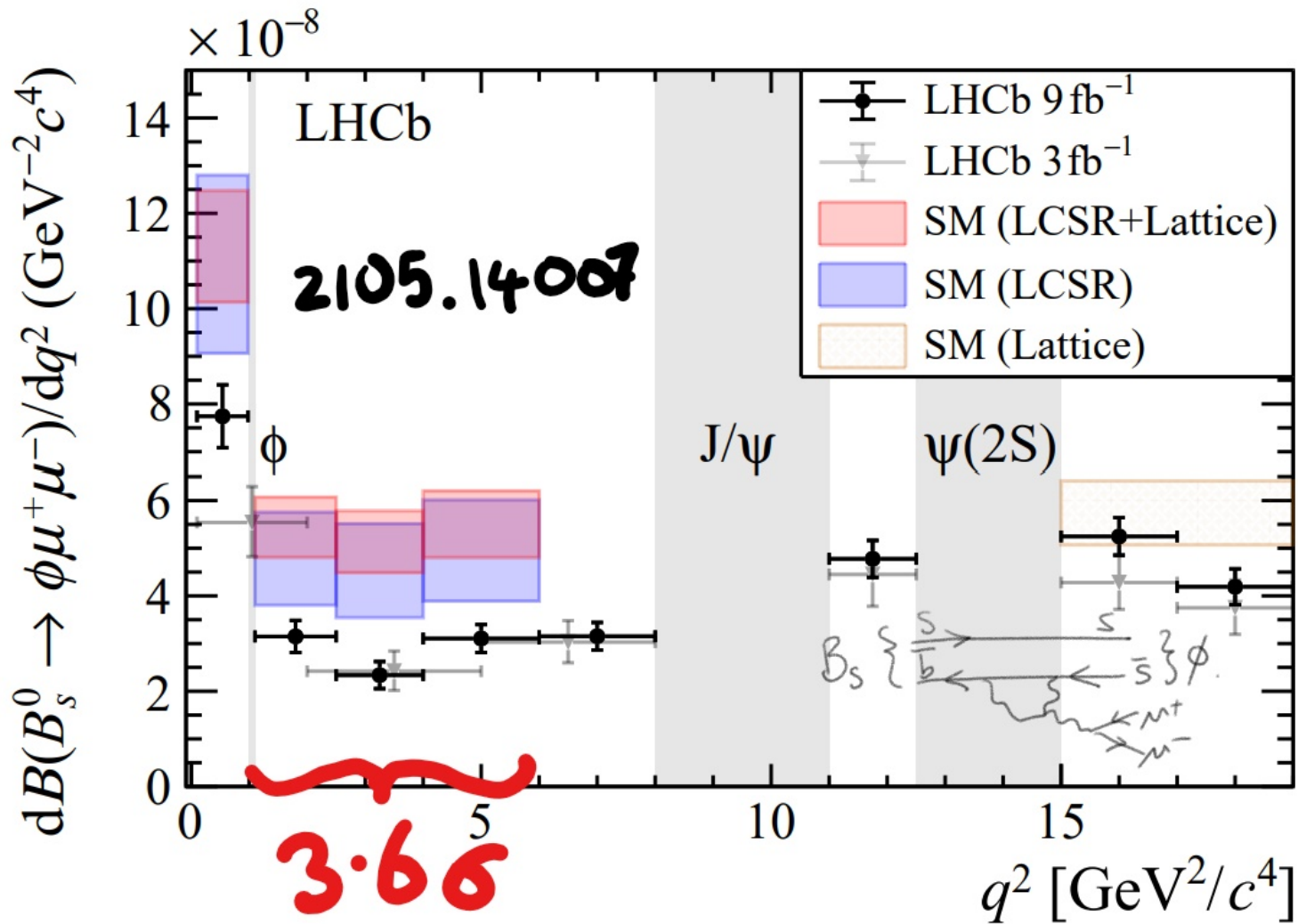
P'_5



$P'_5 = S_5 / \sqrt{F_L(1 - F_L)}$, leading form factor uncertainties cancel⁵

⁵LHCb, 2003.04831

$$B_s \rightarrow \phi \mu^+ \mu^- : \phi = (s\bar{s})$$

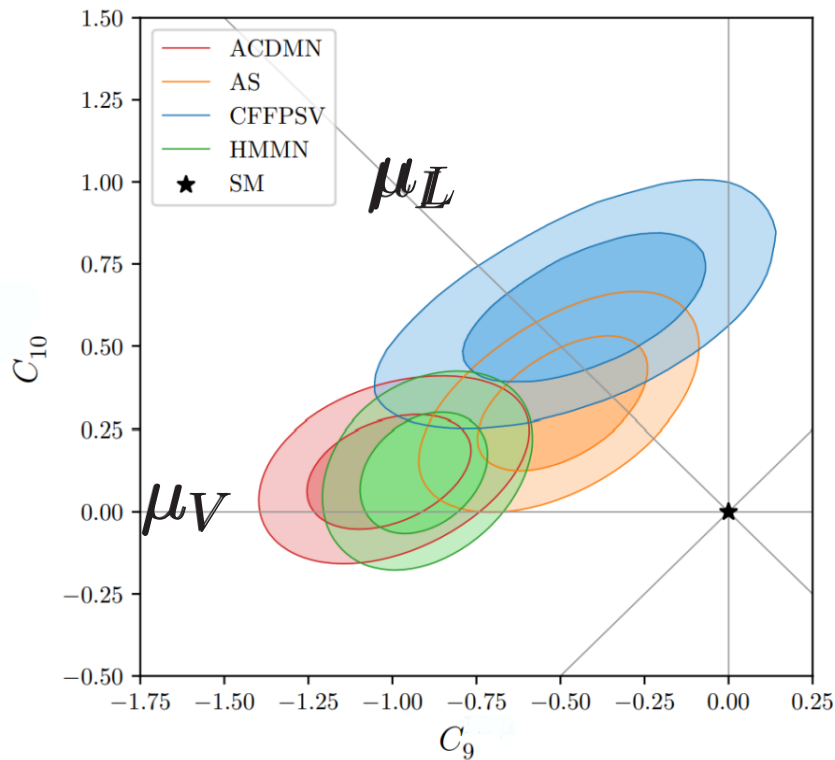


Neutral Current Fits

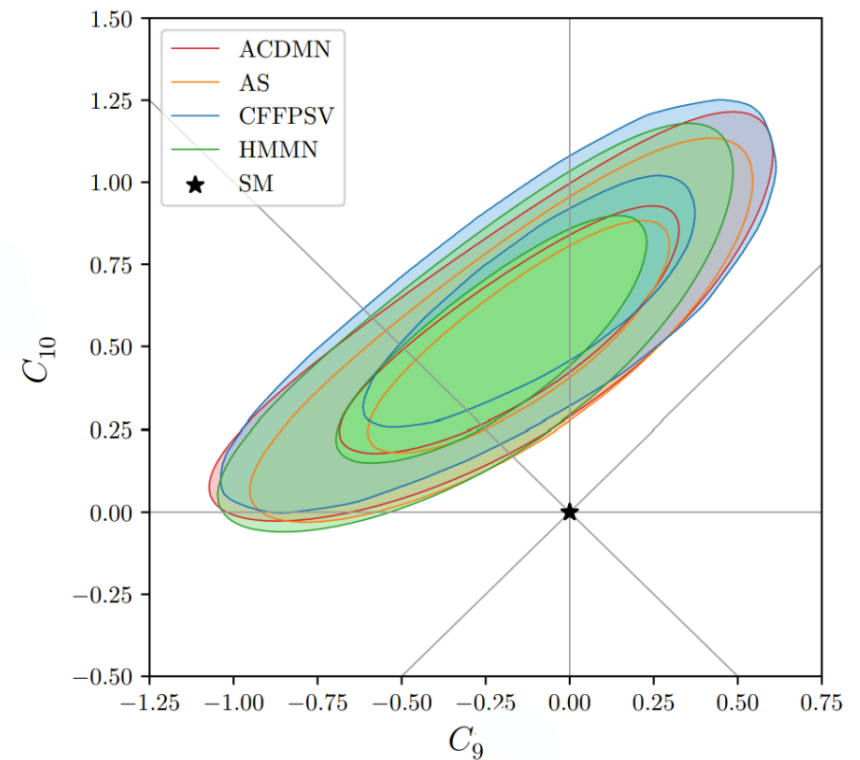
Alguero et al, 2104.08921; Altmannshofer, Stangl, flavio 2103.13370

Ciuchini et al, HEPfit 2011.01212; Hurth et al, superIso 2104.10058;

$$\mathcal{L} = N[C_9(\bar{b}_L\gamma^\mu s_L)(\bar{\mu}\gamma_\mu\mu) + C_{10}(\bar{b}_L\gamma^\mu s_L)(\bar{\mu}\gamma^5\gamma_\mu\mu)] + H.c.$$



global fit



fit to LFU observables + $B_s \rightarrow \mu\mu$

The Flavour Problem

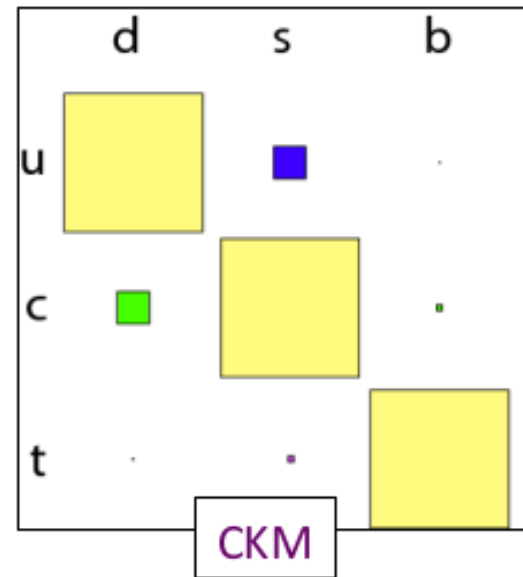
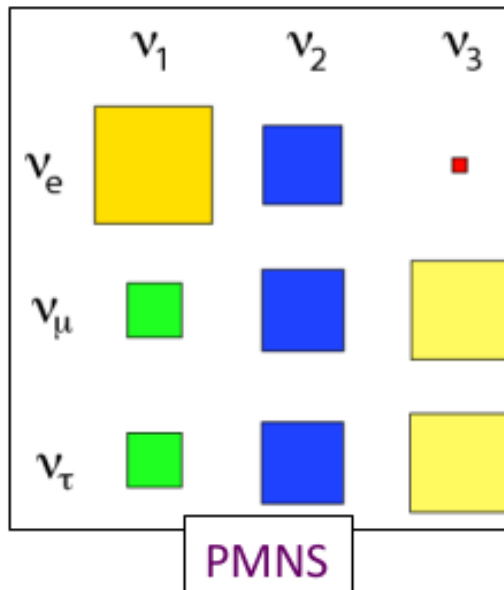
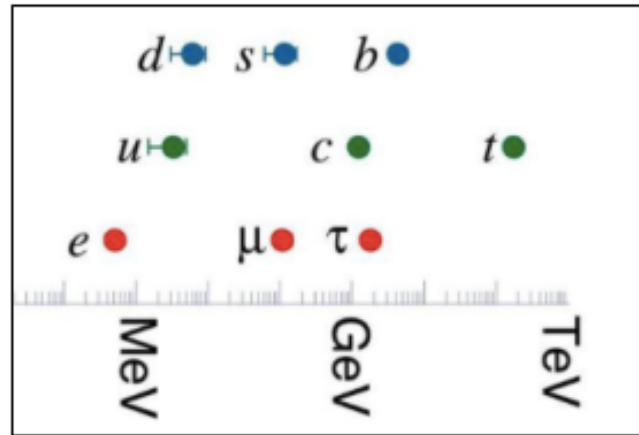
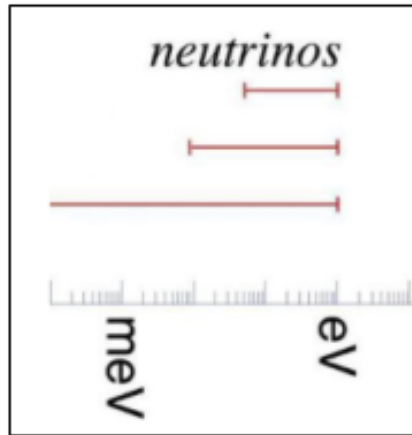


up

charm

top

The Flavour Problem



A Simple Z' Model

BCA, Davighi, 1809.01158: Add complex SM-singlet scalar 'flavon' $\theta_{X \neq 0}$ which breaks gauged $U(1)_X$:

$$\begin{array}{c} SU(3) \times SU(2)_L \times U(1)_Y \times U(1)_X \\ \downarrow \langle \theta \rangle \sim \text{Several TeV} \\ SU(3) \times SU(2)_L \times U(1)_Y \\ \downarrow \langle H \rangle \sim 246 \text{ GeV} \\ SU(3) \times U(1)_{em} \end{array}$$

- SM fermion content
- **Zero** X charges for first two generations
- Solve anomaly cancellation for $U(1)_X$

Unique Solution: $X = Y_3$

$X_{Q'_{1,2}} = 0$	$X_{u_{R'_{1,2}}} = 0$	$X_{d_{R'_{1,2}}} = 0$	$X_{L'_{1,2}} = 0$
$X_{e_{R'_{1,2}}} = 0$	$X_H = -1/2$	$X_{Q'_3} = 1/6$	$X_{u'_{R_3}} = 2/3$
$X_{d'_{R_3}} = -1/3$	$X_{L'_3} = -1/2$	$X_{e'_{R_3}} = -1$	$X_\theta \neq 0$

$$\mathcal{L} = Y_t \overline{Q'_{3L}} H t'_R + Y_b \overline{Q'_{3L}} H^c b'_R + Y_\tau \overline{L'_{3L}} H^c \tau'_R + H.c.,$$

$$\left(\begin{array}{c|c} & \\ \hline & \blacksquare \end{array} \right) \approx \left(\begin{array}{c|c} \cdot & \cdot \\ \cdot & \blacksquare \\ \hline & \blacksquare \end{array} \right)$$

A simple limiting case

$$V_{u_R} = V_{d_R} = V_{e_R}$$

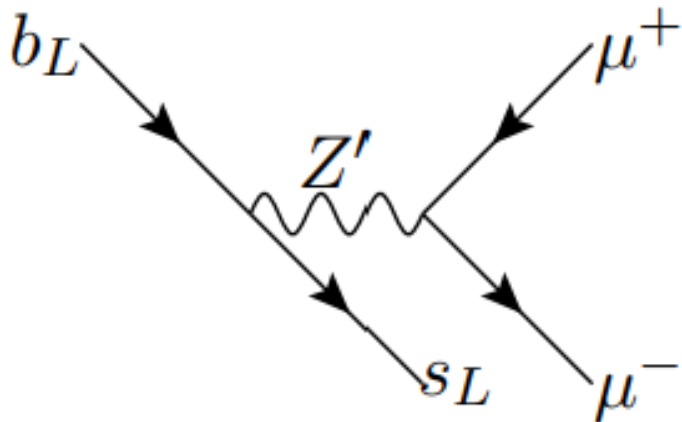
for simplicity and the ease of passing bounds.

$$V_{d_L} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & -\sin \theta_{23} \\ 0 & \sin \theta_{23} & \cos \theta_{23} \end{pmatrix}, \quad V_{e_L} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix},$$

$$\Rightarrow V_{u_L} = V_{d_L} V_{CKM}^\dagger \text{ and } V_{\nu_L} = V_{e_L} U_{PMNS}^\dagger.$$

Important Z' Couplings

$$g_X \left[\begin{array}{c} (\overline{d_L} \ \overline{s_L} \ \overline{b_L}) \begin{pmatrix} 0 & 0 & 0 \\ 0 & \sin^2 \theta_{23} & \frac{1}{2} \sin 2\theta_{23} \\ 0 & \frac{1}{2} \sin 2\theta_{23} & \cos^2 \theta_{23} \end{pmatrix} Z' \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix} \\ -3(\overline{e} \ \overline{\mu} \ \overline{\tau}) \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix} Z' \begin{pmatrix} e \\ \mu \\ \tau \end{pmatrix} \end{array} \right]$$



– LFU Violating, $C_9 \neq 0$

$Z - Z'$ mixing angle

$$\sin \alpha_z \approx \frac{g_X}{\sqrt{g^2 + g'^2}} \left(\frac{M_Z}{M'_Z} \right)^2 \ll 1.$$

This gives small non-flavour universal couplings to the Z boson proportional to g_X and:

$$Z_\mu = \cos \alpha_z \left(-\sin \theta_w B_\mu + \cos \theta_w W_\mu^3 \right) + \sin \alpha_z X_\mu,$$

smelli observables

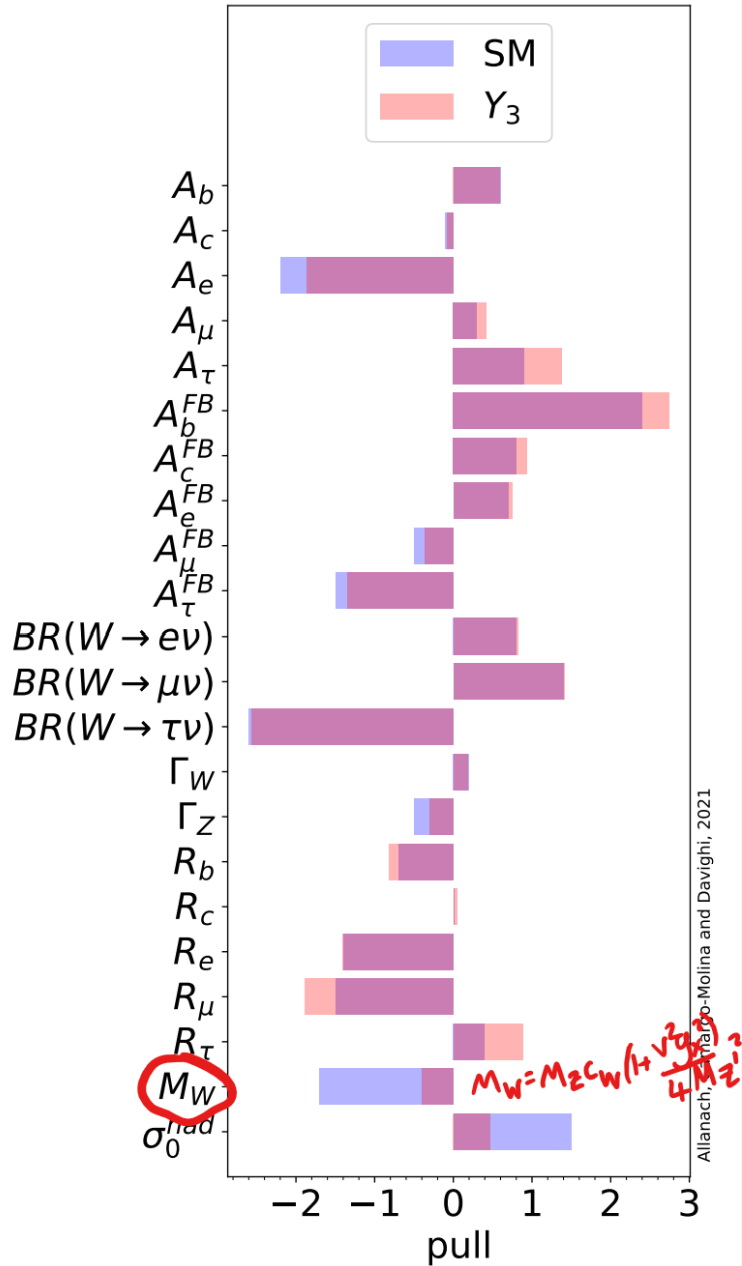
- 167 **quarks**: P'_5 , $BR(B_s \rightarrow \mu^+ \mu^-)$ and others with significant theory errors
- 21 **LFU FCNCs**: R_K, R_{K^*} , $B \rightarrow$ di-tau decays
- 31 EWPOs from LEP **not assuming lepton flavour universality**

Theory uncertainties modelled as multi-variate Gaussians: approximated to be independent of new physics.

SM:

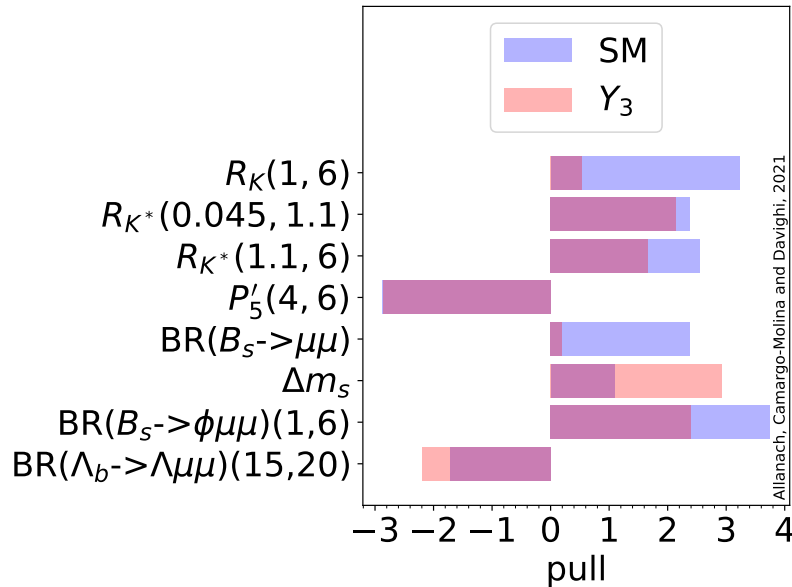
data set	χ^2	n	p -value
quarks	221.6	167	.003
LFU FCNCs	35.3	21	.026
EWPOs	35.7	31	.26
global	292.6	219	.00065

Global Fits $M_{Z'} = 3 \text{ TeV}$

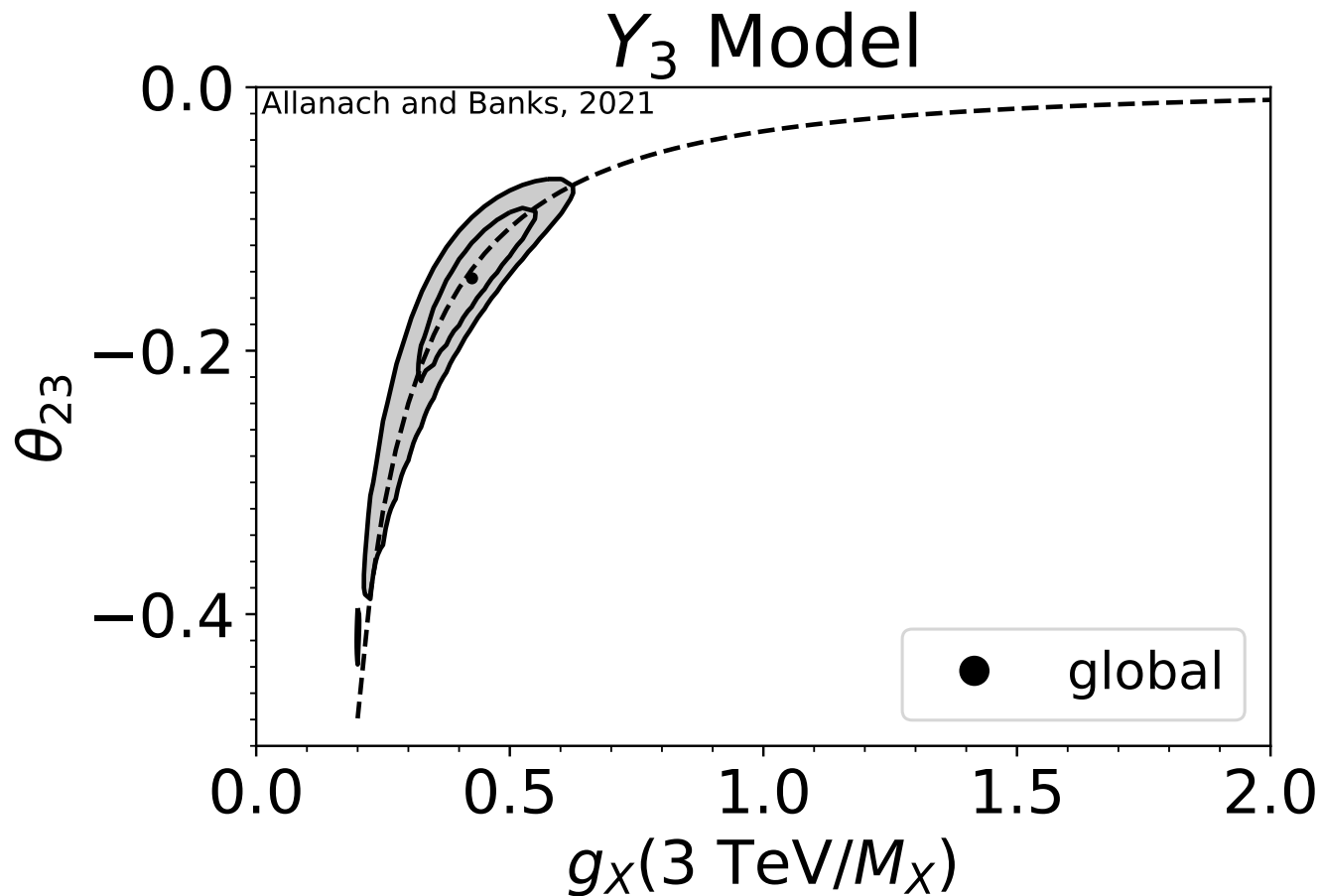


data set	χ^2	n	p -value
quarks	221.6	167	.003
LFU FCNCs	35.3	21	.026
EWPOs	35.7	31	.26
global	292.6	219	.00065

data set	χ^2	n	p -value
quarks	192.5	167	.071
LFU FCNCs	21.0	21	.34
EWPOs	36.0	31	.17
global	249.5	219	.064

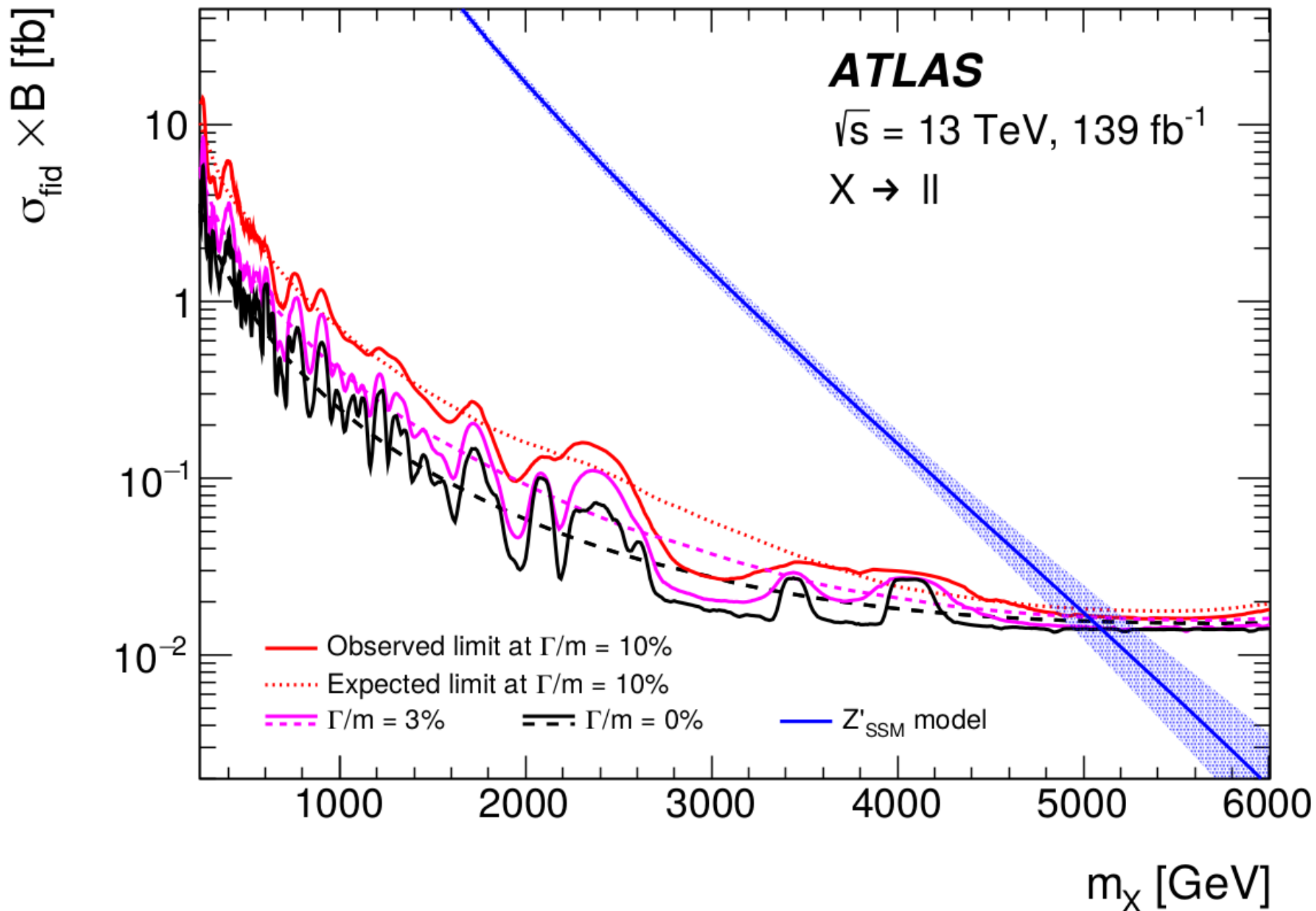


TFHM Fit, 95% CL



Relies on: smelli-2.2.0 (Aebischer, Kumar, Stangl, Straub, 1810.07698),
flavio-2.2.0 (Straub, 1810.08132), Wilson (Aebischer *et al*, 1712.05298)

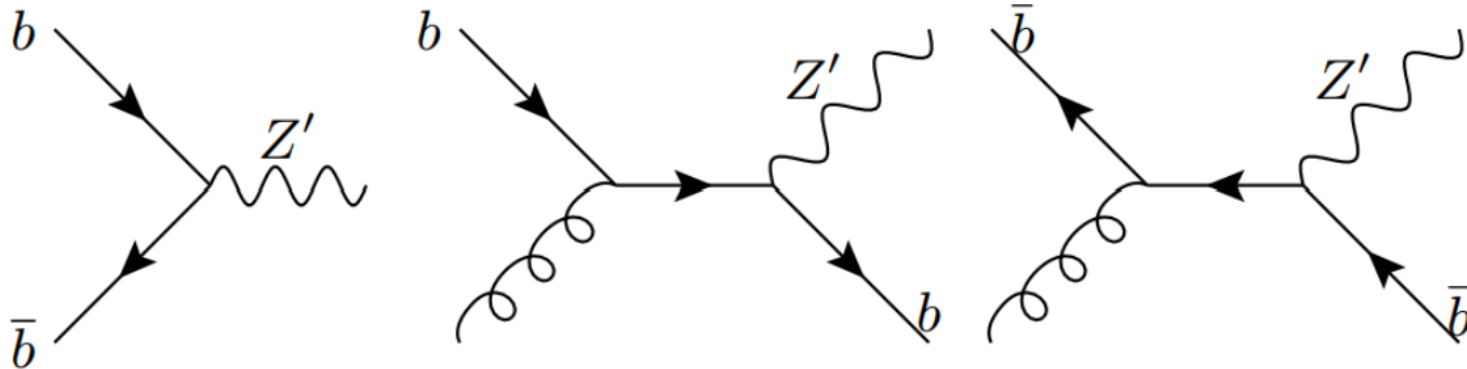
ATLAS l^+l^- limits



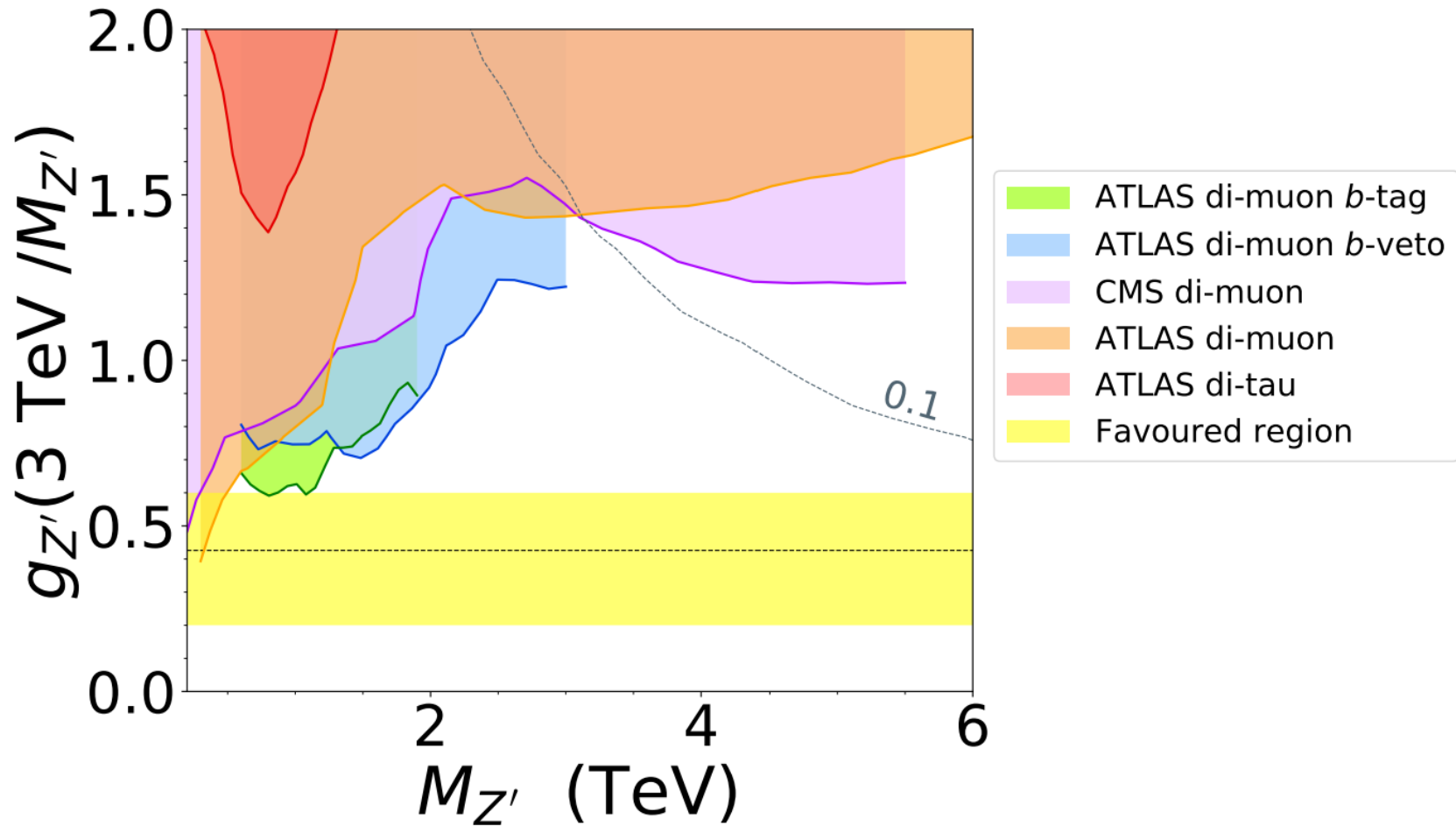
Z' Decay Modes

Mode	BR	Mode	BR	Mode	BR
$t\bar{t}$	0.42	$b\bar{b}$	0.12	$\nu\bar{\nu}'$	0.08
$\mu^+\mu^-$	0.08	$\tau^+\tau^-$	0.30	other $f_i f_j$	$\sim \mathcal{O}(10^{-4})$

LHC Z' Production:

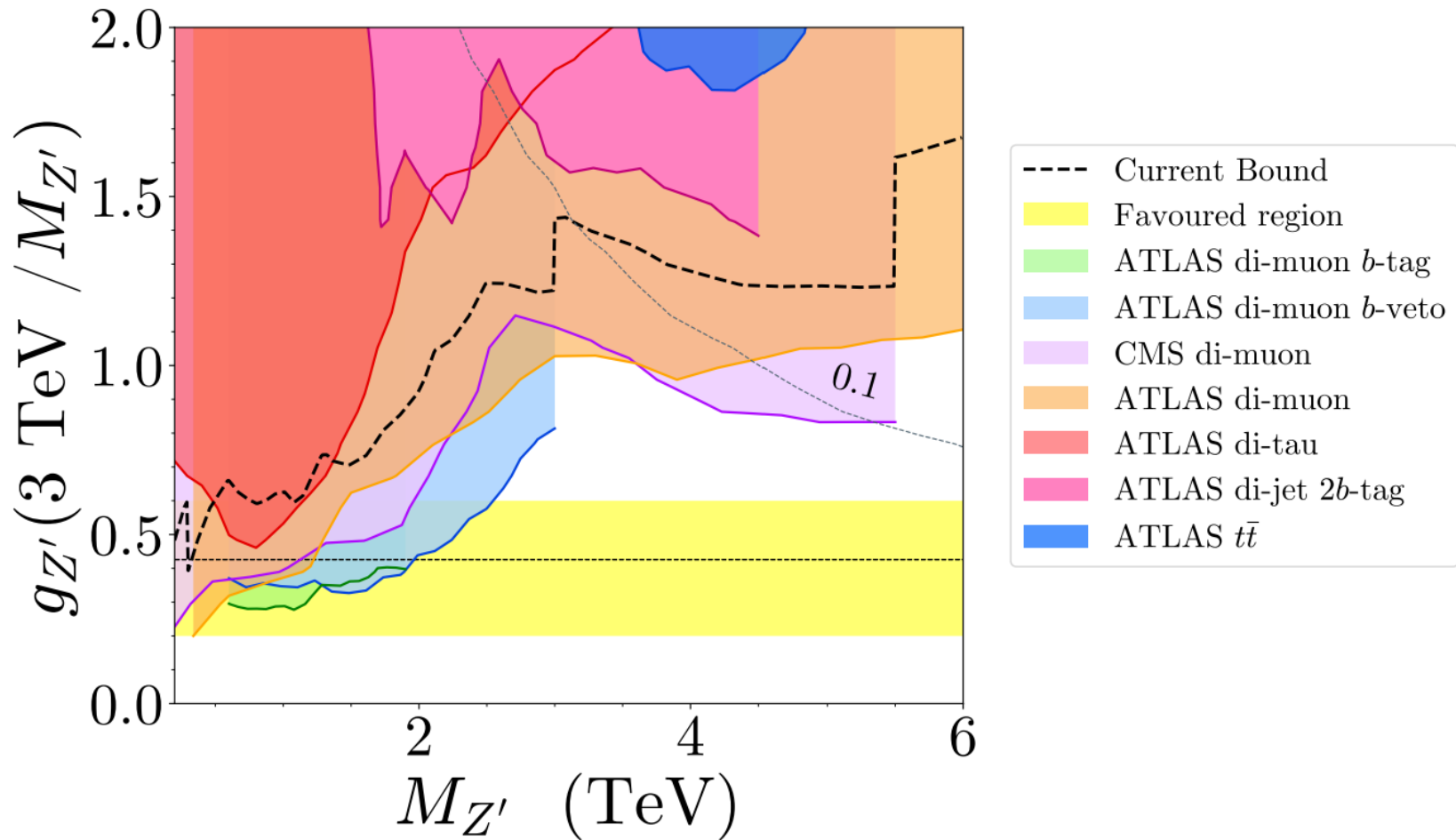


Z' Searches⁶



⁶BCA, Banks, 2111.06691

HL-LHC sensitivity⁷



⁷BCA, Banks, 2111.06691

Why $\bar{b}s\mu^+\mu^-$?

If we take these B -anomalies seriously, we may ask: why are we seeing the first BSM flavour changing effects particularly in the $b \rightarrow s\mu^+\mu^-$ transition, **not another one?**

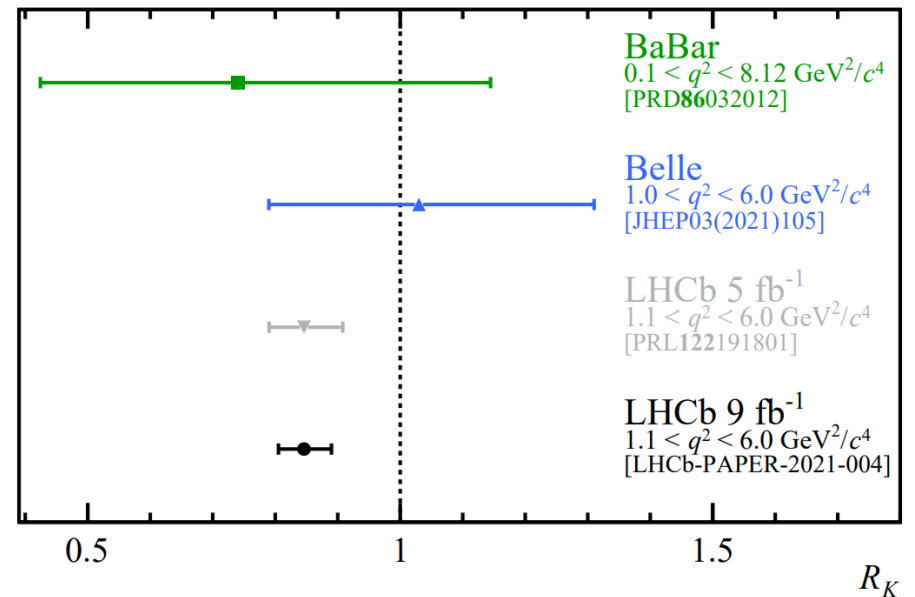
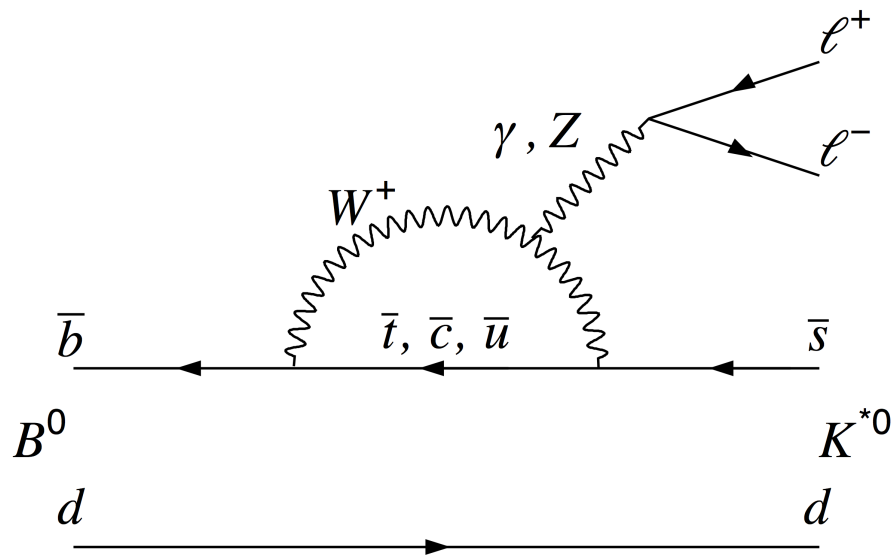
Perhaps it's because, in hindsight:

- The largest BSM flavour effects are in heavier generations
- We have many more bs than ts , particularly in LHCb
- Leptons in final states are good experimentally but not (yet) τ s: they are too difficult!

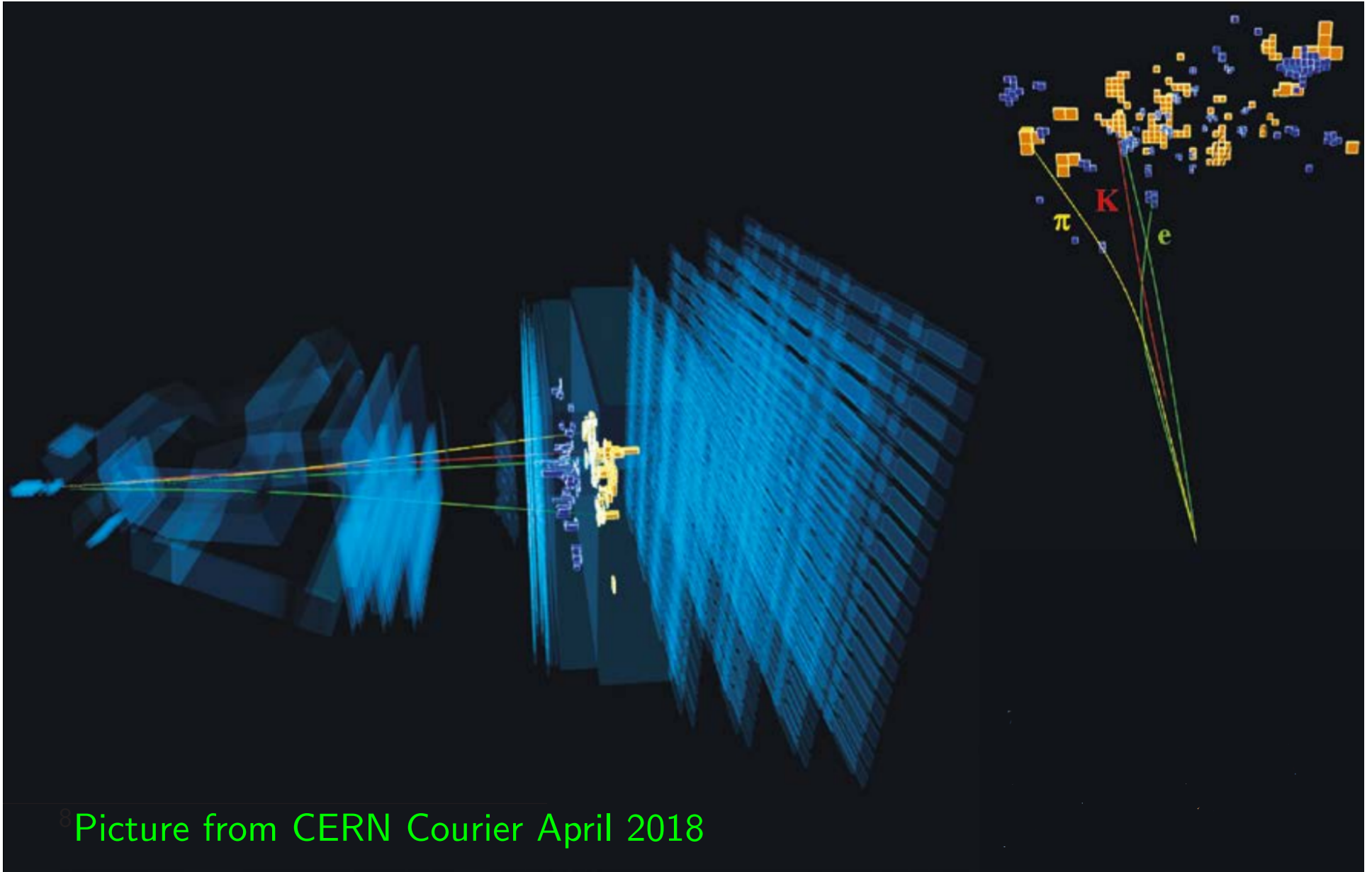
$R_K^{(*)}$ in Standard Model

$$R_K = \frac{BR(B \rightarrow K \mu^+ \mu^-)}{BR(B \rightarrow K e^+ e^-)}, \quad R_{K^*} = \frac{BR(B \rightarrow K^* \mu^+ \mu^-)}{BR(B \rightarrow K^* e^+ e^-)}.$$

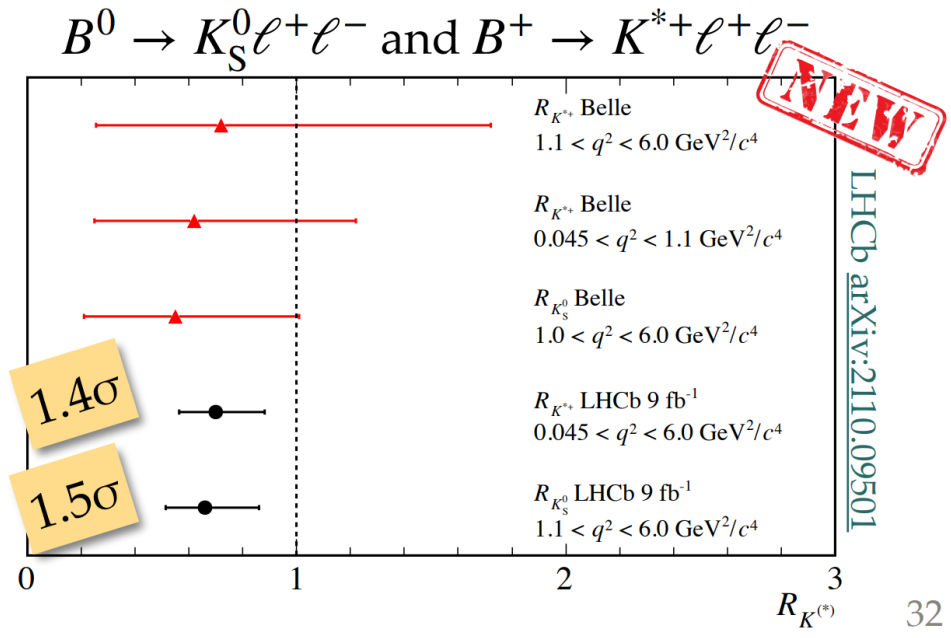
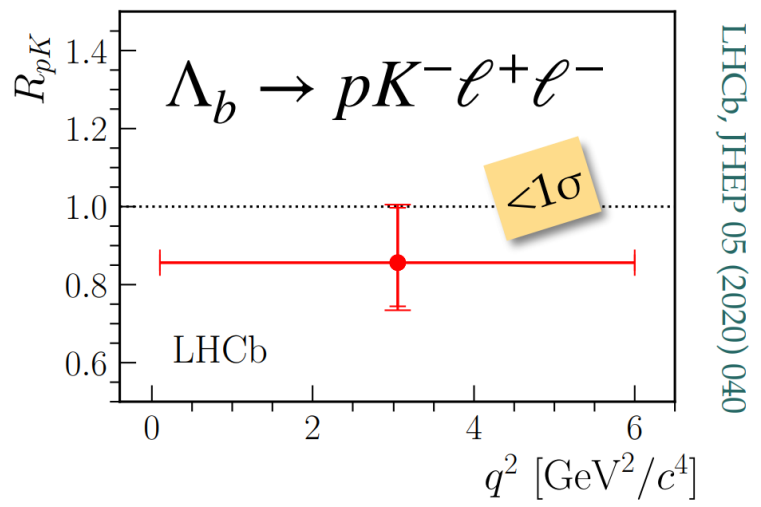
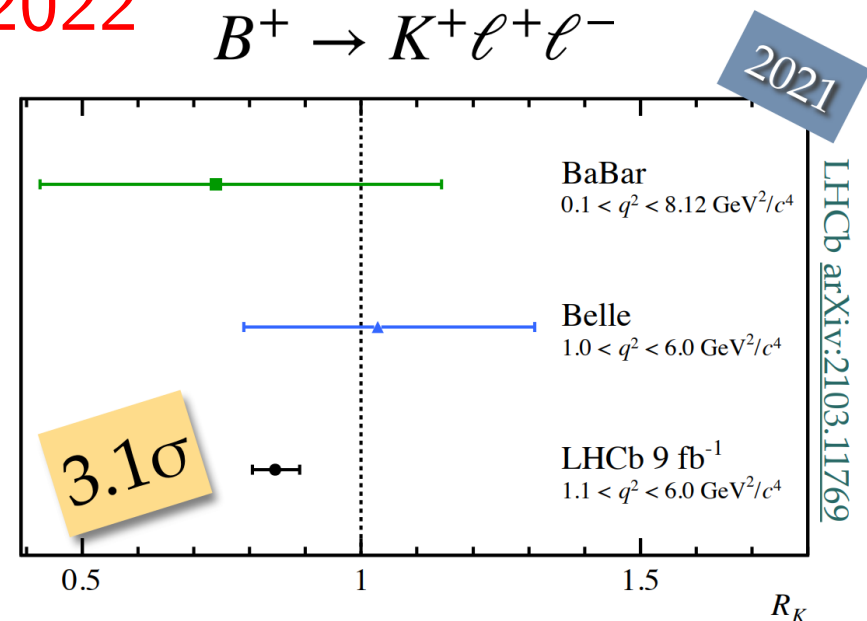
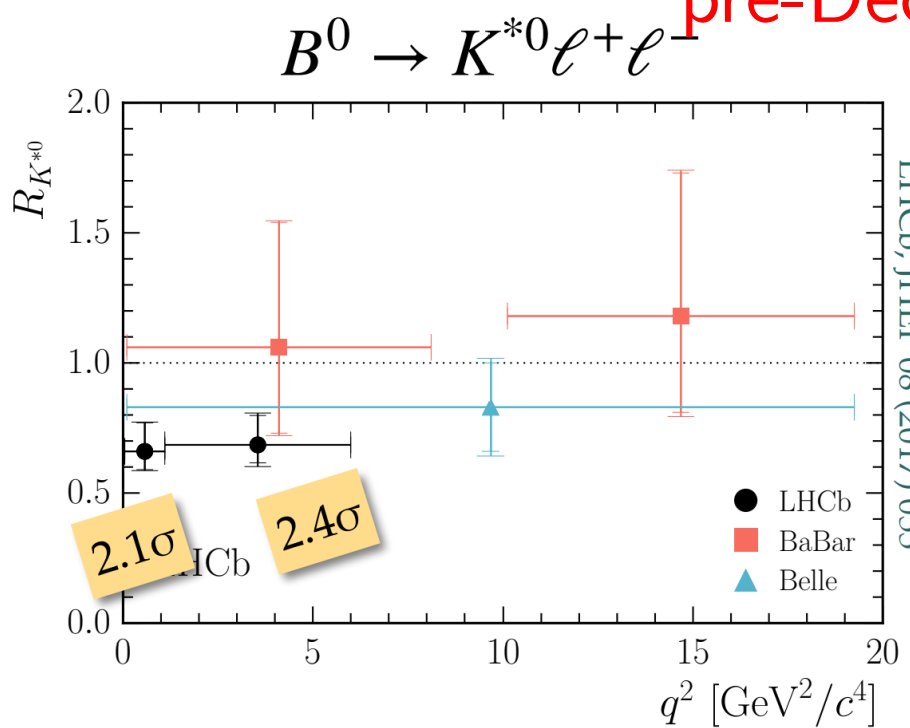
These are **rare decays** (each $BR \sim \mathcal{O}(10^{-7})$) because they are absent at tree level in SM+EW+CKM



LHCb $B^0 \rightarrow K^{0*} e^+ e^-$ Event⁸

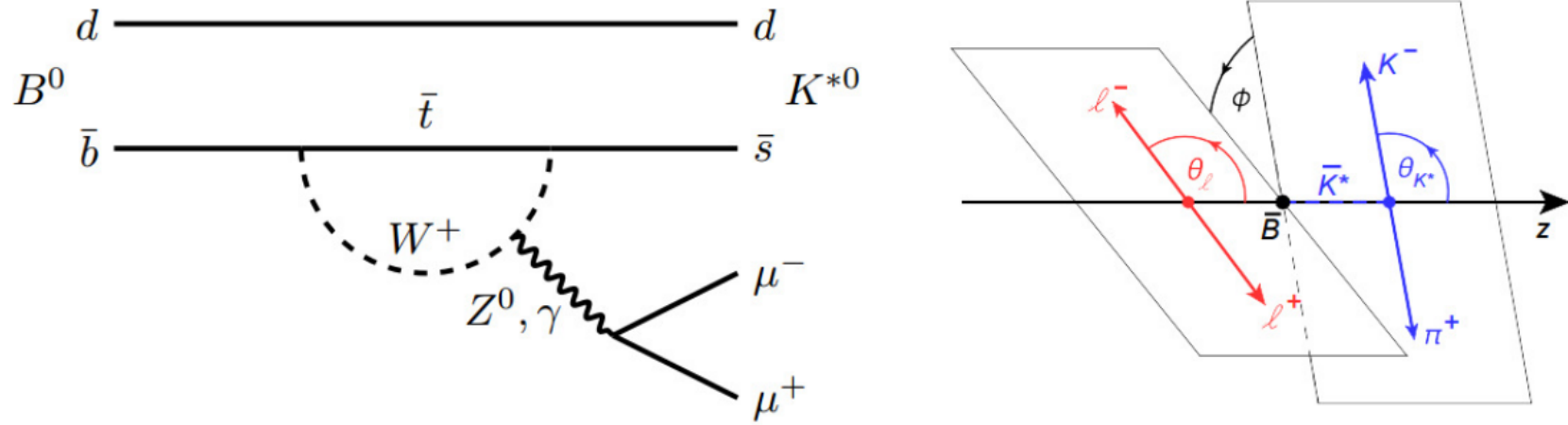


pre-Dec 2022



Stolen from Capdevila et al, *Flavour Anomaly Workshop '21*

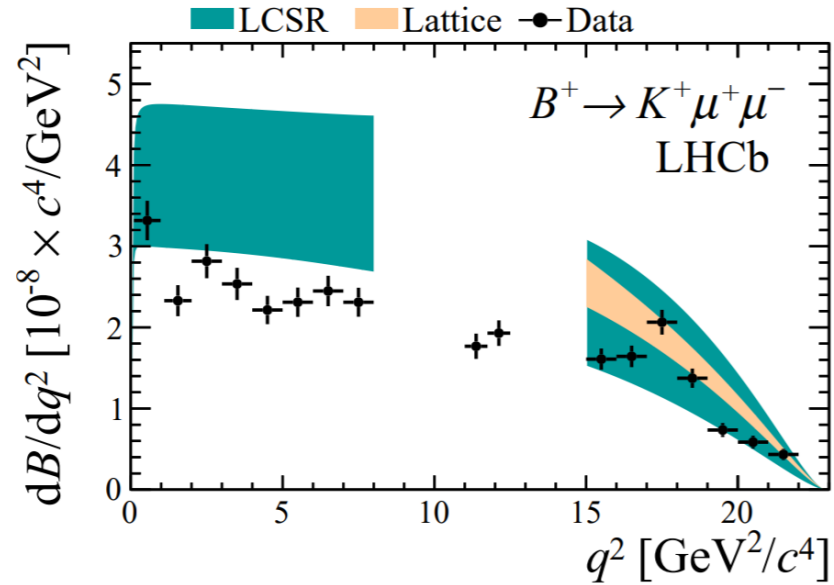
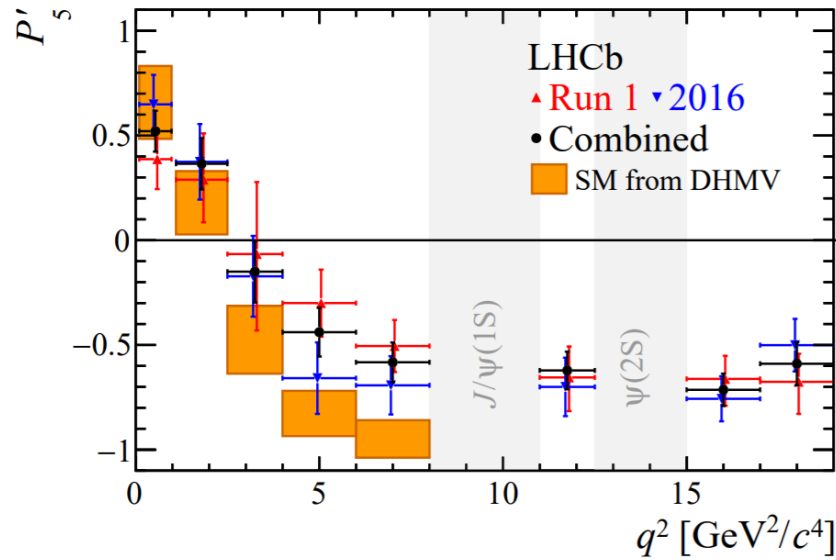
$$B^0 \rightarrow K^{*0} (\rightarrow K^+ \pi^-) \mu^+ \mu^-$$



Decay fully described by three helicity angles $\vec{\Omega} = (\theta_\ell, \theta_K, \phi)$ and $q^2 = m_{\mu\mu}^2$

$$\begin{aligned} \frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} &= \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ &\quad - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi \\ &\quad + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi \\ &\quad + \frac{4}{3} A_{\text{FB}} \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \\ &\quad \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right] \end{aligned}$$

P'_5

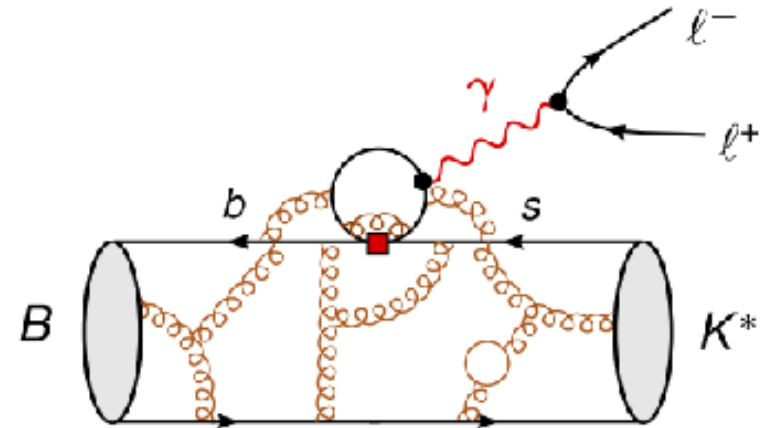


$P'_5 = S_5 / \sqrt{F_L(1 - F_L)}$, leading form factor uncertainties cancel⁹

⁹LHCb, 2003.04831

Hadronic Uncertainties

- ▶ Hadronic effects like charm loop are photon-mediated \Rightarrow vector-like coupling to leptons just like C_9



- ▶ How to disentangle NP \leftrightarrow QCD?
 - ▶ Hadronic effect can have different q^2 dependence
 - ▶ Hadronic effect is lepton flavour universal ($\rightarrow R_K!$)

Wilson Coefficients c_{ij}^l

In SM, can form an **EFT** since $m_B \ll M_W$:

$$\mathcal{L}_{\text{eff}} = \frac{1}{(36 \text{ TeV})^2} c_{ij}^l (\bar{s} \gamma^\mu P_i b) (\bar{l} \gamma_\mu P_j l) \quad (1)$$

One loop weak interactions give $c_{ij}^l \sim \pm \mathcal{O}(1)$ in SM.

$$(1/36 \text{ TeV})^2 = V_{tb} V_{ts}^* \alpha / (4\pi v^2).$$

From now on, c_{ij}^l refer to *beyond* SM contribution.

Which Ones Work?

Options for a single *BSM* operator:

- c_{ij}^e operators fine for $R_{K^{(*)}}$ but are disfavoured by global fits including other observables.
- c_{LR}^μ disfavoured: predicts *enhancement* in both R_K and R_{K^*}
- c_{RR}^μ, c_{RL}^μ disfavoured: they pull R_K and R_{K^*} in *opposite directions*.
- $c_{LL}^\mu = -1.06$ fits well globally¹⁰.

¹⁰D'Amico et al, 1704.05438; Aebischer et al 1903.10434.

Statistics¹¹

	\bar{c}_{LL}^μ	$\sqrt{\chi_{SM}^2 - \chi_{best}^2}$
clean	-1.33 ± 0.34	4.1
dirty	-1.33 ± 0.32	4.6
all	-1.06 ± 0.16	6.5
	$C_9^\mu = (\bar{c}_{LL}^\mu + \bar{c}_{LR}^\mu)/2$	$\sqrt{\chi_{SM}^2 - \chi_{best}^2}$
clean	-1.51 ± 0.46	3.9
dirty	-1.15 ± 0.17	5.5
all	-0.95 ± 0.15	5.8

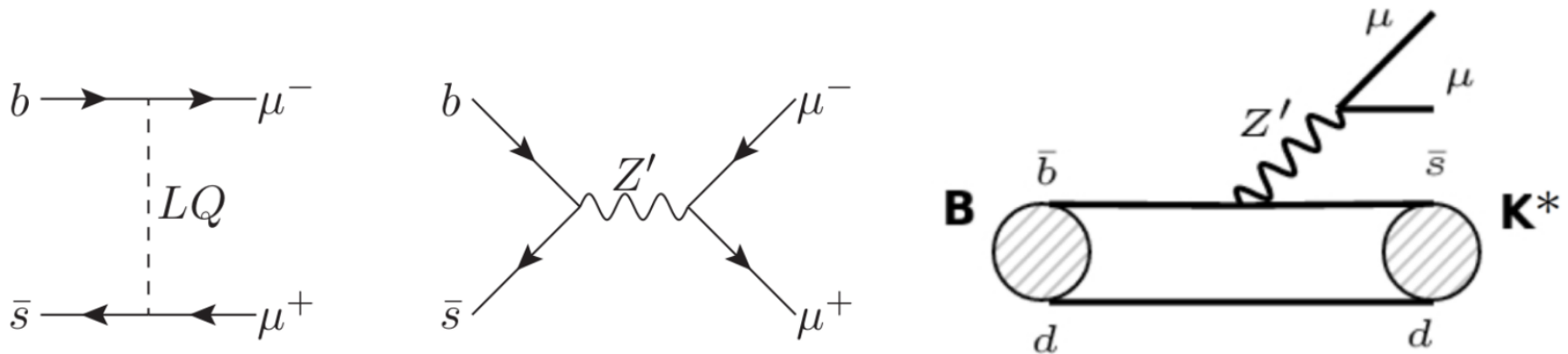
¹¹'clean' ($R_K, R_{K^*}, B_s \rightarrow \mu\mu$) and 'dirty' ($P_5', B \rightarrow \phi\mu\mu$ +100 others).
D'Amico, Nardecchia, Panci, Sannino, Strumia, Torre, Urbano 1704.05438;
Aebischer, Altmanshoffer, Guadagnoli, Reboud, Stangl, Straub, 1903.10434. SM

p -value around 3σ for NCBA's.

$b \rightarrow s\mu\mu$ Simplified Models

A good few $2 - 4\sigma$ Discrepancies with SM predictions. Computing with look elsewhere effect implies a 4.3σ discrepancy with the SM (conservative theory errors).¹²

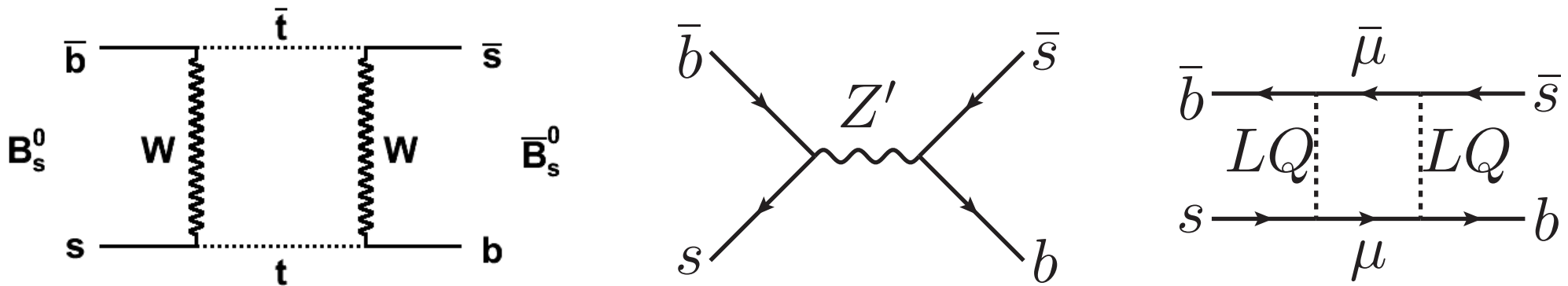
We have tree-level **flavour changing** new physics options:



¹²Isidori, Lancierini, Owen and Serra, arXiv:2104.05631

$B_s - \bar{B}_s$ Mixing

Measurement pretty much agrees with SM calculations.



$$g_{sb} \lesssim \frac{M_{Z'}}{194 \text{ TeV}} \text{ but uncertain}$$

from QCD sum rules and lattice¹³. Weaker on LQs.

$$M_{Z'} \approx 31 \text{ TeV} \times \sqrt{g_{sb}g_{\mu\mu}}, \quad M_{LQ} \approx 31 \text{ TeV} \times \sqrt{g_{s\mu}g_{b\mu}}$$

¹³King, Lenz, Rauh, arXiv:1904.00940

$Z' \rightarrow \mu\mu$ ATLAS 13 TeV 139 fb^{-1}

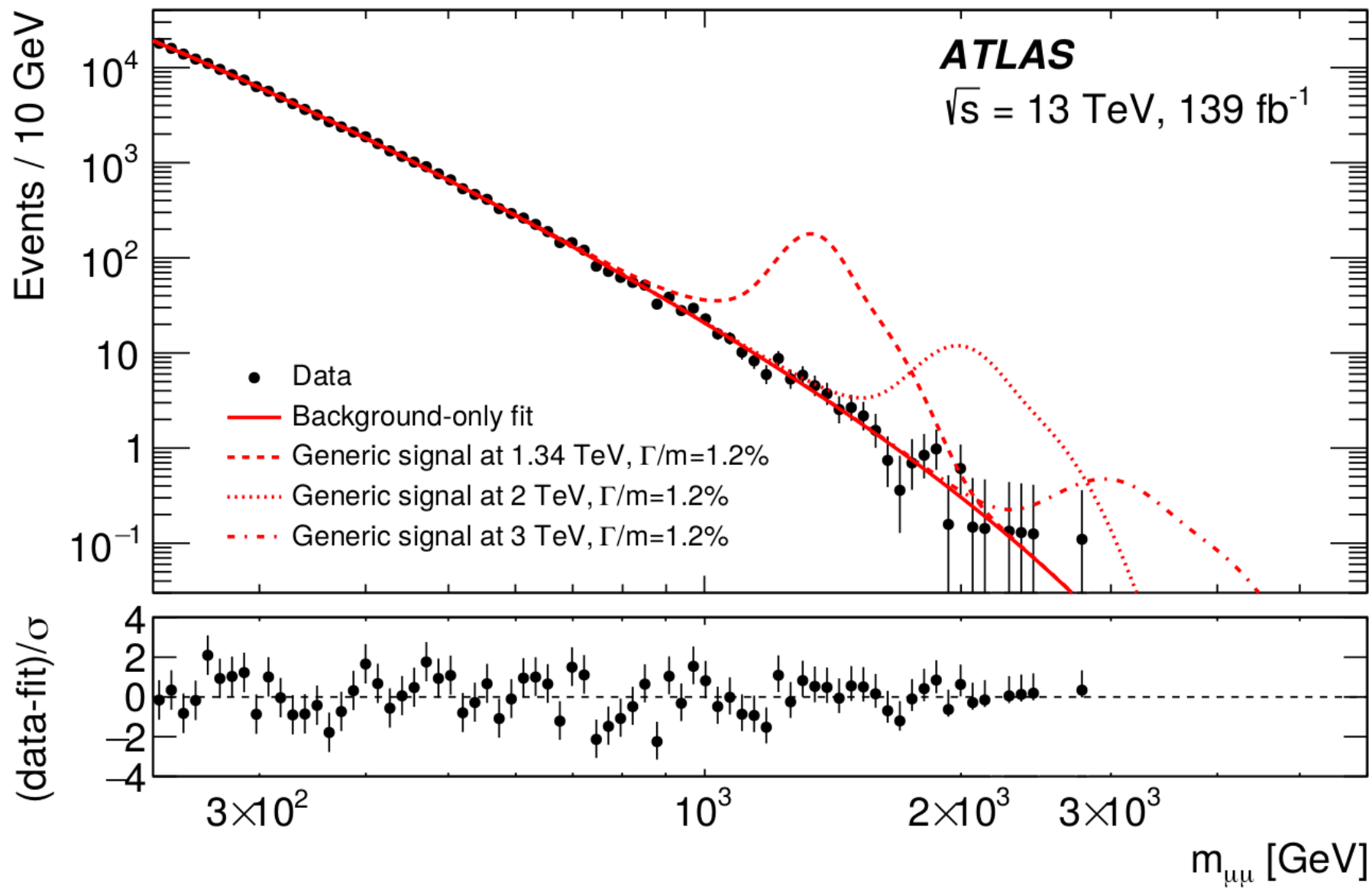
ATLAS analysis: look for two track-based isolated μ ,
 $p_T > 30$ GeV. One reconstructed primary vertex. Keep
only highest scalar sum p_T pair¹⁴

$$m_{\mu_1\mu_2}^2 = (p_1^\mu + p_2^\mu) (p_{1\mu} + p_{2\mu})$$

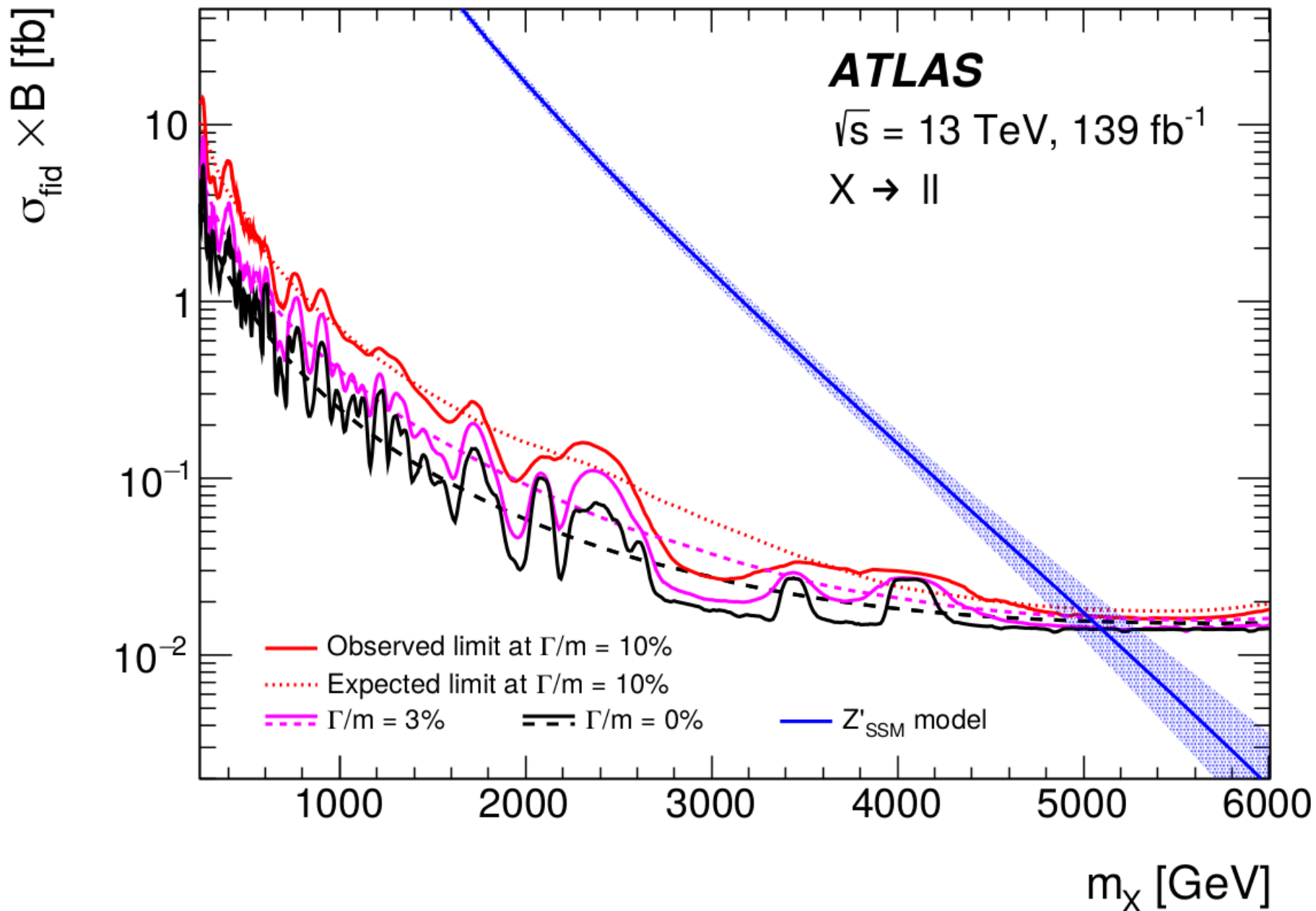
CMS also have released¹⁵ a 139 fb^{-1} analysis.

¹⁴1903.06248

¹⁵2103.02708



ATLAS l^+l^- limits



A Model

BCA, Davighi, [arXiv:1809.01158](https://arxiv.org/abs/1809.01158): Add complex SM singlet scalar θ and gauged $U(1)_F$:

$$\begin{array}{c} SU(3) \times SU(2)_L \times U(1)_Y \times U(1)_F \\ \downarrow \langle \theta \rangle \sim \text{Several TeV} \\ SU(3) \times SU(2)_L \times U(1)_Y \\ \downarrow \langle H \rangle \sim 246 \text{ GeV} \\ SU(3) \times U(1)_{em} \end{array}$$

- SM fermion content
- anomaly cancellation
- 0 F charges for first two generations

The Flavour Problem



up

charm

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A Warm Up: $U(1)$

Pioneering solution to ACCs: [Costa, Dobrescu, Fox, arxiv:1905.13729](#). n chiral fermions with charges z_i :

$$\begin{aligned} z_1^3 + \dots + z_n^3 &= 0, \\ z_1 + \dots + z_n &= 0. \end{aligned} \tag{2}$$

Given 2 solutions \underline{x} , \underline{y} , construct a third by “merger”

$$\{\underline{x}\} \oplus \{\underline{y}\} := \left(\sum_{i=1}^n x_i y_i^2 \right) \{\underline{x}\} - \left(\sum_{i=1}^n x_i^2 y_i \right) \{\underline{y}\}.$$

Want to find suitably general solutions \underline{x} , \underline{y} .

Example: even n

$$\{\underline{x}\} = \{l_1, k_1, \dots, k_m, -l_1, -k_1, \dots, -k_m\}$$

$$\{\underline{y}\} = \{0, 0, l_1, \dots, l_m, -l_1, \dots, -l_m\},$$

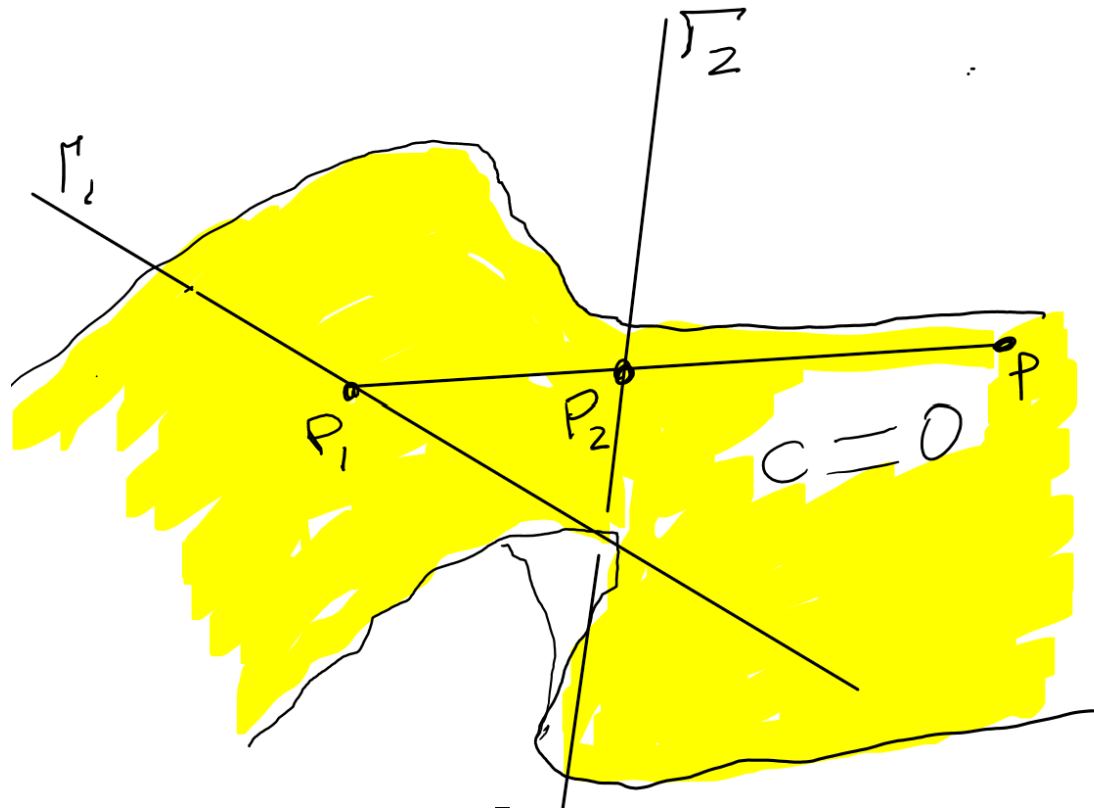
$$m = n/2 - 1 \geq 2, \quad 1 \leq i \leq m$$

$\{\underline{x}\}$ and $\{\underline{y}\}$ are each vector-like solutions but it turns out that $\{\underline{x}\} \oplus \{\underline{y}\}$ is a new **chiral** solution.

$\{\underline{x}\} \oplus \{\underline{y}\}$ parameterises all solutions up to permutations. There is a *similar story* for odd n .

Mordell's Theorem¹⁶

Skew Γ_1, Γ_2 in $c = 0 \Rightarrow$ all rational points on c can be found this way.



¹⁶Mordell (1969) *Diophantine Equations*

Geometric Understanding

In [BCA, Gripaio, Tooby-Smith, arXiv:1912.04804](#), we provide a geometric understanding of this. First, note that each solution in \mathbb{Q} is equivalent to one in \mathbb{Z} by clearing denominators. Using gravitational anomaly cancellation, eliminate z_n to obtain the homogeneous cubic

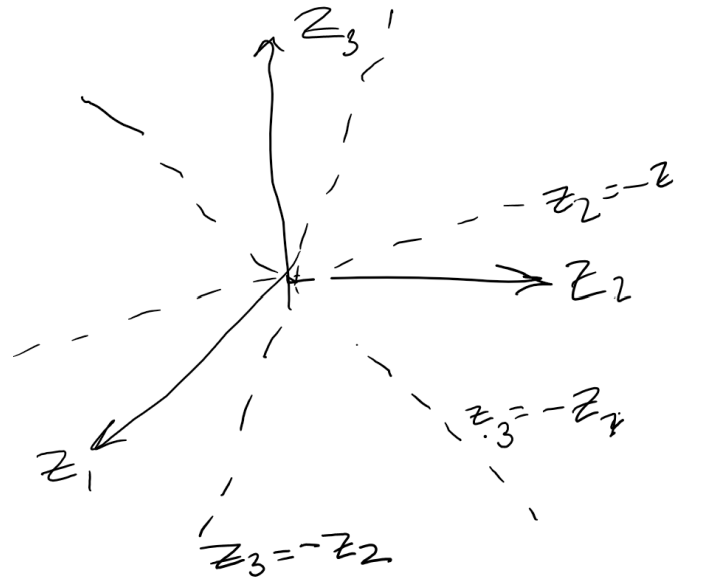
$$\sum_{i=1}^{n-1} z_i^3 - \left(\sum_{i=1}^{n-1} z_i \right)^3 = 0$$

defining a cubic hypersurface in \mathbb{Q}^{n-1} .

Special Surface

In fact, our cubic hypersurface is rather special: no purely cubic terms in any one variable: (add perms)

$n = 3$: $\underline{z} = [-a : 0 : a]$, ie three lines $z_3 = -z_1$, $z_2 = 0$



$n = 4$: $\underline{z} = [-x : -y : x : y]$, $x, y \in \mathbb{Q}$ ie three planes

Strategy

1. Find solutions for SM fermions charges from first 4

2. Apply $GL(3, \mathbb{Z})$ transformation to species F :

$$F_+ := F_1 + F_2 + F_3, F_\alpha := F_1 - F_2, F_\beta := F_2 + F_3.$$

3. Linear equations become

$$D_+ = -2Q_+ - U_+, L_+ = -3Q_+, E_+ = 2Q_+ - U_+.$$

4. Quadratic is a solveable homogeneous diophantine equation of degree 2 in the 12-tuple

$$X := (Q_+, U_+, Q_\alpha, Q_\beta, U_\alpha, U_\beta, D_\alpha, D_\beta, L_\alpha, L_\beta, E_\alpha, E_\beta).$$

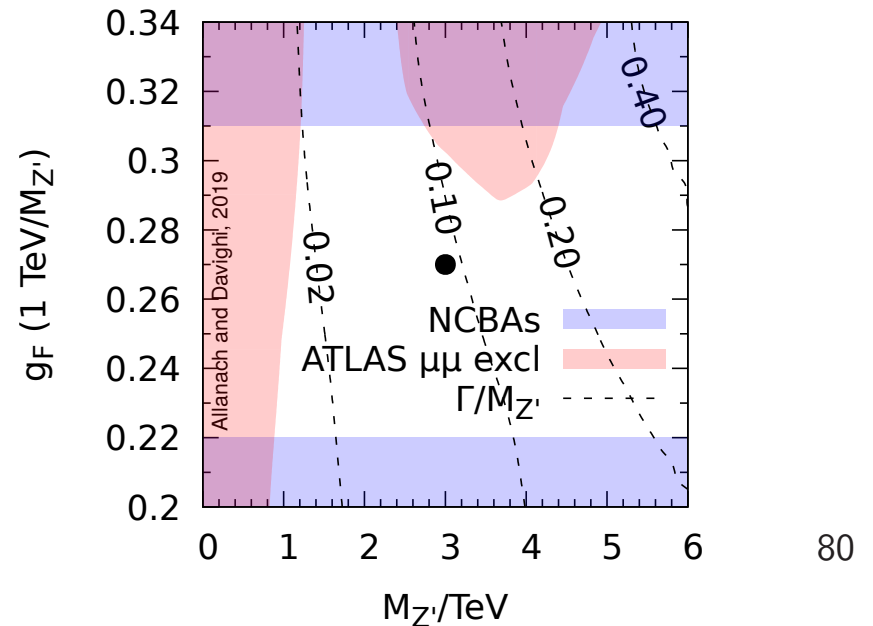
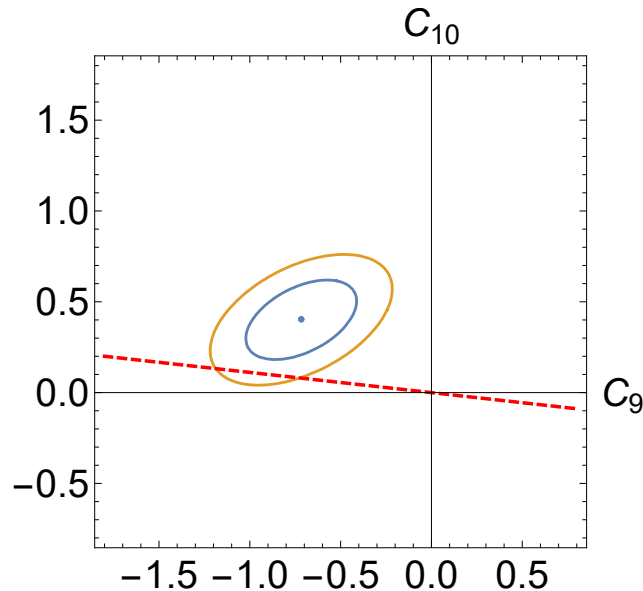
$X^T H X = 0$ defines hypersurface $\Gamma \in P\mathbb{Q}^{11}$.

$$H = \begin{pmatrix} 0 & 0 & -2 & -4 & 0 & 0 & 4 & 8 & -6 & 0 & -4 & -8 \\ & 0 & 0 & 0 & 4 & 8 & 2 & 4 & 0 & 0 & 2 & 4 \\ & & 2 & 3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ & & & 6 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ & & & & -4 & 6 & 0 & 0 & 0 & 0 & 0 & 0 \\ & & & & & -12 & 0 & 0 & 0 & 0 & 0 & 0 \\ & & & & & & 2 & 3 & 0 & 0 & 0 & 0 \\ & & & & & & & 6 & 0 & 0 & 0 & 0 \\ & & & & & & & & -2 & 3 & 0 & 0 \\ & & & & & & & & & 6 & 0 & 0 \\ & & & & & & & & & & 2 & 3 \\ & & & & & & & & & & & 6 \end{pmatrix}.$$

Deformed TFHM

$$\begin{array}{cccc}
 F_{Q'_i} = 0 & F_{u_{R'_i}} = 0 & F_{d_{R'_i}} = 0 & F_H = -1/2 \\
 F_{e_{R'_1}} = 0 & F_{e_{R'_2}} = 2/3 & F_{e_{R'_3}} = -5/3 & \\
 F_{L'_1} = 0 & F_{L'_2} = 5/6 & F_{L'_3} = -4/3 & \\
 F_{Q'_3} = 1/6 & F_{u'_{R3}} = 2/3 & F_{d'_{R3}} = -1/3 & F_\theta \neq 0
 \end{array}$$

$$\mathcal{L} = Y_t \overline{Q'_{3L}} H t'_R + Y_b \overline{Q'_{3L}} H^c b'_R + H.c.,$$



Invisible Width of Z Boson

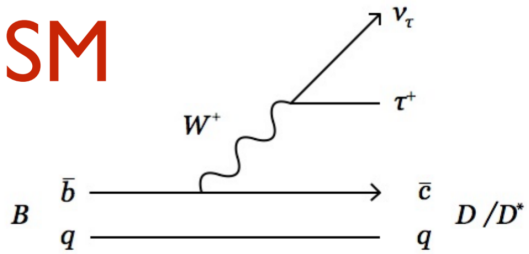
$$\Gamma_{\text{inv}}^{(\text{exp})} = 499.0 \pm 1.5 \text{ MeV}, \text{ whereas } \Gamma_{\text{inv}}^{(\text{SM})} = 501.44 \text{ MeV}.$$

$$\Rightarrow \Delta\Gamma^{(\text{exp})} = \Gamma_{\text{inv}}^{(\text{exp})} - \Gamma_{\text{inv}}^{(\text{SM})} = -2.5 \pm 1.5 \text{ MeV}.$$

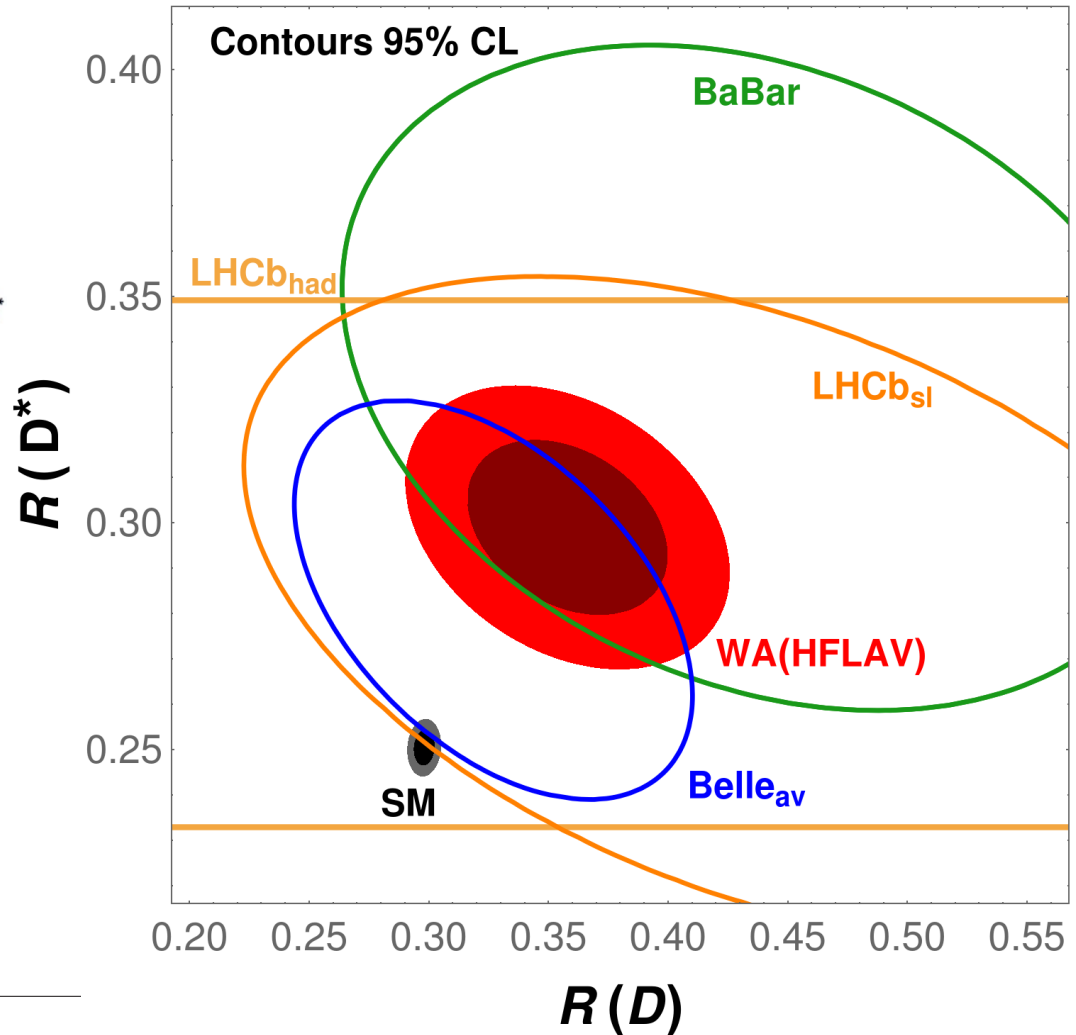
$$\begin{aligned} \mathcal{L}_{\bar{\nu}\nu Z} = & -\frac{g}{2 \cos \theta_w} \bar{\nu}'_{Le} \not{Z} P_L \nu'_{Le} \\ & -\bar{\nu}'_{L\mu} \left(\frac{g}{2 \cos \theta_w} + \frac{5}{6} g_F \sin \alpha_z \right) \not{Z} \nu'_{L\mu} \\ & -\bar{\nu}'_{L\tau} \left(\frac{g}{2 \cos \theta_w} - \frac{8}{6} g_F \sin \alpha_z \right) \not{Z} \nu'_{L\tau}. \end{aligned}$$

$$R_{D^{(*)}} = BR(B^- \rightarrow D^{(*)}\tau\nu) / BR(B^- \rightarrow D^{(*)}\mu\nu)^{17}$$

SM

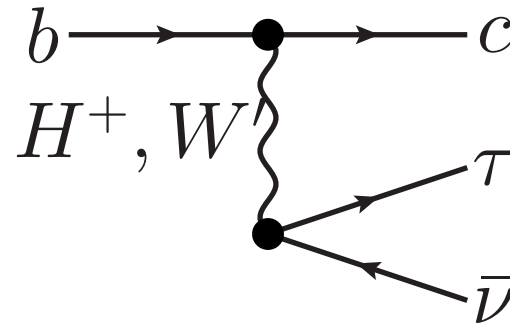
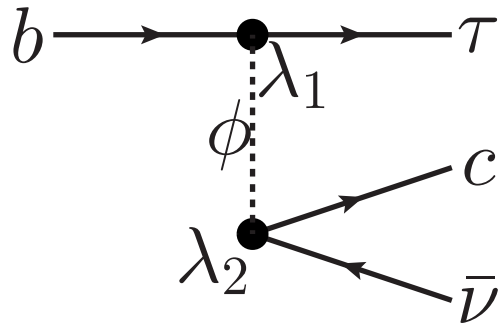


SM: 3.1σ



¹⁷Kind courtesy of M Jung

$R_{D^{(*)}}$: BSM Explanations



Make an effective theory with heavy BSM particle:

$$\mathcal{L}_{WET} = -\frac{2\lambda_1\lambda_2}{M^2} (\bar{c}\gamma^\mu P_L \nu) (\bar{\tau}\gamma_\mu P_L b) + H.c.$$

Fit to data tells us

$$M = 3.4 \text{ TeV} \times \sqrt{\lambda_1\lambda_2}$$

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Going nowhere fast

After the success of the Standard Model, experiments have stopped answering to grand theories. Is particle physics in crisis?

Photo by Getty

Ben Allanach is a professor in the department of applied mathematics and theoretical physics at the University of Cambridge. Along with other members of the Cambridge Supersymmetry Working Group, his research focuses on collider searches for new physics.

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2,900 words

SYNDICATE THIS ESSAY

In recent years, physicists have been watching the data coming in from the Large Hadron Collider (LHC) with a growing sense of unease. We've spent decades devising elaborate accounts for the behaviour of the quantum zoo of subatomic particles, the most basic components of the known universe. The Standard Model is

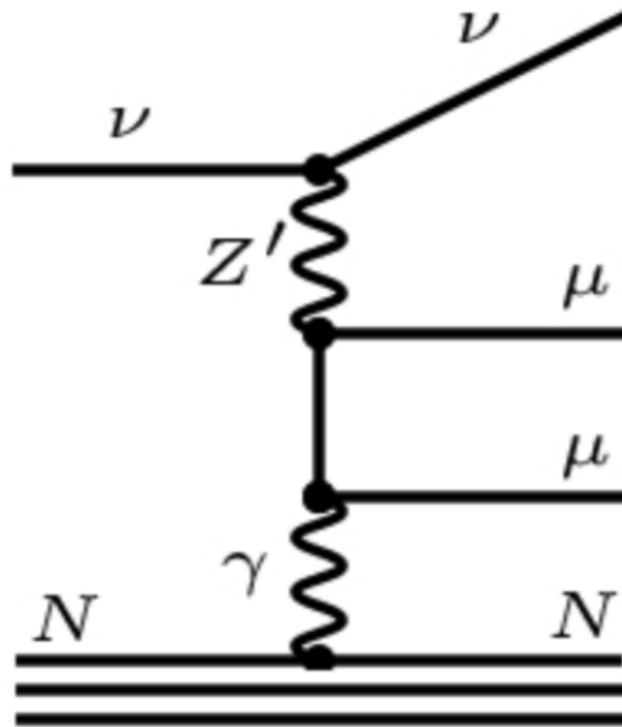
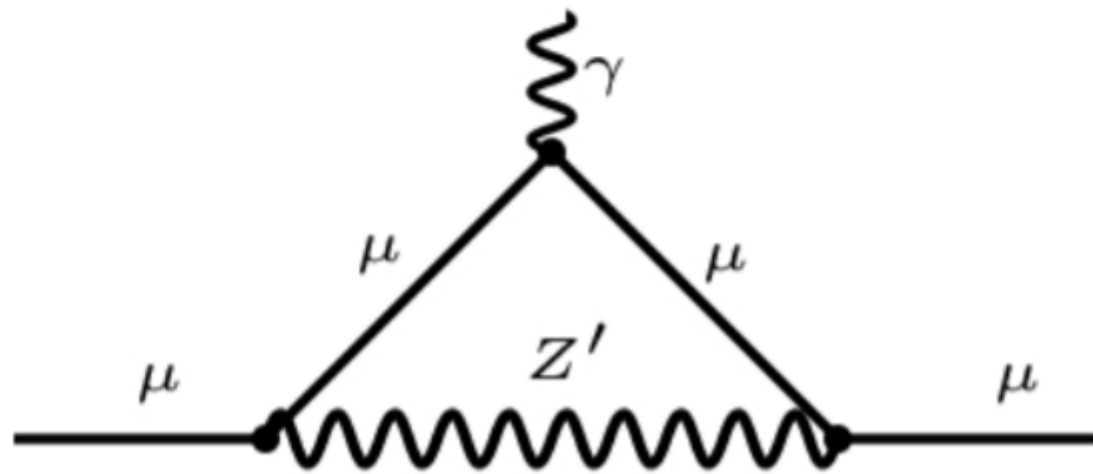
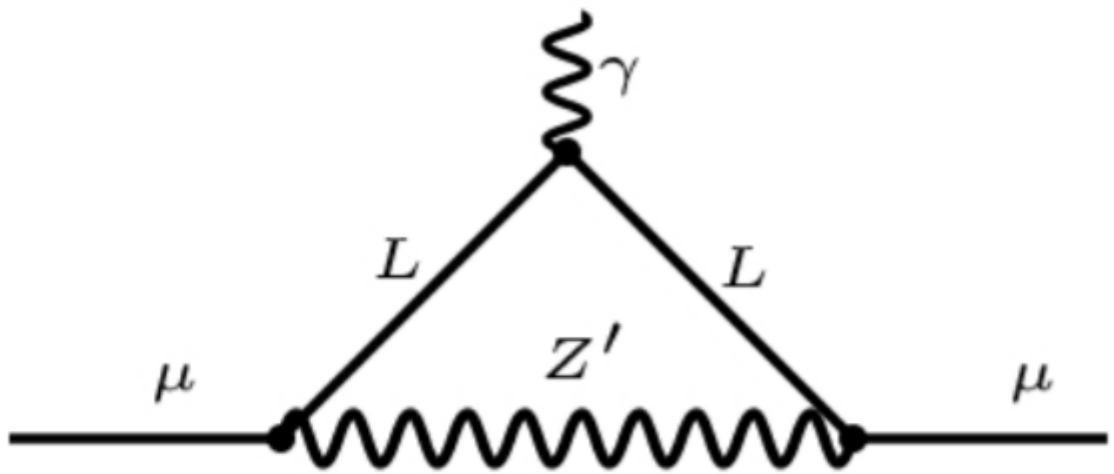


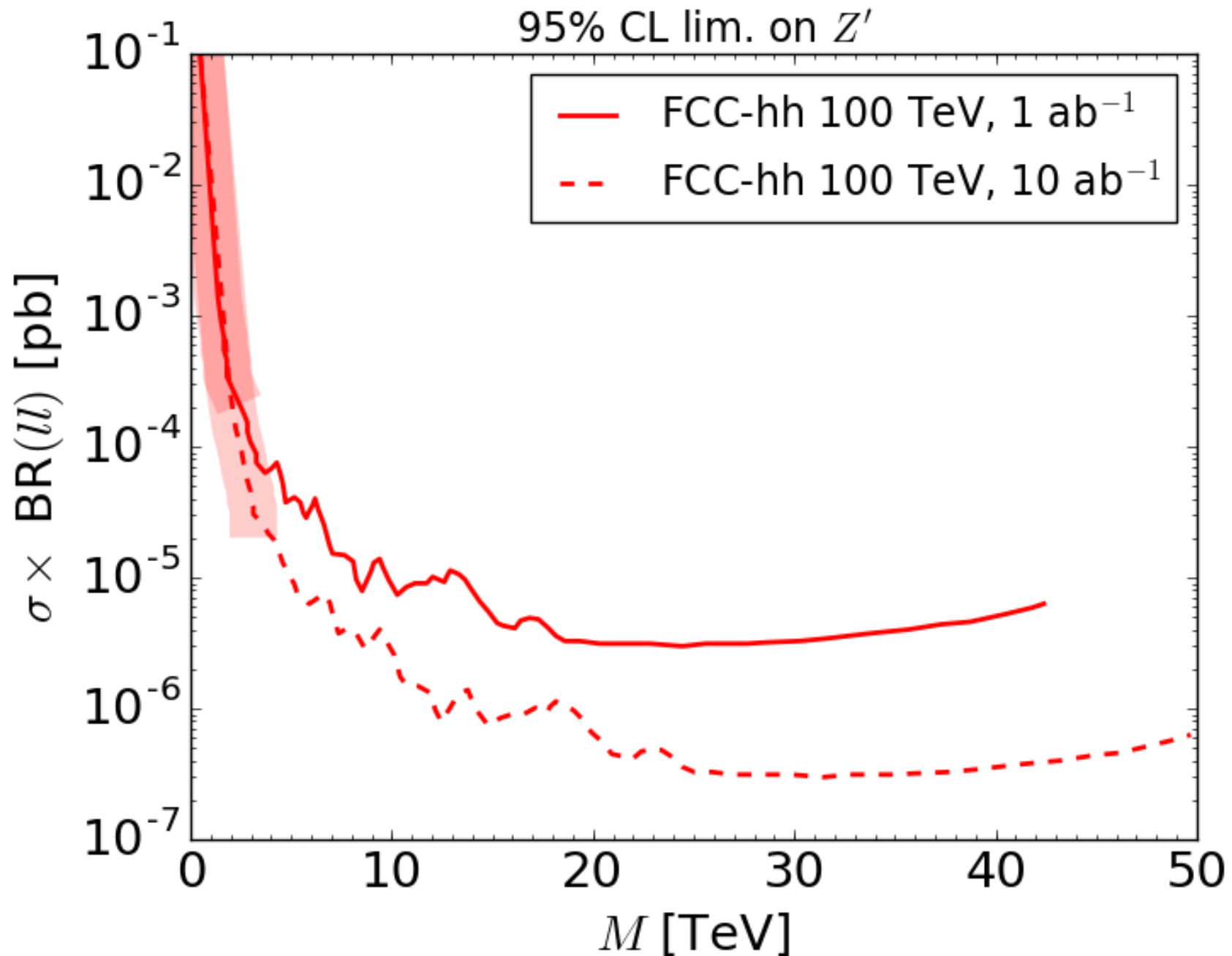
FIG. 10. Neutrino trident process that leads to constraints on the Z^μ coupling strength to neutrinos-muons, namely $M_{Z'}/g_{\nu\mu} \gtrsim 750$ GeV.



Q_{\max}	Solutions	Symmetry	Quadratics	Cubics	Time/sec
1	38	16	144	38	0.0
2	358	48	31439	2829	0.0
3	4116	154	1571716	69421	0.1
4	24552	338	34761022	932736	0.6
5	111152	796	442549238	7993169	6.8
6	435305	1218	3813718154	49541883	56

SM + 3 ν_R : number of solutions etc

13 TeV ATLAS 3.2 fb⁻¹ $\mu\mu$



Neutrino Masses

At dimension 5:

$$\mathcal{L}_{SS} = \frac{1}{2M} (L_3'^T H^c) (L_3' H^c),$$

but if we add RH neutrinos, then integrate them out

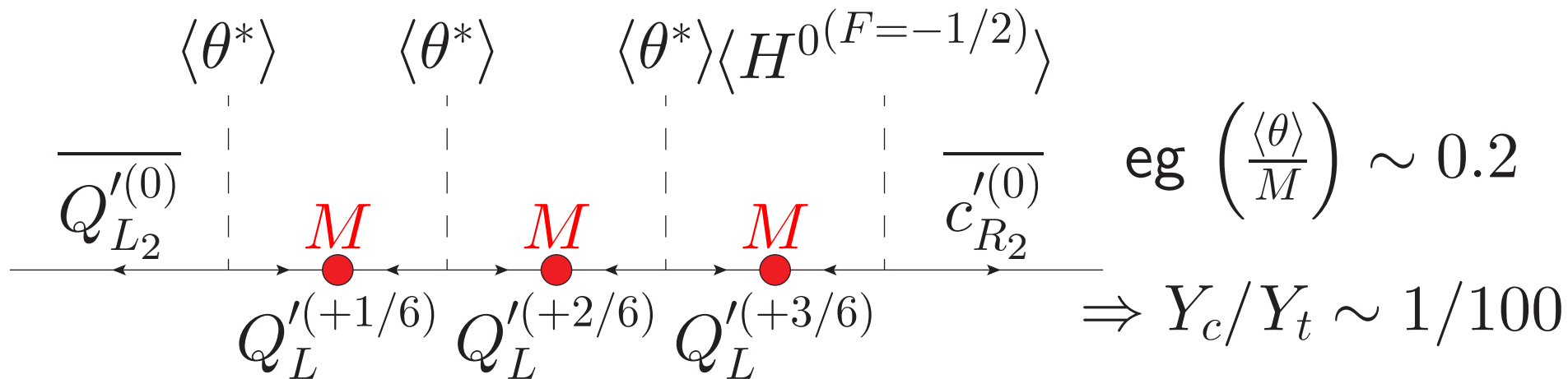
$$\mathcal{L}_{SS} = 1/2 \sum_{ij} (L_i' H^c) (M^{-1})_{ij} (L_j' H^c),$$

where now $(M^{-1})_{ij}$ may well have a non-trivial structure. If $(M^{-1})_{ij}$ are of same order, large PMNS mixing results.

Froggatt Neilsen Mechanism¹⁸

A means of generating the non-renormalisable Yukawa terms, e.g. $F_\theta = 1/6$:

$$Y_c \overline{Q'_{L2}}^{(F=0)} H^{(F=-1/2)} c'_{R2}{}^{(F=0)} \sim \mathcal{O} \left[\left(\frac{\langle \theta \rangle}{M} \right)^3 \overline{Q'_{L2}} H c'_{R2} \right]$$



¹⁸C Froggatt and H Neilsen, NPB147 (1979) 277

LQ Models

Scalar¹⁹ $S_3 = (\bar{3}, 3, 1/3)$ of $SU(2) \times SU(2)_L \times U(1)_Y$:

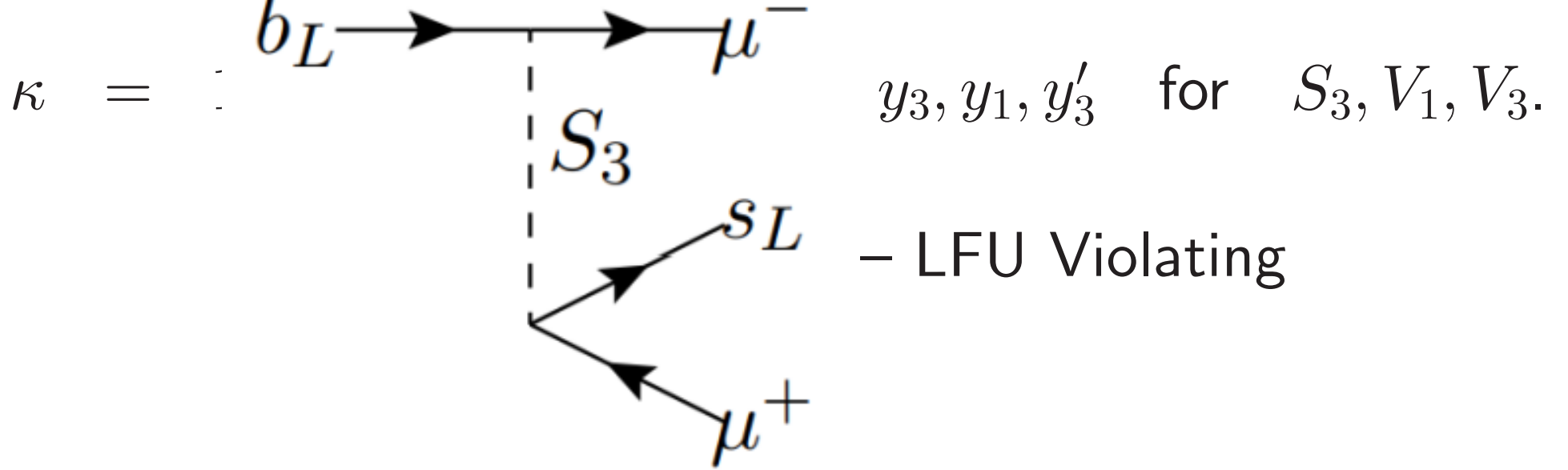
$$\mathcal{L} = \dots + y_{3b\mu} Q_3 L_2 S_3 + y_{3s\mu} Q_2 L_2 S_3 + y_q Q Q S_3^\dagger + \text{h.c.}$$

Vector $V_1 = (\bar{3}, 1, 2/3)$ or $V_3 = (3, 3, 2/3)$

$$\mathcal{L} = \dots + y'_3 V_3^\mu \bar{Q} \gamma_\mu L + y_1 V_1^\mu \bar{Q} \gamma_\mu L + y'_1 V_1^\mu \bar{d} \gamma_\mu l + \text{h.c.}$$

$$\Rightarrow \bar{c}_{LL}^\mu = \kappa \frac{4\pi v^2}{\alpha_{\text{EM}} V_{tb} V_{ts}^*} \frac{y_{3b\mu}^* y_{3s\mu}}{M^2}.$$

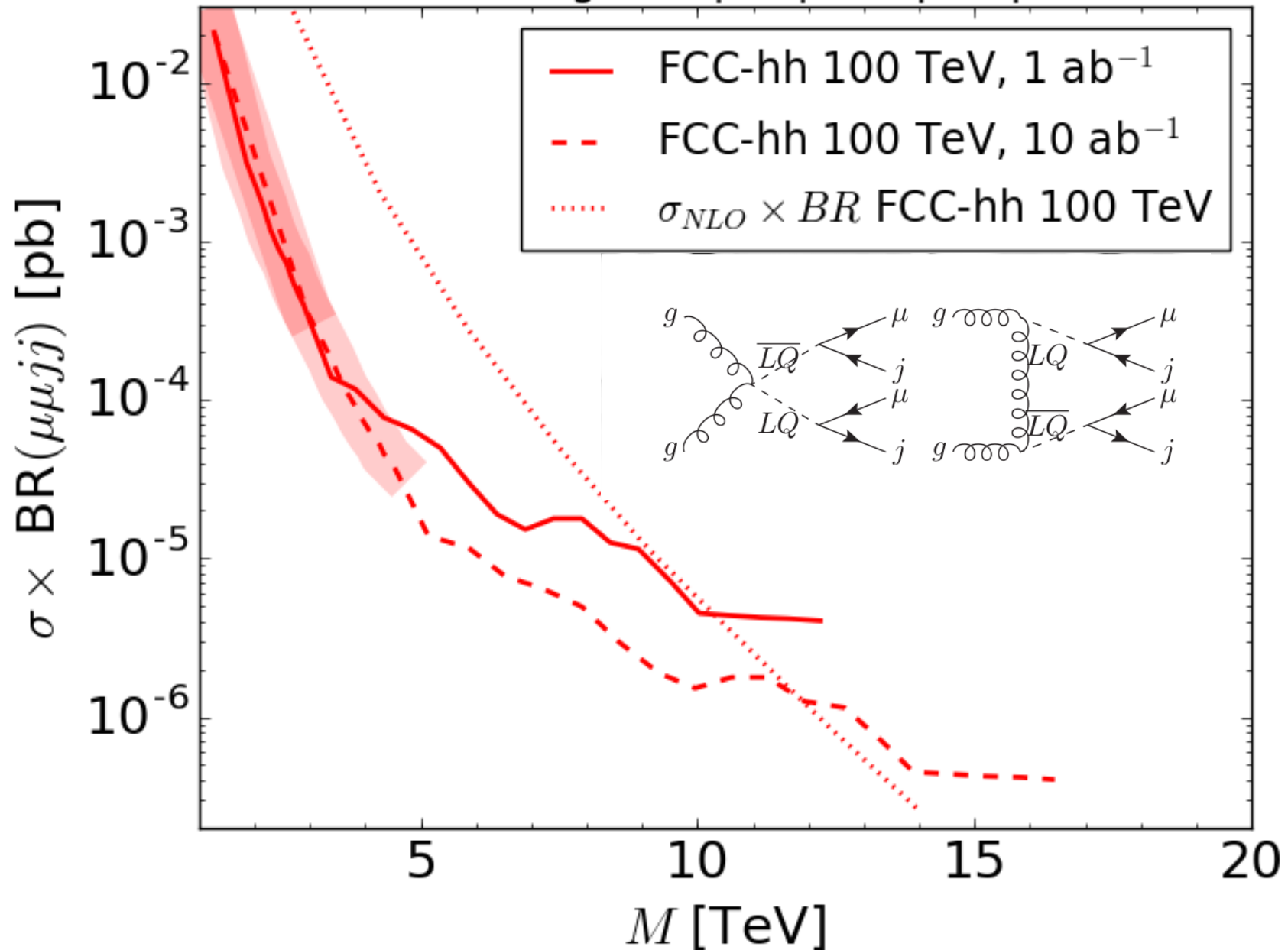
¹⁹Capdevila *et al* 1704.05340, Hiller and Hisandzic 1704.05444, D'Amico *et al* 1704.05438.



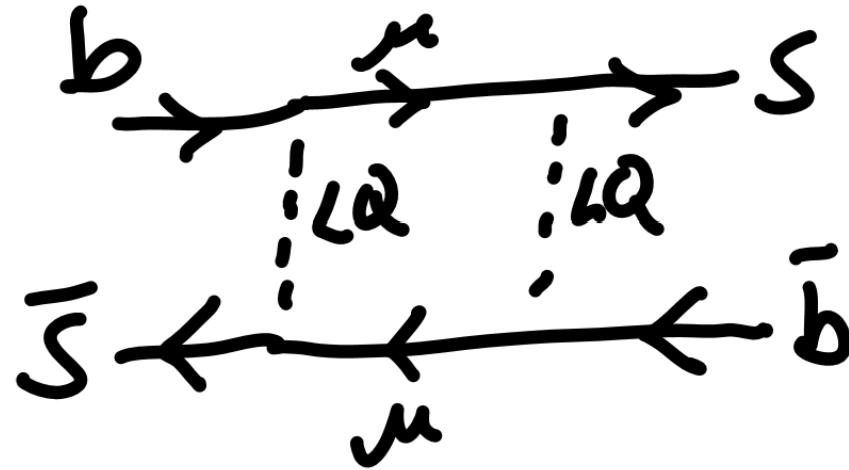
CMS 8 TeV 20fb⁻¹ 2nd gen

CMS-PAS-EXO-12-042: $M > 1.07$ TeV.

95% CL lim. 2nd gen. leptoquark pair production



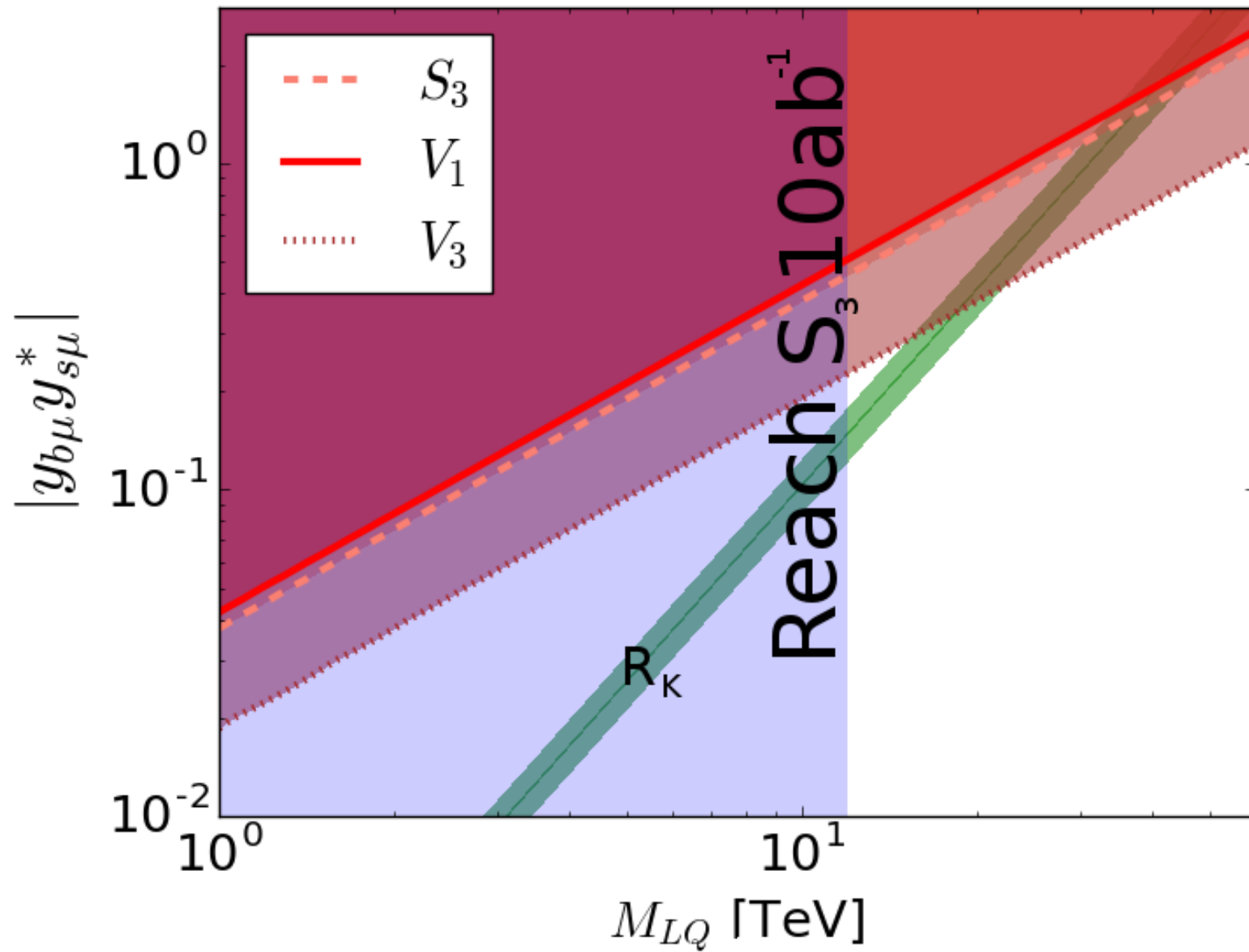
LQ $B_s - \bar{B}_s$ mixing



$$\mathcal{L}_{\bar{b}s\bar{s}b} = k \frac{|y_{b\mu} y_{s\mu}^*|^2}{32\pi^2 M_{LQ}^2} (\bar{b} \gamma_\mu P_L s) (\bar{s} \gamma^\mu P_L b) + \text{h.c.}$$

$y = y_3, y_1, y_3'$ and $k = 5, 4, 20$ for S_3, V_1, V_3 .

Data $\Rightarrow c_{LL}^{bsbs} < 1/(210\text{TeV})^2$.



$M_{LQ} < 41$ TeV. BCA, Gripaos, You, 1710.06363

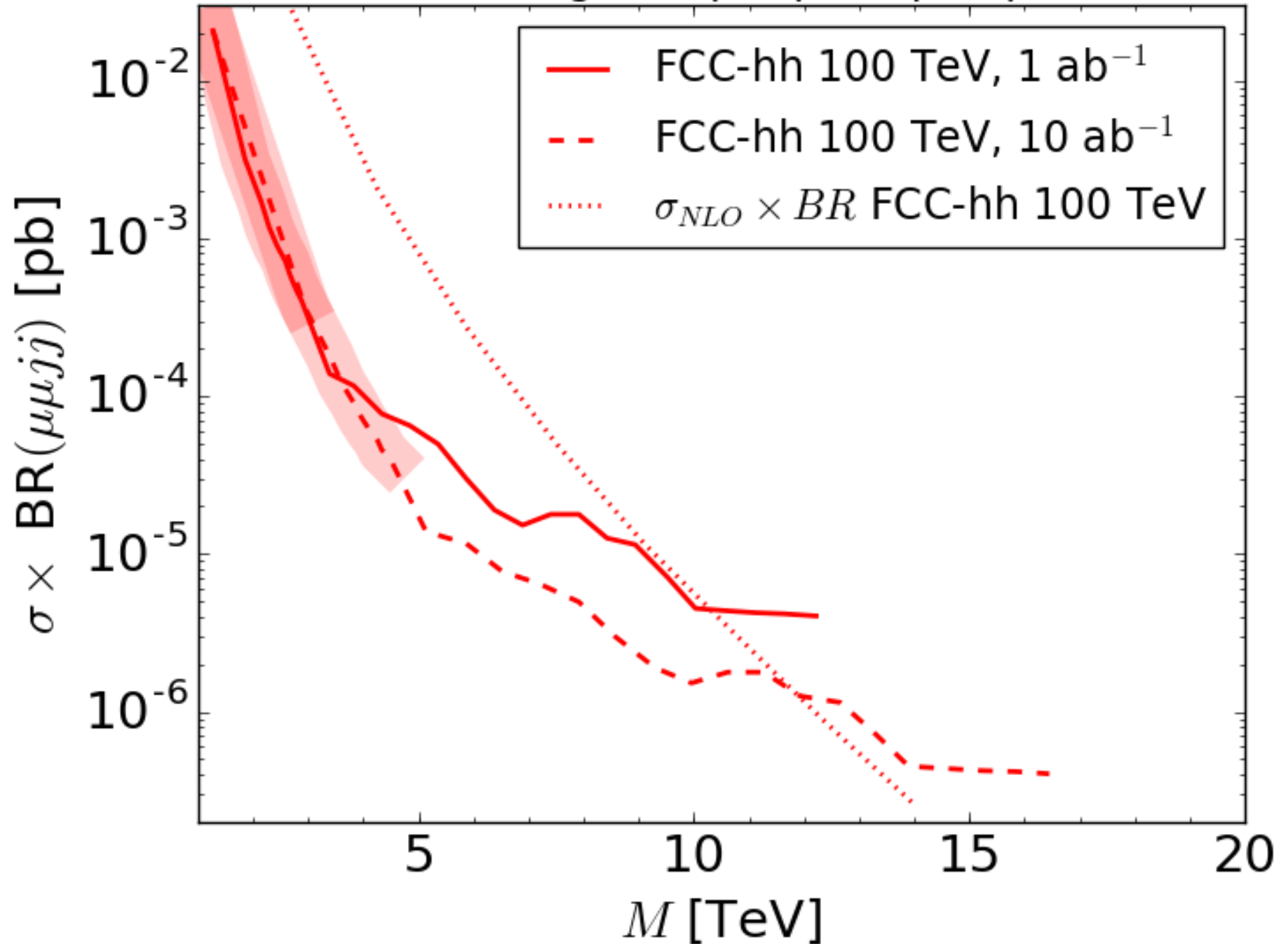
LQ Upper Mass Limits

S_3	41 TeV
V_1	41 TeV
V_3	18 TeV

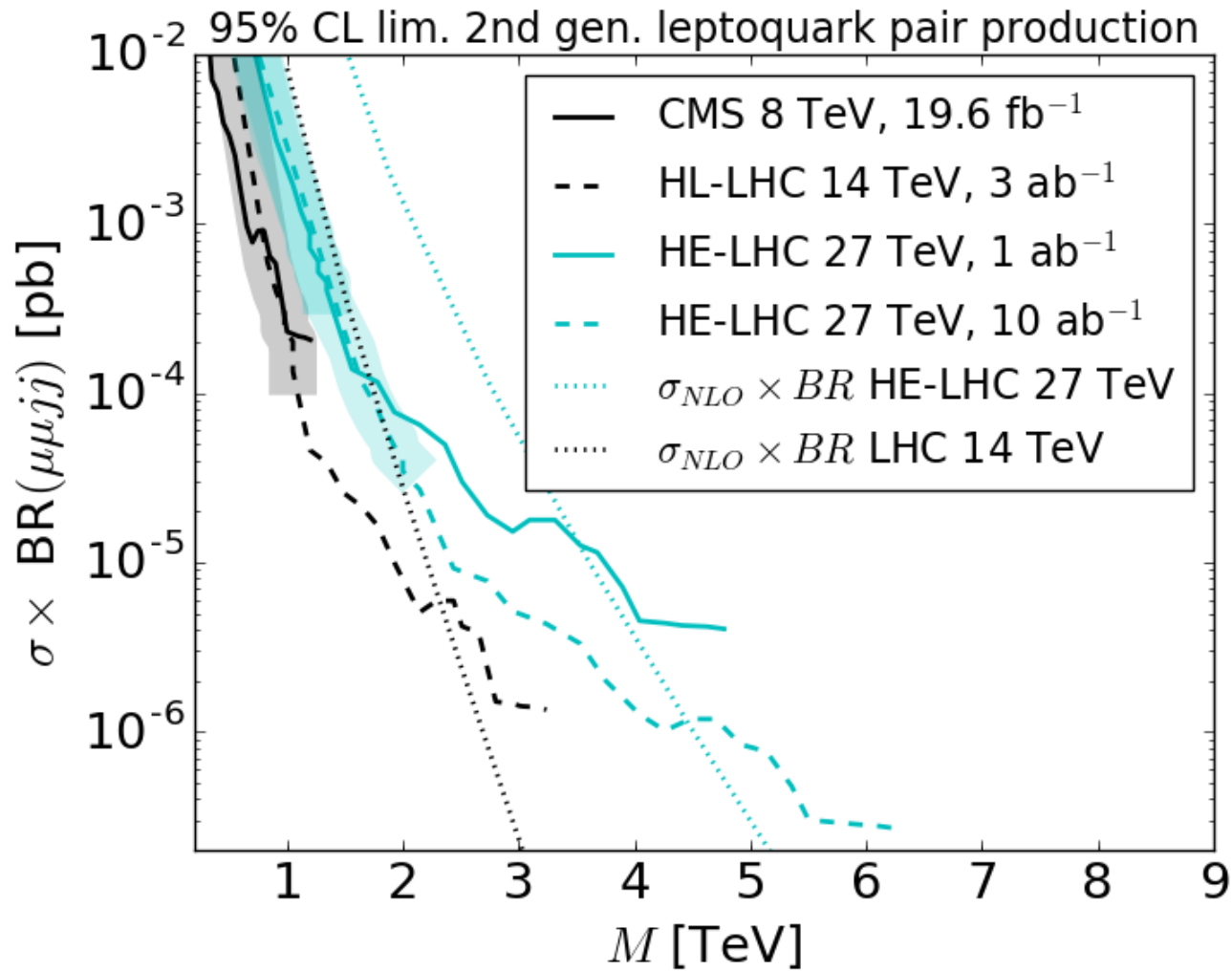
From $B_s - \bar{B}_s$ mixing and fitting b -anomalies.

The pair production cross-section is **insensitive** to the representation of $SU(2)$ in this case.

95% CL lim. 2nd gen. leptoquark pair production



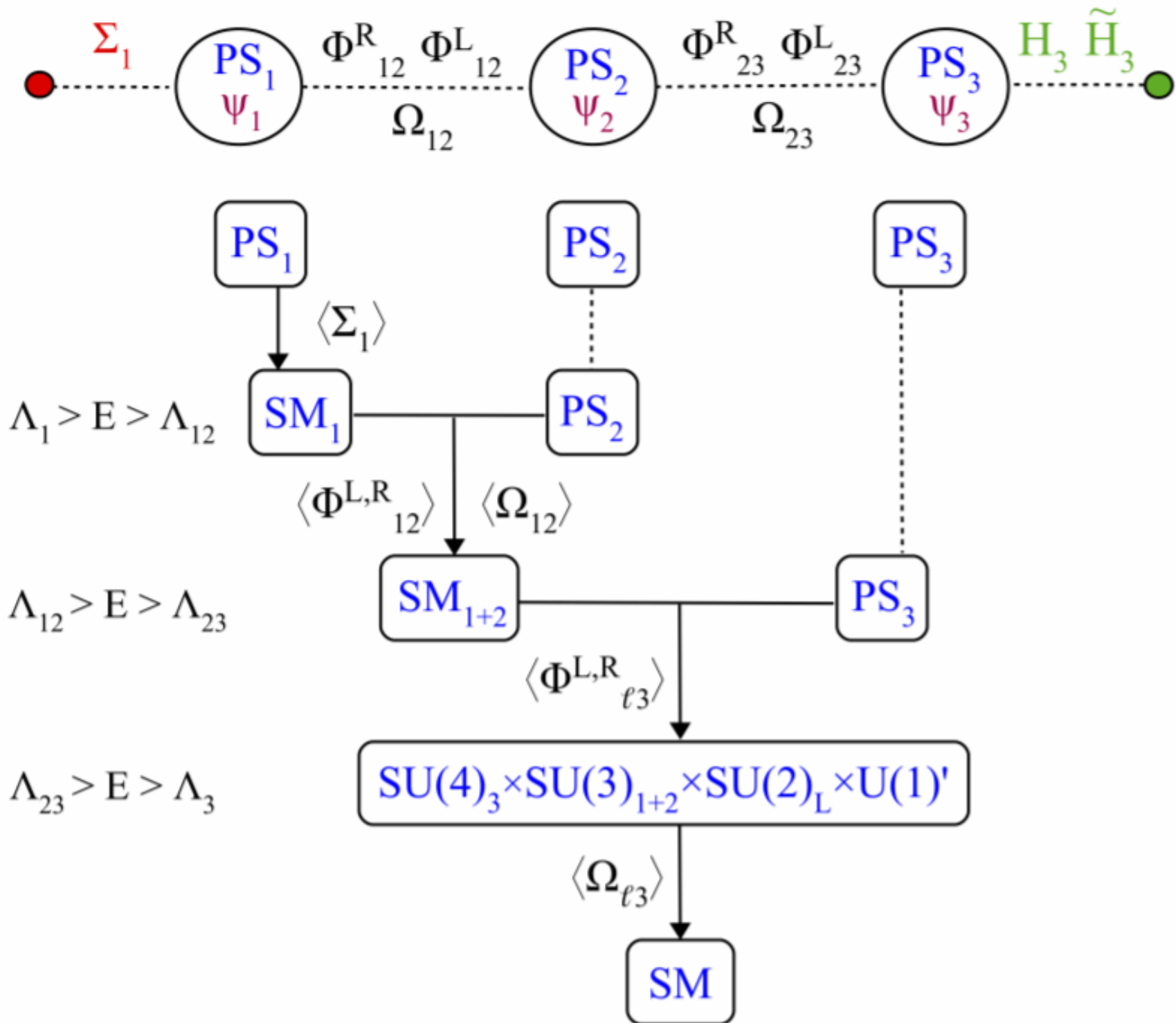
HL-LHC/HE-LHC LQs



Other Flavour Models

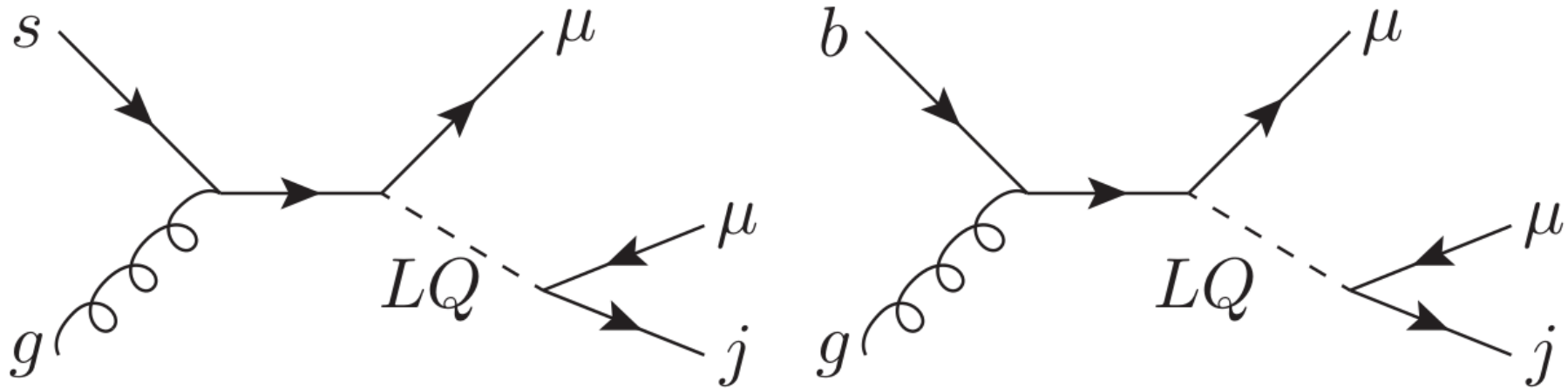
Realising²⁰ the vector LQ solution based on $PS = [SU(4) \times SU(2)_L \times SU(2)_R]^3$. SM-like Higgs lies in third generation PS group, explaining large Yukawas (others come from VEV hierarchies). Get $U(2)_Q \times U(2)_L$ approximate global flavour symmetry.

²⁰Di Luzio Greljo, Nardecchia arXiv:1708.08450, Bordone, Cornella, Fuentes-Martin, Isidori, arXiv:1712.01368



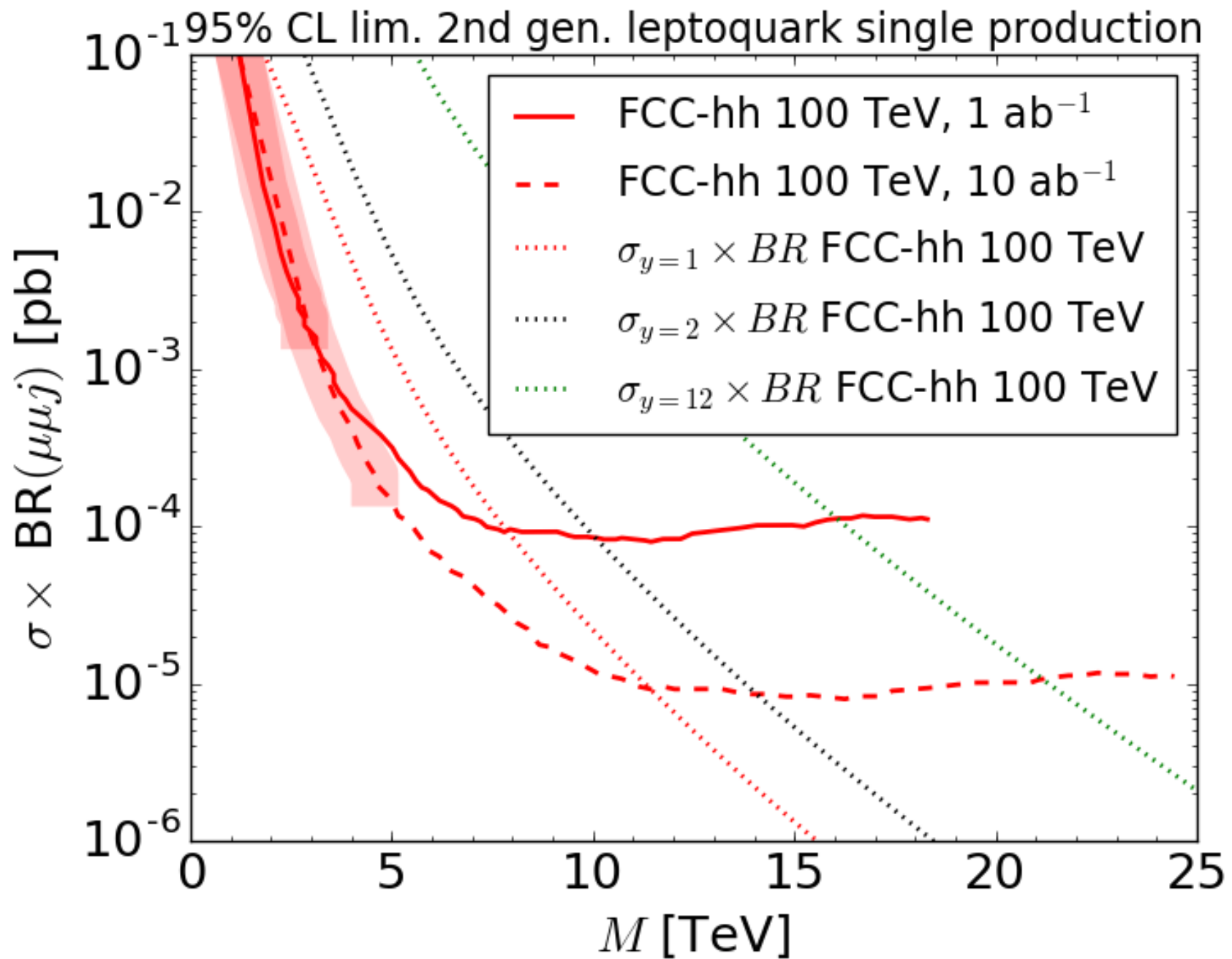
Single Production of LQ

Depends upon **LQ coupling** as well as LQ mass



Current bound by CMS²¹ from 8 TeV 20 fb⁻¹: $M_{LQ} > 660$ GeV for $s\mu$ coupling of 1.

²¹CMS, 1509.03750



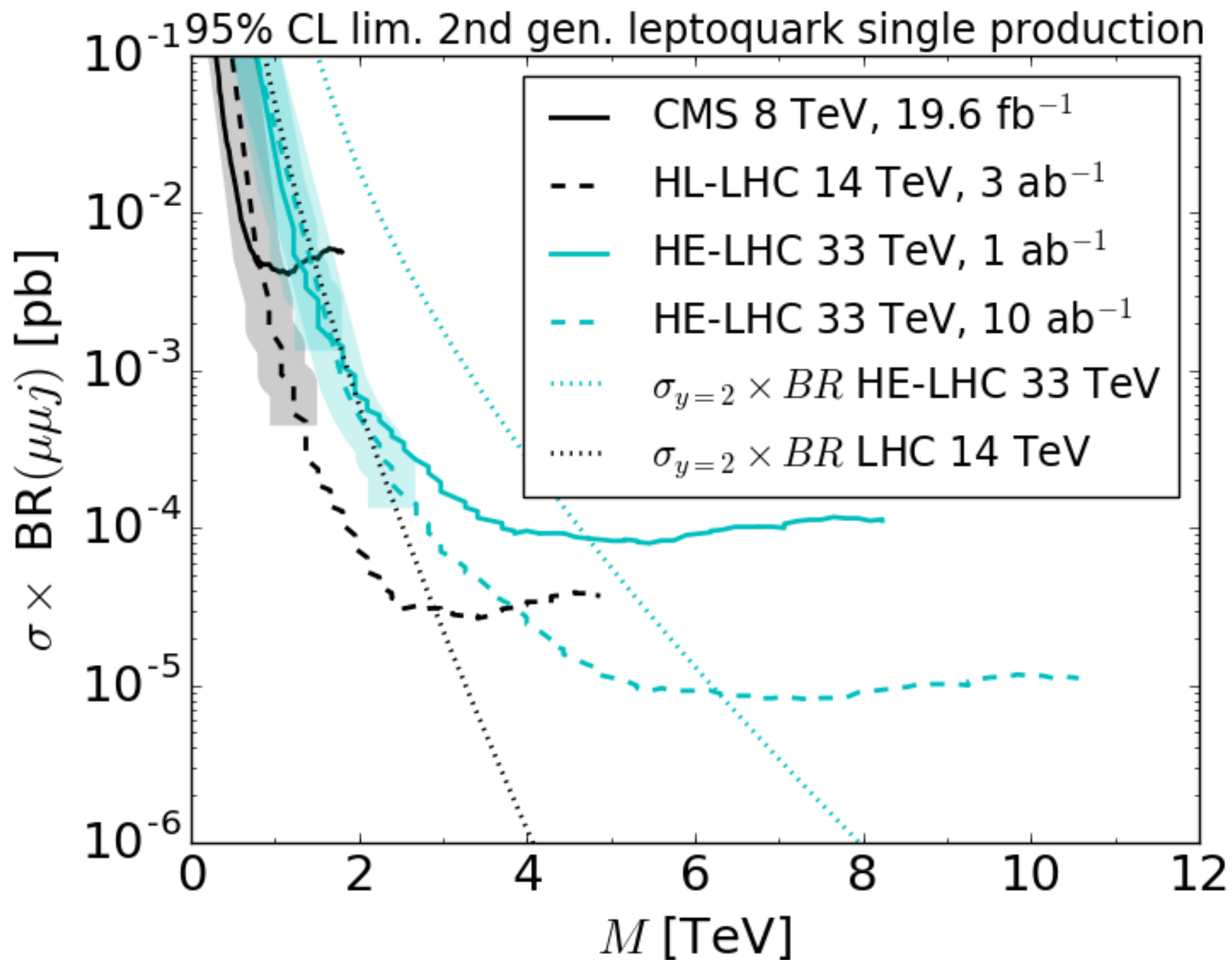
σs for S_3 with $y_{s\mu} = y_{b\mu} = y$.

Single LQ Production σ

$$\hat{\sigma}(qg \rightarrow \phi l) = \frac{y^2 \alpha_S}{96 \hat{s}} (1 + 6r - 7r^2 + 4r(r+1) \ln r) ,$$

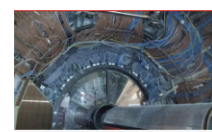
where²² $r = M_{LQ}^2 / \hat{s}$ and we set $y_{s\mu} = y_{b\mu} = y$.

²²Hewett and Pakvasa, PRD **57** (1988) 3165.



In the middle of the [Rencontres de Moriond](#) particle physics conference in Italy, the scientific talks stopped to allow a standing ovation dedicated to the memory and achievements of my inspirational colleague Stephen Hawking, who we heard had died earlier that day.

The talks quickly resumed, which I think Stephen would have approved of. The most striking thing about the scientific content of the conference this year was that a whole day was dedicated to the weirdness in bottom particles that [Tevong You and I wrote about](#) last November. As Marco Nardecchia reviewed in his talk ([PDF](#)), bottom particles produced in the LHCb detector in proton collisions are decaying too often in certain particular ways, compared to predictions from the Standard Model of particle physics. Their decay products are coming out with the wrong angles too often compared with predictions, too.



Anomalous bottoms at Cern and the case for a new collider
[Read more](#)

We were hoping for an update on the data at the conference: the amount of data has roughly doubled since they were last released, and we need to see the new data to be convinced that something really new is happening in the collisions. I strongly suspect that if the effect is seen in the new data, the theoretical physics community will “go nuts” and we will quickly see the resulting avalanche of papers. If the new data look ordinary, the effect will be forgotten and everyone will move on. Taking such measurements correctly takes care and time, however, and the LHCb experiment didn’t release them.

We shall have to wait until other conferences later this year for the LHCb to present its analyses of the new data.

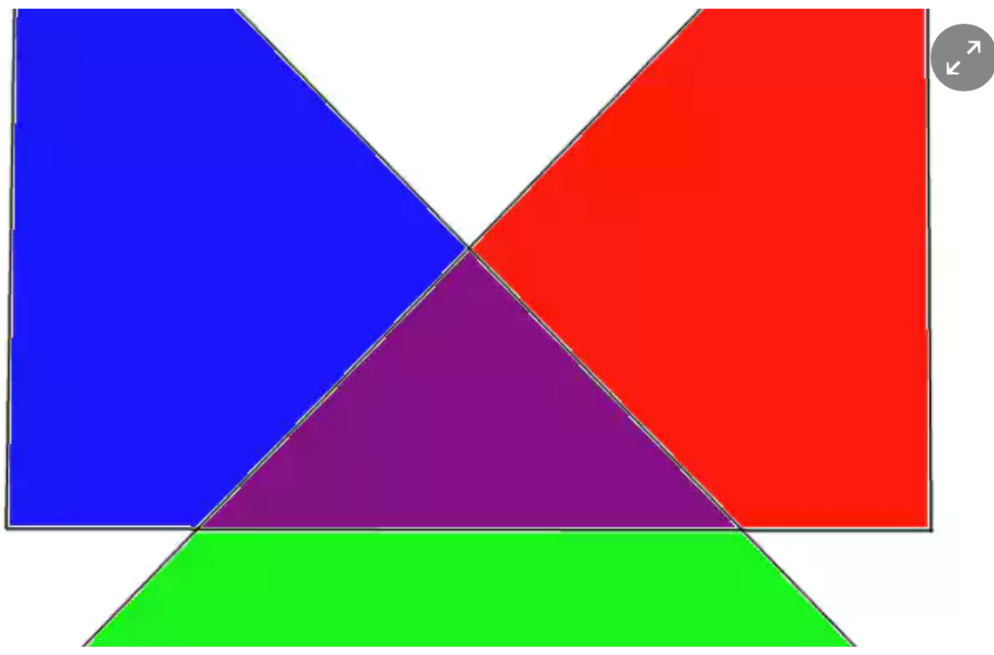
There were interesting theory talks on how new forces could explain the strange properties of the bottom particle decays. The full mathematical models look quite baroque: they need a lot of “bells and whistles” in order to pass other experimental tests. But these models prove that it can be done, and they are quite different to what has been proposed before.

[One of them](#) even unifies different classes of particle (leptons and quarks), describing the lepton as the “fourth colour” of a quark. We are used to the idea that quarks come in three (otherwise identical) copies: physicists label them red, green and blue to distinguish them. As Javier Fuentes-Martin describe ([PDF](#)), once you design the mathematics to make leptons the fourth colour, the existence of a new force-carrying particle with just the correct properties to break up the

Science Life and Physics

Modelling the fourth colour: dispatch from de Moriond

At the particle physics conference, it’s clear inconclusive LHCb data are stimulating strange new ideas



▲ Four colours (or colors?) Photograph: Ben Allanach

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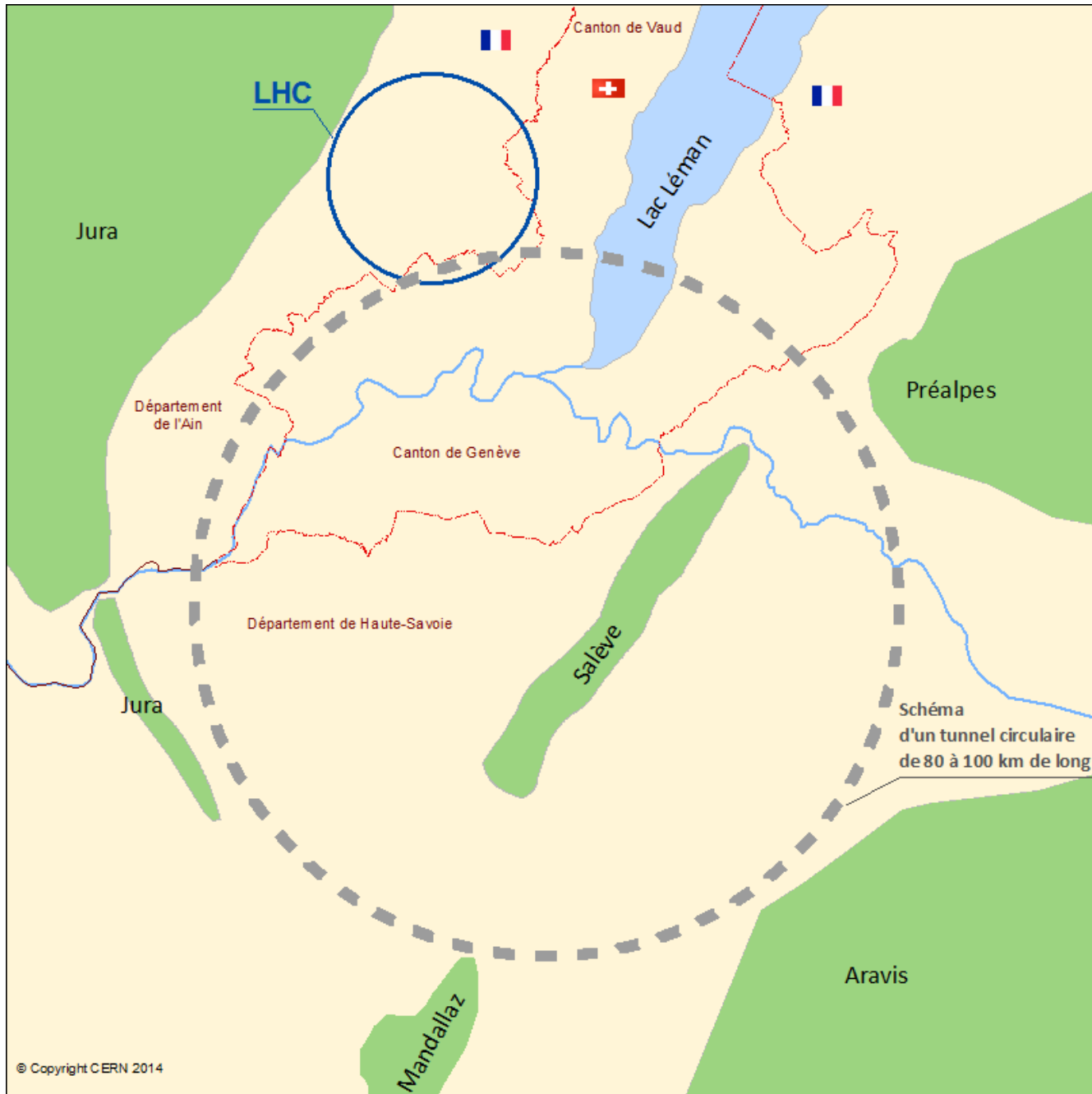
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Cern

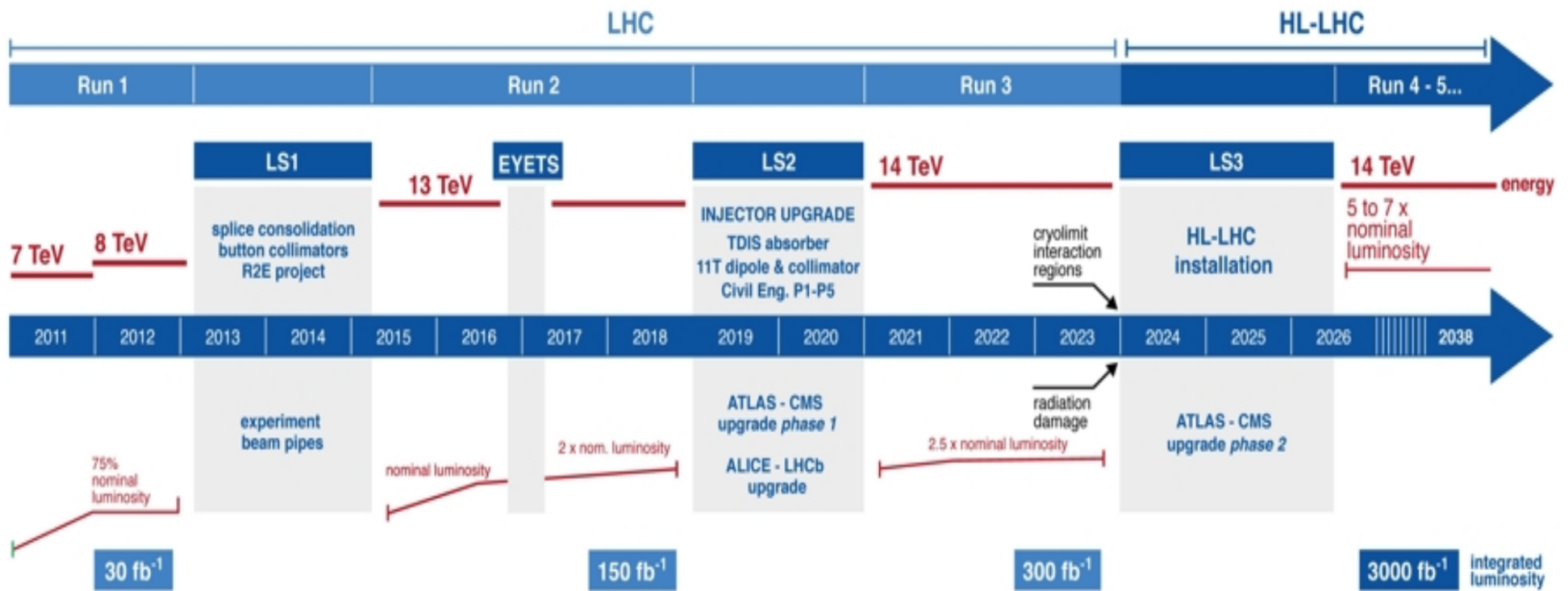
Cern draws up plans for collider four times the size of Large Hadron

The Future Circular Collider would smash particles together in a tunnel 100km long

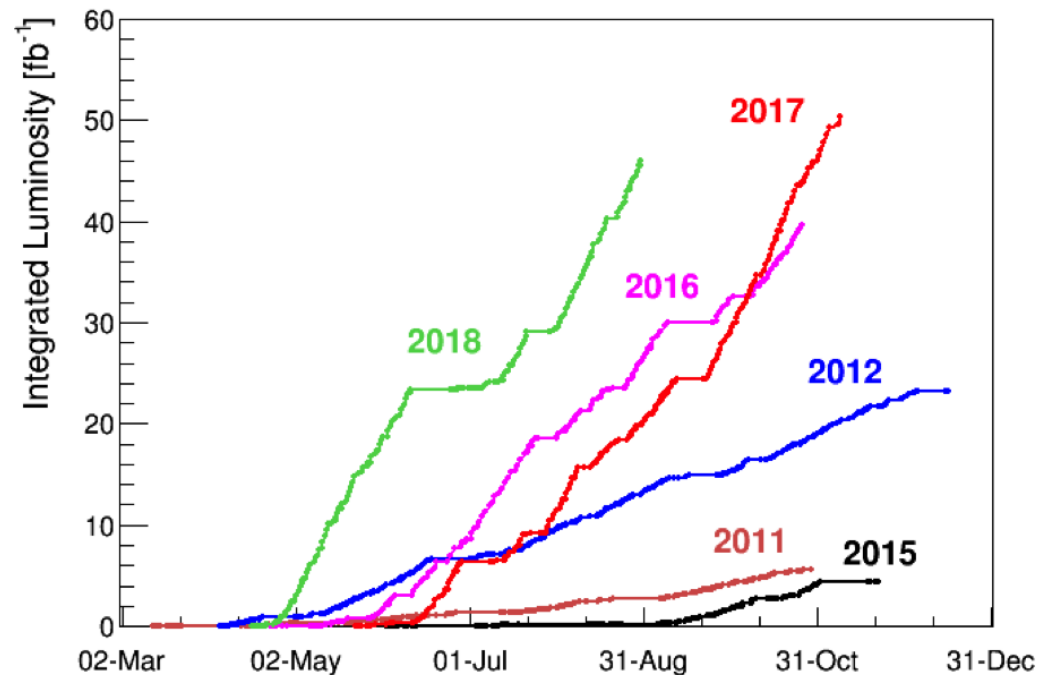




LHC / HL-LHC Plan



LHC Upgrades



High Luminosity (HL) LHC: go to 3000 fb⁻¹ (3 ab⁻¹).

High Energy (HE) LHC: Put FCC magnets (16 Tesla rather than 8.33 Tesla) into LHC ring: roughly *twice* collision energy: 27 TeV.