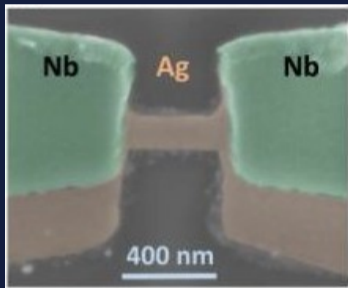


Superfluid transport through a dissipative quantum point contact

Anne-Maria Visuri

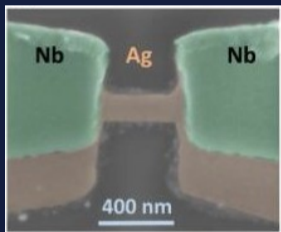


Superconducting contact

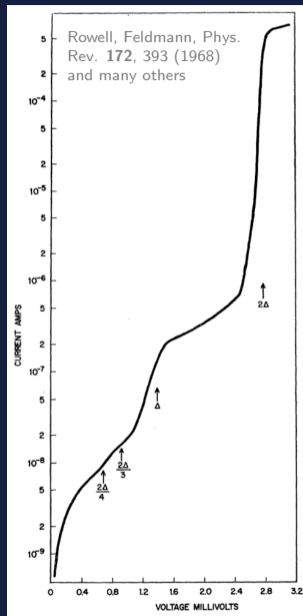


Basset *et al.*, Phys. Rev. Research **1**, 032009(R)
(2019)

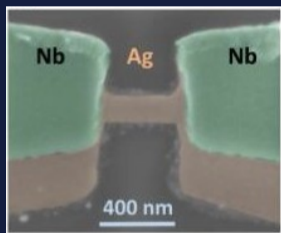
Superconducting contact



Basset *et al.*, Phys. Rev. Research 1, 032009(R) (2019)

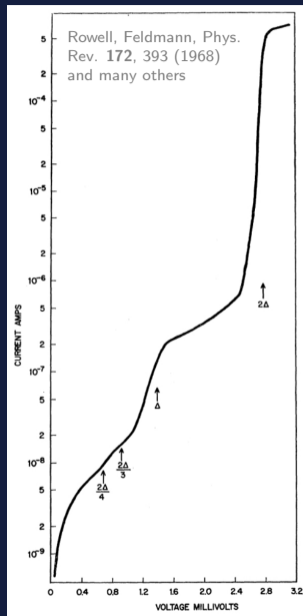
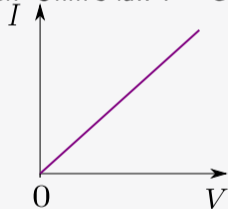


Superconducting contact

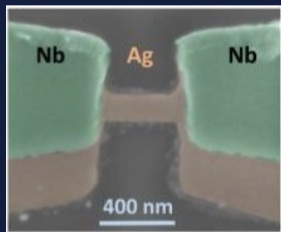


Basset *et al.*, Phys. Rev. Research 1, 032009(R) (2019)

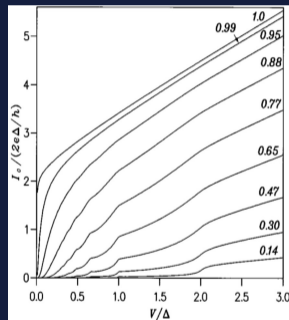
Cf. Ohm's law $I = GV$



Superconducting contact

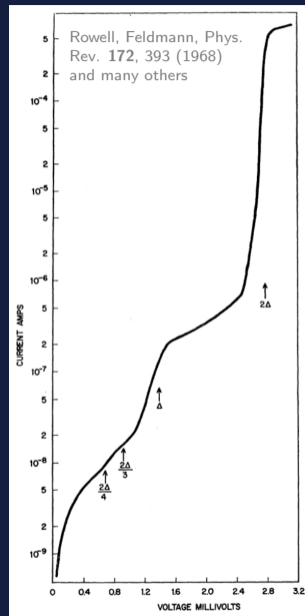


Basset *et al.*, Phys. Rev. Research **1**, 032009(R) (2019)

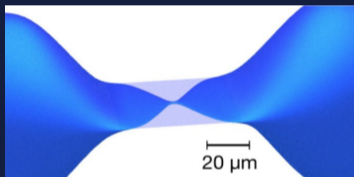


Cuevas *et al.*, Phys. Rev. B **54**, 7366 (1996)

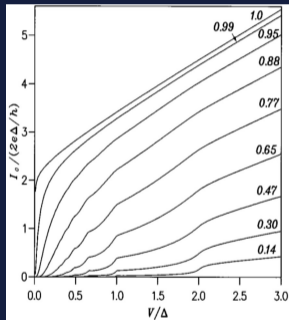
- Klapwijk, Blonder Tinkham, Physica **109**, 1657 (1982)
Blonder, Tinkham, Klapwijk, Phys. Rev. B **25**, 4515 (1982)
Averin, Bardas, Phys. Rev. Lett. **75**, 1831 (1995)



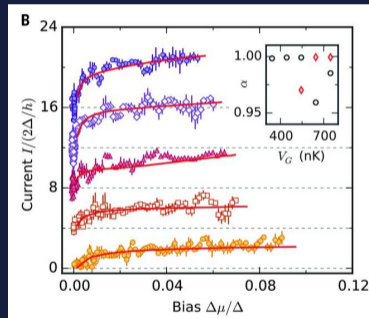
Connected superfluids



modified from Krinner et al., PNAS 113, 8144 (2016)

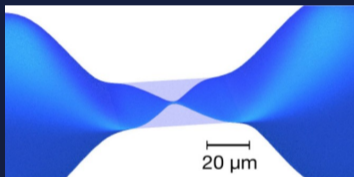


Cuevas et al., Phys. Rev. B 54, 7366 (1996)

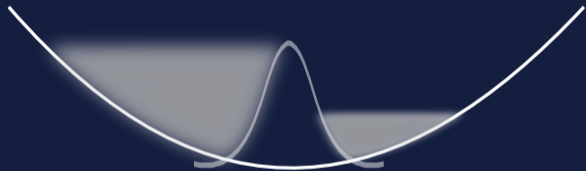


Husmann et al., Science 18, 1498 (2015)

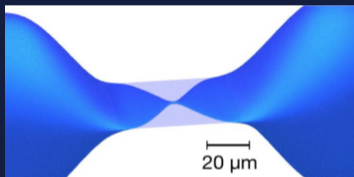
Transport with cold atoms



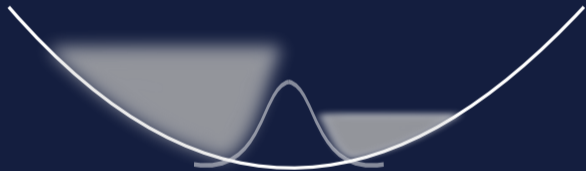
modified from Krinner et al., PNAS 113, 8144
(2016)



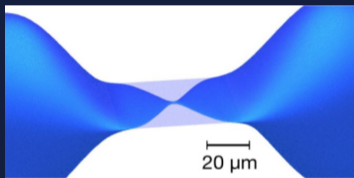
Transport with cold atoms



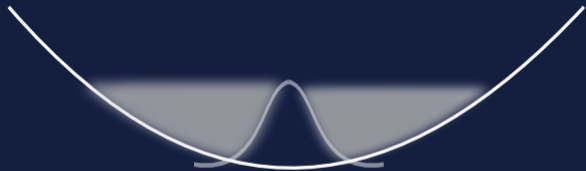
modified from Krinner et al., PNAS 113, 8144
(2016)



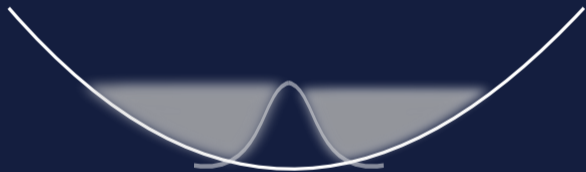
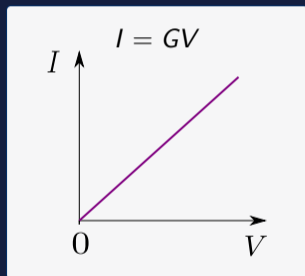
Transport with cold atoms



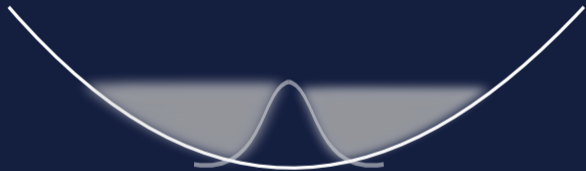
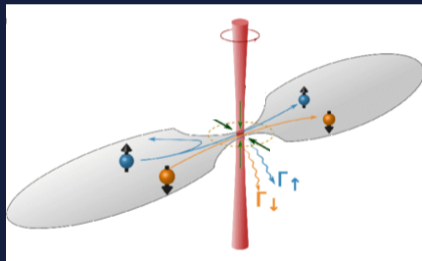
modified from Krinner et al., PNAS 113, 8144
(2016)



Transport of noninteracting fermions

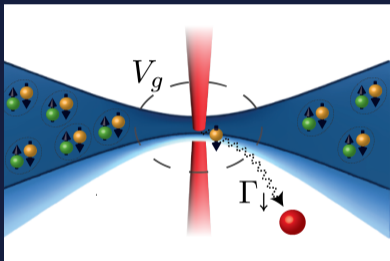


Transport of noninteracting fermions in the presence of dissipation



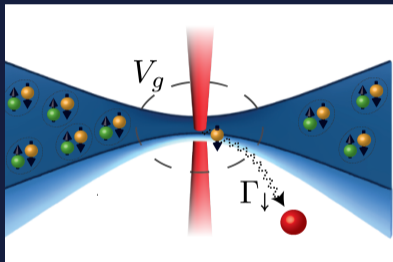
Corman *et al.*, Phys. Rev. A 100, 053605 (2019)

Superfluid transport in the presence of dissipation?

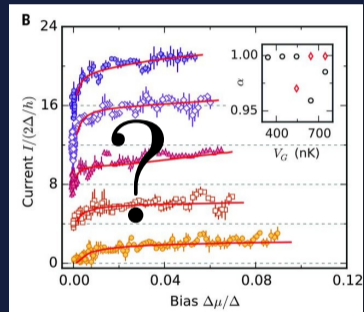
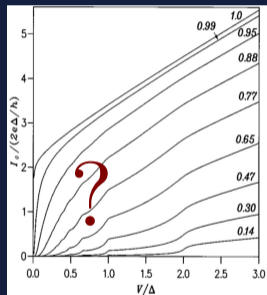


M.-Z. Huang, et al., arXiv:2210.03371

Superfluid transport in the presence of dissipation?



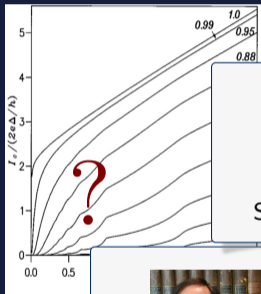
M.-Z. Huang, et al., arXiv:2210.03371



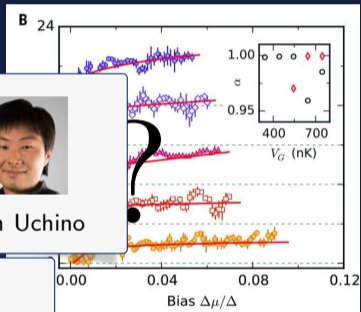
Superfluid transport in the presence of dissipation?



Lithium team, ETH

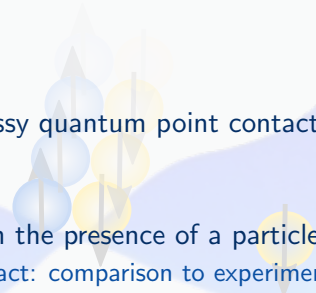


Shun Uchino

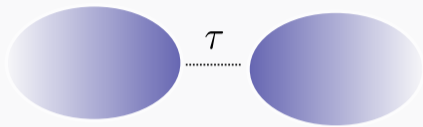


Thierry Giamarchi

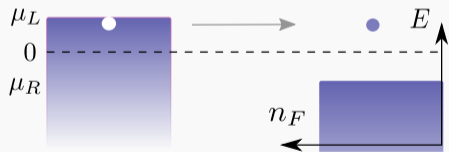
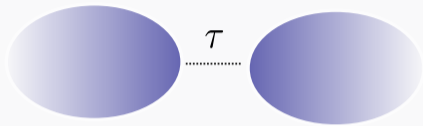
Outline

- 1 Introduction
 - 2 Theoretical description of the lossy quantum point contact
 - ▶ Multiple Andreev reflections
 - ▶ Local particle loss
 - 3 Current-voltage characteristics in the presence of a particle loss
 - ▶ High transparency of the contact: comparison to experiment
 - ▶ Low transparency
- 
- A decorative background graphic showing a quantum point contact (QPC) structure. It features a central constriction in a light blue channel. Several blue and yellow spheres, representing particles, are positioned within the constriction. Grey arrows indicate the direction of particle flow: some point upwards, some downwards, and some are reflected back, illustrating Andreev reflections and particle loss.

Quantum transport: tunneling Hamiltonian

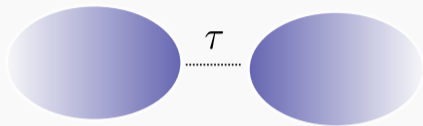


Quantum transport: tunneling Hamiltonian



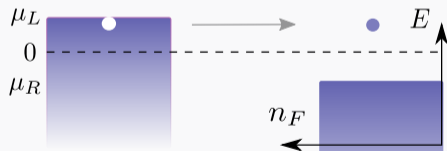
$$n_F(E - \mu) = \frac{1}{e^{\frac{E - \mu}{k_B T}} + 1}$$

Quantum transport: tunneling Hamiltonian

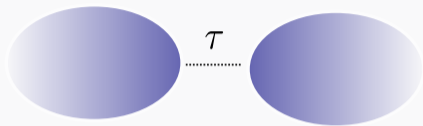


current

$$I = \frac{1}{h} \int_{-\infty}^{\infty} dE T(E) [n_F(E - \mu_L) - n_F(E - \mu_R)]$$



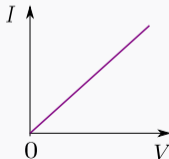
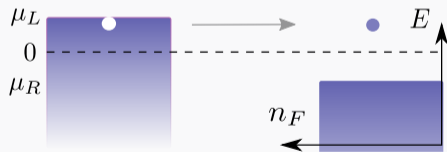
Quantum transport: tunneling Hamiltonian



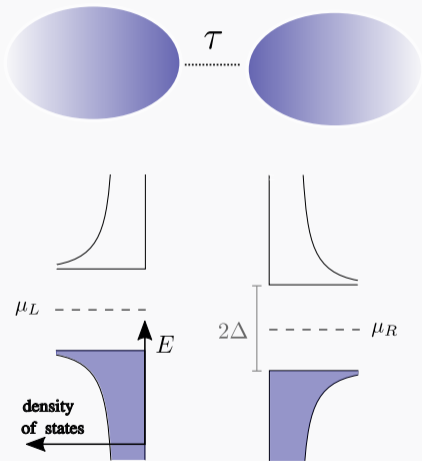
current

$$I = \frac{1}{h} \int_{-\infty}^{\infty} dE T(E) [n_F(E - \mu_L) - n_F(E - \mu_R)]$$
$$= G(\mu_L - \mu_R) = GV$$

G : conductance
 V : voltage



Connected superfluids – tunneling Hamiltonian

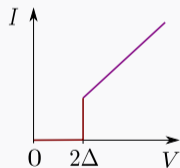
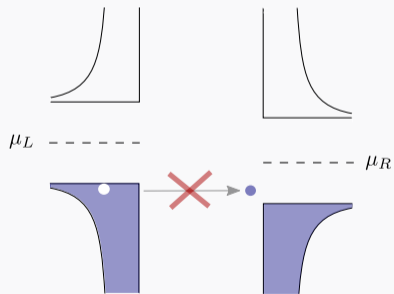
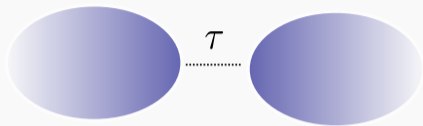


$$H = \sum_{i=L,R} H_i + H_{\text{tun}},$$

$$H_i = \sum_k \begin{pmatrix} \psi_{i\uparrow k}^\dagger & \psi_{i\downarrow -k} \end{pmatrix} \begin{pmatrix} \epsilon_k - \mu_i & \Delta \\ \Delta & -(\epsilon_{-k} - \mu_i) \end{pmatrix} \begin{pmatrix} \psi_{i\uparrow k} \\ \psi_{i\downarrow -k}^\dagger \end{pmatrix}$$

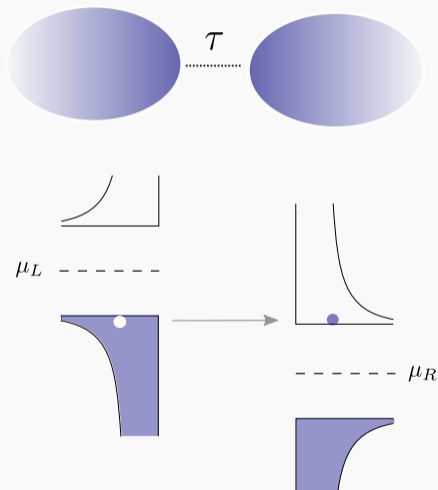
$$H_{\text{tun}} = -\tau \sum_{\sigma=\uparrow,\downarrow} [\psi_{R\sigma}^\dagger(\mathbf{r}=\mathbf{0})\psi_{L\sigma}(\mathbf{r}=\mathbf{0}) + \text{H.c.}]$$

Single-particle tunneling



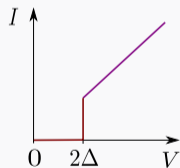
first-order tunneling, $V = \mu_L - \mu_R$

Single-particle tunneling



$$I \propto \int_{-\infty}^{\infty} dE \rho(E - \mu_L) \rho(E - \mu_R) \times [n_F(E - \mu_L) - n_F(E - \mu_R)]$$

$\rho(E)$: density of states

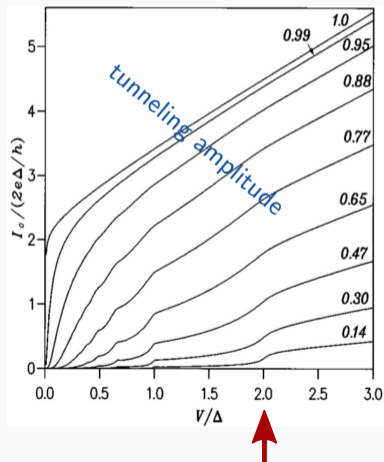
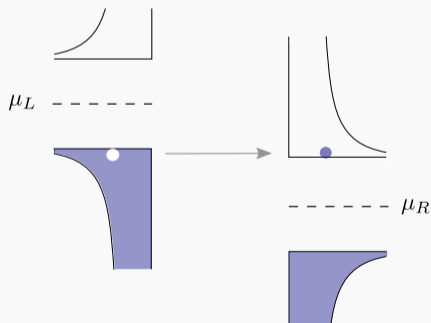


first-order tunneling, $V = \mu_L - \mu_R$

Blonder, Tinkham, Klapwijk, Phys. Rev. B 25, 4515 (1982)

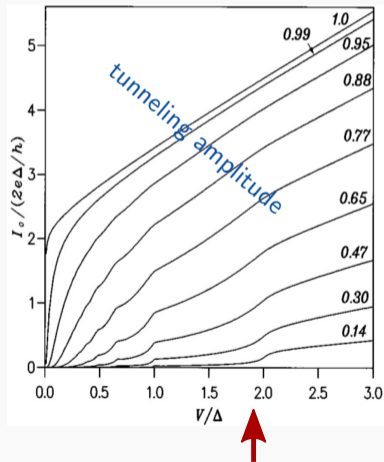
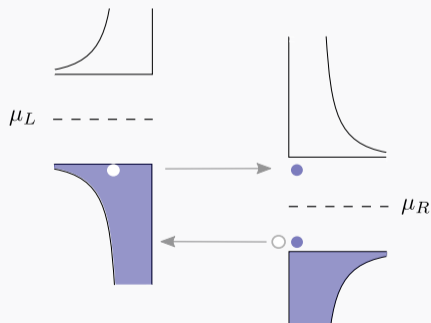
Sub-gap currents

- ▶ Multiple Andreev reflections lead to a nonzero current at $V < 2\Delta$.



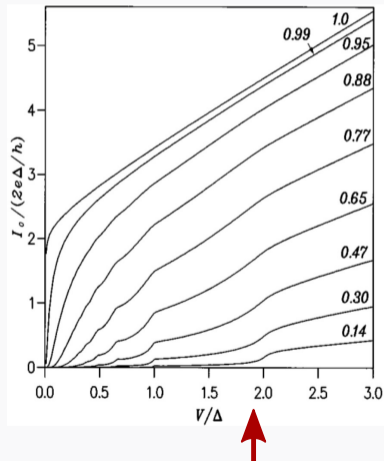
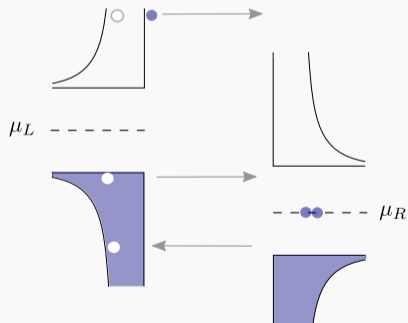
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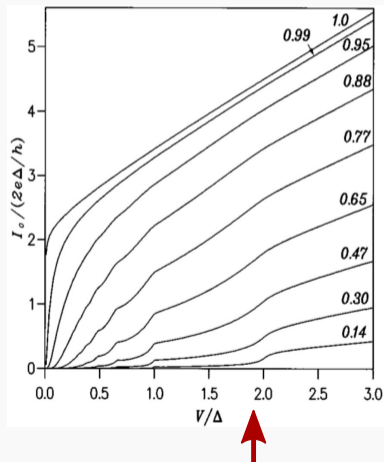
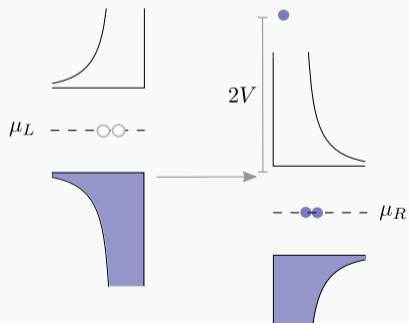
Sub-gap currents

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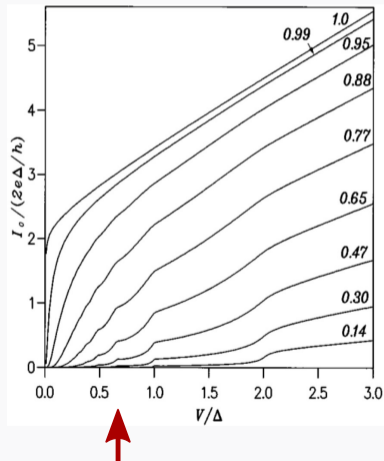
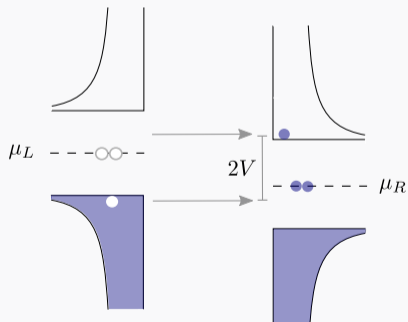
Sub-gap currents

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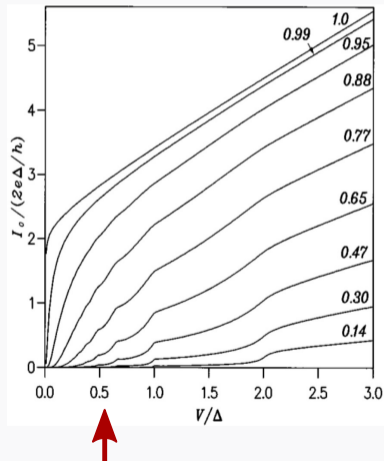
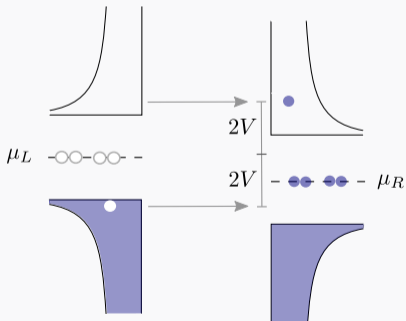
Sub-gap currents

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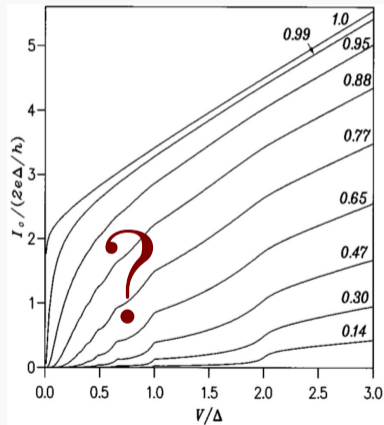
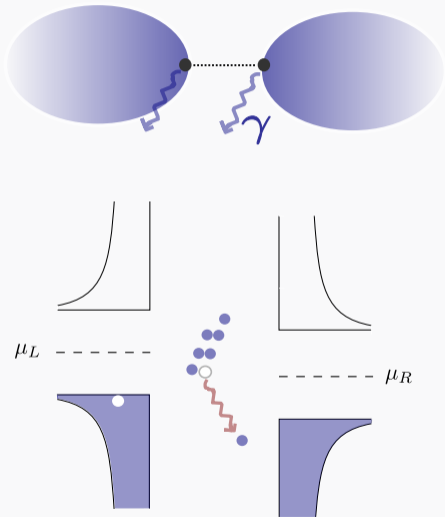


Sub-gap currents

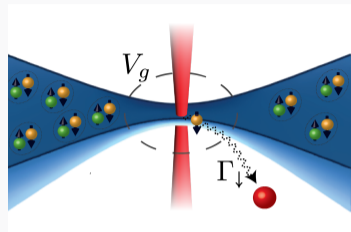
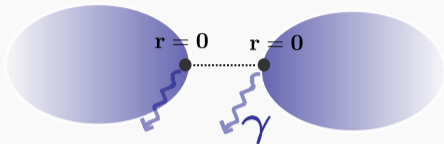
- ▶ Smaller voltage \rightarrow more pairs ($n \sim \frac{2\Delta}{2V}$) required for the single quasiparticle to tunnel.
- ▶ Current proportional to τ^{2n} .



Particle loss?



Particle loss at the “contacts”



M.-Z. Huang et al., arXiv:2210.03371

$$\frac{d\rho}{dt} = -i[H, \rho] + \sum_{\sigma=\uparrow,\downarrow} \sum_{i=L,R} \gamma_{\sigma} \left[\psi_{i\sigma}(0) \rho \psi_{i\sigma}^{\dagger}(0) - \frac{1}{2} \left\{ \psi_{i\sigma}^{\dagger}(0) \psi_{i\sigma}(0), \rho \right\} \right]$$

- ▶ Conserved current $I = i\tau \sum_{\sigma=\uparrow,\downarrow} \left(\langle \psi_{R\sigma}^{\dagger}(0) \psi_{L\sigma}(0) \rangle - \langle \psi_{L\sigma}^{\dagger}(0) \psi_{R\sigma}(0) \rangle \right)$
- ▶ Nonequilibrium correlation functions \rightarrow Keldysh formalism

Particle loss at the “contacts”

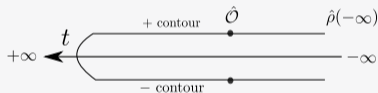
Nonequilibrium - Keldysh formalism

- ▶ Expectation values calculated as path integrals along a closed time contour,

$$\langle \psi_a \bar{\psi}_b \rangle = \int \mathcal{D}[\psi, \bar{\psi}] \psi_a \bar{\psi}_b e^{iS[\psi, \bar{\psi}]} = iG_{ab},$$

where the action is written in matrix form as

$$S[\bar{\psi}, \psi] = \int_{-\infty}^{\infty} dt \bar{\psi}(t) G^{-1}(t) \psi(t).$$

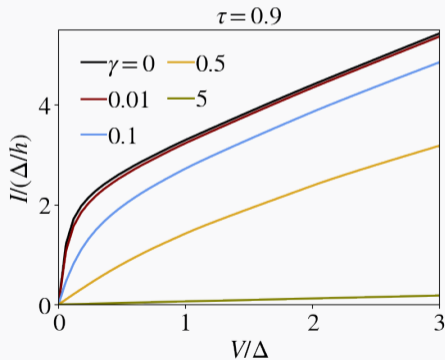


Here, $\psi = (\psi^+, \psi^-)$: two copies of the fields for each point in time.

- ▶ The action is the sum $S = S_L + S_R + S_{\text{tun}} + S_{\text{loss}}$.

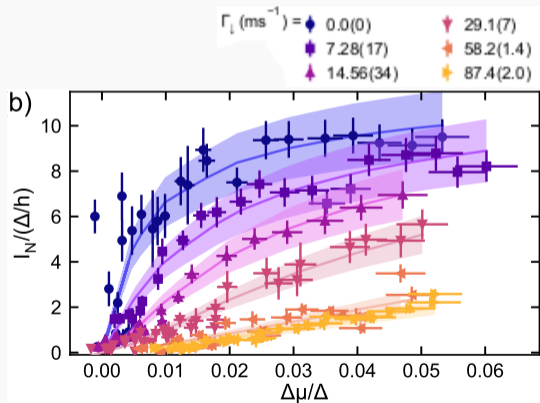
High transparency

- ▶ Current is reduced by the particle loss but not sharply suppressed at $V < 2\Delta$.



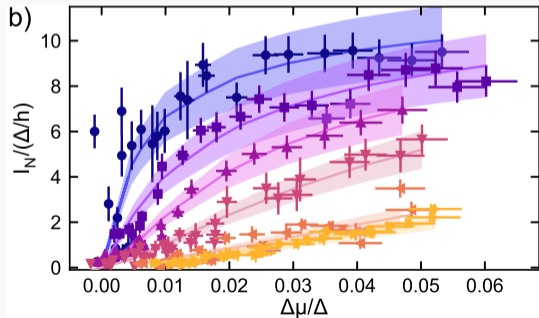
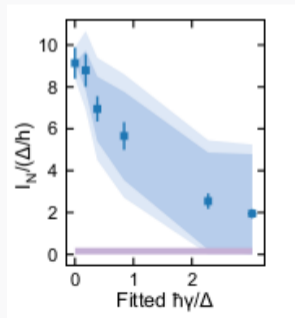
High transparency: compare to experimental data

- ▶ Current is reduced by the particle loss but not sharply suppressed at $V < 2\Delta$.
 - ▶ Results for $\tau \approx 1$ supported by experimental data.

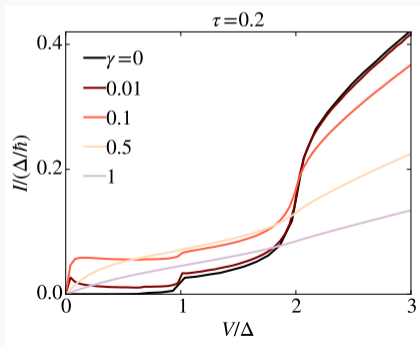


High transparency: compare to experimental data

- ▶ Current is reduced by the particle loss but not sharply suppressed at $V < 2\Delta$.
 - ▶ Results for $\tau \approx 1$ supported by experimental data.
- ▶ Superfluid transport “survives” up to large dissipation strengths $\gamma \gtrsim \Delta$.

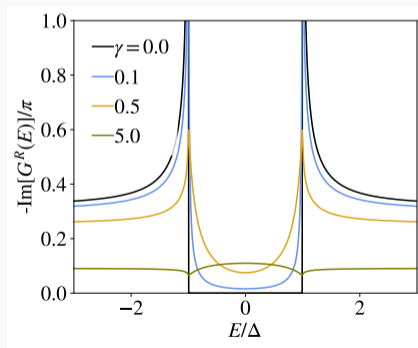
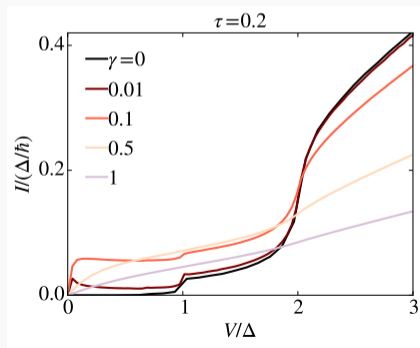


Low transparency: current enhanced at small voltage



Low transparency: current enhanced at small voltage

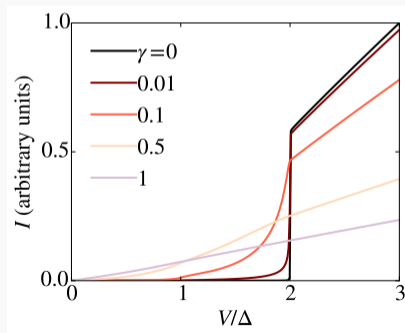
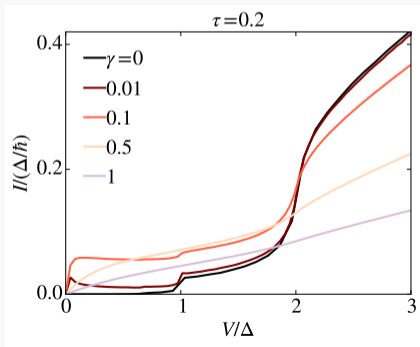
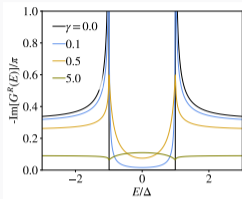
- ▶ Modified local density of states leads to an enhancement?



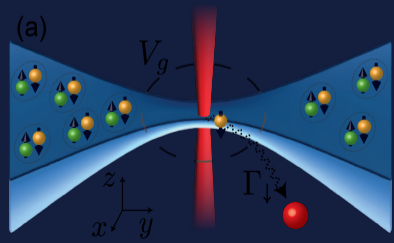
Low transparency: current enhanced at small voltage

- ▶ Modified local density of states leads to an enhancement?
- ▶ Weak-tunneling approximation

$$I \propto \int_{-\infty}^{\infty} dE \rho(E - \mu_L) \rho(E - \mu_R) [n_F(E - \mu_L) - n_F(E - \mu_R)].$$



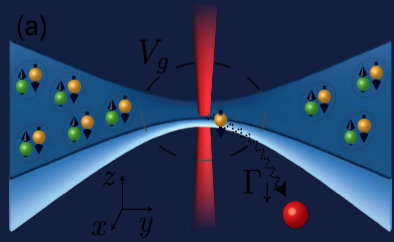
Summary



Superfluid transport due to multiple Andreev reflections is surprisingly robust to local particle losses.

M.-Z. Huang, J. Mohan, A.-M. Visuri, P. Fabritius, M. Talebi, S. Wili, S. Uchino, T. Giamarchi, T. Esslinger, arXiv:2210.03371

Summary



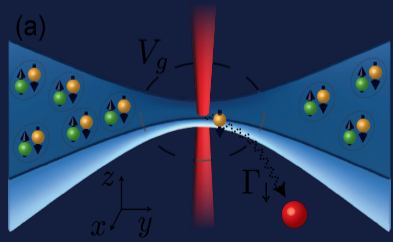
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Current is enhanced by dissipation at small voltages.

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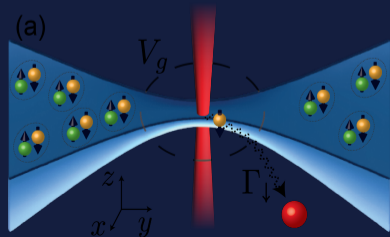
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Summary and outlook

Spin bias in superfluid reservoirs, pair loss, dephasing...



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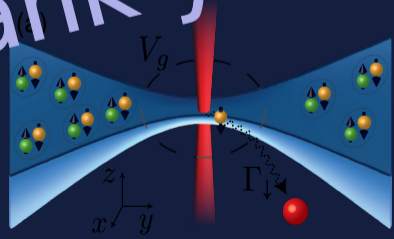
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Summary
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Thank you!

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Fermions with spin

- ▶ Action for the reservoirs $i = L, R$ in ω basis:

$$S = \int \frac{d\omega}{2\pi} \bar{\Psi}(\omega) G^{-1}(\omega) \Psi(\omega),$$

where $\Psi = (\psi_{i\uparrow}^1 \bar{\psi}_{i\downarrow}^1 \psi_{i\uparrow}^2 \bar{\psi}_{i\downarrow}^2)^T$.

- ▶ The inverse Green's function G^{-1} has the structure

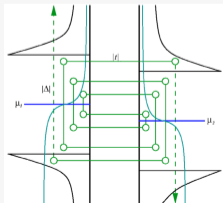
$$G^{-1} = \begin{pmatrix} 0 & [g^A]^{-1} \\ [g^R]^{-1} & [g^K]^{-1} \end{pmatrix},$$

with the elements

$$[g^{R,A}]^{-1} = \begin{pmatrix} \uparrow\uparrow & \uparrow\downarrow \\ \downarrow\uparrow & \downarrow\downarrow \end{pmatrix}.$$

- ▶ Multiple Andreev reflections described by infinite-size matrix

$$G^{-1} = \begin{pmatrix} \Omega_{L\uparrow} & \mathcal{T} & \Delta_L & 0 & 0 & \dots \\ \mathcal{T} & \Omega_{R\uparrow} & 0 & 0 & \Delta_R & \\ \Delta_L & 0 & \Omega_{L\downarrow} & -\mathcal{T} & 0 & \\ 0 & 0 & -\mathcal{T} & \Omega_{R\downarrow} & 0 & 0 \\ 0 & \Delta_R & 0 & 0 & \Omega_{R\downarrow} & -\mathcal{T} \\ \vdots & & & 0 & -\mathcal{T} & \ddots \end{pmatrix}$$



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which can be truncated to obtain

$$\langle \psi_a \bar{\psi}_b \rangle = \int \mathcal{D}[\psi, \bar{\psi}] \psi_a \bar{\psi}_b e^{iS[\psi, \bar{\psi}]} = iG_{ab}.$$

Fermions with spin

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with elements

$$[g^{R,A}]^{-1} = \begin{pmatrix} \frac{(\bar{\omega} \pm i\eta)}{W\sqrt{\Delta^2 - (\bar{\omega} \pm i\eta)^2}} \pm \frac{i\gamma_{\uparrow}}{2} & \frac{\Delta}{W\sqrt{\Delta^2 - (\bar{\omega} \pm i\eta)^2}} \\ \frac{\Delta}{W\sqrt{\Delta^2 - (\bar{\omega} \pm i\eta)^2}} & \frac{(\bar{\omega} \pm i\eta)}{W\sqrt{\Delta^2 - (\bar{\omega} \pm i\eta)^2}} \pm \frac{i\gamma_{\downarrow}}{2} \end{pmatrix},$$

$$[g^K(\bar{\omega})]_{11}^{-1} = -([g^A]_{11}^{-1} - [g^R]_{11}^{-1}) [1 - 2n_F(\bar{\omega})] + i\gamma_{\uparrow}$$

$$[g^K(\bar{\omega})]_{22}^{-1} = -([g^A]_{22}^{-1} - [g^R]_{22}^{-1}) [1 - 2n_F(\bar{\omega})] - i\gamma_{\downarrow}$$

$$[g^K(\bar{\omega})]_{12}^{-1} = -([g^A]_{12}^{-1} - [g^R]_{12}^{-1}) [1 - 2n_F(\bar{\omega})]$$

$$[g^K(\bar{\omega})]_{21}^{-1} = -([g^A]_{21}^{-1} - [g^R]_{21}^{-1}) [1 - 2n_F(\bar{\omega})].$$