

CHIRAL EFTS FOR SINGLE- AND DOUBLE-HEAVY HADRONIC MOLECULES

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Systematic Approaches to QCD

$$\mathcal{L}_{\text{QCD}} = \sum_f \bar{q}_f (\gamma_\mu D^\mu - m_f) q_f - \frac{1}{4} \text{Tr} (F^{\mu\nu} F_{\mu\nu})$$

with $D^\mu = \partial^\mu + ig_s \sum_a t^a A^{a\mu}$ and $F^{\mu\nu} = [D^\mu, D^\nu]$ systematically studied for low Q^2 by

- Lattice QCD

Numerical solution in discretised space-time

- Effective Field Theories

- Quarks and gluons as degrees of freedom

Neubert, Beneke, Wise, Manohar, Brambilla, Vairo, Soto, ...

- Born-Oppenheimer EFT

Brambilla et al., Braaten/Bruschini

- Hadrons as degrees of freedom

⇒ Ideal to study hadronic molecules

previous and this talk

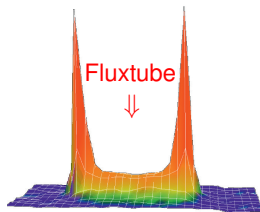
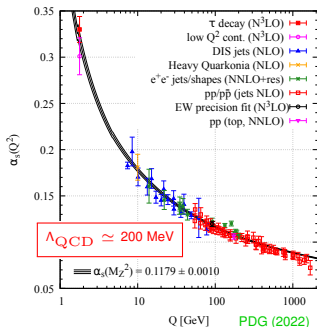
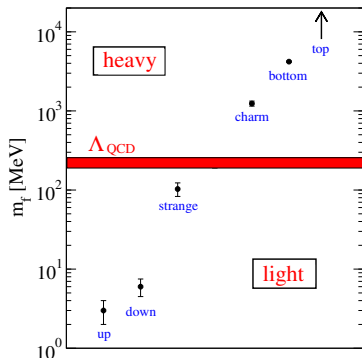


figure courtesy of G. Bali



Quarkmasses and EFTs



Since α_s probed at different scales,
 Λ_{QCD} sorts quarks into

- light (up, down, strange) and
- heavy (charm, bottom, top)
(top too short lived to hadronize)

Groups show different phenomenology
(QCD has no SU(4)-flavor sym.)

Limit of massless light Quarks + infinitely heavy heavy Quarks

Weinberg, Gasser, Leutwyler, Meißner ... and Isgur, Wise, Neubert, Beneke, Manohar, Caswell, Lepage, Brambilla, Vairo, ...

- L and R light Quarks decouple + spontaneous symmetry breaking
- Independence of Heavy Quark Spin and Flavour

⇒ Heavy Hadron Chiral Perturbation Theory (HHChPT)



Outline:

- Investigate states beyond naive quark model ($\bar{q}q$, qqq)
- Identify observables sensitive to molecular structures
- Provide predictions

Outline for the rest of the talk

- The Weinberg criterion: What is a molecule?
- Singly heavy molecules: Chiral symmetry at work
- Doubly heavy molecules: New types of nuclei
- Summary

Hadronic Molecule

Diquark–Anti-diquark

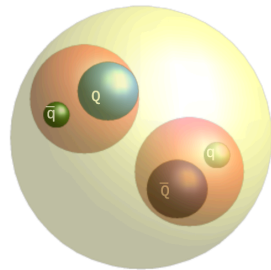
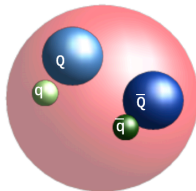


Figure courtesy of Soeren Lange



Hadronic Molecules

review article: Guo et al., Rev. Mod. Phys. 90(2018)015004

- **Few-hadron states**, bound by residual strong force no fluxtubes but **meson exchange** (e.g. π)
- **do exist**: light nuclei.
e.g. **deuteron** as pn & **hypertriton** as Λd bound state
- are located typically **close to relevant continuum threshold**;
 $E_B^{\text{deuteron}} = 2.22 \text{ MeV}$; $E_B^{\text{hypertriton}} = (0.13 \pm 0.05) \text{ MeV}$ (to Λd)
- **Observable (Weinberg compositeness)**: using $\gamma = \sqrt{2\mu E_B}$

$$\frac{g_{\text{eff}}^2}{4\pi} = \frac{4M^2\gamma}{\mu}(1 - \lambda^2) \rightarrow a = -2 \left(\frac{1 - \lambda^2}{2 - \lambda^2} \right) \frac{1}{\gamma}; \quad r = - \left(\frac{\lambda^2}{1 - \lambda^2} \right) \frac{1}{\gamma}$$

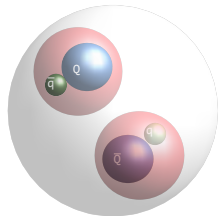
with $(1 - \lambda^2)$ =probability for molecular component in wave function

Corrections are $\mathcal{O}(\gamma R)$ — positive for r in single channel

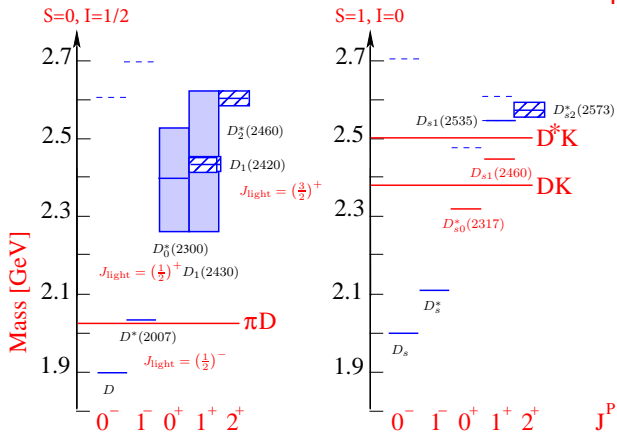
Range corrections: Song, Dai, Oset (2022); Li, Guo, Pang, Wu (2022); Kinugawa, Hyodo (2022)

Are there hadronic molecules with other building blocks?

extensions/further studies: Baru et al., Sekihara, Hyodo, Oset, Oller, Nieves, Jido, Hosaka, Guo ...



Singly heavy states: D -mesons



Quark Modell: M. Di Piero and E. Eichten, PRD 64 (2001) 114004

All those puzzles disappear, if the states are hadronic molecules

Puzzles: Why are/is

- $M(D_{s1}) - M(D_{s0}^*) \simeq M(D^*) - M(D)$?
- $M(D_{s1})$ & $M(D_{s0}^*)$ so light?
- $M(D_0^*) \simeq M(D_{s0}^*)$?
 $M(D_1) \simeq M(D_{s1})$?
- Why do we have
 $M(D_0)^{\text{ChPT}} \approx M(D_0)^{\text{lat.}}$
 $\ll M(D_0)^{\text{exp.}}$?



Goldstone boson- $D^{(*)}$ scattering

- In the chiral limit ($m_u = m_d = m_s = 0$): **Goldstone Theorem**
 \implies GBs (π, η, K) **massless & decouple** for vanishing momenta
- Leading order HHChPT has **no free parameters**

\implies **Weinberg–Tomozawa term** for $P\phi$ scattering in channel a :

$$\mathcal{A}_a = C_a E_{\phi a} / F_0^2 \quad (F_0 = \pi \text{ decay constant})$$

Interaction of **kaons significantly stronger** than that of pions

\implies **group theory** fixes the C_a :

$S = 2$
 $S = 1$
 $S = 0$
 $S = -1$

$[\bar{3}] \otimes [8] = [\bar{15}] \oplus [6] \oplus [\bar{3}]$

$[\bar{15}]$ repulsive,
 $[6]$ attractive,
 $[\bar{3}]$ most attractive

Albaladejo et al., PLB767(2017)465

- NLO: 6 parameters; **controlled quark mass dependence**



Unitarisation (ChPT \rightarrow UChPT)

- Chiral perturbation theory **only perturbatively consistent with unitarity**
- Energy dependent interaction **hits unitarity bound** quickly

\Rightarrow **Unitarisation**; allows for generation of **bound states and resonances**

Truong, Dorado, Pelaez, Kaiser, Weise, Oller, Oset, Lutz, Kolomeitsev, Guo, Meißner, C.H., ...

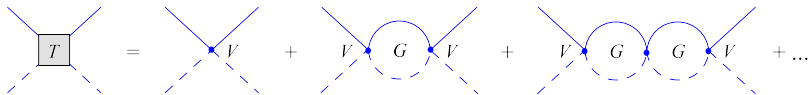
Observe $\text{Im}(t(s)) = \sigma(s) |t(s)|^2$ implies $\text{Im}(t(s)^{-1}) = -\sigma(s)$

\Rightarrow write subtracted **dispersion integral** for $t(s)^{-1}$

\Rightarrow fix $\text{Re}(t(s)^{-1})$ by matching to ChPT

Oller and Meißner, PLB500(2001)263

Effectively this gives



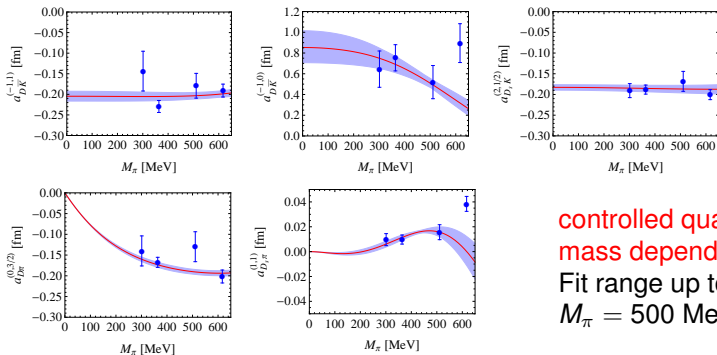
with ChPT expression for V ... and **additional parameter $a(\mu)$** (from the loop)

Dependence on unitarization method & left-hand cuts needs to be clarified!

Lutz et al., PRD106(2022)114038; Korpa et al., PRD107(2023)L031505

Fit to lattice data

fit 6+1 para. to lattice data for $a_{D_x \phi}^{(S,I)}$ in selected channels + $D_{(s)}$ masses



controlled quark
mass dependence
Fit range up to
 $M_\pi = 500$ MeV

- $\pi/K/\eta-D^{(*)}/D_s^{(*)}$ scattering fixed (chiral sym: πD int. weaker than KD)
- $D_{s0}^*(2317)$ emerges as molecule with $M_{D_{s0}^*} = 2315_{-28}^{+18}$ MeV
since $E_b(D_{s0}) = E_b(D_{s1}^*) + \mathcal{O}(1/M_D) \implies$ puzzle 1+2 solved



The $S = 0$ sector

Lattice: @ $M_\pi = 391$ MeV pole at 2275.9 ± 0.9 MeV

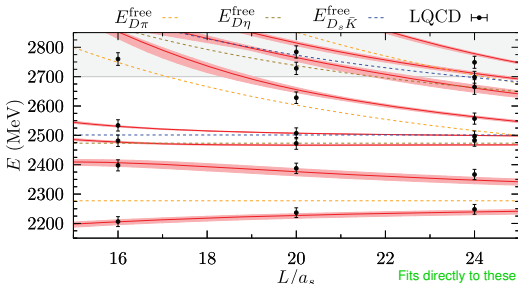
Had.Spec.Coll. JHEP10(2016)011

@ $M_\pi = 239$ MeV pole at $2196 \pm 64 - i(210 \pm 110)$ MeV

HadSpec, JHEP07(2021)123

UChPT for $M_\pi = 391$ (parameters fixed in 2013):

Albaladejo et al., PLB767(2017)465

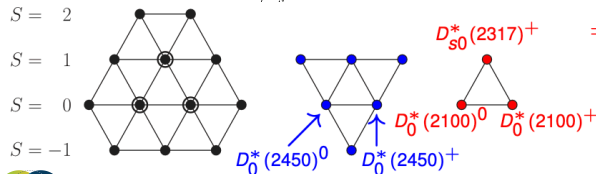


finds poles for

- $M_\pi \simeq 391$ MeV at
(2264, 0) MeV [000] &
(2468, 113) MeV [110]
- $M_\pi = 139$ MeV at
(2105, 102) MeV [100] &
(2451, 134) MeV [110]

why second pole was first missed: Asokan et al., EPJC83(2023)850

Fits directly to these data: Guo et al., EPJC 79(2019)13; Lutz et al., PRD106(2022)114038



\Rightarrow puzzle 3 solved

- Quark Model only $[\bar{3}]$
- Diquark Model all

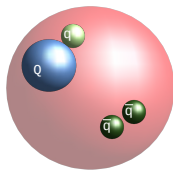
Compact tetraquarks

Heavy-light diquarks, cq , in flavor

$$[3]_{\{cq\}}$$

Light diquarks, $\bar{q}\bar{q}$ in flavor

$$[\bar{3}]_{\bar{q}} \otimes [\bar{3}]_{\bar{q}} = \underbrace{[3]_{\{\bar{q}\bar{q}\}}}_{\text{anti-sym.}} \oplus \underbrace{[\bar{6}]_{\{\bar{q}\bar{q}\}}}_{\text{sym.}}$$



Fermi symmetry: $[\text{color}] \otimes [\text{flavor}] \otimes [\text{spin}]$ anti-symmetric

diquarks anti-sym. in color (attractive one gluon exchange) \implies

- $\bar{q}\bar{q}$ spin 0 (anti-sym.) must be combined with flavor $[3]_{\{\bar{q}\bar{q}\}}$

adding cq diquark: $[3]_{\{cq\}}^{0/1} \otimes [3]_{\{\bar{q}\bar{q}\}}^0 = [\bar{3}]_{\{cq\}\{\bar{q}\bar{q}\}}^{0\otimes 0/1\otimes 0} \oplus [6]_{\{cq\}\{\bar{q}\bar{q}\}}^{0\otimes 0/1\otimes 0}$

L. Maiani et al. PRD110 (2024) 3

- $\bar{q}\bar{q}$ spin 1 (sym.) must be combined with flavor $[\bar{6}]_{\{\bar{q}\bar{q}\}}$

adding cq diquark: $[3]_{\{cq\}}^{0/1} \otimes [\bar{6}]_{\{\bar{q}\bar{q}\}}^1 = [\bar{3}]_{\{cq\}\{\bar{q}\bar{q}\}}^{0\otimes 1/1\otimes 1} \oplus [\bar{15}]_{\{cq\}\{\bar{q}\bar{q}\}}^{0\otimes 1/1\otimes 1}$

't Hooft int. pushes $[\bar{3}]$ up: Dmitrasinovic, PRD70(2004)096011

From phenomenology: $M_{cq}^{S=1} - M_{cq}^{S=0} \approx M_{qq}^{S=1} - M_{qq}^{S=0} \approx 150 \text{ MeV}$



Comparison of 1^+ and 0^+

lightest **compact tetraquarks**:

$$\text{spin } 0: [\bar{3}]_{\{cq\}}^{0\otimes 0} \oplus [6]_{\{cq\}}^{0\otimes 0} \{q\bar{q}\};$$

$$\text{spin } 1: [\bar{3}]_{\{cq\}}^{1\otimes 0} \oplus [6]_{\{cq\}}^{1\otimes 0} \{q\bar{q}\} \oplus [\bar{15}]_{\{cq\}}^{0\otimes 1} \{q\bar{q}\};$$



spin 1 and 0 behave
differently

lightest **hadronic molecules**:

$$\text{spin } 0: [\bar{3}]_{\{c\bar{q}\}}^{0\otimes 0} \oplus [6]_{\{c\bar{q}\}}^{0\otimes 0} \{q\bar{q}\};$$

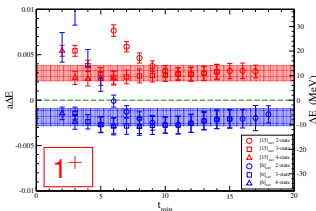
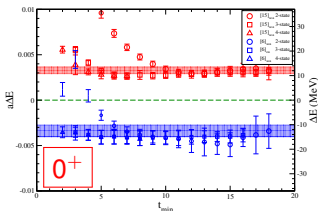
$$\text{spin } 1: [\bar{3}]_{\{c\bar{q}\}}^{1\otimes 0} \oplus [6]_{\{c\bar{q}\}}^{1\otimes 0} \{q\bar{q}\} \quad [\bar{15}] \text{ absent};$$



spin 1 and 0 behave
equally

To see which scenario is realised: **Lattice simulation**

E.B. Gregory et al., EPJA61(2025)226



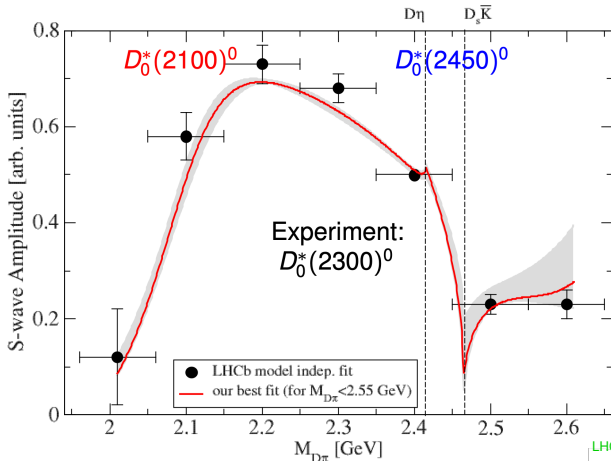
consistent levels
for 0^+ and 1^+

$[\bar{15}]$ repulsive

$\Rightarrow D_0$ states
molecular

$D\pi$ S-wave from $B^- \rightarrow D^+\pi^-\pi^-$

Du et al., PRD98(2018)094018; for more results see Du et al., PRD99(2019)114002, PRL126(2021)192001



LHCb, PRD94(2016)072001

Effect of higher thresholds enhanced, by pole at $\sqrt{s_p} \sim (2451 - i134)$ MeV
 on nearby unphysical sheet \Rightarrow puzzle 4 solved

Charmed states: Q&A

Why are $M(D_{s1})$ & $M(D_{s0}^*)$
so light?

Since they are **are DK and D^*K**
bound states (=hadronic molecules)

Why is $M(D_{s1}) - M(D_{s0}^*)$
 $\simeq M(D^*) - M(D)$?

Since spin symmetry gives equal binding

Why is $M(D_0^*) \simeq M(D_{s0}^*)$?
and $M(D_1) \simeq M(D_{s1})$?

Since listings need to be corrected:
Lightest **D_0 @2100 MeV & D_1 @2240 MeV**

Why do we have
 $M(D_0^*)^{\text{ChPT}} \simeq M(D_0)^{\text{lat.}}$
 $\ll M(D_0)^{\text{exp.}}$?

Since structure at 2300 MeV is
made of two poles
analogous to $\Lambda(1405)$ from 2 poles
Oller and Meißner, PLB500(2001)263

Combination of EFT, lattice QCD and experiment provides **consistent picture**
for the **whole family of states**

\Rightarrow **blueprint for other reactions**

EFT for doubly heavy states

Schemes currently proposed (only initial work cited)—analogous to NN

- **Contact EFT**: no pions
- **X-EFT**: pert. pions
- **chiral EFT**: non.-pert. pions
 - largest energy range of applicability
 - Pion dynamics fully under control

AlFiky et al., PLB640(2006)238

Fleming et al., PRD76(2007)034006

Baru et al., PRD84(2011)074029

⇒ use this in what follows

Thus we solve LS-equation

Du et al., PRD105(2022)014024

$$T = V + VGT \text{ with } V_{LO} = \begin{array}{c} \begin{array}{ccc} {}^3S_1 & \text{---} & {}^3S_1 \\ {}^3D_1 & \text{---} & {}^3D_1 \end{array} \\ \text{OPE} \end{array} + \begin{array}{ccc} & \diagdown & \\ {}^3S_1 & & {}^3S_1 \\ & \diagup & \\ & C_0 & \end{array}$$

employing the expansion parameter $\chi = M_\pi/\Lambda_\chi \approx 0.1$

@ LO : One to two free parameters per isospin (for each cut off)

@ NLO: energy dep. & M_π^2 dependent counter terms + loops.

However, loops absorbed into counter terms

Chacko et al. PRD 111 (2025)034042



Example: Pentaquarks as Molecules

Predicted in phenomenological analysis

J. J. Wu, R. Molina, E. Oset and B. S. Zou, PRL 105(2010), 232001

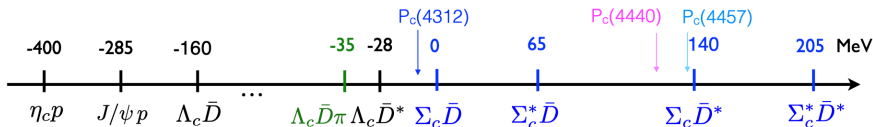
Various pion less EFT studies

Nieves, Oset, Geng, Valderrama,

We applied pion full EFT & fit to data

M. L. Du et al., PRL 124 (2020) 7, 072001

Potentially relevant thresholds:



Systematic study of pertinent channels — Idea:

- Formation of states in $\Sigma_c^{(*)} \bar{D}^{(*)}$ channels (elastic channels)
- Aim at fitting experimental data for $\Lambda_b \rightarrow K p J/\psi$
- Predictions for $\Lambda_b \rightarrow K \Sigma_c^{(*)} \bar{D}^{(*)}$ and $\Lambda_b \rightarrow K \eta_c p$
- Is there room for $\Lambda_b \rightarrow K \Lambda_c \bar{D}^{(*)}$? (Predicted by many models)



Formalism

$$V_{\text{LO}}^{\text{eff}} = \text{[Diagram 1]} + \text{[Diagram 2]} + \text{[Diagram 3]}$$

Diagram 1: A vertex with four external lines meeting at a central black dot. A red arrow points downwards from the dot.

 Diagram 2: Two horizontal lines connected by a vertical dashed line labeled π .

 Diagram 3: Two external lines meeting at a vertex, with a curved line (loop) between them. The top part of the loop is solid and labeled $\eta_c, J/\Psi, \dots$. The bottom part is dashed and labeled p .

HQSS: 2 S-S wave LECs at $O(Q^0)$
 1 S-D wave LEC at $O(Q^2)$

Long range: OPE

Imaginary part from inelastic channels

Total number of parameters **without/with** the $\Lambda_c \bar{D}^{(*)}$ channels

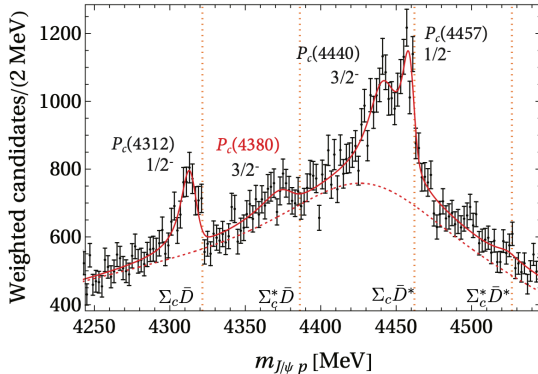
- elastic channels:** $\Sigma_c^{(*)}$ has $j_{\text{light}} = 1$; $D^{(*)}$ has $j_{\text{light}} = 1/2$
 \implies **2 counter terms** with $j_{\text{light}} = 1/2$ & $j_{\text{light}} = 3/2$, respectively
- $J/\psi p$ and $\eta_c p$: transitions in S and D wave
 \implies 2 parameters for $\Sigma_c^{(*)} \bar{D}^{(*)} \rightarrow p(J/\psi/\eta_c)$
- $\Lambda_c^{(*)}$ has $j_{\text{light}} = 0$; $D^{(*)}$ has $j_{\text{light}} = 1/2$
 \implies **1** parameter for $\Lambda_c \bar{D}^{(*)} \rightarrow \Sigma_c^{(*)} \bar{D}^{(*)}$
- 1 (2)** parameters for the promoted S – D counter terms
 \implies **5 parameters (7 parameters)** control the scattering,

but the 2 first are most important

.... and 7 parameters to control the production

Results for $\Lambda_b \rightarrow KpJ/\psi$

data: LHCb, PRL122 (2019)222001



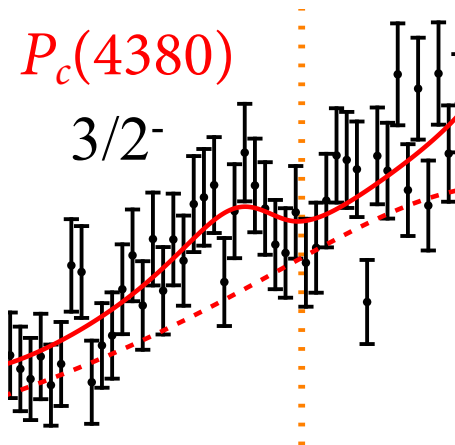
- Data described well ($\chi^2/dof \approx 1$)
- Without OPE two good fits (different order of the $\Sigma \bar{D}^*$ states)
- With OPE unique fit
- Observe indications for narrow $P_c(4380)$

⇒ Fit provides 1 $\Sigma_c \bar{D}$, 1 $\Sigma_c^* \bar{D}$, 2 $\Sigma_c \bar{D}^*$ and 3 $\Sigma_c^* \bar{D}^*$ molecules (compared to 10 for the diquark picture with different J^P)

⇒ basically 2 parameters fixed by fitting 3 states

⇒ Not all show up in the data (importance of production vector?)

Zooming in



Spin symmetric couplings
give **additional states**

Source coupling of $\Sigma_c^* D$ chan-
nel different from 0 by **1.7σ**

Its confirmation would provide
support for molecular picture!

three states still missing!!

The amount of **spin symmetry violation** is specific to the structure

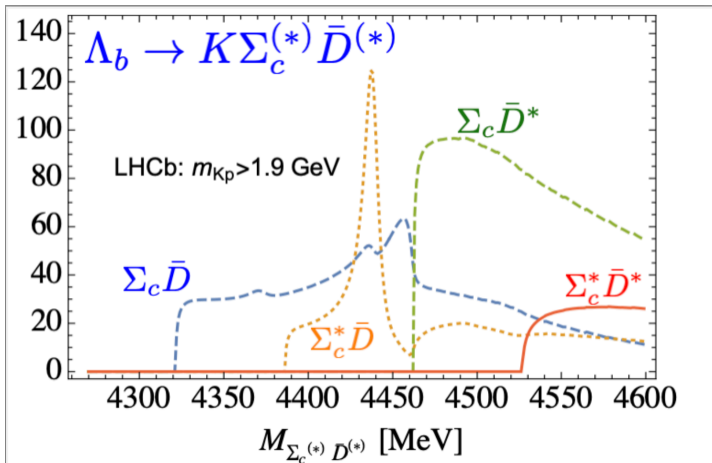
⇒ Molecules follow the thresholds!

M. Cleven et al., PRD92(2015)014005

Signatures in elastic channels

Typical spectrum

Du et al., JHEP 08 (2021) 157

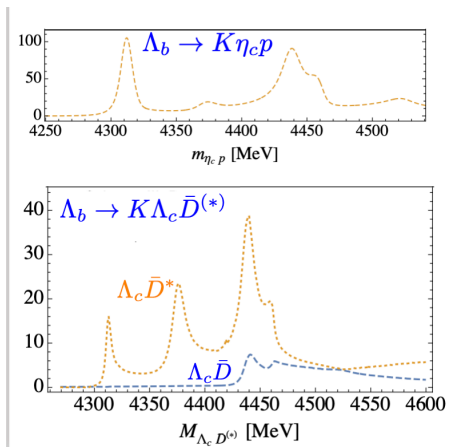


strong threshold enhancement - unavoidable for hadronic molecules

Signatures in inelastic channels

Du et al., JHEP 08 (2021) 157

- For $\Sigma_c^{(*)} \bar{D}^{(*)} \rightarrow \Lambda_c \bar{D}^{(*)}$ OPE + two add. para. (S-S and S-D)



- $\eta_c p$ channel similar to $J/\psi p$ (spin symmetry!)
- $\Lambda_c \bar{D}^{(*)}$ final states **not constrained yet**
- Shown: **Some typical spectrum**
- Data even compatible with very weak signal
- $(\Lambda_c \bar{D} \rightarrow \Sigma_c \bar{D})_{S\text{-wave}} = 0$
 $(\Lambda_c \bar{D} \rightarrow \Sigma_c^* \bar{D})_{DS\text{-wave}} = 0$

Summary and Perspectives

- The recent and future data have the potential to allow us to identify the prominent components in exotic states

to-do for experiment

- **Continue** great performance! Especially needed:
 - data for **different quantum numbers** and
 - data for **line shapes** in different systems

to-do for theory

- Provide more predictions for the **different scenarios** in **EFTs** as well as **lattice QCD**
- Go beyond most simple approaches
e.g. study **interplay of regular quarkonia with exotics**
 - potentially significant mixing

Kalashnikova et al., PRD80(2009)074004; Takizawa et al., PTEP(2013)093D01; Ortega et al., JPG 40(2013)065107;
Coito et al., EPJC73(2013)2351; Cincioglu et al., EPJC76(2016)576

- negligible mixing

van Beveren et al., PLB641(2006)265; Hammer et al., EPJA52(2016)330, C.H. et al., PRD106(2022)114003

⇒ Exploit further **BOEFT** and **Dyson-Schwinger approaches**