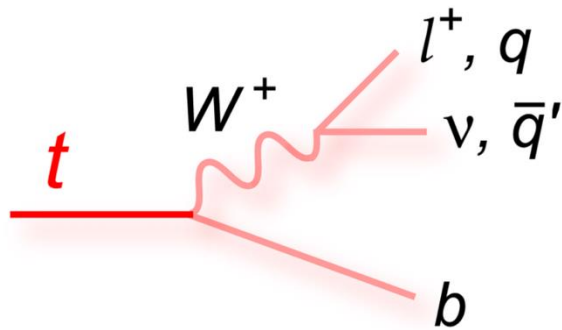
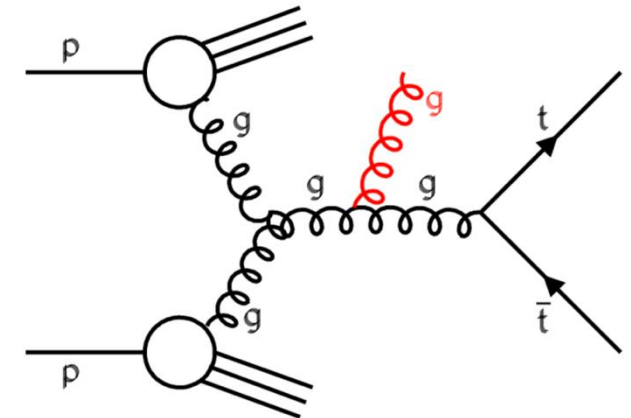


Challenges in Modelling $pp \rightarrow tt + X$ @ NLO



MALGORZATA WOREK



OUTLINE OF THE TALK

1. Introduction
2. Part I – Fixed-order predictions: full off-shell NLO QCD predictions
3. Part II – Fixed-order predictions: Complete NLO predictions
4. Part III – Parton-shower based predictions: NLO + PS predictions
5. Summary
6. Open Questions

INTRODUCTION

LARGE HADRON COLLIDER

- Current status: LHC RUN 3 @ 13.6 TeV
- HL-LHC planned from 2030 to 2041

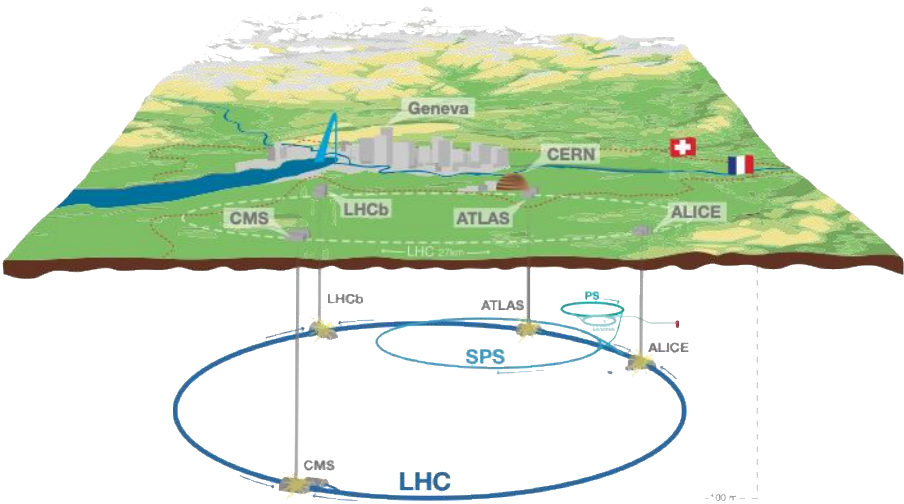
Integrated Luminosity $\mathcal{L}_{\text{int}} = \int_0^T \mathcal{L}(t') dt'$

Run 1	Run 2	Run 3	HL-LHC
30 fb ⁻¹	190 fb ⁻¹	500 fb ⁻¹	3000 - 4000 fb ⁻¹

$\mathcal{L}_{\text{int}} \cdot \sigma_p = \text{number of events of interest}$



Overall view of the LHC



OPEN-PHO-CHART-2014-006

KEY PHYSICS GOALS

- A. Understand Standard Model better, not only what particles we have, but also how they interact with each other
- B. Establish structure of Higgs boson sector
- C. Search for signs of new physics BSM

The core physics topics at the LHC (colour-coded by directly-probed energy scales)



- **DIRECT SEARCHES**

- Many proposals for New Physics
- No model of NP really stands out
- No obvious candidates to look for

- **INDIRECT SEARCHES**

- New Physics as small corrections to SM reactions

- **PRECISION SM MEASUREMENTS**

- High Luminosity LHC

- **HIGH PRECISION THEORETICAL PREDICTIONS**

- Top Quark & Higgs boson

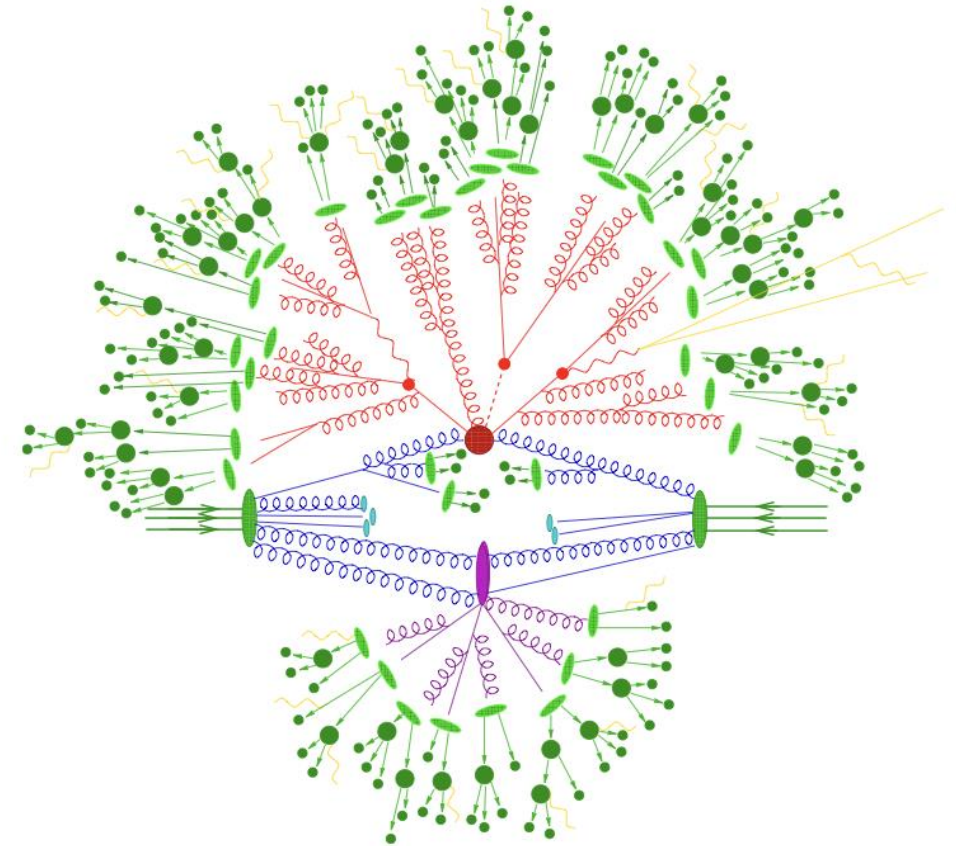
COMPLEMENTARY

KEY PHYSICS GOALS

- *A synergy between theory & experiment is key to foster discoveries at the HL-LHC*
- *Shed more light on Higgs-boson sector*
- *Carefully examine top-quark sector for deviations from SM*
- On theory side, path to precision runs through several directions:
 - *Perturbative accuracy of amplitude calculations*
 - *Numerical stability of integration & subtraction of IR divergencies*
 - *Robust assessment of theoretical uncertainties*
 - *Modelling realistic final states in fiducial phase-space regions*
 - *Modelling resonant particles*
 - *Parton shower effects*
 - *Non perturbative aspects*
- **PRECISION & ACCURACY** → Determine which effects are important & have to be included

Pictorial representation of a $pp \rightarrow ttH$ event as produced by an event generator

SHERPA, JHEP 02 (2009) 007



$$\sigma_X = \sum_{a,b} \int_0^1 dx_1 dx_2 f_a(x_1, \mu_F^2) f_b(x_2, \mu_F^2) \times \hat{\sigma}_{ab \rightarrow X}(x_1, x_2, \alpha_S(\mu_R^2), \frac{Q^2}{\mu_F^2}, \frac{Q^2}{\mu_R^2})$$

THEORETICAL PREDICTIONS FOR $\tau\tau$ + DECAYS

di-lepton

- **NLO QCD** (full off-shell)

Bevilacqua, Czakon, van Hameren, Papadopoulos, Worek, JHEP 02 (2011) 083
Denner, Dittmaier, Kallweit, Pozzorini, Phys. Rev. Lett. 106 (2011) 052001
Denner, Dittmaier, Kallweit, Pozzorini, JHEP 1210 (2012) 110
Heinrich, Maier, Nisius, Schlenk, Winter, JHEP 06 (2014) 158
Frederix, Phys. Rev. Lett. 112 (2014) 8, 082002

- **NLO EW**

Denner, Pellen, JHEP 08 (2016) 155

- **NNLO QCD** (NWA)

Behring, Czakon, Mitov, Papanastasiou, Poncelet, Phys. Rev. Lett. 123, (2019) 082001
Czakon, Mitov, Poncelet, JHEP 05 (2021) 212

- **NNLO QCD** (DPA)

Buonocore, Grazzini, Kallweit, Lindert, Savoini, JHEP 10 (2025) 195

lepton + jet

- **NLO QCD** (full off-shell)

Denner, Pellen, JHEP 02 (2018) 013

- **Complete NLO** → First complete calculation with NLO QCD & EW corrections including all Born-level channels & all initial & final states & all off-shell effects

Mans, Stremmer, Worek, e-Print: 2512.18391 [hep-ph]

NNLO QCD (NNLO + PS $\Rightarrow$ MINNLO)

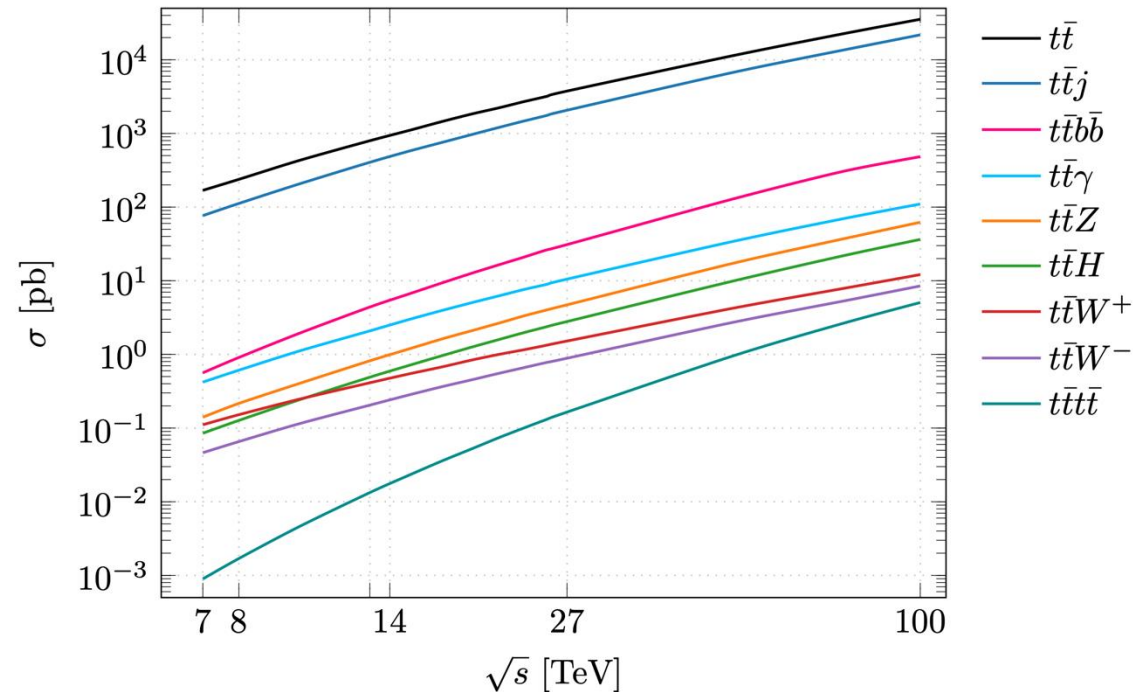
Mazzitelli, Monni, Nason, Re, Wiesemann, Zanderighi, Phys. Rev. Lett. 127 (2021) 062001
Mazzitelli, Monni, Nason, Re, Wiesemann, Zanderighi, JHEP 04 (2022) 079

- Focus so far has been on *di-leptonic* channel → $l + j$ mode is now catching up

TOP-QUARK PAIR PRODUCTION +X @ LHC

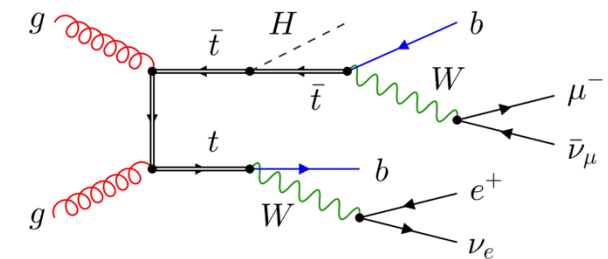
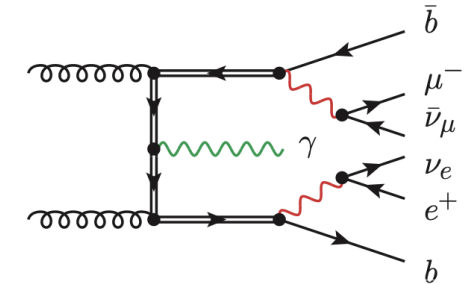
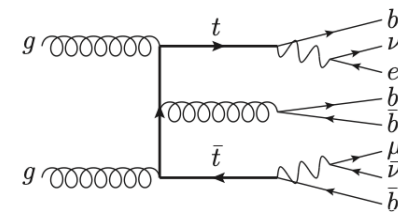
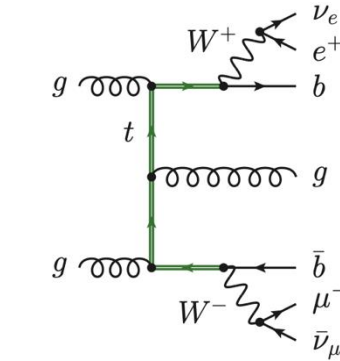
State of the art: NLO

- More exclusive final states are produced @ LHC



SNOWMASS 21, Report of Energy Frontier Topical Group 3, arXiv:2209.11267 [hep-ph]

- Only selected results for $pp \rightarrow t\bar{t} + X$ to illustrate some issues
- HELAC-NLO**: Results for all these processes & more:
 - $pp \rightarrow ttjj$, $pp \rightarrow tt\gamma\gamma$ & $pp \rightarrow ttWj$
- See also results by *Ansgar Denner & collaborators*



Main Focus:

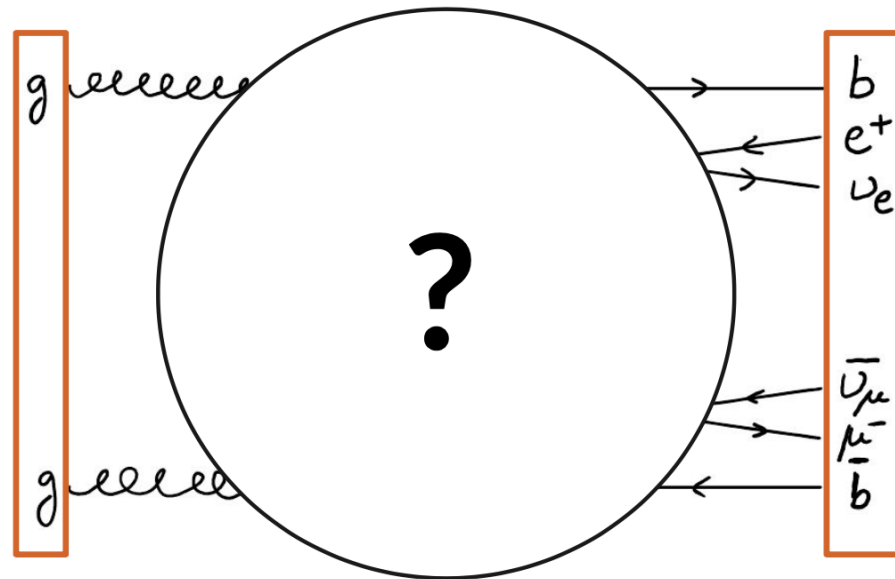
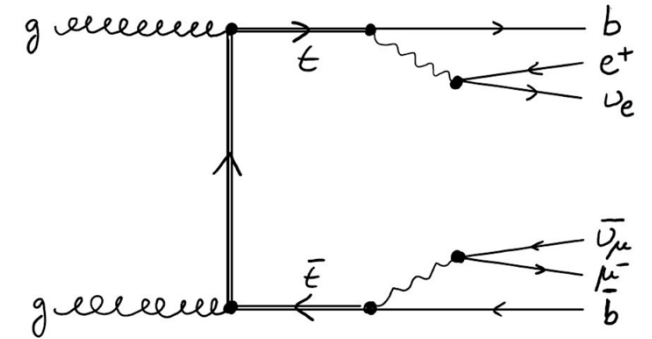
Precise & accurate modelling of realistic final states in fiducial phase-space regions

TT PRODUCTION WITH REALISTIC FINAL STATES

- Modelling of unstable particles

$$pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu \text{ at } \mathcal{O}(\alpha_s^2\alpha^4)$$

tt in di-lepton decay channel

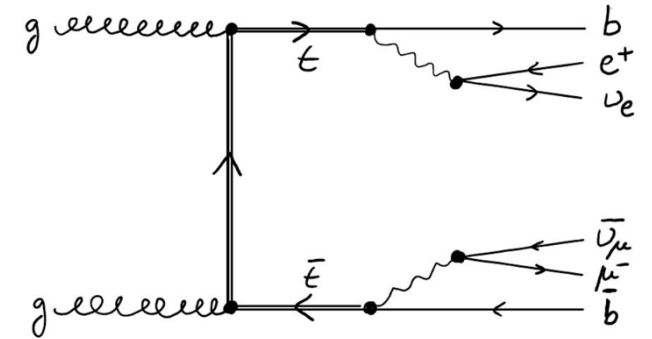


TT PRODUCTION WITH REALISTIC FINAL STATES

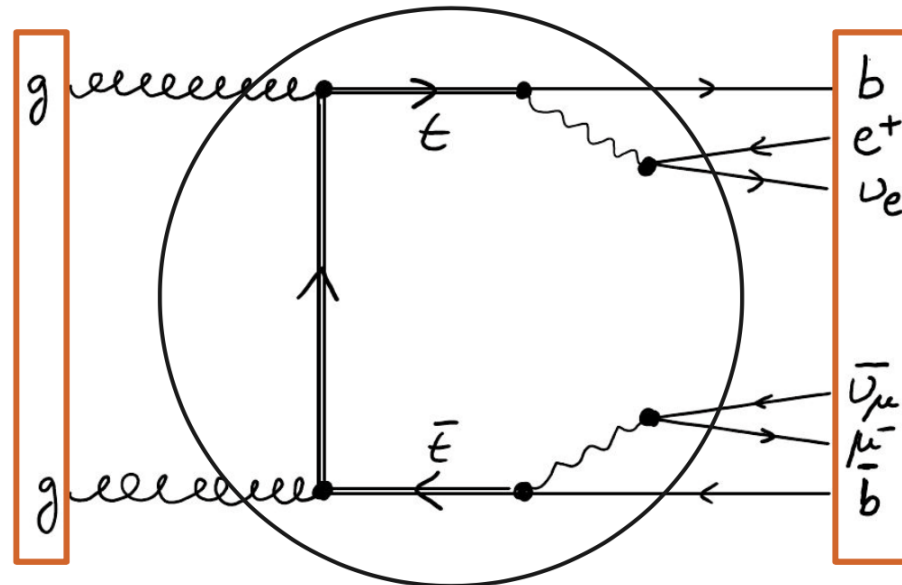
- Modelling of unstable particles

$$pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu \text{ at } \mathcal{O}(\alpha_s^2\alpha^4)$$

tt in di-lepton decay channel



Double-
resonant
diagram

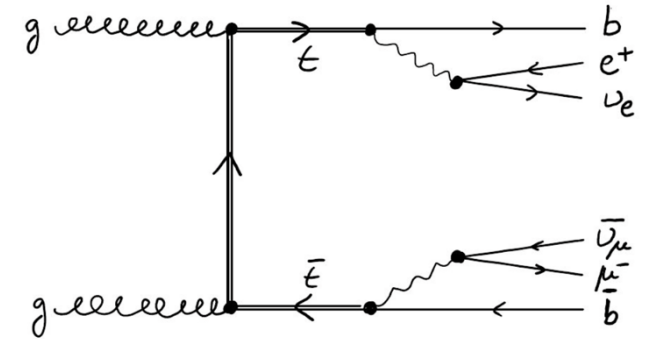


TT PRODUCTION WITH REALISTIC FINAL STATES

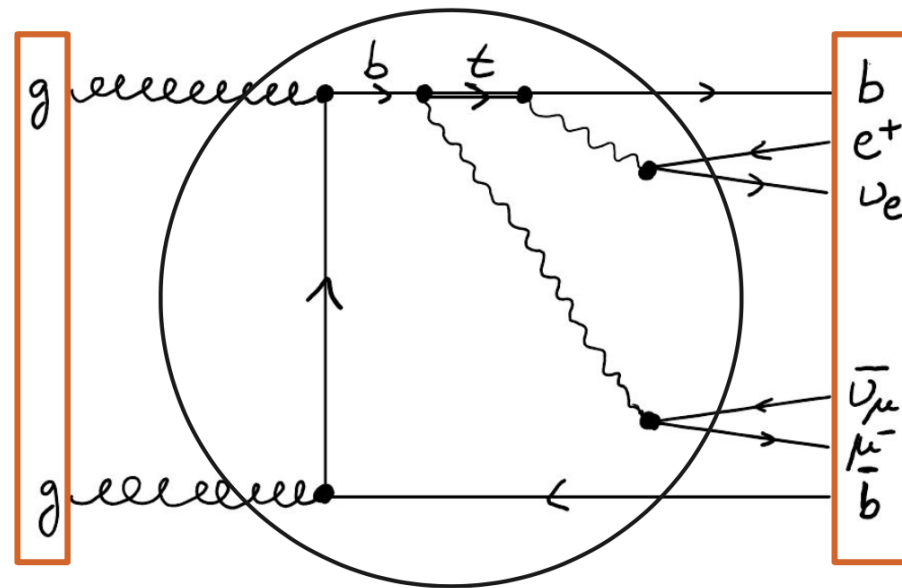
- Modelling of unstable particles

$$pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu \text{ at } \mathcal{O}(\alpha_s^2\alpha^4)$$

tt in di-lepton decay channel



Single-
resonant
diagram

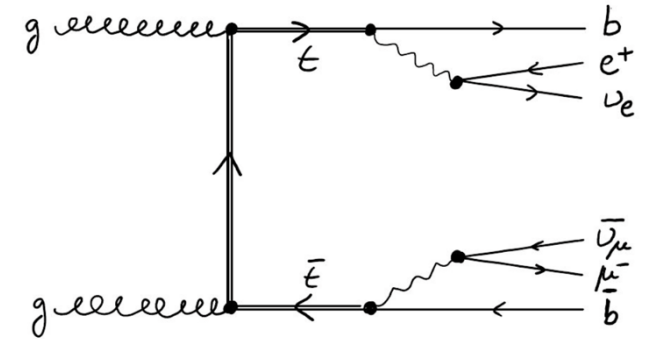


TT PRODUCTION WITH REALISTIC FINAL STATES

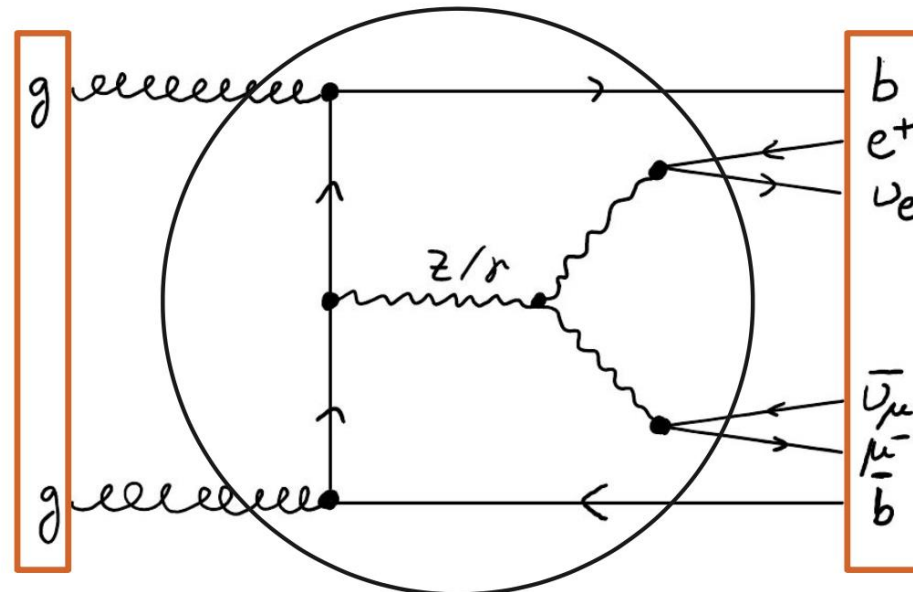
- Modelling of unstable particles

$$pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu \text{ at } \mathcal{O}(\alpha_s^2\alpha^4)$$

tt in di-lepton decay channel



Non-
resonant
diagram



TT PRODUCTION IN NWA

- Modelling of unstable particles

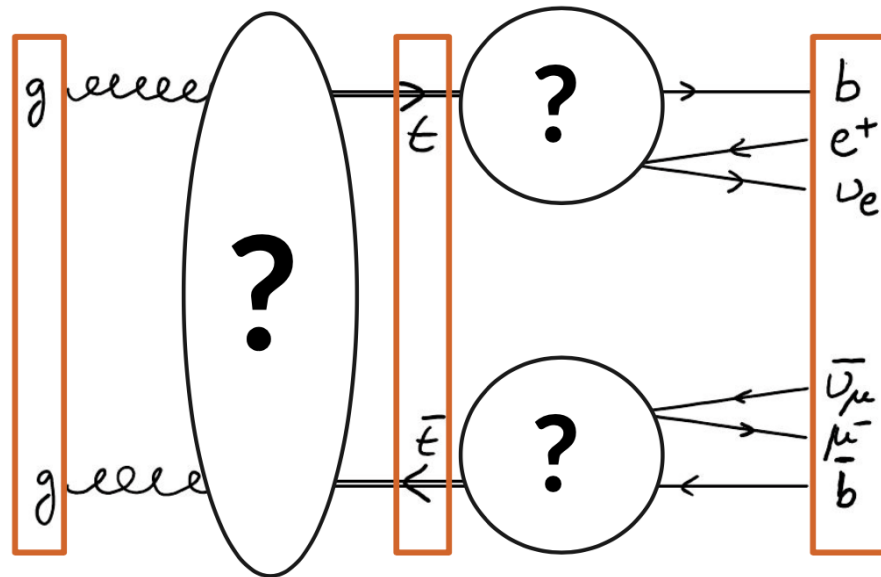
$$pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu \text{ at } \mathcal{O}(\alpha_s^2\alpha^4)$$

$$\frac{\Gamma_W}{m_W} > \frac{\Gamma_t}{m_t} \gg \frac{\Gamma_H}{m_H},$$

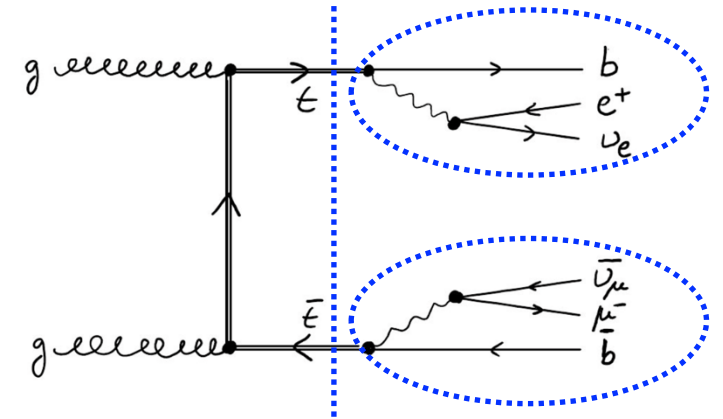
$$2.6\% > 0.8\% \gg 0.003\%.$$

Narrow-width approximation (NWA)
 → Fix intermediate state to be on-shell

$$\frac{\Gamma}{m} \rightarrow 0$$



tt in di-lepton decay channel



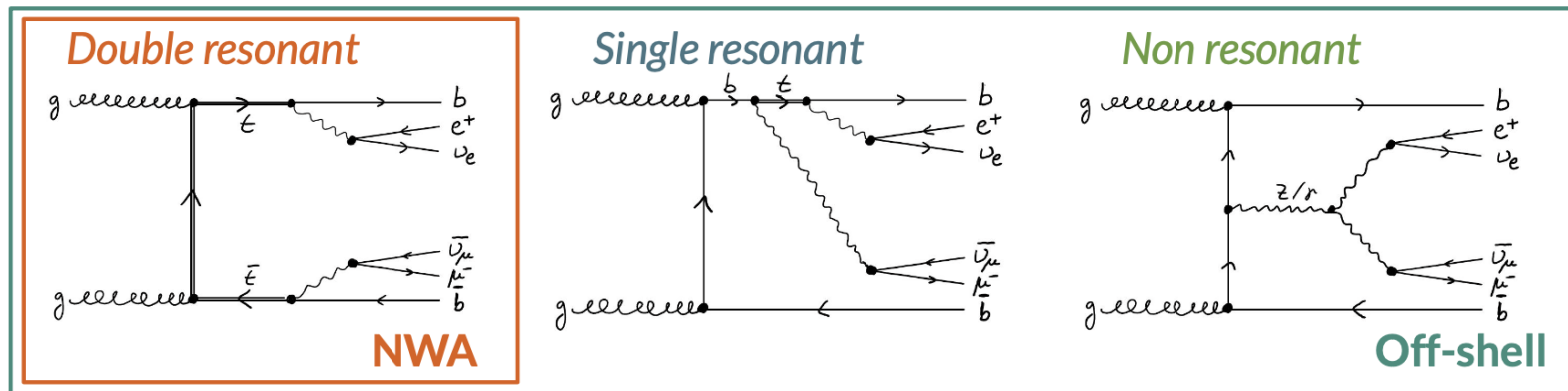
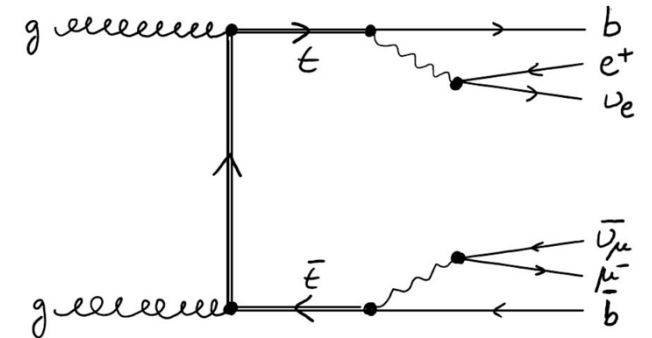
- NLO QCD correction separately to production & decays
- Nonfactorizable NLO corrections are missing
- No cross-talk between production & both decays
- NLO spin correlations

TT PRODUCTION

- Modelling of unstable particles

$$pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu \text{ at } \mathcal{O}(\alpha_s^2\alpha^4)$$

tt in di-lepton decay channel



- FULL OFF-SHELL** = **DR** + **SR** + **NR** + interferences + Breit-Wigner propagators
- NWA** = **DR contributions** & unstable *t* & *W* restricted to on-shell states

TT PRODUCTION WITH PARTON SHOWERS

- NLO QCD corrections to stable $pp \rightarrow tt + X$ matched to parton-showers: POWHEG & MC@NLO
 - *NLO QCD for production only*
 - *Decays of top quarks included with LO spin correlations*
 - Double resonant contributions only
 - Single & non-resonant contributions still missing as well as their interference effects
 - ✓ Can be added tt & tW using DS or DR
 - Scale settings & theoretical uncertainties based on production stage only
- *Another approach for tt production is bb4l-dl generators*
 - Full off-shell predictions at NLO QCD in *di-lepton & l+j* channels matched to (semi-classical) PS using a resonance-aware matching

POWHEG-BOX + LO DECAYS

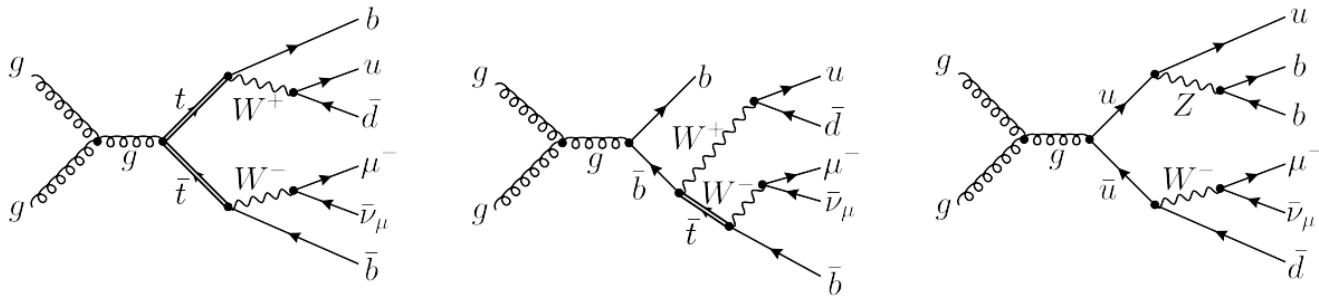
MG5_AMC@NLO + MADSPIN

- Collinear parton splitting or soft gluon emission
 - Dominant contributions resummed
- Connection to non-perturbative aspects
 - Hadronic final states
- Assess if parton showers can reproduce all contributions required at NLO QCD
- Identify regions of phase space & specific observables which are sensitive to parton shower effects

COMPLETE NLO CORRECTIONS

$$pp \rightarrow \ell^- \bar{\nu}_\ell j_b j_b jj + X$$

$$\alpha_s^2 \alpha^4$$

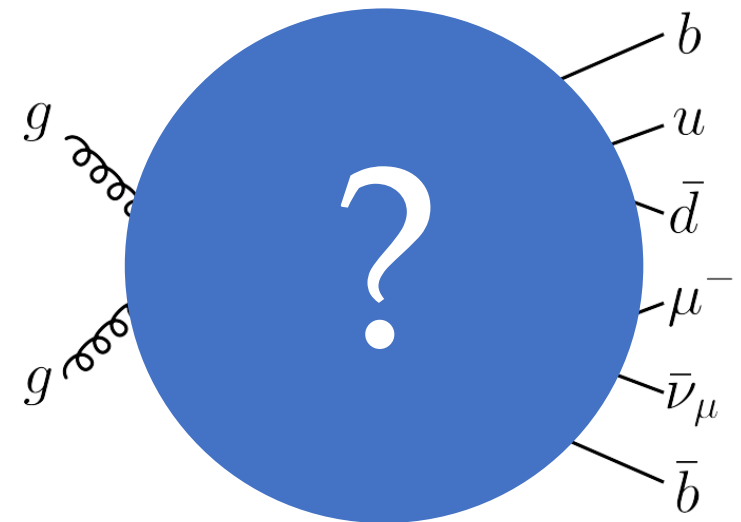
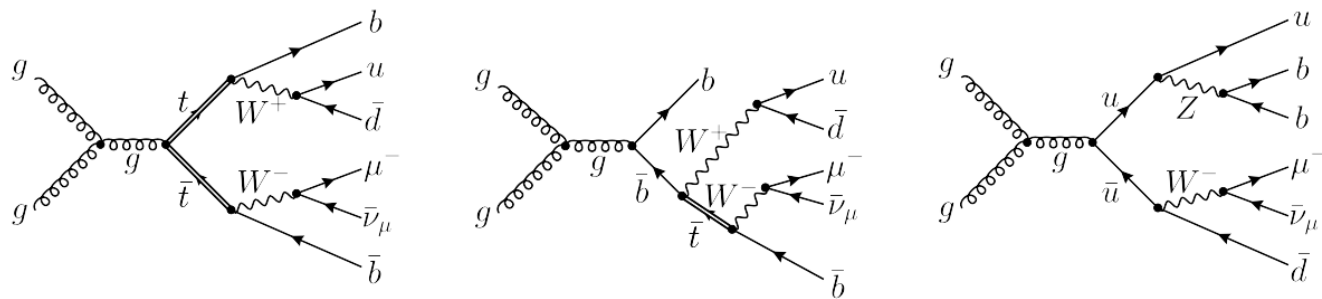


- Diagrams with two, one & no top-quark resonances contributing

COMPLETE NLO CORRECTIONS

$$pp \rightarrow \ell^- \bar{\nu}_\ell jjb\bar{b}jj + X$$

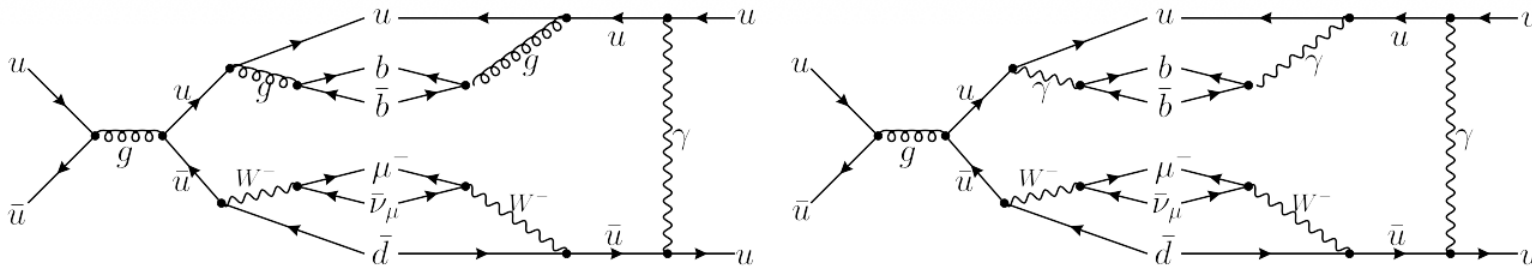
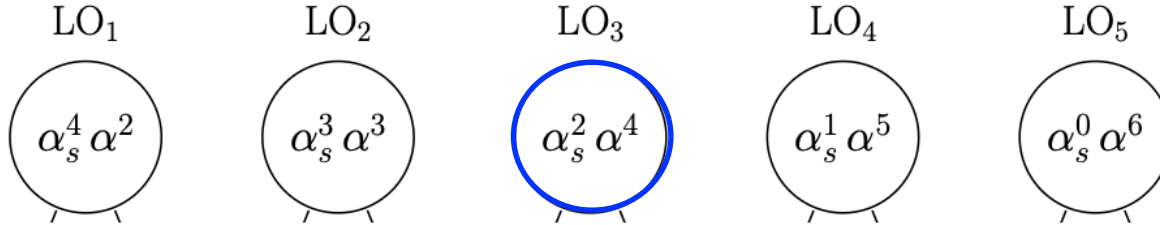
$$\alpha_s^2 \alpha^4$$



- Diagrams with two, one & no top-quark resonances contributing

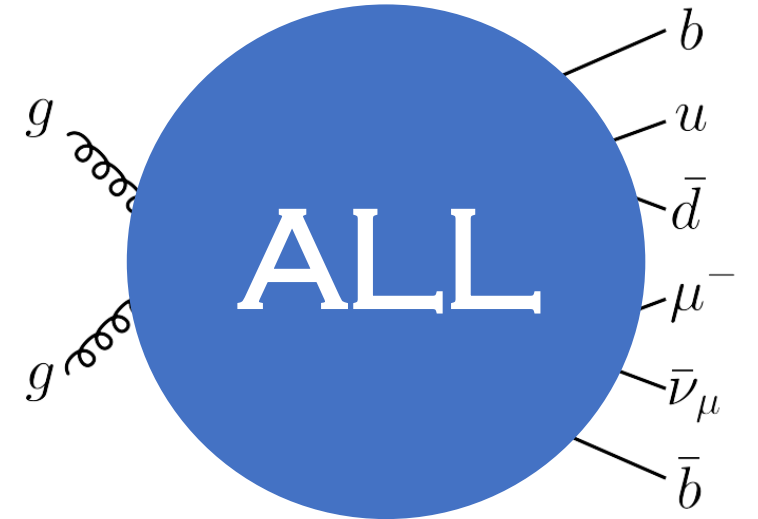
COMPLETE NLO CORRECTIONS

$$pp \rightarrow \ell^- \bar{\nu}_\ell j_b j_b jj + X$$



Feynman diagrams contributing at **LO₂** (left) and **LO₄** (right) via interference effects

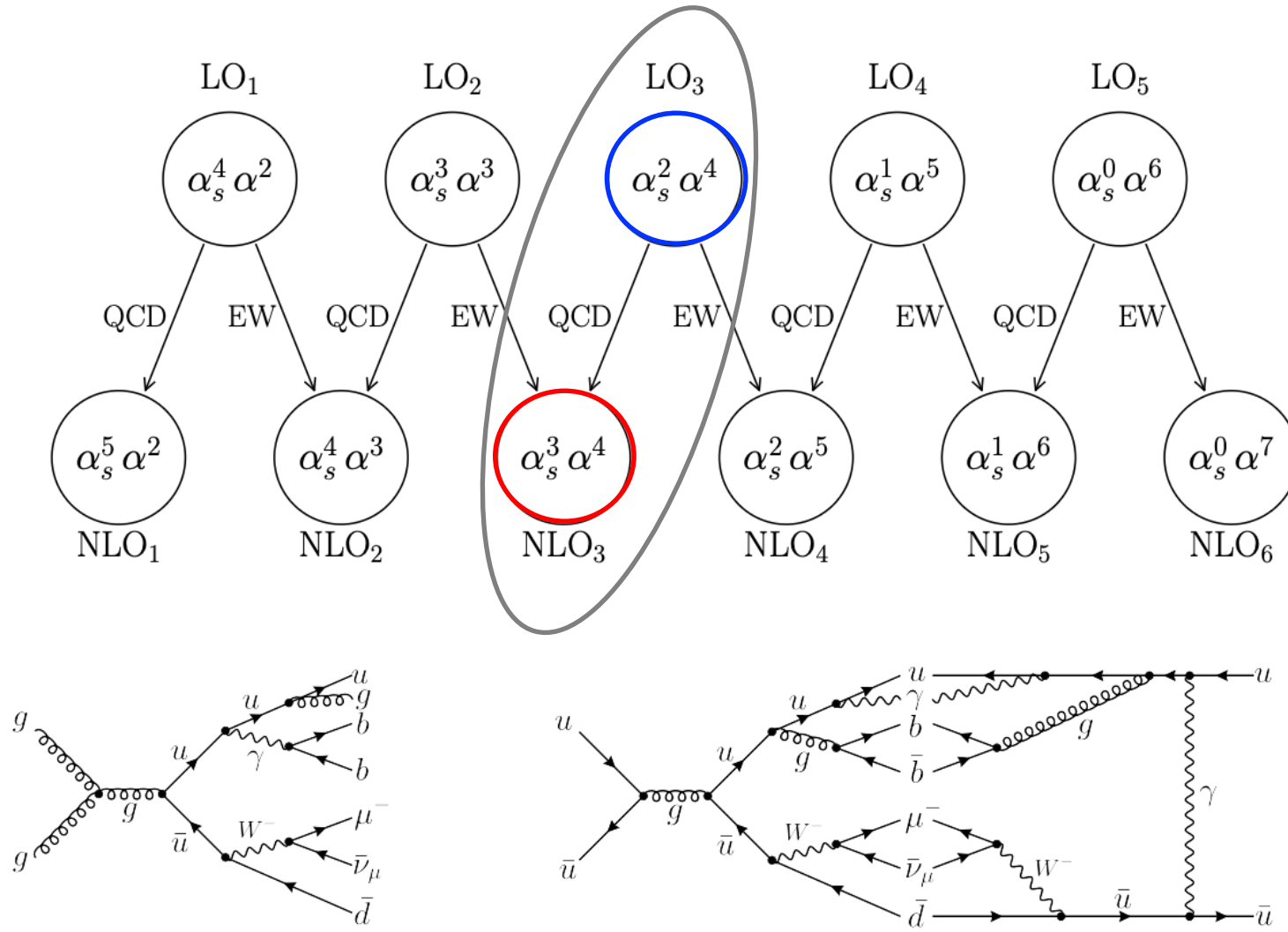
- **LEFT:** interference effects between **LO₁** & **LO₃**
- **RIGHT:** interference effects between **LO₃** & **LO₅**



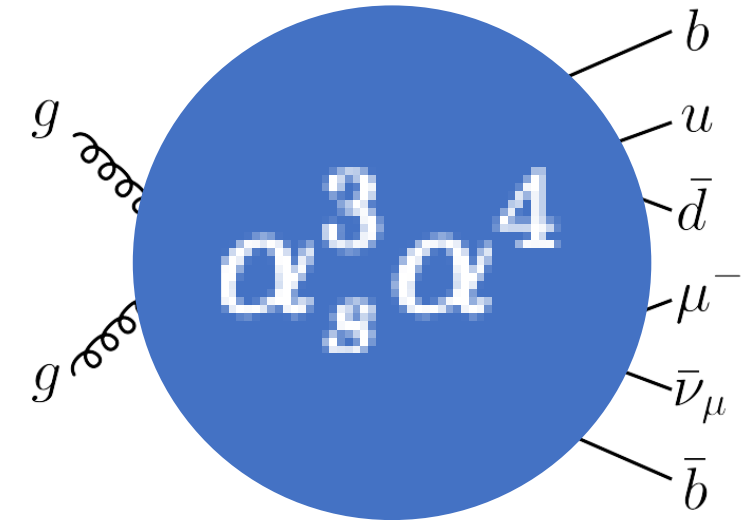
$$\text{LO} = \sum_{i=1}^5 \text{LO}_i$$

COMPLETE NLO CORRECTIONS

$$pp \rightarrow \ell^- \bar{\nu}_\ell j_b j_b jj + X$$



- Real-emission Feynman diagrams contributing at **NLO₃**

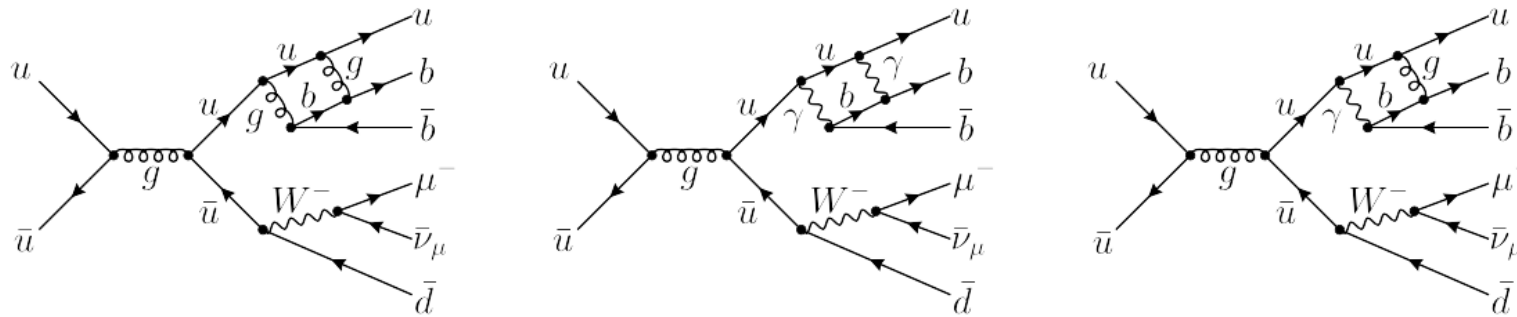
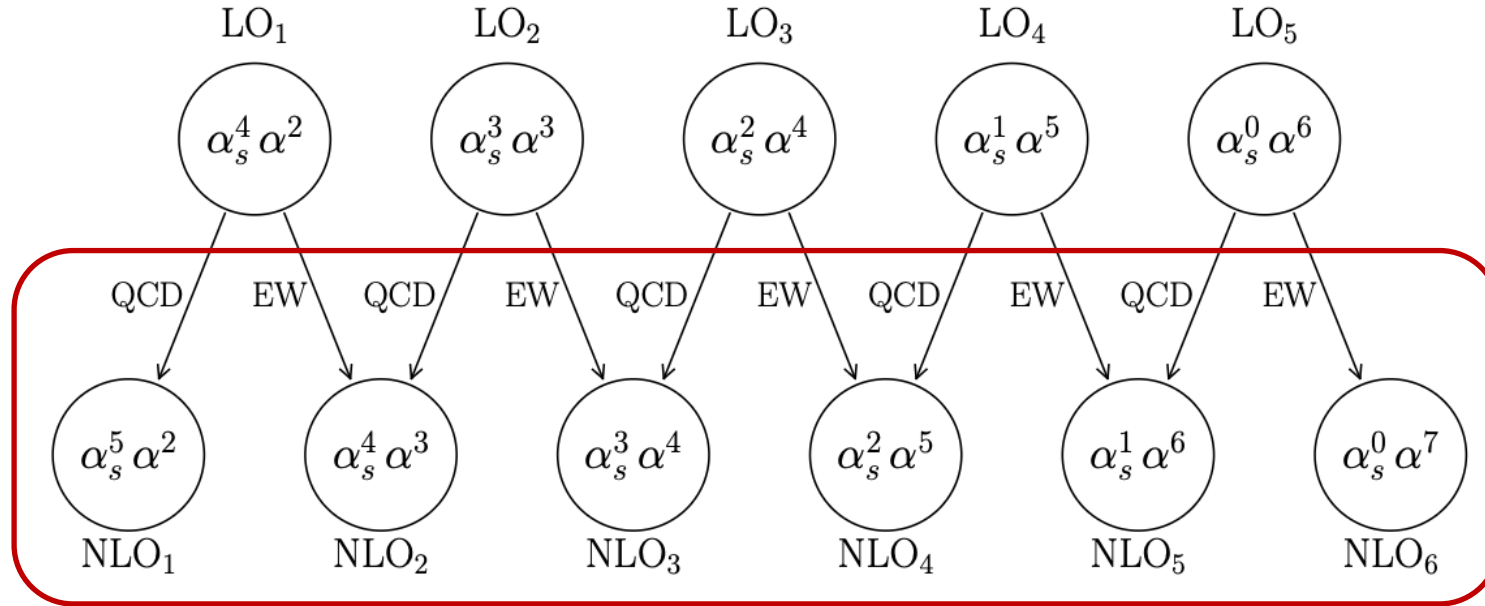


$$\text{NLO}_{\text{QCD}} = \text{Born} + \text{NLO}_3$$

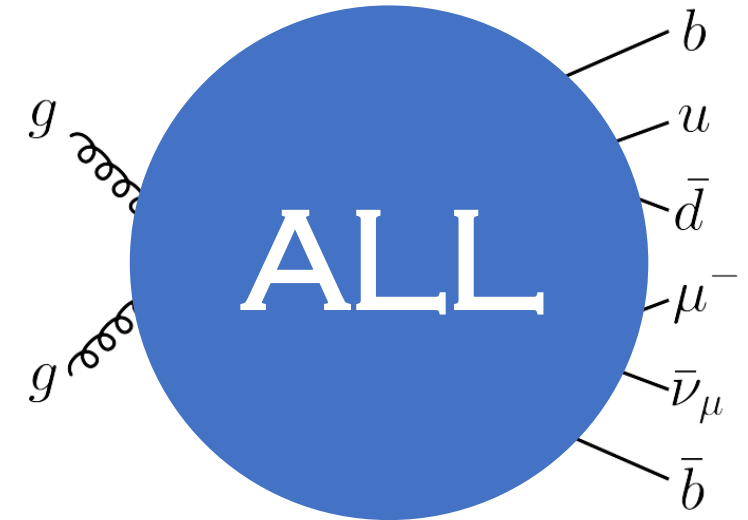
$$\text{Born} = \sum_{i=1}^5 \text{Born}_i$$

COMPLETE NLO CORRECTIONS

$$pp \rightarrow \ell^- \bar{\nu}_\ell j_b j_b jj + X$$



- QCD corrections, EW corrections & Both type of corrections
- QCD & EW corrections cannot be considered separately
- Must be combined together for proper cancellation of all IR singularities



$$\text{NLO} = \text{Born} + \sum_{i=1}^6 \text{NLO}_i$$

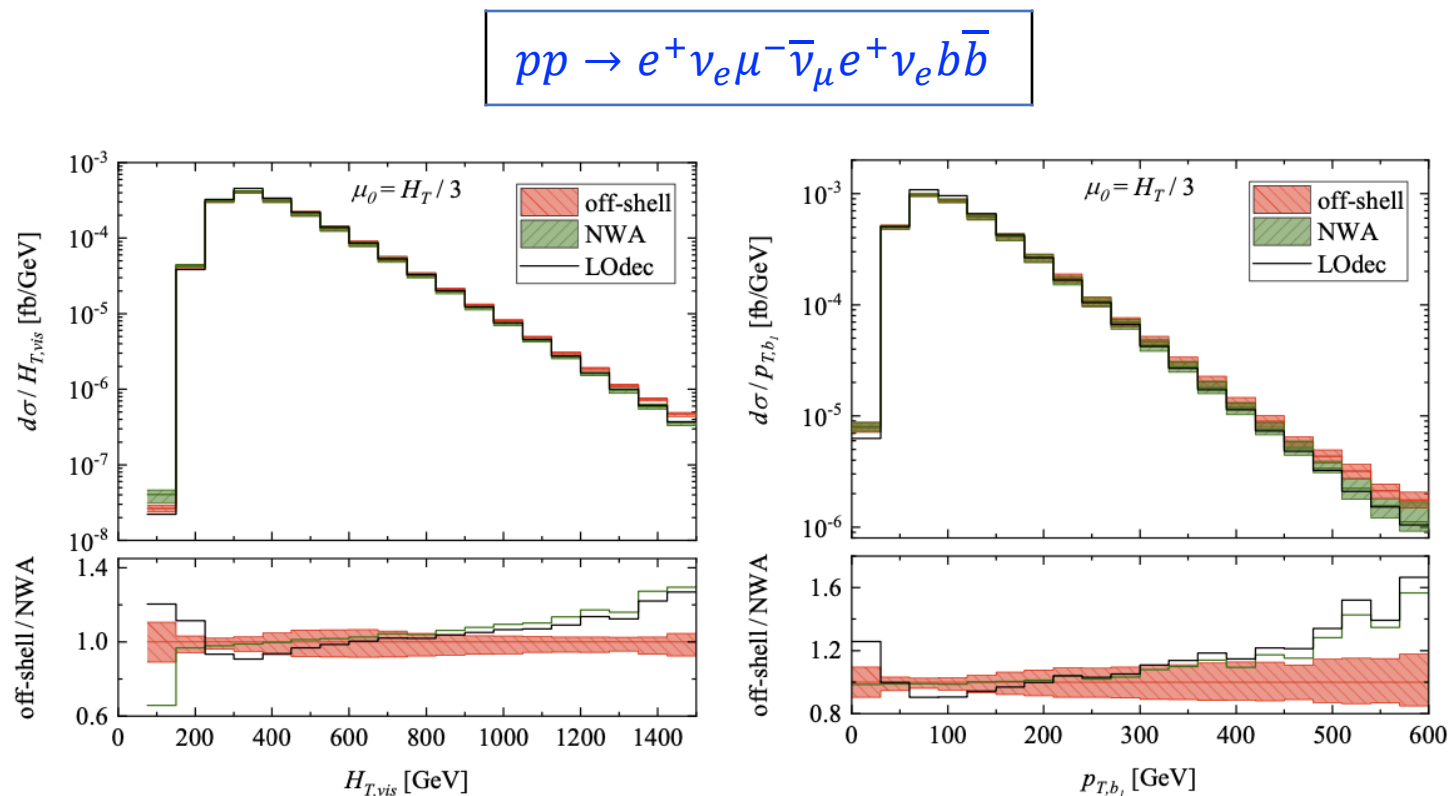
$$\text{Born} = \sum_{i=1}^5 \text{Born}_i$$

PART I – FIXED-ORDER PREDICTIONS: FULL OFF-SHELL NLO QCD

WHEN DO WE NEED FULL OFF-SHELL PREDICTIONS

Bevilacqua, Bi, Hartanto, Kraus, Worek, JHEP 08 (2020) 043

MODELLING APPROACH	σ^{LO} [ab]	σ^{NLO} [ab]
full off-shell ($\mu_0 = m_t + m_W/2$)	$106.9^{+27.7 (26\%)}_{-20.5 (19\%)}$	$123.2^{+6.3 (5\%)}_{-8.7 (7\%)}$
full off-shell ($\mu_0 = H_T/3$)	$115.1^{+30.5 (26\%)}_{-22.5 (20\%)}$	$124.4^{+4.3 (3\%)}_{-7.7 (6\%)}$
NWA ($\mu_0 = m_t + m_W/2$)	$106.4^{+27.5 (26\%)}_{-20.3 (19\%)}$	$123.0^{+6.3 (5\%)}_{-8.7 (7\%)}$
NWA ($\mu_0 = H_T/3$)	$115.1^{+30.4 (26\%)}_{-22.4 (19\%)}$	$124.2^{+4.1 (3\%)}_{-7.7 (6\%)}$
NWA _{LOdecay} ($\mu_0 = m_t + m_W/2$)		$127.0^{+14.2 (11\%)}_{-13.3 (10\%)}$
NWA _{LOdecay} ($\mu_0 = H_T/3$)		$130.7^{+13.6 (10\%)}_{-13.2 (10\%)}$



INTEGRATED LEVEL

- Full off-shell effects **0.2%**
- NLO QCD corrections to decays **3%-5%**

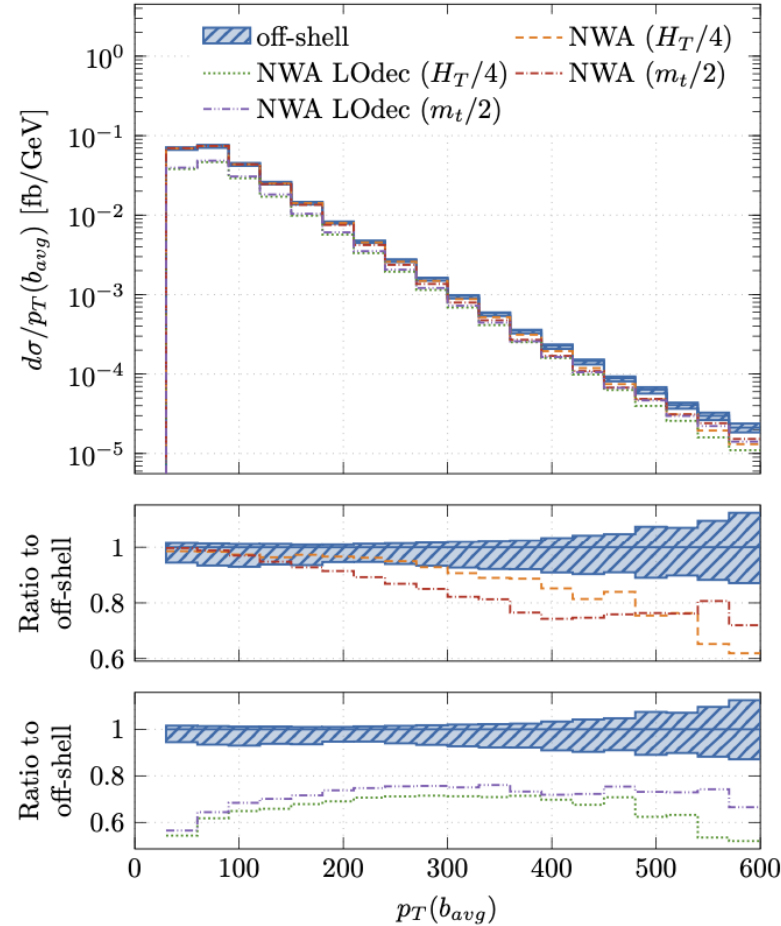
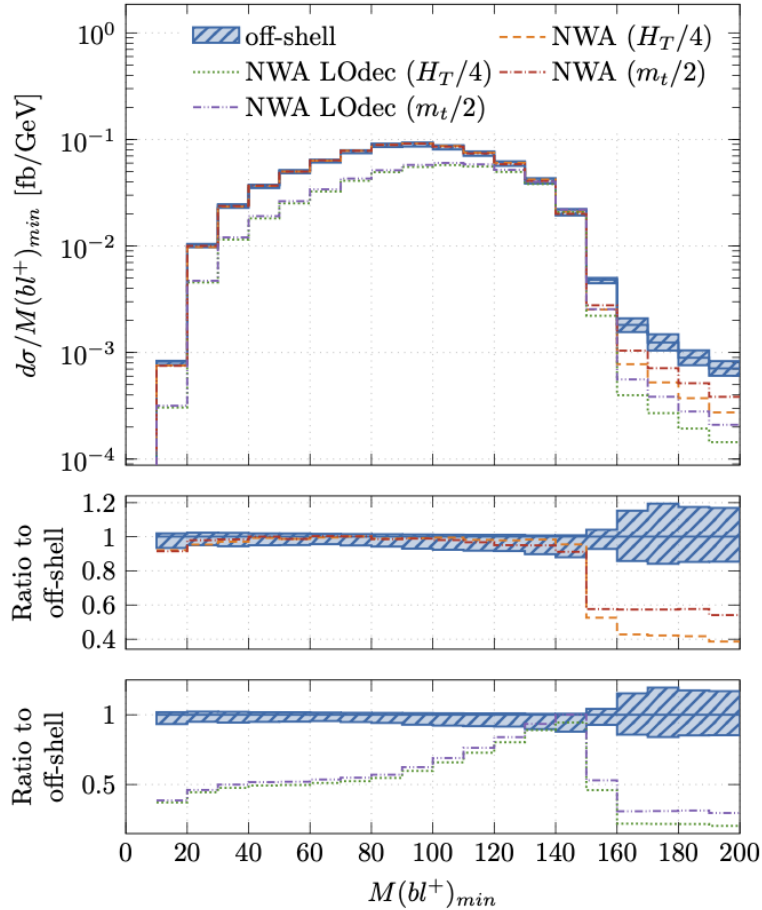
DIFFERENTIAL LEVEL

- Off-shell effects up to **60% - 70%**
- Substantial differences between **NWA & NWA_{LODECAY}**

HOW GOOD IS NWA

Bevilacqua, Hartanto, Kraus, Weber, Worek, JHEP 03 (2020) 154

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$$



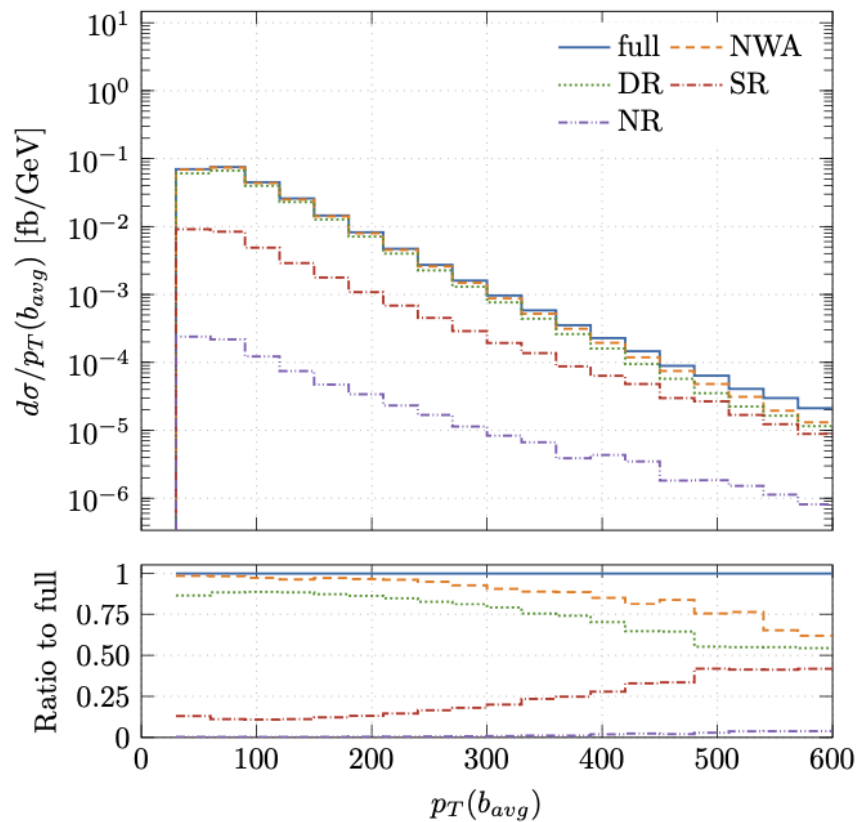
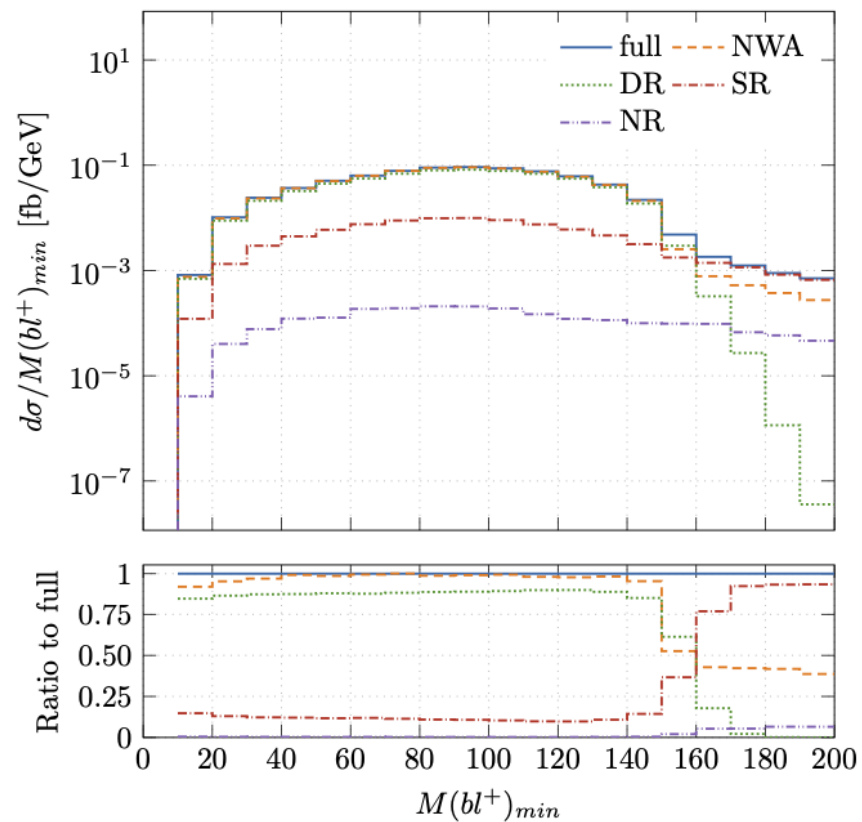
DIMENSIONFUL OBSERVABLES

- Substantial differences between **NWA & NWA_{LODECAY}** when γ only in production stage
- NLO + PS not suitable to describe **$pp \rightarrow t\bar{t}\gamma$** process
- Off-shell effects up to **50% – 60%**
- Specific phase-space regions
 - Kinematical edges**
 - High p_T regions**

VARIOUS PHASE-SPACE REGIONS

Bevilacqua, Hartanto, Kraus, Weber, Worek, JHEP 03 (2020) 154

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$$



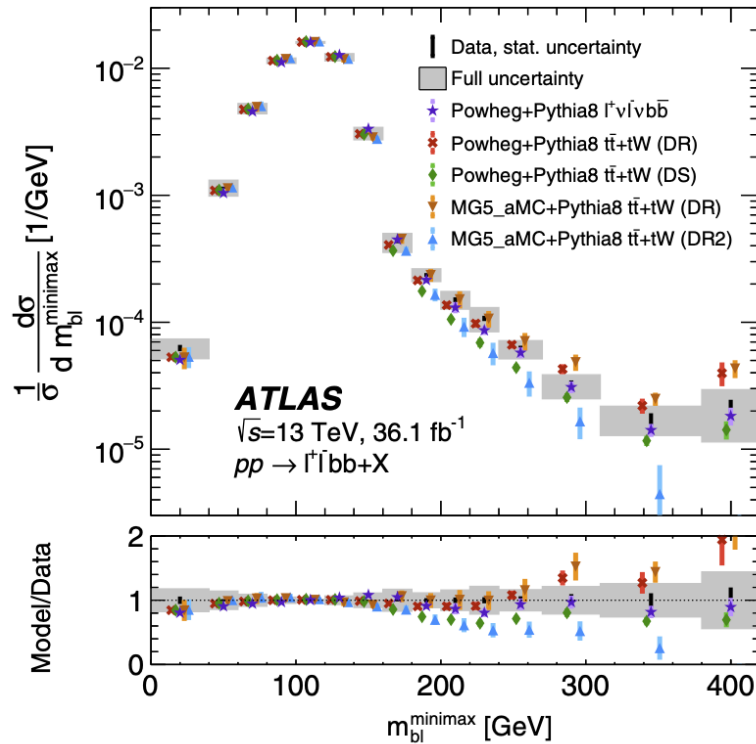
DIMENSIONFUL OBSERVABLES

- Sensitive to non-factorizable top quark corrections
- Effects up to **50% – 60%**
- Specific phase space regions
 - *Kinematical edges*
 - *High p_T regions*

COMPETING EFFECTS

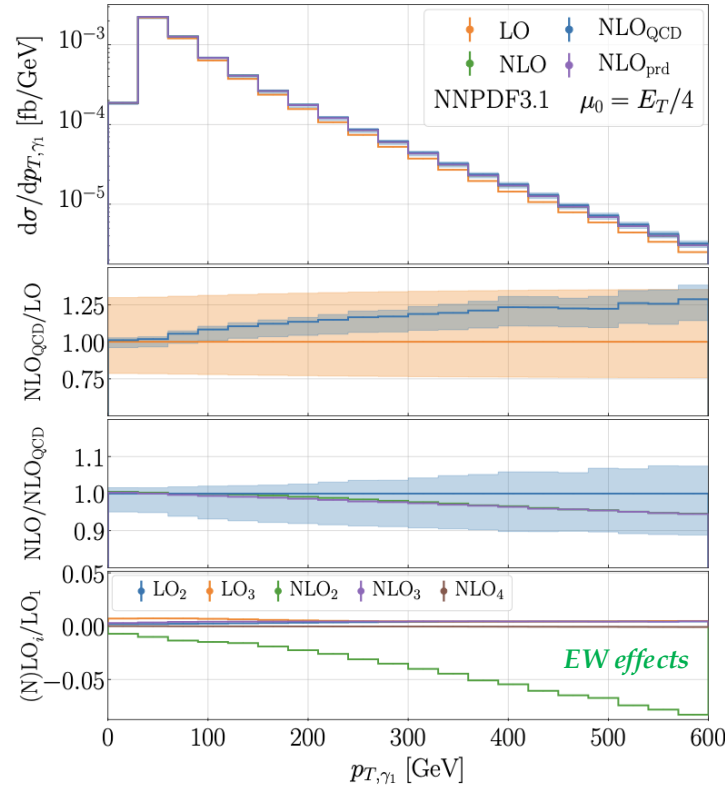
$$pp \rightarrow \ell^+ \nu_\ell \ell^- \bar{\nu}_\ell b \bar{b} (\gamma)$$

ATLAS, Phys. Rev. Lett. 121 (2018) 15, 152002

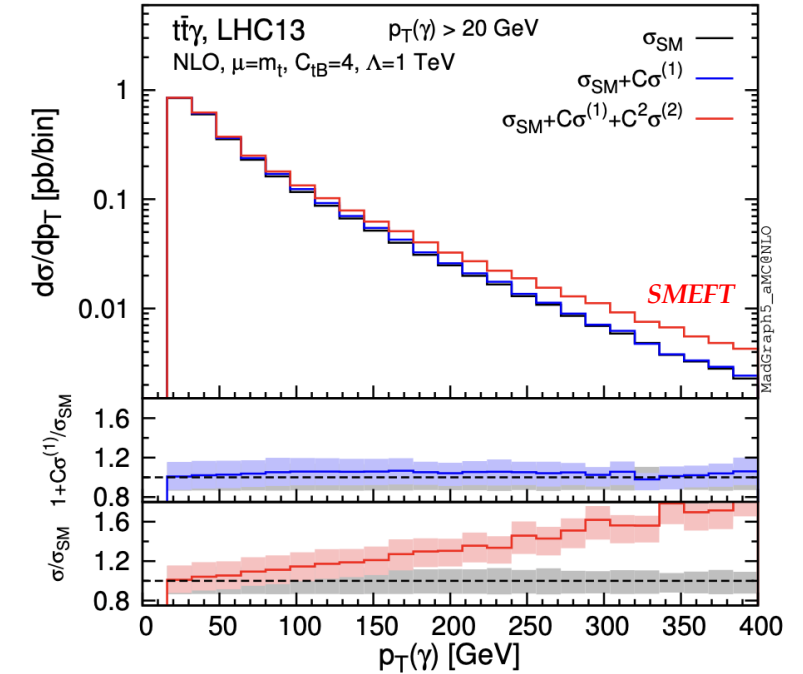


bb4l versus standard MC

Stremmer, Worek, JHEP 07 (2024) 091



Bylund, Maltoni, Tsinikos, Vryonidou, Zhang, JHEP 05 (2016) 052



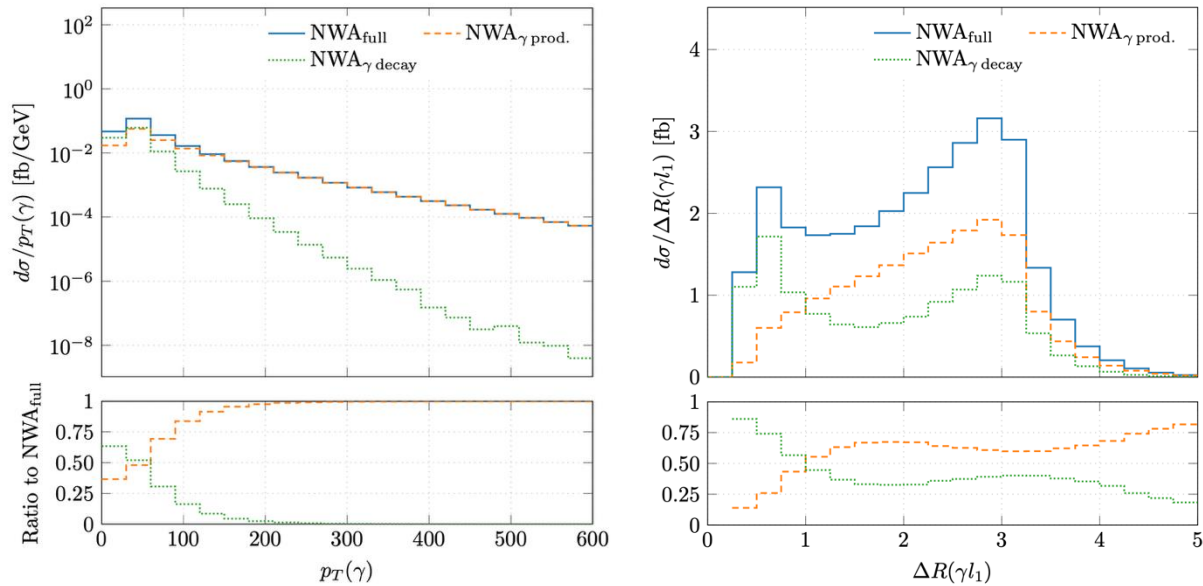
$$\sigma = \sigma_{SM} + \sum_i \frac{C_i}{(\Lambda/1\text{TeV})^2} \sigma_i^{(1)} + \sum_{i \leq j} \frac{C_i C_j}{(\Lambda/1\text{TeV})^4} \sigma_{ij}^{(2)}$$

- Full off-shell effects relevant in high p_T tails & for kinematical edges
- Other relevant effects in the same phase-space regions → EW Sudakov logarithms → SMEFT contributions

PHOTON IN PRODUCTION & DECAYS

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$$

- Integrated level for $p_{T,b} > 40$ GeV & $p_{T,\gamma} > 25$ GeV:
 - Prod. Contribution* at the level of **57%**
 - Decay contribution* at the level of **43%**



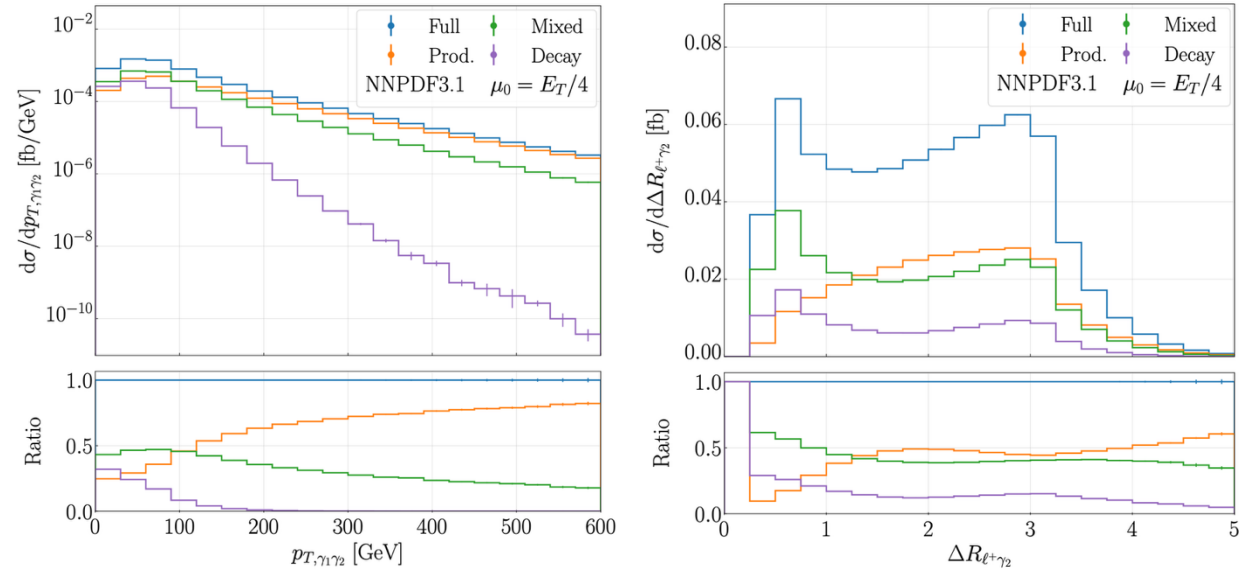
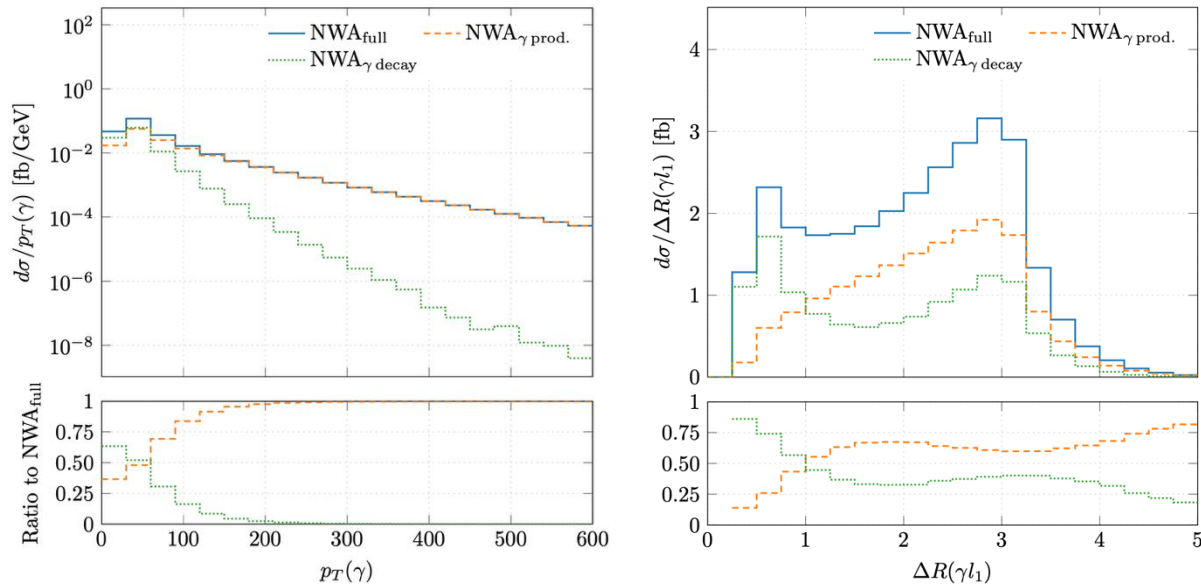
PHOTON IN PRODUCTION & DECAYS

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$$

$$pp \rightarrow \ell^+ \nu_\ell \ell^- \bar{\nu}_\ell b \bar{b} \gamma \gamma$$

- Integrated level for $p_{T,b} > 40$ GeV & $p_{T,\gamma} > 25$ GeV:
 - Prod. Contribution** at the level of **57%**
 - Decay contribution** at the level of **43%**

- Integrated level for $p_{T,b} > 25$ GeV & $p_{T,\gamma} > 25$ GeV:
 - Mixed contribution** at the level of **44%**
 - Prod. contribution** at the level of **40%**
 - Decay contribution** is about half the size **16%**



- Different phase-space regions with various effects
- $pp \rightarrow tt\gamma(\gamma)$ process cannot be described correctly by standard NLO+PS predictions

APPLICATION: YUKAWA COUPLING

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} H$$

α_{CP}		Off-shell	NWA	Off-shell effects
0 (SM)	σ_{LO} [fb]	$2.0313(2)^{+0.6275(31\%)}_{-0.4471(22\%)}$	$2.0388(2)^{+0.6290(31\%)}_{-0.4483(22\%)}$	-0.37%
	σ_{NLO} [fb]	$2.466(2)^{+0.027(1.1\%)}_{-0.112(4.5\%)}$	$2.475(1)^{+0.027(1.1\%)}_{-0.113(4.6\%)}$	-0.36%
	$\sigma_{\text{NLO}_{\text{LOdec}}}$ [fb]	—	$2.592(1)^{+0.161(6.2\%)}_{-0.242(9.3\%)}$	
$\mathcal{K} = \sigma_{\text{NLO}}/\sigma_{\text{LO}}$		1.21	1.21 (LOdec: 1.27)	
$\pi/4$	σ_{LO} [fb]	$1.1930(2)^{+0.3742(31\%)}_{-0.2656(22\%)}$	$1.1851(1)^{+0.3707(31\%)}_{-0.2633(22\%)}$	0.66%
	σ_{NLO} [fb]	$1.465(2)^{+0.016(1.1\%)}_{-0.071(4.8\%)}$	$1.452(1)^{+0.015(1.0\%)}_{-0.069(4.8\%)}$	0.89%
	$\sigma_{\text{NLO}_{\text{LOdec}}}$ [fb]	—	$1.517(1)^{+0.097(6.4\%)}_{-0.144(9.5\%)}$	
$\mathcal{K} = \sigma_{\text{NLO}}/\sigma_{\text{LO}}$		1.23	1.23 (LOdec: 1.28)	
$\pi/2$	σ_{LO} [fb]	$0.38277(6)^{+0.13123(34\%)}_{-0.09121(24\%)}$	$0.33148(3)^{+0.11240(34\%)}_{-0.07835(24\%)}$	13.4%
	σ_{NLO} [fb]	$0.5018(3)^{+0.0083(1.2\%)}_{-0.0337(6.7\%)}$	$0.4301(2)^{+0.0035(0.8\%)}_{-0.0264(6.1\%)}$	14.3%
	$\sigma_{\text{NLO}_{\text{LOdec}}}$ [fb]	—	$0.4433(2)^{+0.0323(7.3\%)}_{-0.0470(11\%)}$	
$\mathcal{K} = \sigma_{\text{NLO}}/\sigma_{\text{LO}}$		1.31	1.30 (LOdec: 1.34)	

- Off-shell effects @ integrated fiducial cross-section level:

- Small for *CP-even* and *CP-mixed* Higgs boson
- Large effects for *CP-odd* Higgs boson

Herrmann, Stremmer, Worek, JHEP 09 (2022) 138

- Higgs characterisation framework

Mixing angle

$$\mathcal{L}_{t\bar{t}H} = -\bar{\psi}_t \frac{Y_t}{\sqrt{2}} (\underbrace{\kappa_{Ht\bar{t}} \cos(\alpha_{\text{CP}})}_{\text{CP-even}} + i \underbrace{\kappa_{At\bar{t}} \sin(\alpha_{\text{CP}})}_{\text{CP-odd}} \gamma_5) \psi_t H,$$

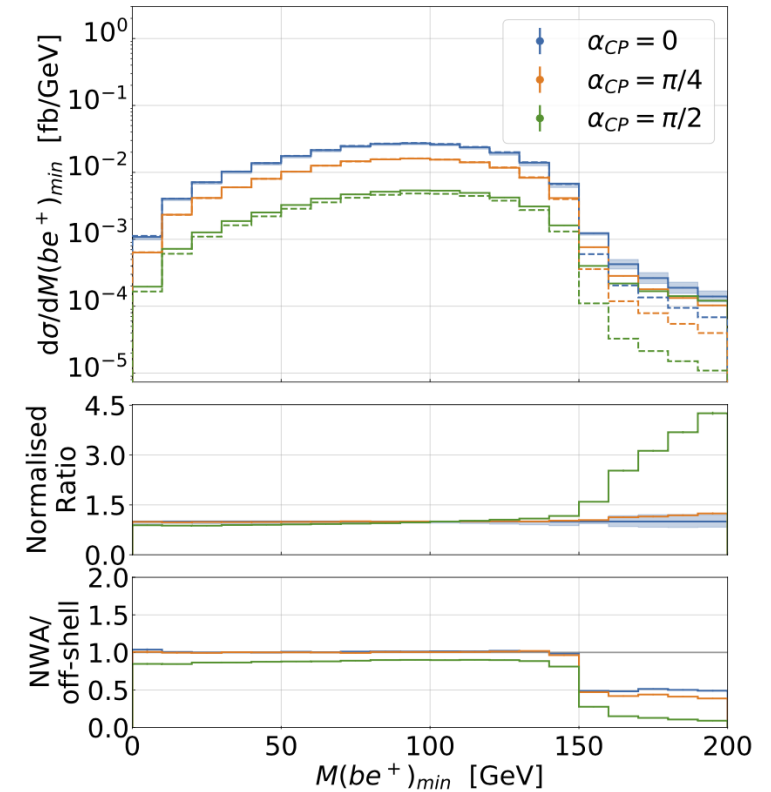
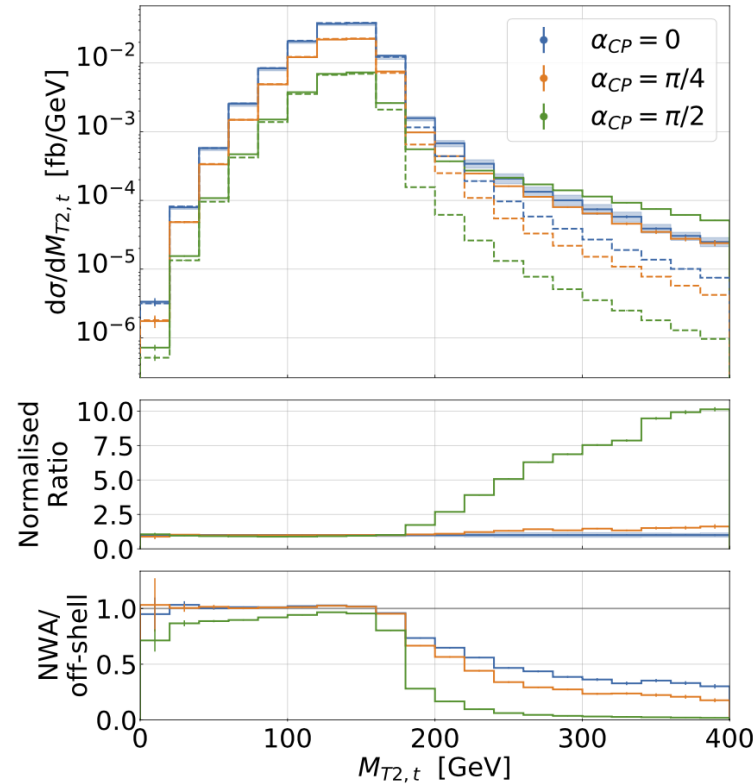
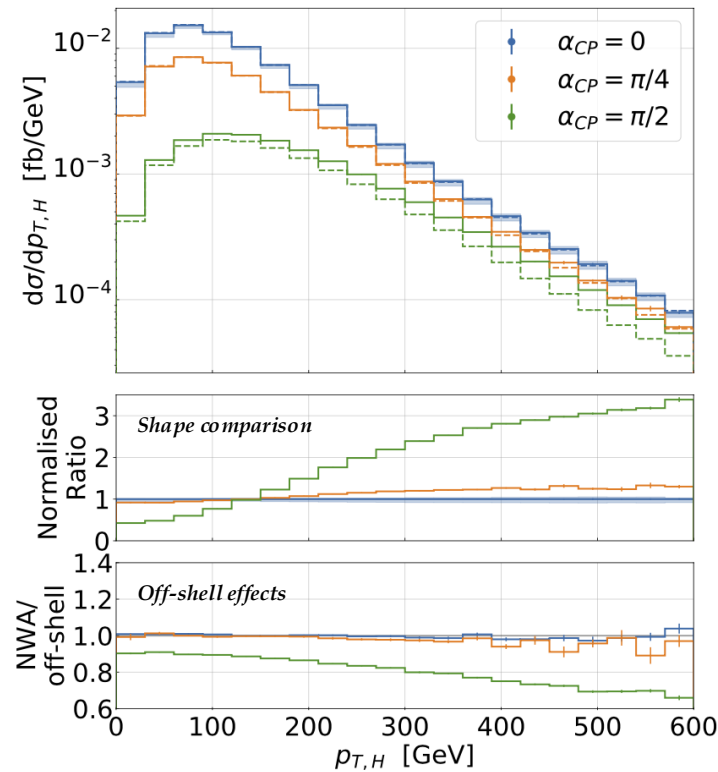
$$\mathcal{L}_{HVV} = \kappa_{HVV} \left(\frac{1}{2} g_{HZZ} Z_\mu Z^\mu + g_{HWW} W_\mu^+ W^{-\mu} \right) H,$$

Coupling choices: $\kappa_{At\bar{t}} = 2/3$ & $\kappa_{Ht\bar{t}} = 1$ & $\kappa_{HVV} = 1$
 Ensure consistency with current experimental bounds (ggF, VBF)

Artoisenet et al., JHEP 11 (2013) 043
 Maltoni et al., Eur. Phys. J. C 74 (2014) 1, 2710
 Demartin et al., Eur. Phys. J. C 74 (2014) 9, 3065
 Demartin et al., Eur. Phys. J. C 75 (2015) 6, 267

APPLICATION: YUKAWA COUPLING

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} H$$

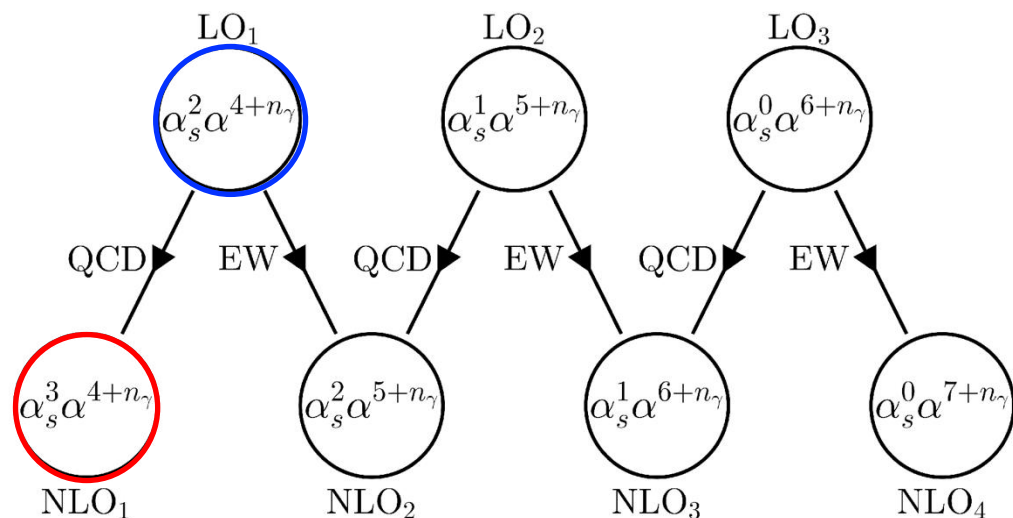


- *CP-even*
- *CP-mixed*
- *CP-odd*
- Solid line full off-shell results, dashed line NWA

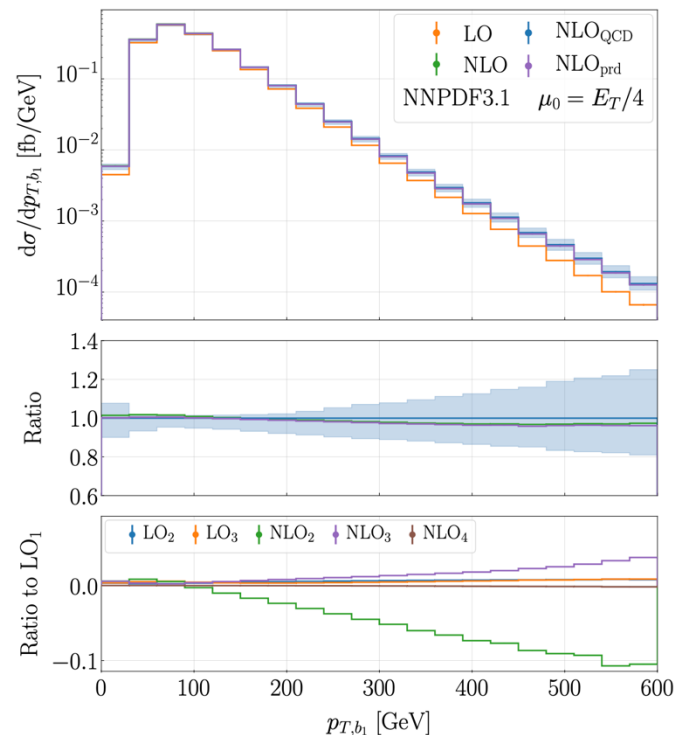
- Off-shell effects @ differential fiducial cross-section level:
 - Large effects on size and shape for *CP-odd* Higgs boson
 - Only small effects for *CP-even* and *CP-mixed*
 - *Reason: SR contributions ~ tWHb production*

PART II – FIXED-ORDER PREDICTIONS: COMPLETE NLO

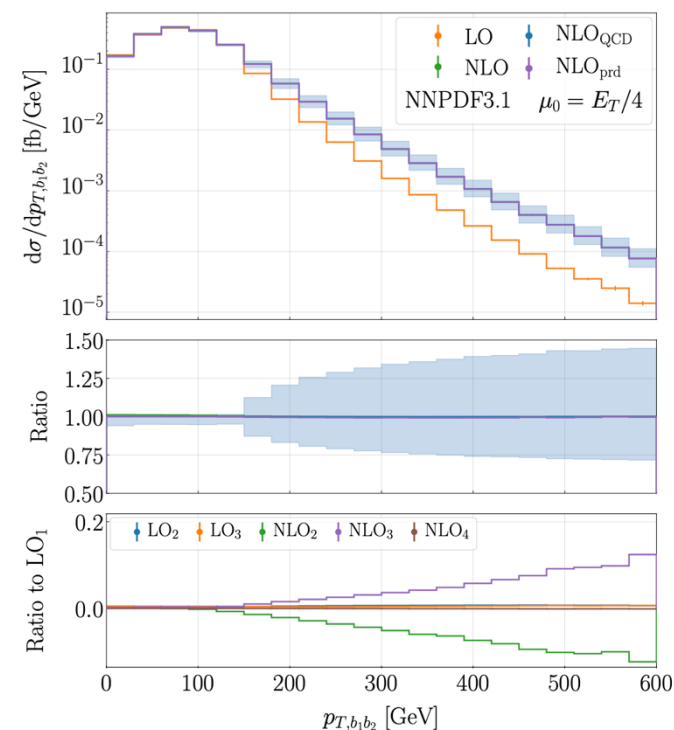
COMPLETE NLO CORRECTIONS



		σ_i [fb]	Ratio to LO ₁
LO ₁	$\mathcal{O}(\alpha_s^2 \alpha^5)$	55.604(8) ^{+31.4%} _{-22.3%}	1.00
LO ₂	$\mathcal{O}(\alpha_s^1 \alpha^6)$	0.18775(5) ^{+20.1%} _{-15.4%}	+0.34%
LO ₃	$\mathcal{O}(\alpha_s^0 \alpha^7)$	0.26970(4) ^{+14.3%} _{-16.9%}	+0.49%
NLO ₁	$\mathcal{O}(\alpha_s^3 \alpha^5)$	+3.44(5)	+6.19%
NLO ₂	$\mathcal{O}(\alpha_s^2 \alpha^6)$	-0.1553(9)	-0.28%
NLO ₃	$\mathcal{O}(\alpha_s^1 \alpha^7)$	+0.2339(3)	+0.42%
NLO ₄	$\mathcal{O}(\alpha_s^0 \alpha^8)$	+0.001595(8)	+0.003%
LO		56.061(8) ^{+31.2%} _{-22.1%}	1.0082
NLO _{QCD}		59.05(5) ^{+1.6%} _{-5.9%}	1.0620
NLO _{prd}		59.08(5) ^{+1.5%} _{-5.9%}	1.0626
NLO		59.59(5) ^{+1.6%} _{-5.9%}	1.0717



Stremmer, Worek, JHEP 07 (2024) 091

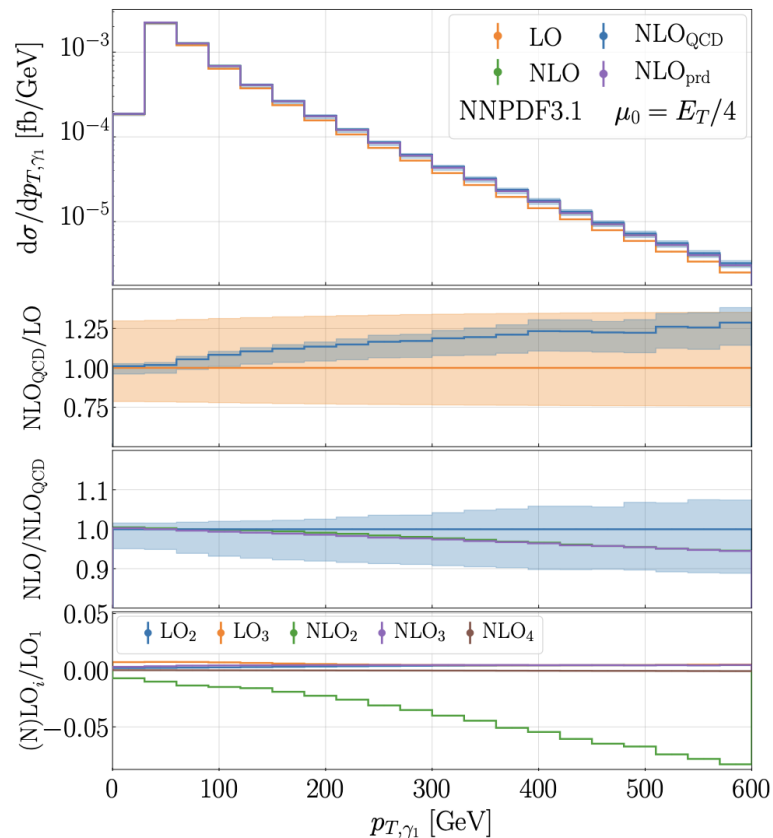
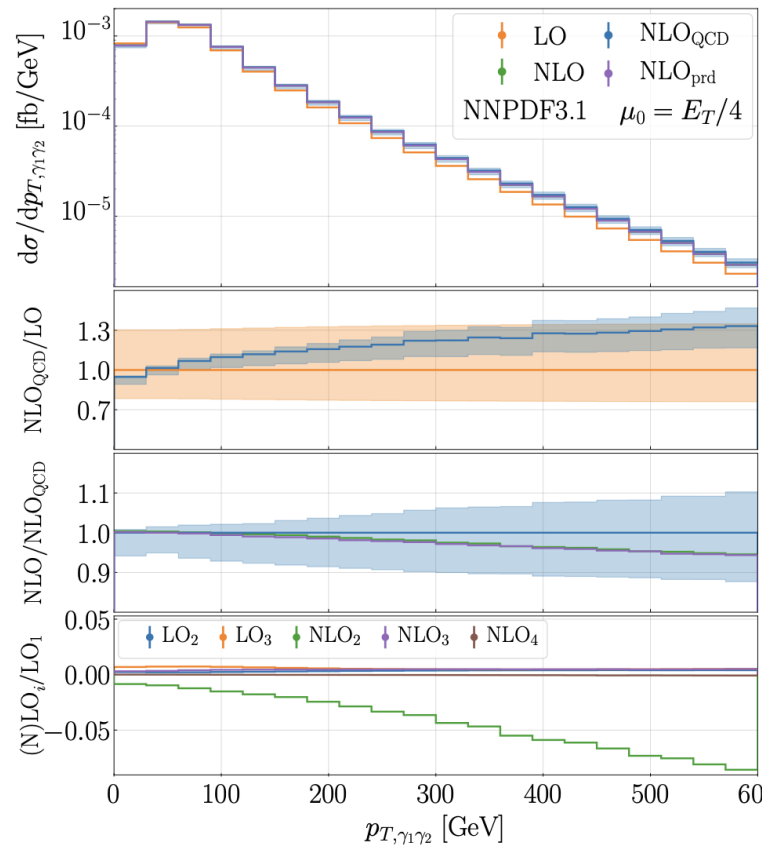


- EW Sudakov logarithms in **NLO₂** leads to reduction in tails of up to **10%** compared to **NLO_{QCD}** result
- Accidental cancellations between **NLO₂** & **NLO₃** → Should be considered together
- NLO_{prd}** approximation models complete **NLO** result very well

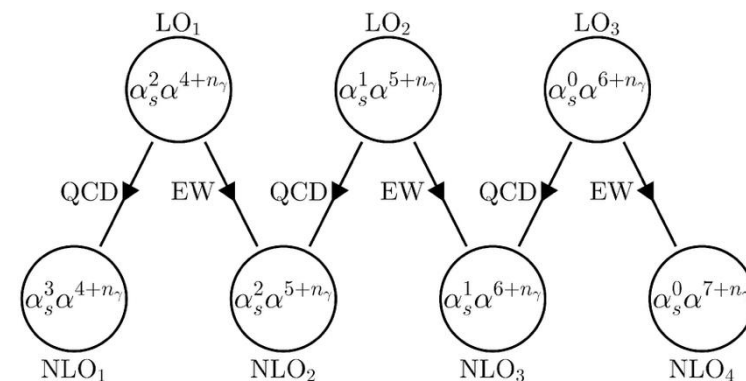
$$\text{NLO}_{\text{prd}} = \text{LO}_1 + \text{LO}_2 + \text{LO}_3 + \text{NLO}_1 + \text{NLO}_{2,\text{prd}} + \text{NLO}_{3,\text{prd}} + \text{NLO}_{4,\text{prd}}$$

COMPLETE NLO CORRECTIONS

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma \gamma$$



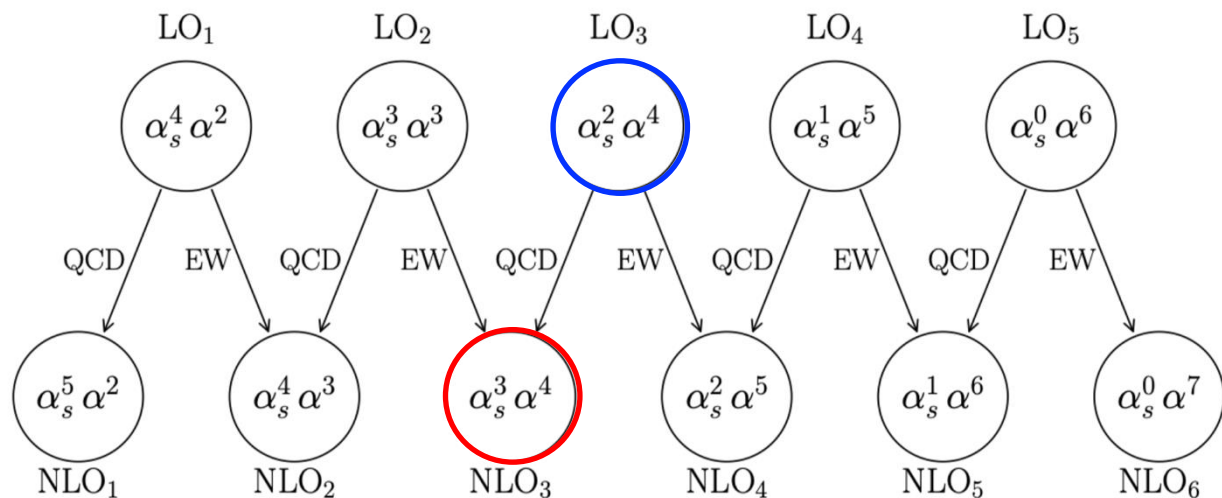
- EW Sudakov logarithms in **NLO₂** leads to reduction in tails of up to **10%** compared to **NLO_{QCD}** result



COMPLETE NLO CORRECTIONS

$$pp \rightarrow \mu^- \bar{\nu}_\mu jj b \bar{b}$$

Mans, Stremmer, Worek, e-Print: 2512.18391 [hep-ph]



$$\text{LO} = \sum_{i=1}^5 \text{LO}_i \quad \text{Born} = \sum_{i=1}^5 \text{Born}_i \quad \text{NLO}_{\text{QCD}} = \text{Born} + \text{NLO}_3$$

$$\text{NLO} = \text{Born} + \sum_{i=1}^6 \text{NLO}_i$$

- Q_{cut} reduces QCD background NLO₁
- **Born₃ & NLO₃** dominate
- Subleading LO/NLO contribute $\lesssim 1\%$

		σ_i [pb]	Ratio to Born ₃
Born ₁	$\mathcal{O}(\alpha_s^4 \alpha^2)$	0.138(2)	0.44%
Born ₂	$\mathcal{O}(\alpha_s^3 \alpha^3)$	0.0002(1)	0.00%
Born ₃	$\mathcal{O}(\alpha_s^2 \alpha^4)$	31.264(4)	100.00%
Born ₄	$\mathcal{O}(\alpha_s^1 \alpha^5)$	0.1336(1)	0.43%
Born ₅	$\mathcal{O}(\alpha_s^0 \alpha^6)$	0.0968(1)	0.31%
NLO ₁	$\mathcal{O}(\alpha_s^5 \alpha^2)$	+ 0.144(4)	+ 0.46%
NLO ₂	$\mathcal{O}(\alpha_s^4 \alpha^3)$	- 0.0022(4)	- 0.01%
NLO ₃	$\mathcal{O}(\alpha_s^3 \alpha^4)$	- 1.90(2)	- 6.10%
NLO ₄	$\mathcal{O}(\alpha_s^2 \alpha^5)$	+ 0.112(2)	+ 0.36%
NLO ₅	$\mathcal{O}(\alpha_s^1 \alpha^6)$	+ 0.1864(6)	+ 0.60%
NLO ₆	$\mathcal{O}(\alpha_s^0 \alpha^7)$	+ 0.00228(2)	+ 0.01%
LO		27.241(2) ^{+30.7%} _{-22.0%}	0.87
Born		31.634(4) ^{+30.7%} _{-22.0%}	1.01
NLO _{QCD}		29.72(2) ^{+1.4%} _{-6.0%}	0.95
NLO		30.16(2) ^{+1.5%} _{-5.6%}	0.96

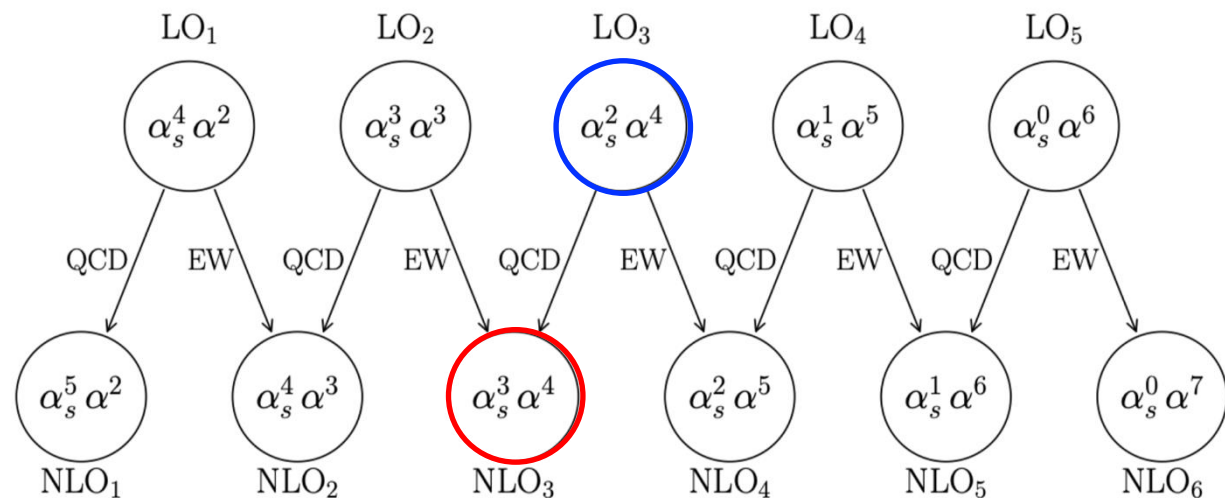
$$|M_{jj} - m_W| < Q_{\text{cut}}$$

$$Q_{\text{cut}} = 20 \text{ GeV}$$

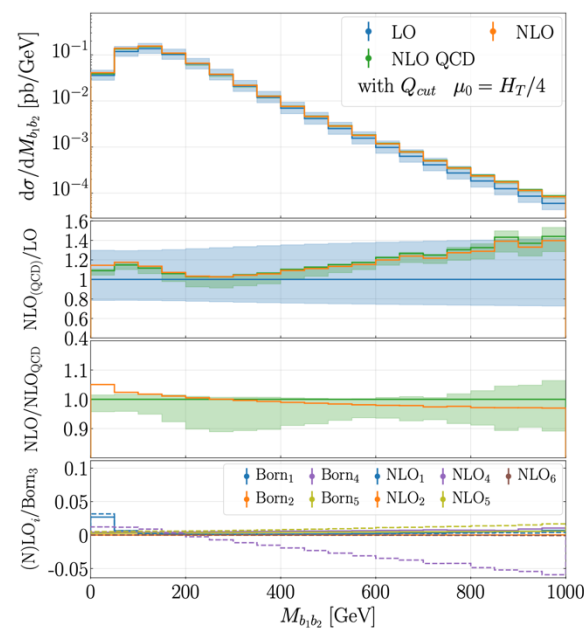
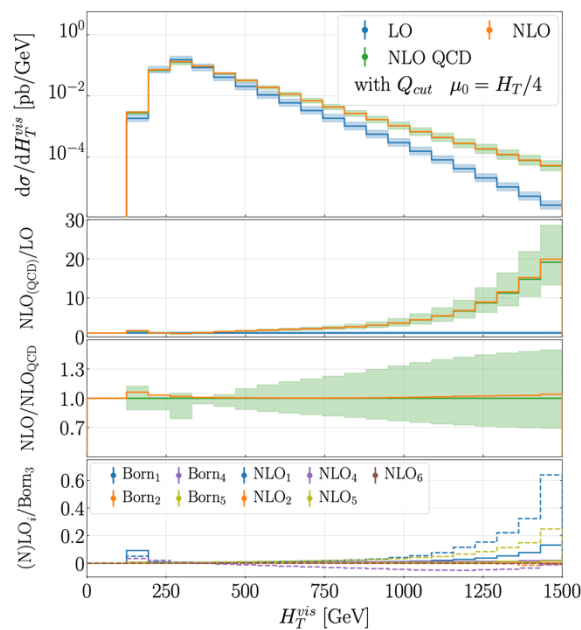
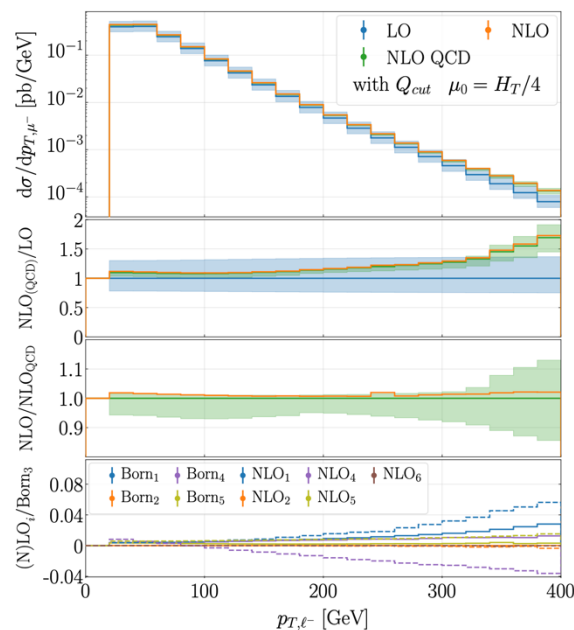
COMPLETE NLO CORRECTIONS

$$pp \rightarrow \mu^- \bar{\nu}_\mu jj b \bar{b}$$

Mans, Stremmer, Worek, e-Print: 2512.18391 [hep-ph]



- Last panels depict **Born_i** (solid lines) & **NLO_i** (dashed lines) normalised to dominant **Born₃** & **NLO₃** not shown
- $p_{T,l} \rightarrow$ Cancellations between **NLO₁** & **NLO₄**



$$|M_{jj} - m_W| < Q_{cut}$$

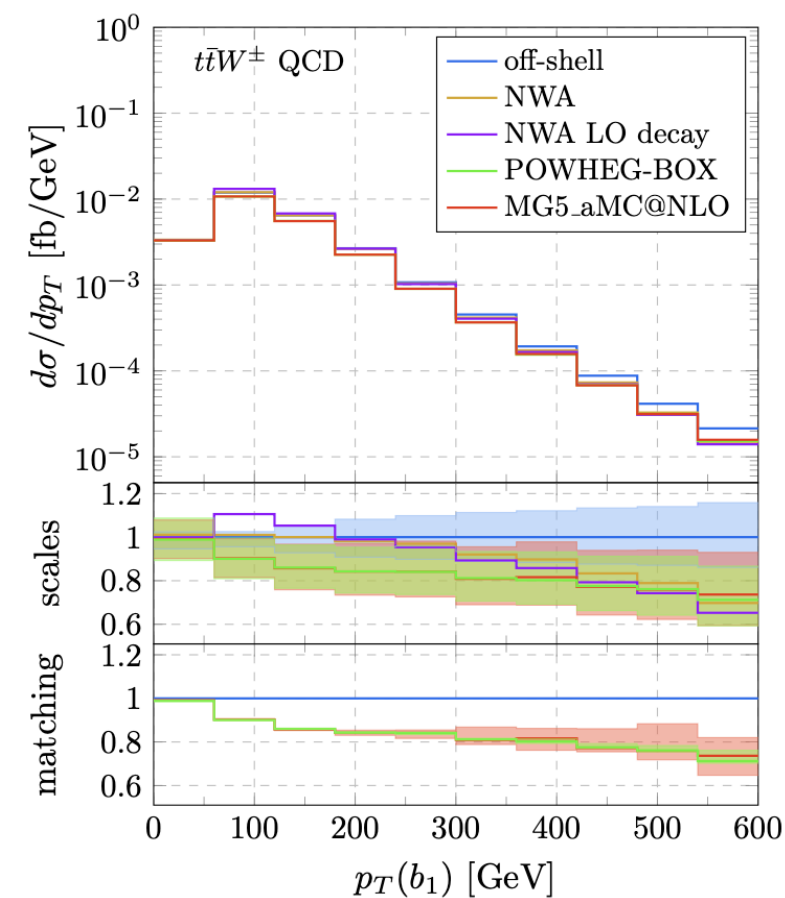
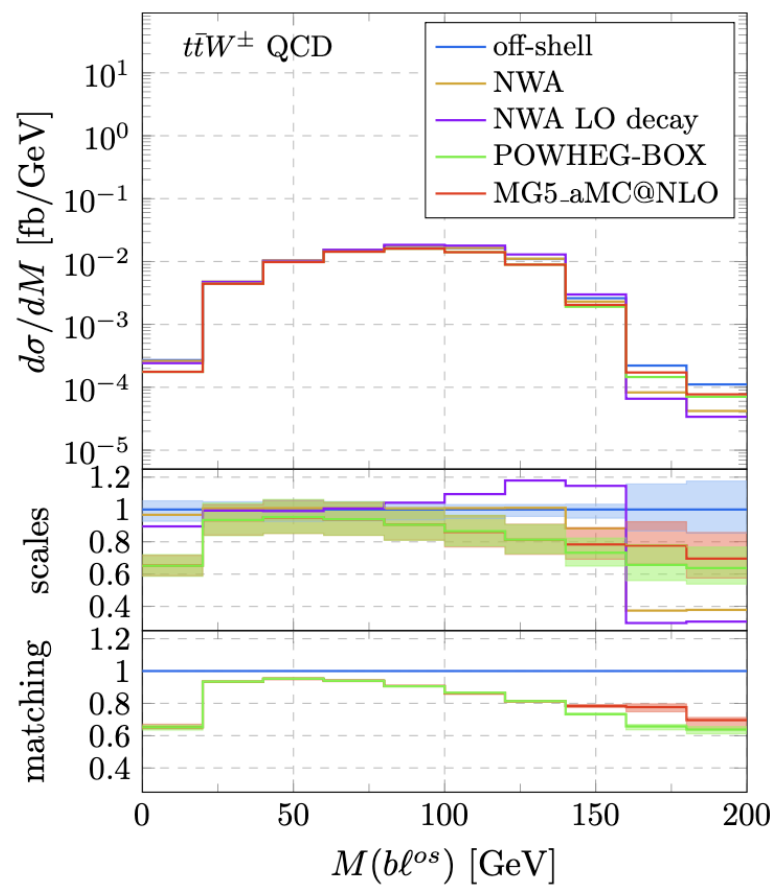
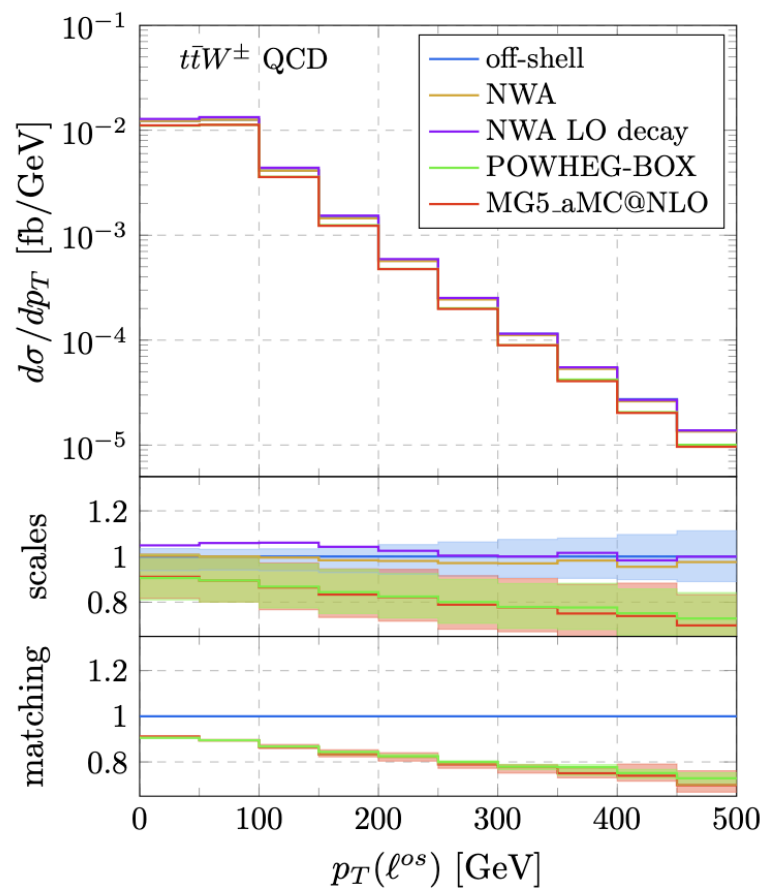
$$Q_{cut} = 20 \text{ GeV}$$

PART III – PARTON-SHOWER BASED PREDICTIONS: NLO QCD + PS

FIXED ORDER VERSUS PARTON-SHOWER

- $l^{os} \rightarrow$ Opposite-Sign lepton

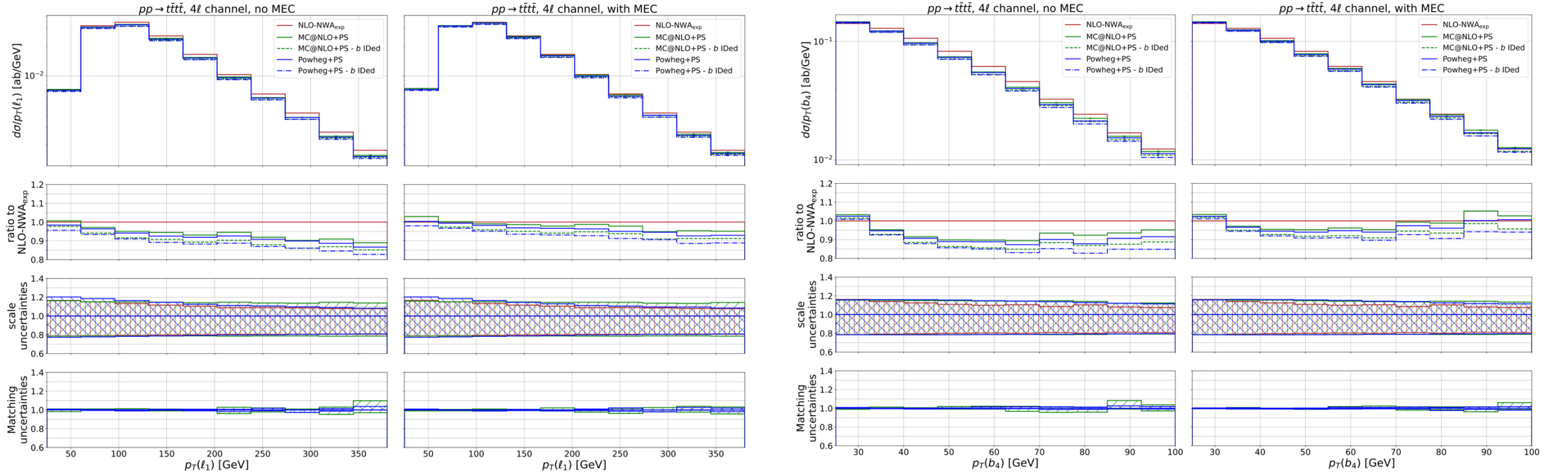
$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu e^+ \nu_e b \bar{b}$$



Bevilacqua, Bi, Cordero, Hartanto, Kraus, Nasufi, Reina, Worek, *Phys. Rev. D* 105 (2022) 1, 014018

FIXED ORDER VERSUS PARTON-SHOWER WITH MEC

$$pp \rightarrow l^+ \nu_l l^- \bar{\nu}_l l^+ \nu_l l^- \bar{\nu}_l b \bar{b} b \bar{b}$$



- Emission in $t \rightarrow bW$ decay is corrected by means of $t \rightarrow bWg$ tree-level matrix element

COMPARISON WITH LHC DATA

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j$$

$$m_t$$

EUROPEAN ORGANISATION FOR NUCLEAR RESEARCH (CERN)



JHEP 12 (2025) 023
DOI: [10.1007/JHEP12\(2025\)023](https://doi.org/10.1007/JHEP12(2025)023)



CERN-EP-2025-135
11th December 2025

Measurement of the top-quark pole mass in dileptonic $t\bar{t} + 1$ -jet events at $\sqrt{s} = 13$ TeV with the ATLAS experiment

The ATLAS Collaboration

A measurement of the top-quark pole mass m_t^{pole} is presented in $t\bar{t}$ events with an additional jet, $t\bar{t} + 1$ -jet, produced in pp collisions at $\sqrt{s} = 13$ TeV. The data sample, recorded with the ATLAS experiment during Run 2 of the LHC, corresponds to an integrated luminosity of 140 fb^{-1} . Events with one electron and one muon of opposite electric charge in the final state are selected to measure the $t\bar{t} + 1$ -jet differential cross-section as a function of the inverse of the invariant mass of the $t\bar{t} + 1$ -jet system. Iterative Bayesian Unfolding is used to correct the data to enable comparison with fixed-order calculations at next-to-leading-order accuracy in the strong coupling. The process $pp \rightarrow t\bar{t}j$ ($2 \rightarrow 3$), where top quarks are taken as stable particles, and the process $pp \rightarrow b\bar{b}l^+\nu l^-\bar{\nu}j$ ($2 \rightarrow 7$), which includes top-quark decays to the dilepton final state and off-shell effects, are considered. The top-quark mass is extracted using a χ^2 fit of the unfolded normalized differential cross-section distribution. The results obtained with the $2 \rightarrow 3$ and $2 \rightarrow 7$ calculations are compatible within theoretical uncertainties, providing an important consistency check. The more precise determination is obtained for the $2 \rightarrow 3$ measurement: $m_t^{\text{pole}} = 170.7 \pm 0.3$ (stat.) ± 1.4 (syst.) ± 0.3 (scale) ± 0.2 (PDF $\oplus \alpha_s$) GeV, which is in good agreement with other top-quark mass results.

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ATLAS Collaboration JHEP 12 (2025) 023

Bevilacqua, Hartanto, Kraus, Worek, Phys. Rev. Lett. 116 (2016) 5, 052003

Bevilacqua, Hartanto, Kraus, Worek, JHEP 11 (2016) 098

Bevilacqua, Hartanto, Kraus, Schulze, Worek, JHEP 03 (2018) 169

$$\mathcal{R}(\rho_s; m_t^{\text{pole}}) = \frac{1}{\sigma_{t\bar{t}+1\text{-jet}}} \cdot \frac{d\sigma_{t\bar{t}+1\text{-jet}}}{d\rho_s}, \text{ with } \rho_s = \frac{2m_0}{\sqrt{s_{t\bar{t}+1\text{-jet}}}}$$

■ $2 \rightarrow 3$:

$$m_t^{\text{pole}} = 170.73 \pm 0.33 \text{ (stat.)} \pm 1.36 \text{ (syst.)} {}^{+0.34}_{-0.28} \text{ (scale)} \pm 0.24 \text{ (PDF} \oplus \alpha_s \text{) GeV.}$$

■ $2 \rightarrow 7$:

$$m_t^{\text{pole}} = 171.69 \pm 0.41 \text{ (stat.)} \pm 1.68 \text{ (syst.)} {}^{+0.66}_{-1.34} \text{ (scale)} {}^{+0.49}_{-0.46} \text{ (PDF} \oplus \alpha_s \text{) GeV.}$$

■ *Central value of $2 \rightarrow 7$ result is approximately 1 GeV higher than for $2 \rightarrow 3$ case*

■ Difference is covered by scale uncertainties of theoretical prediction

■ *Theoretical error grows from 0.3 – 0.4 GeV in $2 \rightarrow 3$ to 1 GeV in $2 \rightarrow 7$*

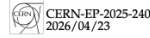
arXiv:2507.02632v2 [hep-ex] 10 Dec 2025

COMPARISON WITH LHC DATA

EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH (CERN)



CMS-TOP-23-002



CERN-EP-2025-240
2026/04/23

Inclusive and differential measurements of the $t\bar{t}\gamma$ cross section and the $t\bar{t}\gamma/t\bar{t}$ cross section ratio in proton-proton collisions at $\sqrt{s} = 13$ TeV

The CMS Collaboration*

Abstract

Inclusive and differential cross section measurements of top quark pair ($t\bar{t}$) production in association with a photon (γ) are performed as a function of lepton, photon, top quark, and $t\bar{t}$ kinematic observables, using data from proton-proton collisions at $\sqrt{s} = 13$ TeV, corresponding to an integrated luminosity of 138 fb^{-1} , collected at the CERN LHC with the CMS detector. Events containing two leptons (electrons or muons) and a photon in the final state are considered. The fiducial cross section of $t\bar{t}\gamma$ is measured to be $137 \pm 8\text{ fb}$, in a phase space including events with a high momentum, isolated photon. The fiducial cross section of $t\bar{t}\gamma$ is also measured to be $56 \pm 5\text{ fb}$ when considering only events where the photon is emitted in the production part of the process. Both measurements are in agreement with the theoretical predictions, of $126 \pm 19\text{ fb}$ and $57 \pm 5\text{ fb}$, respectively. Differential measurements are performed at the particle and parton levels. Additionally, inclusive and differential ratios between the cross sections of $t\bar{t}\gamma$ and $t\bar{t}$ production are measured. The inclusive ratio is found to be 0.0133 ± 0.0005 , in agreement with the standard model prediction of 0.0127 ± 0.0008 . The top quark charge asymmetry in $t\bar{t}\gamma$ production is also measured to be -0.012 ± 0.042 , compatible with both the standard model prediction and with no asymmetry.

Published in the Journal of High Energy Physics as doi:10.1007/JHEP04(2026)086.

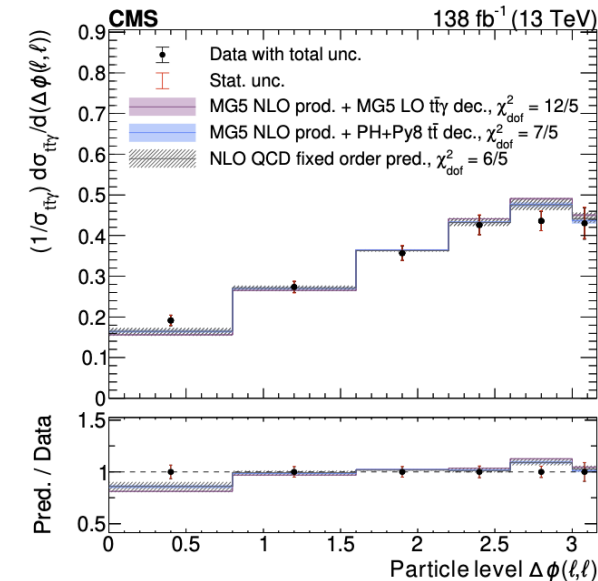
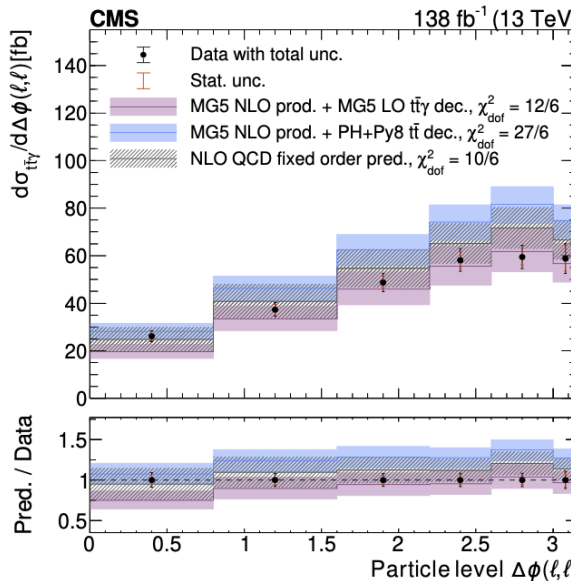
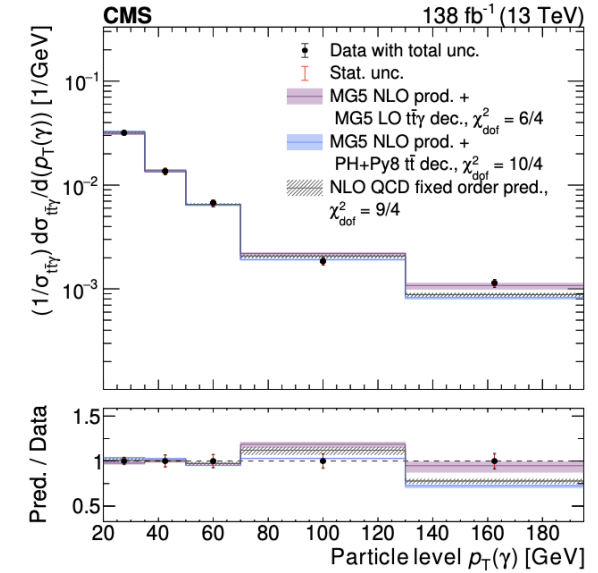
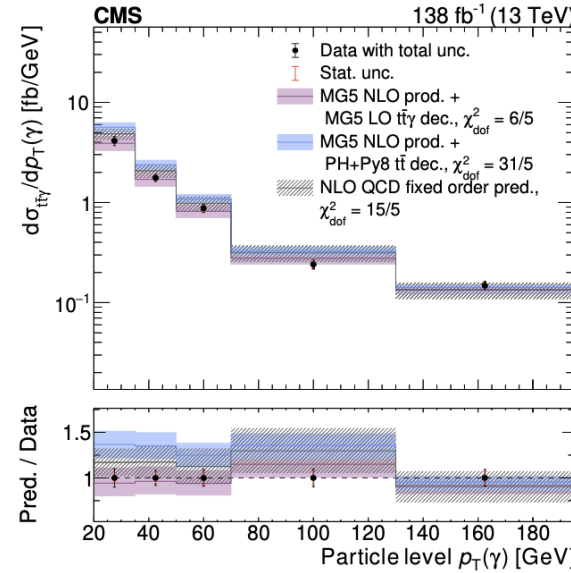
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*See Appendix A for the list of collaboration members

CMS Collaboration, JHEP 04 (2026) 086

Bevilacqua, Hartanto, Kraus, Weber, Worek JHEP 10 (2018) 158 &
JHEP 01 (2019) 188 & JHEP 03 (2020) 154
Stremmer, Worek, JHEP 08 (2023) 179

$$pp \rightarrow \ell^+ \nu_\ell \ell^- \bar{\nu}_\ell b \bar{b} \gamma$$



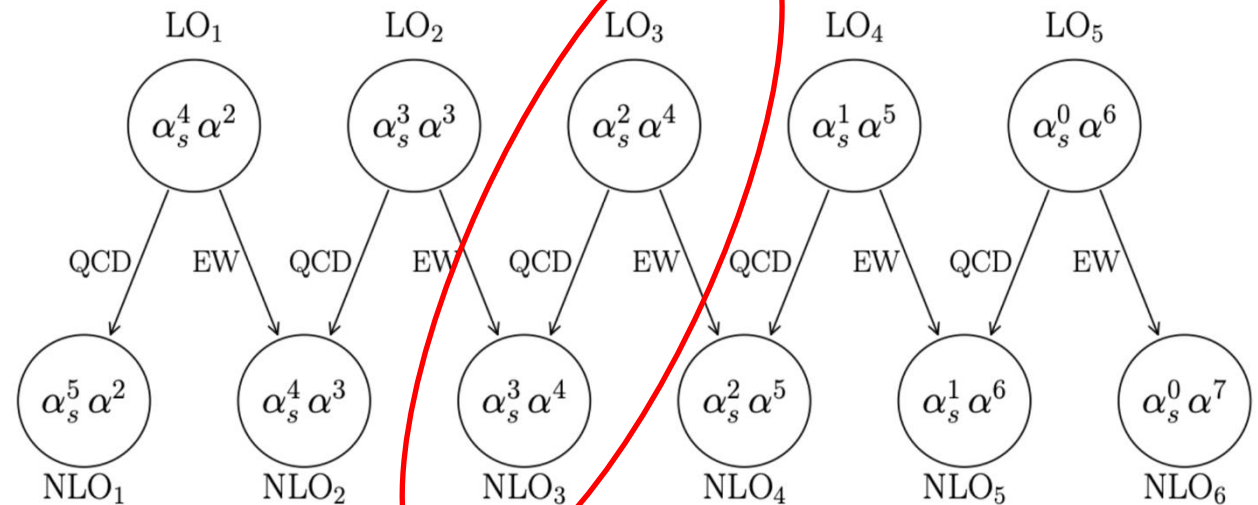
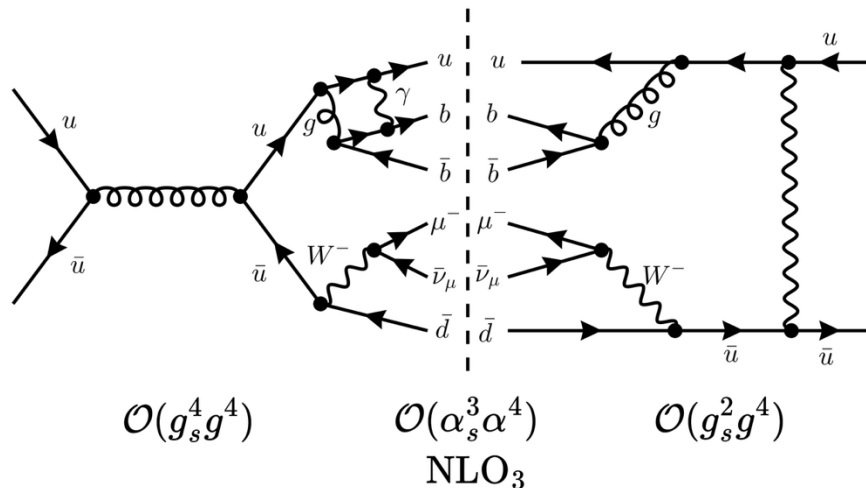
VARIOUS THEORETICAL PREDICTIONS

- FULL OFF-SHELL $PP \rightarrow TT+X$ VERSUS ON-SHELL $PP \rightarrow TT+X + PP \rightarrow TWB+X$
 - Coherent sum versus incoherent sum
 - Comparison of various approaches important
 - Full off-shell = DR + SR + NR + interferences + Breit-Wigner propagators
 - NWA = DR restricts unstable t & W to on-shell states
 - Parton-shower based predictions = $pp \rightarrow tt + X$ production @ NLO + LO decays with spin correlations
 - ✓ *Spin correlations important to probe new physics scenarios*
- UNDERSTAND VARIOUS THEORETICAL APPROACHES IS IMPORTANT AS THEY CAN IMPACT:
 - IR-safe (integrated) cross sections: Normalisation
 - IR-safe (differential) cross section distributions: Shape of distributions
 - SM parameter extraction: m_t & Γ_t
 - SM observables: Top Charge Asymmetry
 - BSM exclusion limits: $pp \rightarrow tt + \text{Dark Matter}$ with backgrounds $pp \rightarrow tt$ & $pp \rightarrow ttZ$ ($Z \rightarrow \nu\nu$)
 - New Physics Modelling: $pp \rightarrow ttH$ with anomalous couplings $\rightarrow pp \rightarrow ttH$ in SMEFT
 - Systematic uncertainties: Subtraction of $pp \rightarrow tWb$ from $pp \rightarrow tt$
 - Matching to parton showers: Resonant aware matching when NLO decays are included

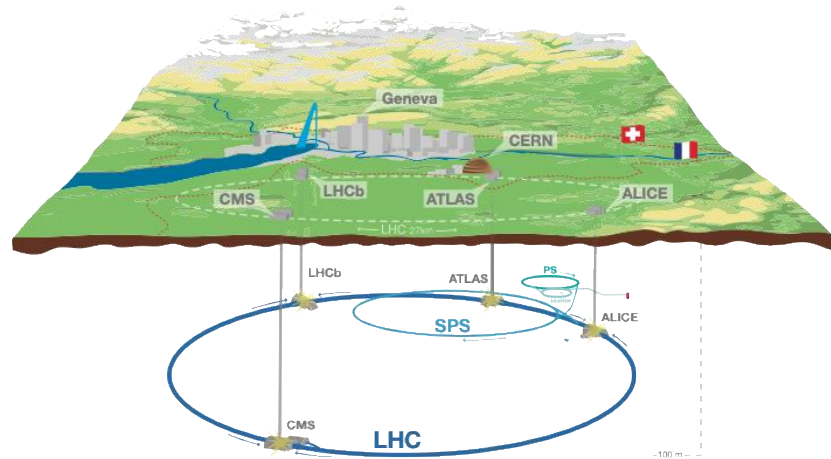
OPEN QUESTIONS & PROBLEMS

- FULL OFF-SHELL PREDICTIONS: $pp \rightarrow t\bar{t} \text{ \& } t\bar{t} + X$, $X = H, \gamma, W^\pm(\rightarrow \ell \nu_\ell), Z(\rightarrow \nu_\ell \bar{\nu}_\ell), Z(\rightarrow \ell \ell), j, b\bar{b}, W^\pm j$
 - *Multilepton final states only*
 - Combined NLO EW & NLO QCD results as well as complete NLO predictions only for a few selected cases
 - Matching to PS for $t\bar{t}$ production only $\rightarrow$ *bb4l* & only with **POWHEG**
 - Time-consuming computations requiring large computer resources & storage
 - $l+j$ top-quark decay channel only for $t\bar{t}$ $\rightarrow$ Additional problems with IR safety
 - *Fully hadronic final states are completely missing*

$$pp \rightarrow \mu^- \bar{\nu}_\mu jj b\bar{b}$$



SUMMARY

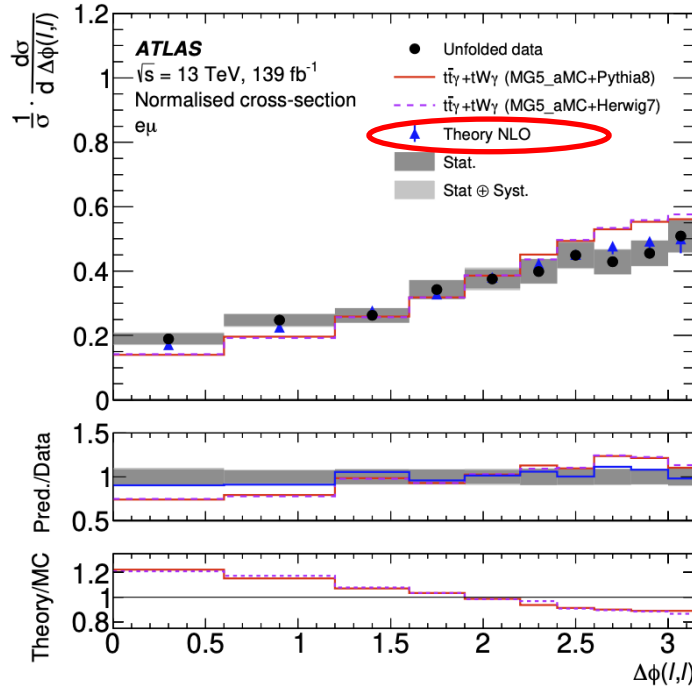


- **PROPER MODELLING OF TOP-QUARK PRODUCTION & DECAY ESSENTIAL**
 - Already now in presence of inclusive phase-space regions
- **NLO QCD** corrections to $pp \rightarrow t\bar{t} \text{ \& \> } t\bar{t} + X$
 - **FULL OFF-SHELL PREDICTIONS:**
 - ✓ $X = H, \gamma, W^\pm, Z(\rightarrow \nu_\ell \bar{\nu}_\ell), Z(\rightarrow \ell\ell), j, b\bar{b}, W^\pm j$
 - **NWA RESULTS:** $X = jj, \gamma\gamma, tt$
- **IMPORTANT**
 - Corrections to production & decays important
 - Complete off-shell effects important
 - ✓ *kinematical edges & high p_T*
 - Same phase-space regions are also sensitive to
 - ✓ EW higher-order corrections
 - ✓ Subleading contributions
 - ✓ New Physics effects
 - Photon emissions must be properly included at all stages
 - *Matching to parton showers → To be used in addition to accurate matrix-element predictions, not instead of them*
- **EVEN MORE IMPORTANT FOR**
 - Exclusive phase-space regions & HL-LHC
 - New Physics searches & Exclusion limits
 - SM parameter extraction & Various observables

BACKUP

COMPARISONS WITH LHC DATA

$$pp \rightarrow \ell^+ \nu_\ell \ell^- \bar{\nu}_\ell b \bar{b} \gamma$$

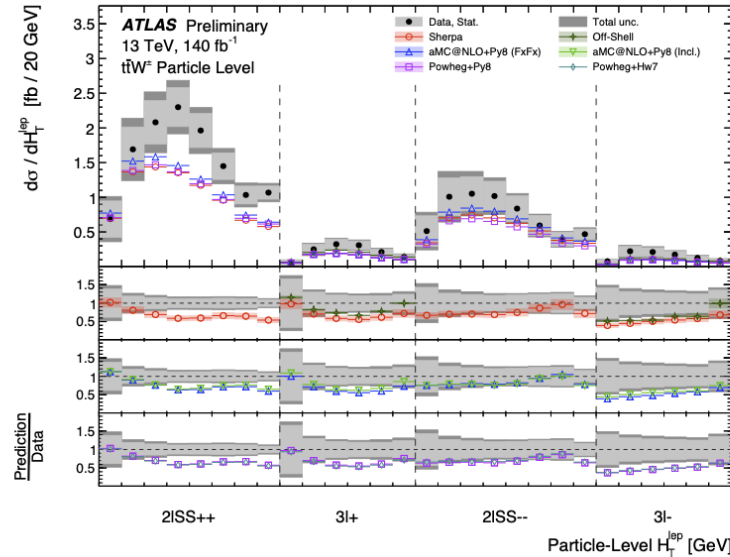


- NLO QCD full off-shell predictions for $t\bar{t}\gamma \rightarrow$ DI-LEPTON CHANNEL

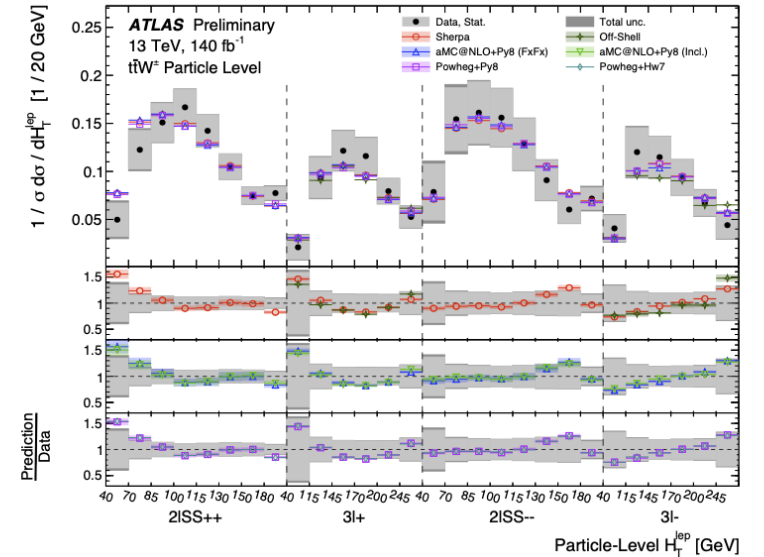
Bevilacqua, Hartanto, Kraus, Weber, Worek
 JHEP 10 (2018) 158 & JHEP 01 (2019) 188 & JHEP 03 (2020) 154

ATLAS Collaboration, JHEP 09 (2020) 049

$$pp \rightarrow \ell^+ \nu_\ell \ell^- \bar{\nu}_\ell \ell^\pm \nu_\ell b \bar{b}$$



$$H_T^{\text{lep}} = p_T^{\ell^+} + p_T^{\ell^-} + p_T^{\ell^\pm}$$



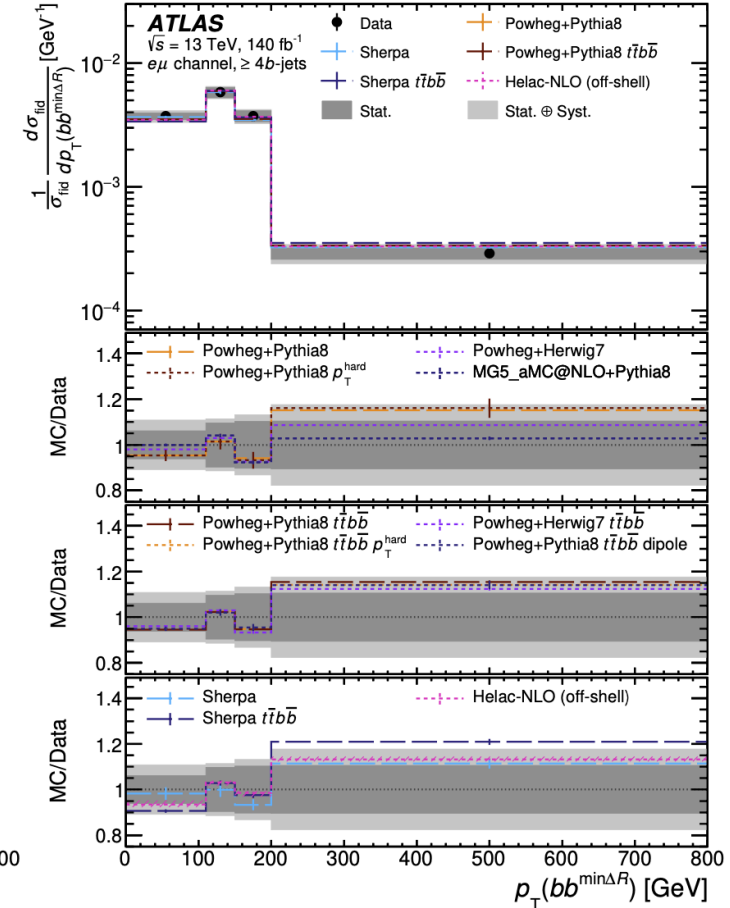
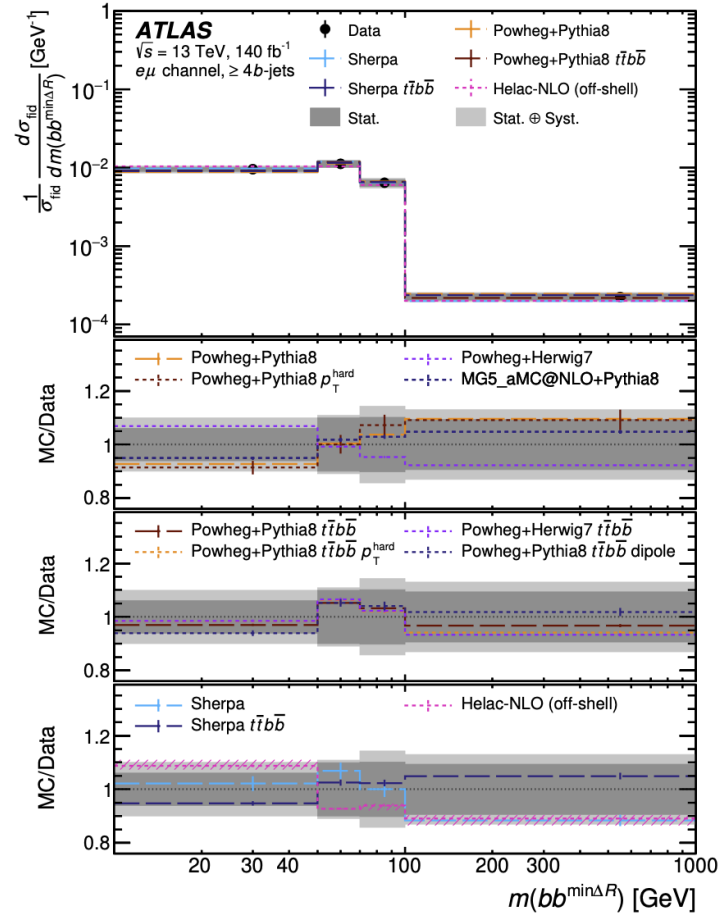
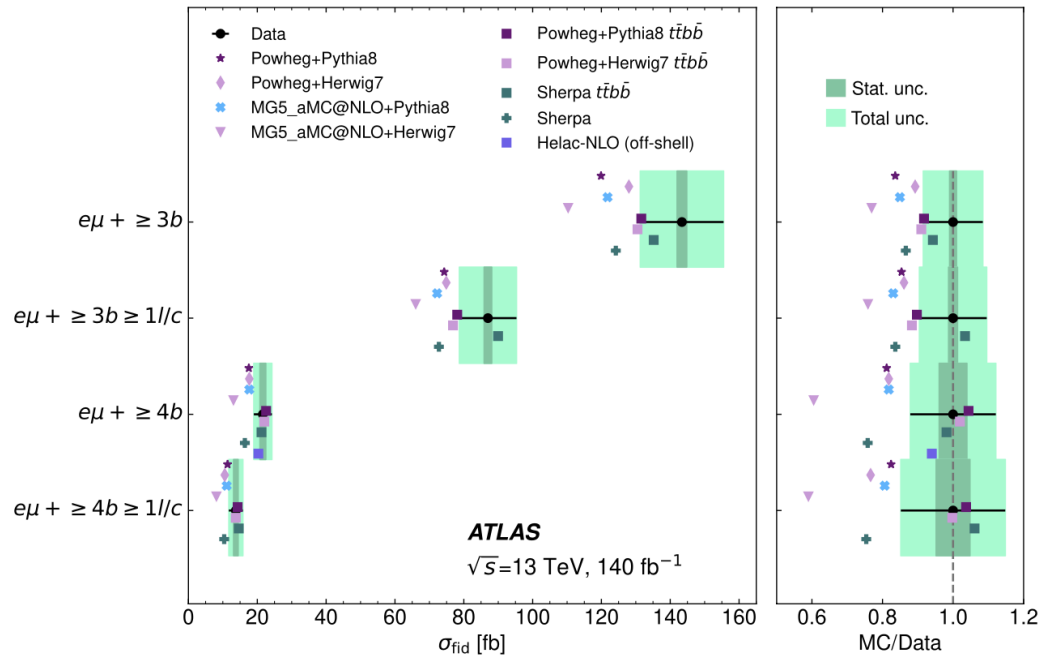
- NLO QCD full off-shell predictions for $t\bar{t}W \rightarrow$ MULTI-LEPTON CHANNEL

Bevilacqua, Bi, Hartanto, Kraus, Worek, JHEP 08 (2020) 043
 Bevilacqua, Bi, Hartanto, Kraus, Nasufi, Worek, Eur. Phys. J. C 81 (2021) 7, 675
 Bevilacqua, Bi, Cordero, Hartanto, Kraus, Nasufi, Reina, Worek, Phys. Rev. D 105 (2022) 1, 014018

ATLAS Collaboration, JHEP 05 (2024) 131

COMPARISONS WITH LHC DATA

$$pp \rightarrow \ell^+ \nu_\ell \ell^- \bar{\nu}_\ell b \bar{b} b \bar{b}$$



- NLO QCD full off-shell predictions for $t\bar{t}b\bar{b} \rightarrow$ DI-LEPTON CHANNEL

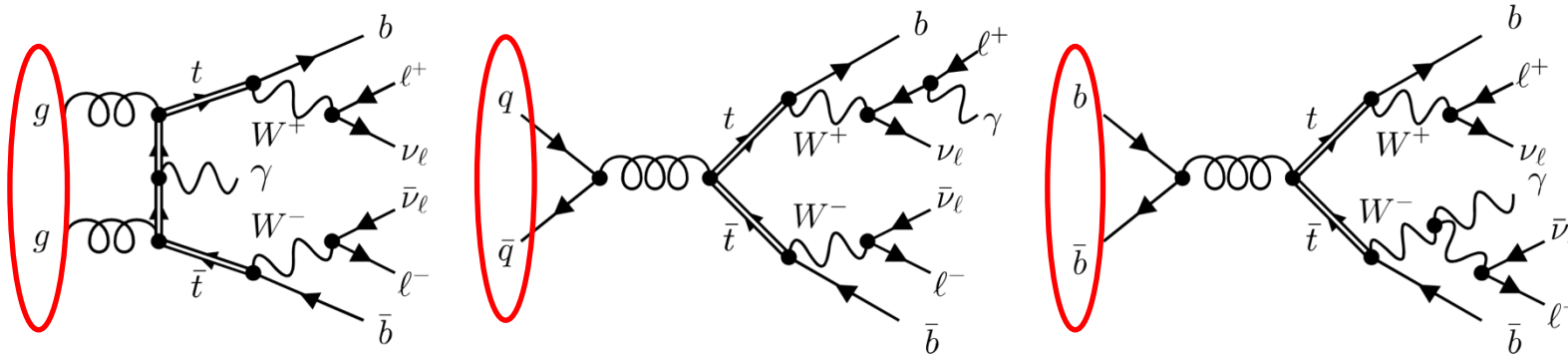
Bevilacqua, Bi, Hartanto, Kraus, Lupattelli, Worek, JHEP 08 (2021) 008 & Phys.Rev.D 107 (2023) 1, 014028

ATLAS Collaboration, JHEP 01 (2025) 068

DEFINITION OF LO_1

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$$

- LO_1 : Dominant contributions at $\mathcal{O}(\alpha_s^2 \alpha^{4+n_\gamma})$ with n_γ being number of photons appearing @ Born-level



- Typical QCD production of top-quark pair with photons with following partonic subprocesses

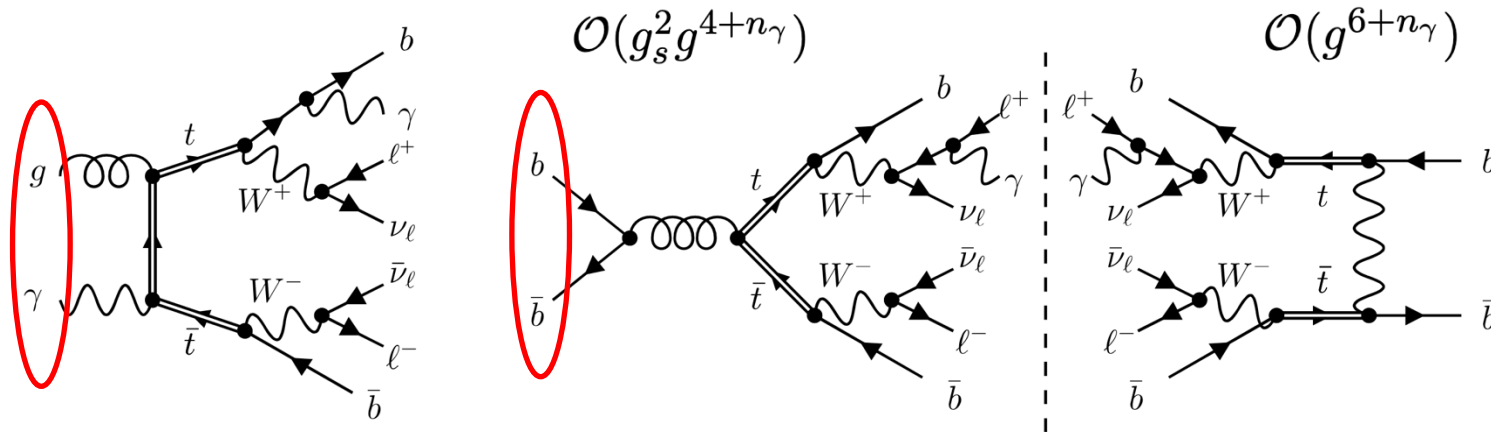
$$gg \rightarrow \ell^+ \nu_\ell \ell^- \bar{\nu}_\ell b \bar{b} \gamma(\gamma),$$

$$q\bar{q}/\bar{q}q \rightarrow \ell^+ \nu_\ell \ell^- \bar{\nu}_\ell b \bar{b} \gamma(\gamma), \quad b\bar{b}/\bar{b}b \rightarrow \ell^+ \nu_\ell \ell^- \bar{\nu}_\ell b \bar{b} \gamma(\gamma),$$

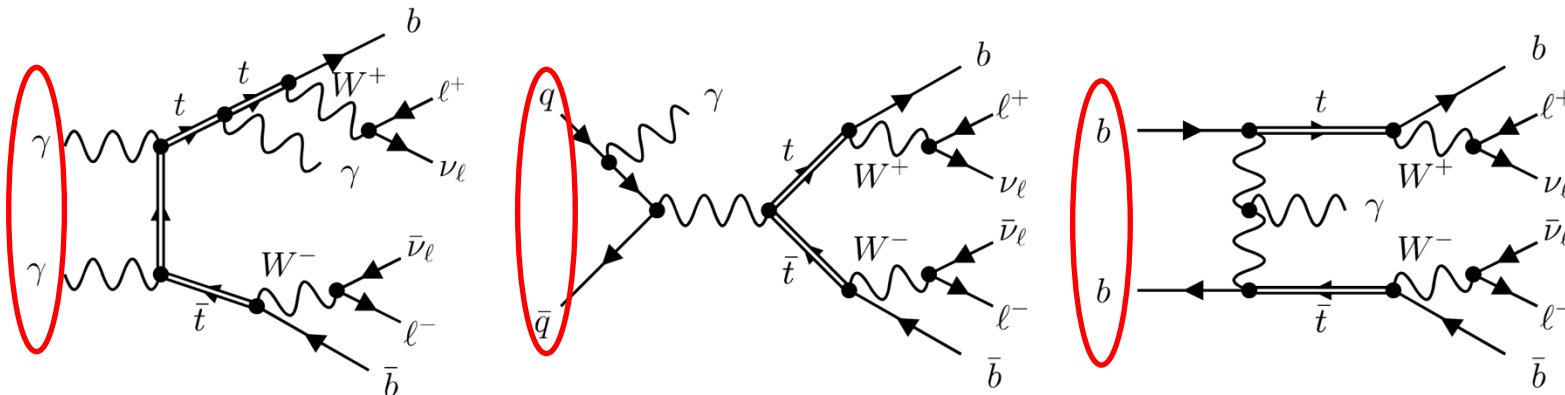
DEFINITION OF LO_2 & LO_3

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$$

- LO_2 : Contributions at $\mathcal{O}(\alpha_s^1 \alpha^{5+n_\gamma})$



- LO_3 : Purely EW induced production of top-quark pair at $\mathcal{O}(\alpha^{6+n_\gamma})$
 - Suppressed by power coupling & without gluon PDFs



- Interference between gluon mediated diagrams with Z/γ mediated ones vanishes due to colour for qq initial state
- Interference does not vanish for $b\bar{b}$ due to t -channel diagrams with intermediate W boson
- When CKM matrix is not diagonal these contributions for qq initial state can also be non-zero but are CKM-suppressed

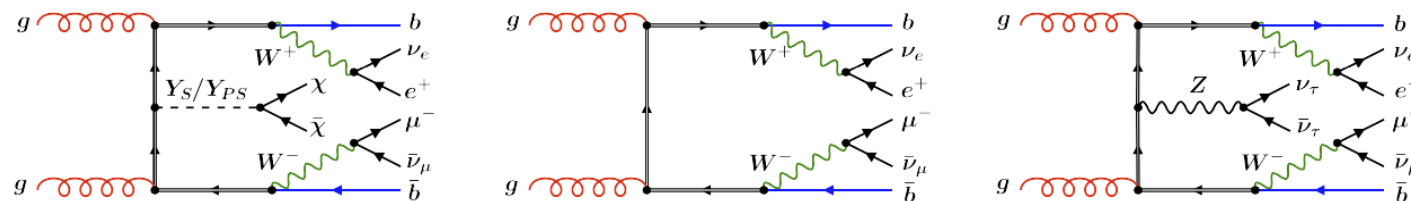
$$\text{LO} = \text{LO}_1 + \text{LO}_2 + \text{LO}_3$$

APPLICATION: BSM EXCLUSION LIMITS

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \chi \chi$$

- BSM $\rightarrow$ Kinematical edges & high p_T regions
- $t\bar{t} + DM \rightarrow$ Top quark backgrounds: $t\bar{t}$ & $t\bar{t}Z$
- OBSERVABLE $\rightarrow M_{T2,W}$ & $M_{T2,t}$ & p_T^{miss}

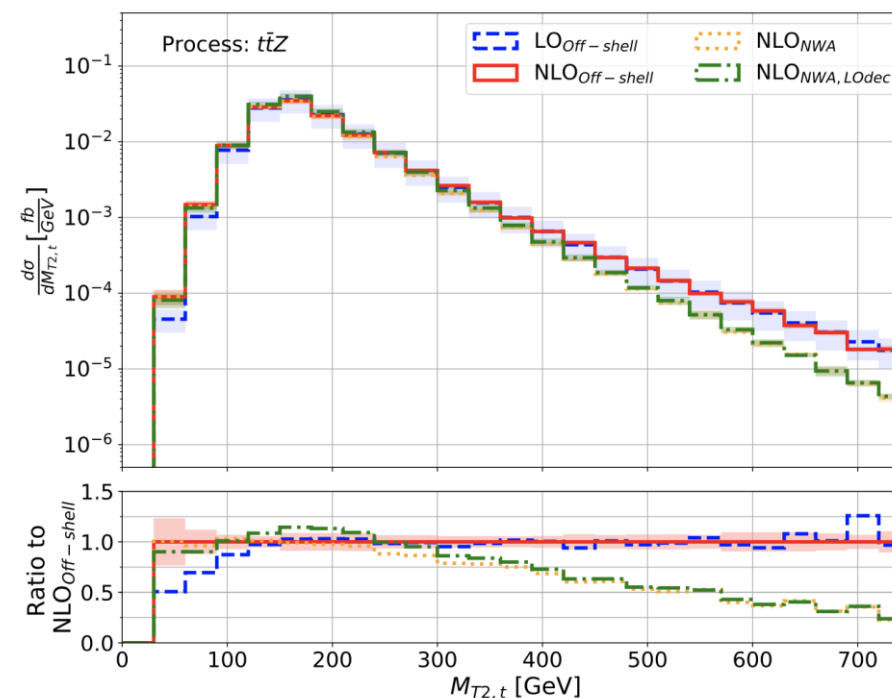
$$pp \rightarrow t\bar{t} + Y_{S/PS} \rightarrow W^+ W^- b \bar{b} + Y_{S/PS} \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} + \chi \chi$$



Before & after applying additional cuts

Process	Order	Scale	σ_{uncut} [fb]	σ_{cut} [fb]	$\sigma_{\text{cut}}/\sigma_{\text{uncut}}$	Events for $L = 300 \text{ fb}^{-1}$
$t\bar{t}$ NWA	LO	$H_T/4$	1061	0	0.0%	0
	LO	$E_T/4$	984	0	0.0%	0
	LO	m_t	854	0	0.0%	0
	NLO	$H_T/4$	1097	0	0.0%	0
	NLO, LO dec	$H_T/4$	1271	0	0.0%	0
$t\bar{t}Z$ NWA	LO	$H_T/3$	0.1223	0.0130	11%	47
	LO	$E_T/3$	0.1052	0.0116	11%	42
	LO	$m_t + m_Z/2$	0.1094	0.0134	12%	48
	NLO	$H_T/3$	0.1226	0.0130	11%	47
	NLO, LO dec	$H_T/3$	0.1364	0.0140	10%	50
$t\bar{t}$ Off-shell	LO	$H_T/4$	1067	0.0144	0.0013%	17
	LO	$E_T/4$	989	0.0131	0.0013%	16
	LO	m_t	861	0.0150	0.0017%	18
	NLO	$H_T/4$	1101	0.0156	0.0014%	19
$t\bar{t}Z$ Off-shell	LO	$H_T/3$	0.1262	0.0135	11%	49
	LO	$E_T/3$	0.1042	0.0115	11%	41
	LO	$m_t + m_Z/2$	0.1135	0.0140	12%	50
	NLO	$H_T/3$	0.1269	0.0134	11%	48

- After cuts 25% of events come from $t\bar{t}$
- NLO smaller uncertainties w.r.t LO, NLO + LO decays



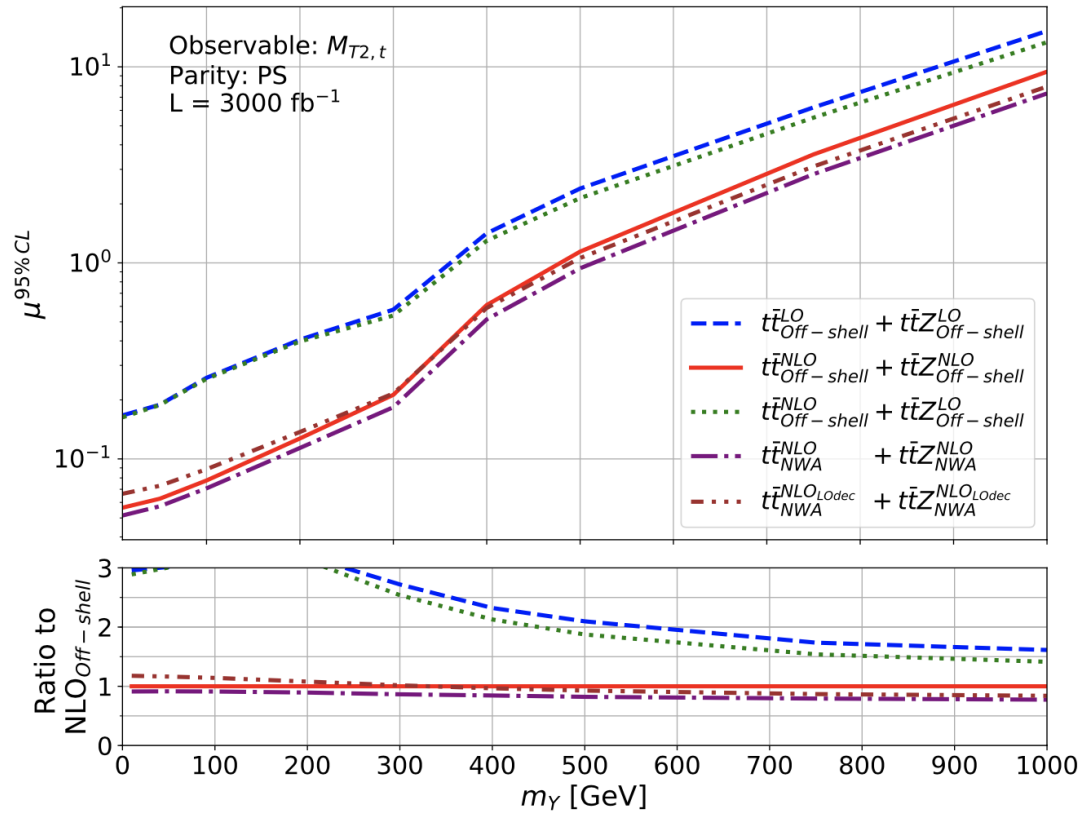
Herrmann, Worek, Eur. Phys. J. C 81 (2021) 11, 1029

APPLICATION: BSM EXCLUSION LIMITS

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \chi \chi$$

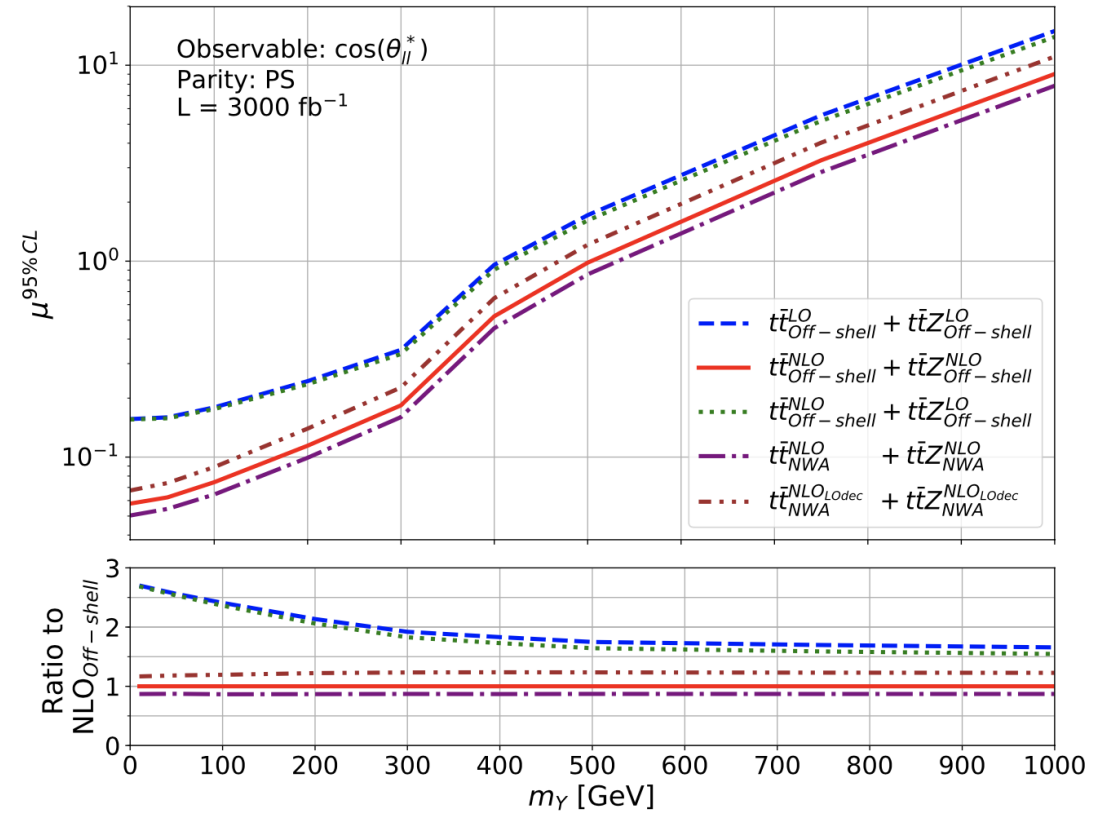
- Comparison of signal strength exclusion limits

Herrmann, Worek, Eur. Phys. J. C 81 (2021) 11, 1029



$$M_{T2,t}^2 = \min_{\substack{\mathbf{p}_T^{\nu_1} + \mathbf{p}_T^{\nu_2} \\ = \mathbf{p}_{T,miss}}} [\max\{M_T^2(\mathbf{p}_T^{(lb)_1}, \mathbf{p}_T^{\nu_1}),$$

$$M_T^2(\mathbf{p}_T^{(lb)_2}, \mathbf{p}_T^{\nu_2})\}]$$



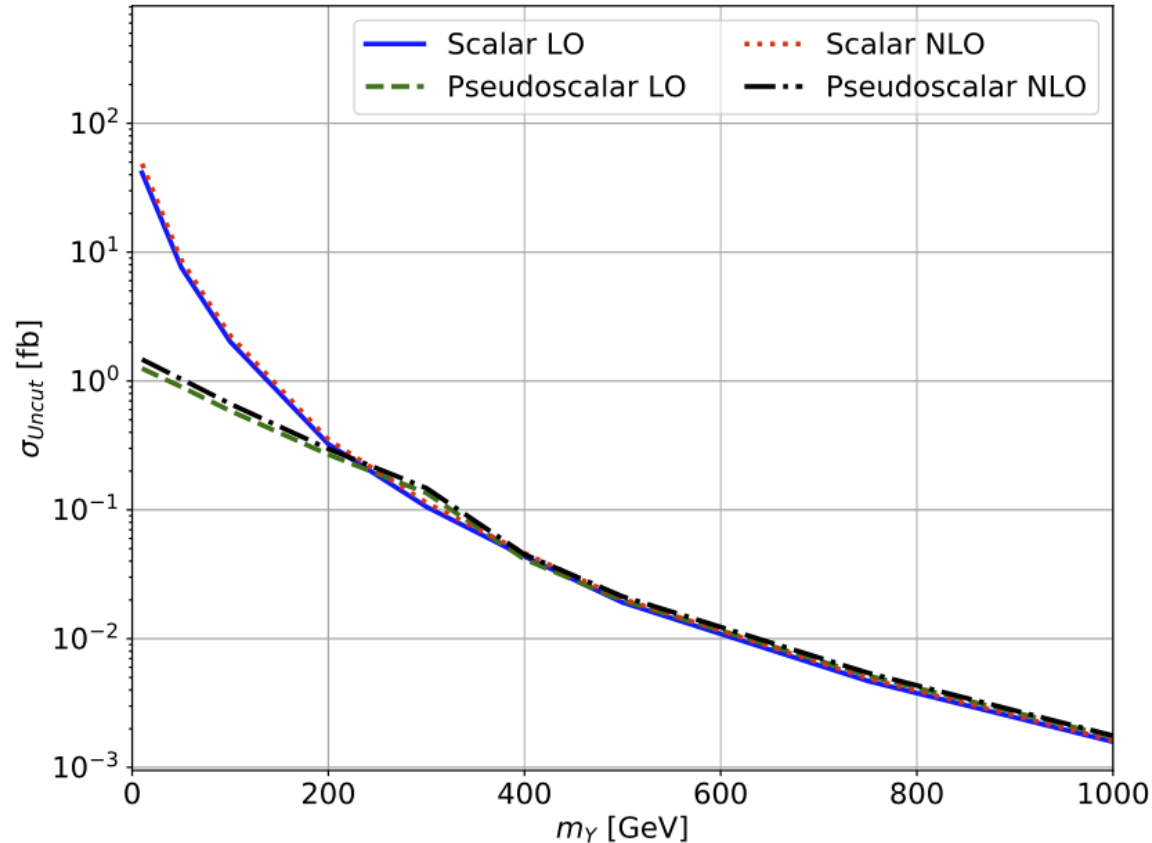
$$\cos(\theta_{ll}^*) = \tanh(|\eta_{l_1} - \eta_{l_2}|/2)$$

$$M_T^2(\mathbf{p}_T^{(lb)_i}, \mathbf{p}_T^{\nu_i}) = M_{(lb)_i}^2 + 2(E_T^{(lb)_i} E_T^{\nu_i} - \mathbf{p}_T^{(lb)_i} \cdot \mathbf{p}_T^{\nu_i})$$

APPLICATION: YUKAWA COUPLING

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} H$$

Herrmann, Worek, Eur. Phys. J. C 81 (2021) 11, 1029



- Cross section for $pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu\chi\bar{\chi}$ with scalar & pseudoscalar mediators depending on the mass m_γ

- Production of pseudoscalar in association with top quarks is suppressed compared to scalar for masses below ~ 200 GeV if the two couplings $\kappa_{Ht\bar{t}} = \kappa_{At\bar{t}} = 1$

Haisch, Pani, Polesello, JHEP 02 (2017) 131

- This difference can be understood when looking at $t \rightarrow t + H/A$ fragmentation functions

$$f_{t \rightarrow t+H}(x) = \frac{\kappa_{Ht\bar{t}}^2}{(4\pi)^2} \left[\frac{4(1-x)}{x} + x \ln \left(\frac{s}{m_t^2} \right) \right]$$

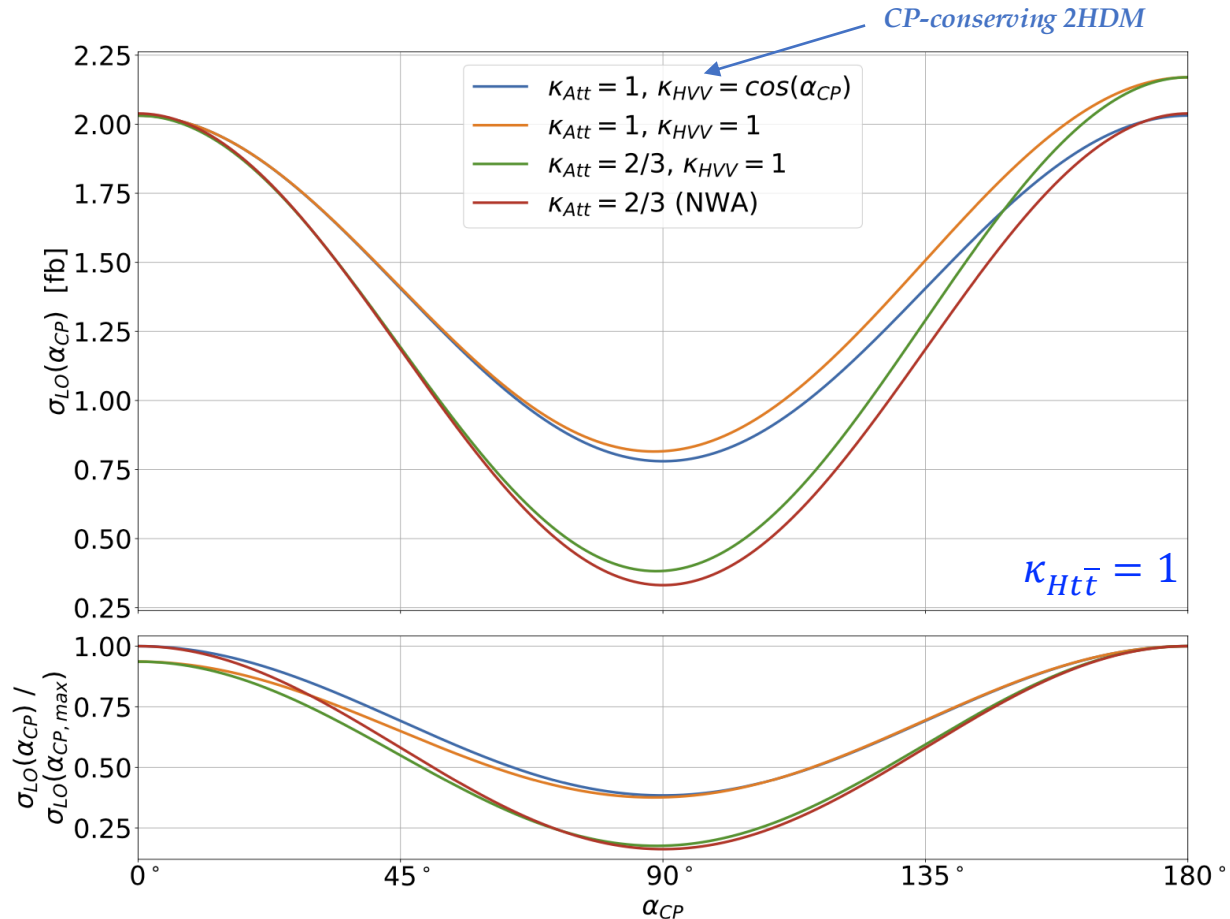
$$f_{t \rightarrow t+A}(x) = \frac{\kappa_{At\bar{t}}^2}{(4\pi)^2} \left[x \ln \left(\frac{s}{m_t^2} \right) \right],$$

Dawson, Reina, Phys. Rev. D 57 (1998) 5851

- x momentum fraction that Higgs boson carries
- Scalar fragmentation function has additional $1/x$
- Enhanced production of soft scalar compared to pseudoscalars

APPLICATION: YUKAWA COUPLING

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} H$$



- Cross sections in NWA symmetric with respect to $\alpha_{CP} \rightarrow \pi - \alpha_{CP}$
- Equivalent to changing sign of Y_t
- In full off-shell case symmetry is present if we set $\kappa_{HVV}(\alpha_{CP}) = \cos(\alpha_{CP})$
- Symmetry is broken if we take $\kappa_{HVV} = 1$
- **Interference:** Higgs boson radiated off $W/Z \Rightarrow$ **SR & NR** $\Rightarrow$ Higgs boson emitted top quarks $\Rightarrow$ **DR & SR**
 - **CP-even**
 - **CP-mixed**
 - **CP-odd**

APPLICATION: TOP QUARK CHARGE ASYMMETRY

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu e^+ \nu_e b \bar{b}$$

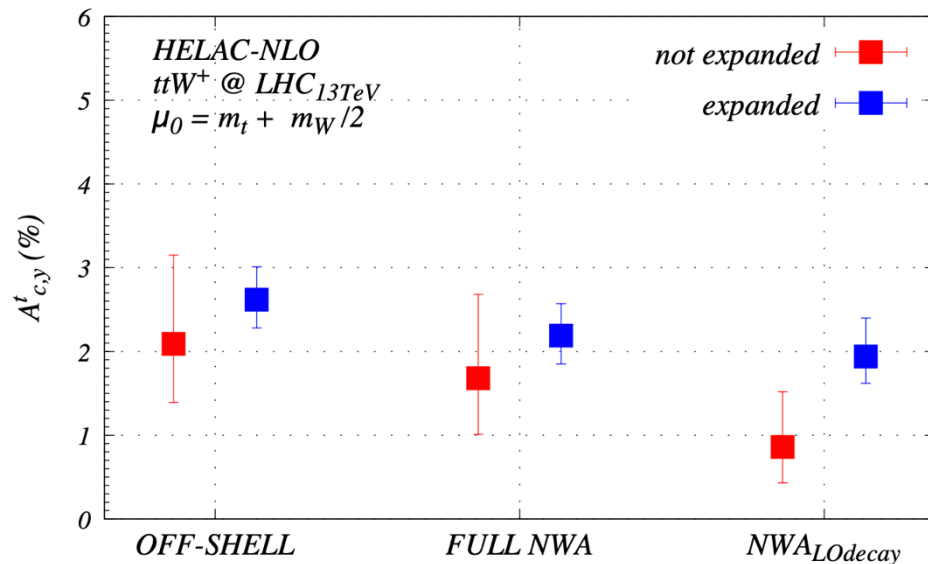
Searching for more precise observables

Bevilacqua, Bi, Hartanto, Kraus, Nasufi, Worek, Eur. Phys. J. C 81 (2021) 7, 675

$$A_c^t = \frac{\sigma_{\text{bin}}^+ - \sigma_{\text{bin}}^-}{\sigma_{\text{bin}}^+ + \sigma_{\text{bin}}^-}, \quad \sigma_{\text{bin}}^\pm = \int \theta(\pm \Delta|y|) \theta_{\text{bin}} d\sigma$$

$$\Delta|y| = |y_t| - |y_{\bar{t}}|$$

- Asymmetry larger than for $pp \rightarrow t\bar{t}$
- Top quark momenta must be reconstructed
- Scale setting not important $\rightarrow$ Fixed & dynamical scale choice gives similar results
- Top-quark modelling important



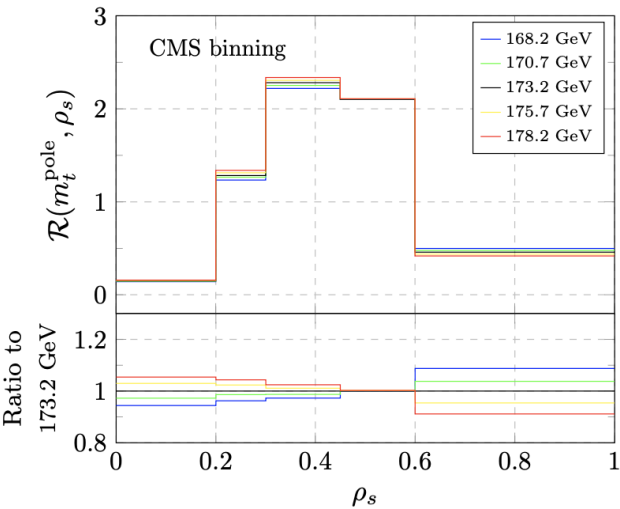
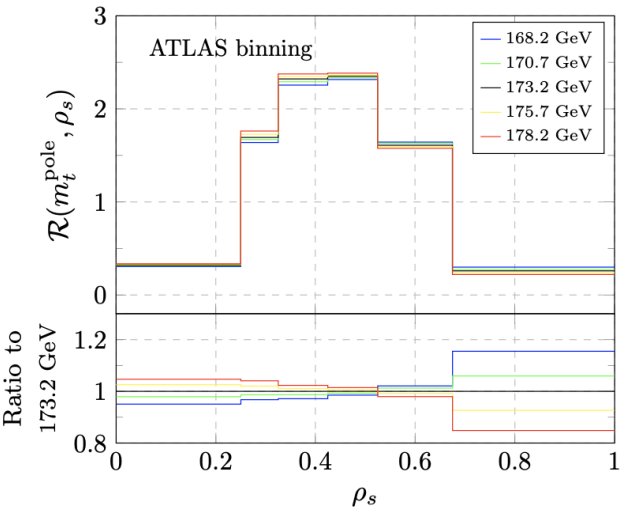
- A_c^t charge asymmetry @ NLO for $pp \rightarrow t\bar{t}W^+$

$t\bar{t}W^+$	OFF-SHELL	FULL NWA	NWA _{LOdecay}
$\mu_0 = H_T/3$			
$A_{c,y}^t$ [%]	$2.36(8)^{+1.19(50\%)}_{-0.77(33\%)}$	$1.93(5)^{+1.23(64\%)}_{-0.72(37\%)}$	$1.11(3)^{+0.55(49\%)}_{-0.53(48\%)}$
$A_{c,exp,y}^t$ [%]	$2.66(10)^{+0.38(14\%)}_{-0.34(13\%)}$	$2.20(5)^{+0.45(20\%)}_{-0.31(14\%)}$	$2.08(5)^{+0.24(11\%)}_{-0.40(19\%)}$
$t\bar{t}W^+$	OFF-SHELL	FULL NWA	NWA _{LOdecay}
$\mu_0 = m_t + m_W/2$			
$A_{c,y}^t$ [%]	$2.09(8)^{+1.06(51\%)}_{-0.70(33\%)}$	$1.68(4)^{+1.00(60\%)}_{-0.67(40\%)}$	$0.86(3)^{+0.66(77\%)}_{-0.43(50\%)}$
$A_{c,exp,y}^t$ [%]	$2.62(10)^{+0.39(15\%)}_{-0.34(13\%)}$	$2.19(4)^{+0.38(17\%)}_{-0.34(16\%)}$	$1.94(5)^{+0.46(24\%)}_{-0.32(16\%)}$

APPLICATION: TOP QUARK MASS

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} j$

$$\mathcal{R}(m_t^{pole}, \rho_s) = \frac{1}{\sigma_{t\bar{t}j}} \frac{d\sigma_{t\bar{t}j}}{d\rho_s}(m_t^{pole}, \rho_s), \quad \text{with} \quad \rho_s = \frac{2m_0}{M_{t\bar{t}j}}$$



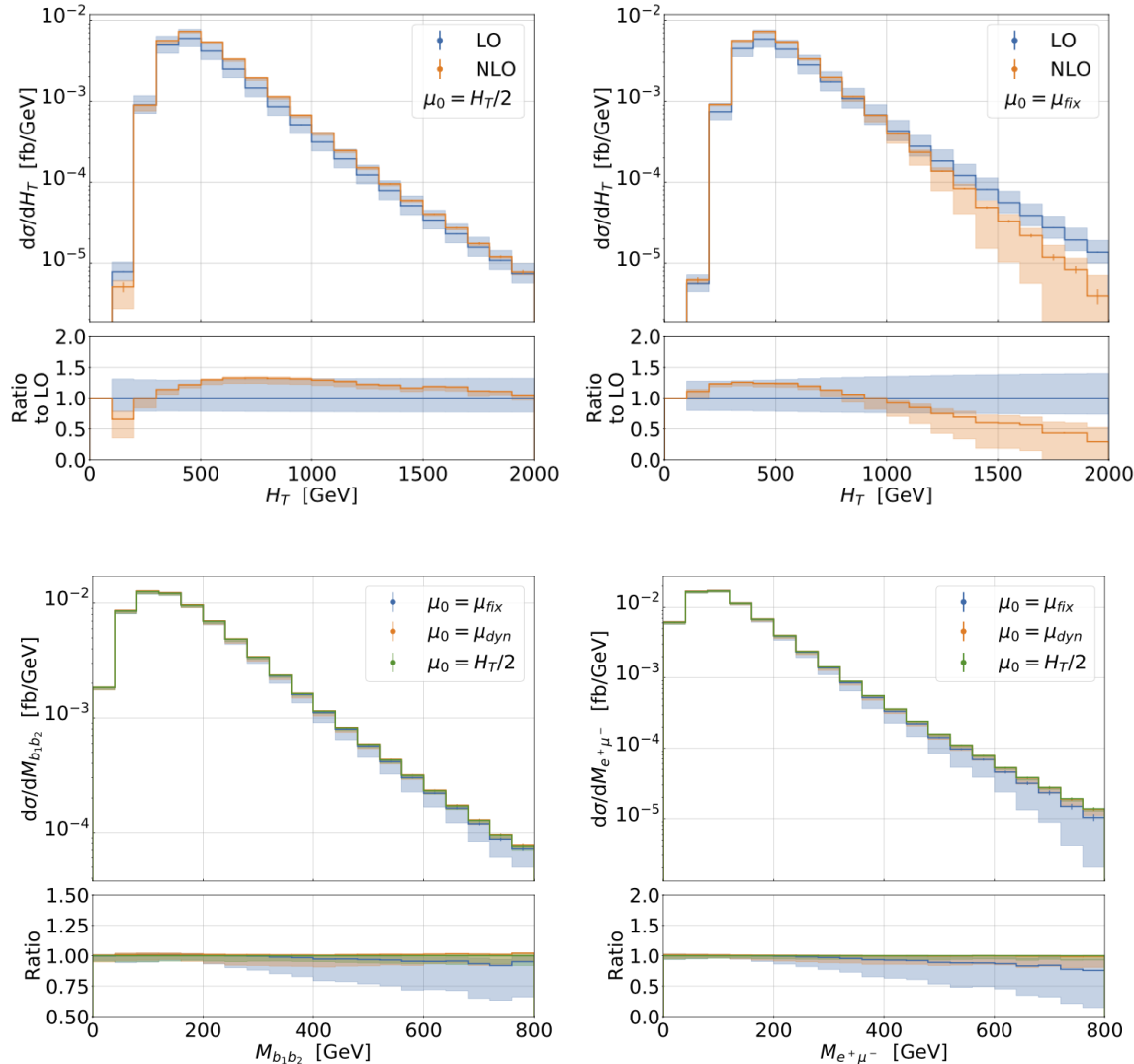
Theory, NLO QCD CT14 PDF	$m_t^{out} \pm \delta m_t^{out}$ [GeV]	Averaged $\chi^2/\text{d.o.f.}$	Probability $p\text{-value}$	$m_t^{in} - m_t^{out}$ [GeV]
31 bins				
Full, $\mu_0 = H_T/2$	173.09 ± 0.42	1.04	0.41 (0.8 σ)	+0.11
Full, $\mu_0 = E_T/2$	172.45 ± 0.39	1.12	0.30 (1.0 σ)	+0.75
Full, $\mu_0 = m_t$	173.76 ± 0.40	1.87	0.003 (3.0 σ)	-0.56
NWA, $\mu_0 = m_t$	175.65 ± 0.31	2.99	$7 \cdot 10^{-8}$ (5.4 σ)	-2.45
NWA _{Prod.} , $\mu_0 = m_t$	169.59 ± 0.30	3.10	$2 \cdot 10^{-8}$ (5.6 σ)	+3.61
5 bins				
Full, $\mu_0 = H_T/2$	173.08 ± 0.40	0.94	0.44 (0.8 σ)	+0.12
Full, $\mu_0 = E_T/2$	172.48 ± 0.38	1.58	0.18 (1.3 σ)	+0.72
Full, $\mu_0 = m_t$	173.75 ± 0.40	6.76	$2 \cdot 10^{-5}$ (4.3 σ)	-0.55
NWA, $\mu_0 = m_t$	175.49 ± 0.30	5.31	$2 \cdot 10^{-4}$ (3.7 σ)	-2.29
NWA _{Prod.} , $\mu_0 = m_t$	169.39 ± 0.47	3.42	$8 \cdot 10^{-3}$ (2.6 σ)	+3.81
ATLAS binning				
Full, $\mu_0 = H_T/2$	173.06 ± 0.44	0.97	0.44 (0.8 σ)	+0.14
Full, $\mu_0 = E_T/2$	172.36 ± 0.44	1.38	0.23 (1.2 σ)	+0.84
Full, $\mu_0 = m_t$	173.84 ± 0.42	5.12	$1 \cdot 10^{-4}$ (3.9 σ)	-0.64
NWA, $\mu_0 = m_t$	175.23 ± 0.37	5.28	$7 \cdot 10^{-5}$ (4.0 σ)	-2.03
NWA _{Prod.} , $\mu_0 = m_t$	169.43 ± 0.50	2.61	0.02 (2.3 σ)	+3.77
CMS binning				
Full, $\mu_0 = H_T/2$	173.09 ± 0.50	0.96	0.43 (0.8 σ)	+0.11
Full, $\mu_0 = E_T/2$	172.22 ± 0.48	1.32	0.26 (1.1 σ)	+0.98
Full, $\mu_0 = m_t$	174.02 ± 0.46	6.57	$3 \cdot 10^{-5}$ (4.2 σ)	-0.82
NWA, $\mu_0 = m_t$	175.74 ± 0.34	6.00	$8 \cdot 10^{-5}$ (3.9 σ)	-2.54
NWA _{Prod.} , $\mu_0 = m_t$	170.22 ± 0.53	2.19	0.07 (1.8 σ)	+2.98

- Sensitivity to scale setting & top quark modelling

NLO QCD CORRECTIONS & SCALE SETTING

Stremmer, Worek, JHEP 02 (2022) 196

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} H$$



FIXED SCALE CHOICE

- Perturbative instabilities in $\sim$ TeV regions
- LO & NLO uncertainties band do not overlap
- Scale uncertainties @ NLO larger than @ LO
- For some scale choices NLO results negative

DYNAMICAL SCALE CHOICE

- Stabilizes tails
- NLO uncertainties bands within LO ones

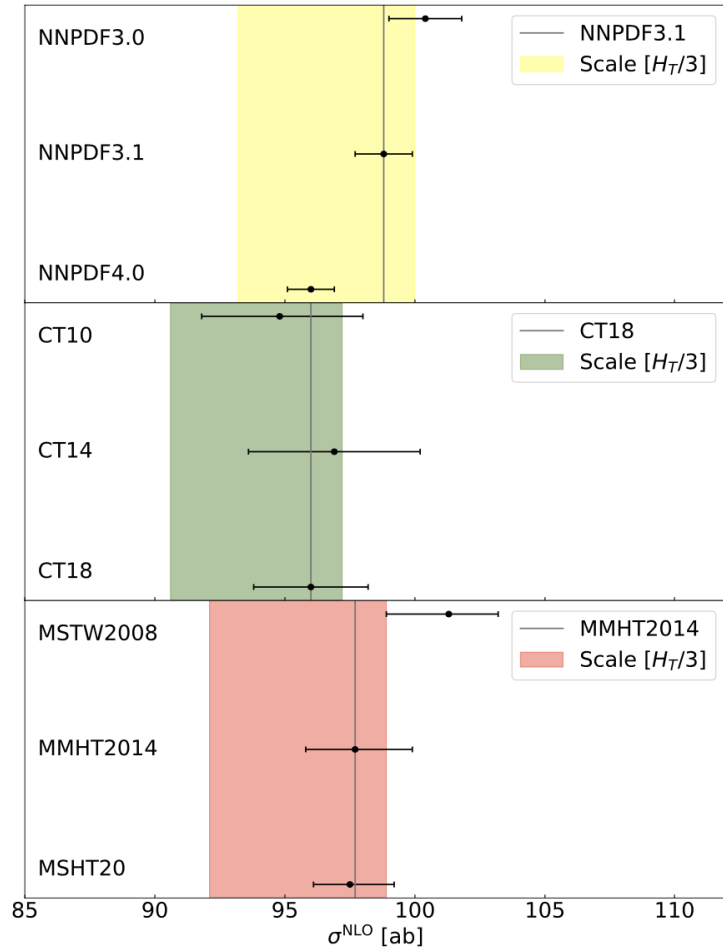
$$H_T = p_{T,b_1} + p_{T,b_2} + p_{T,e^+} + p_{T,\mu^-} + p_{T,miss} + p_{T,H}$$

$$\mu_{dyn} = (m_{T,t} m_{T,\bar{t}} m_{T,H})^{\frac{1}{3}} \quad m_T = \sqrt{m^2 + p_T^2}$$

$$\mu_{fix} = m_t + \frac{m_H}{2} = 236 \text{ GeV}$$

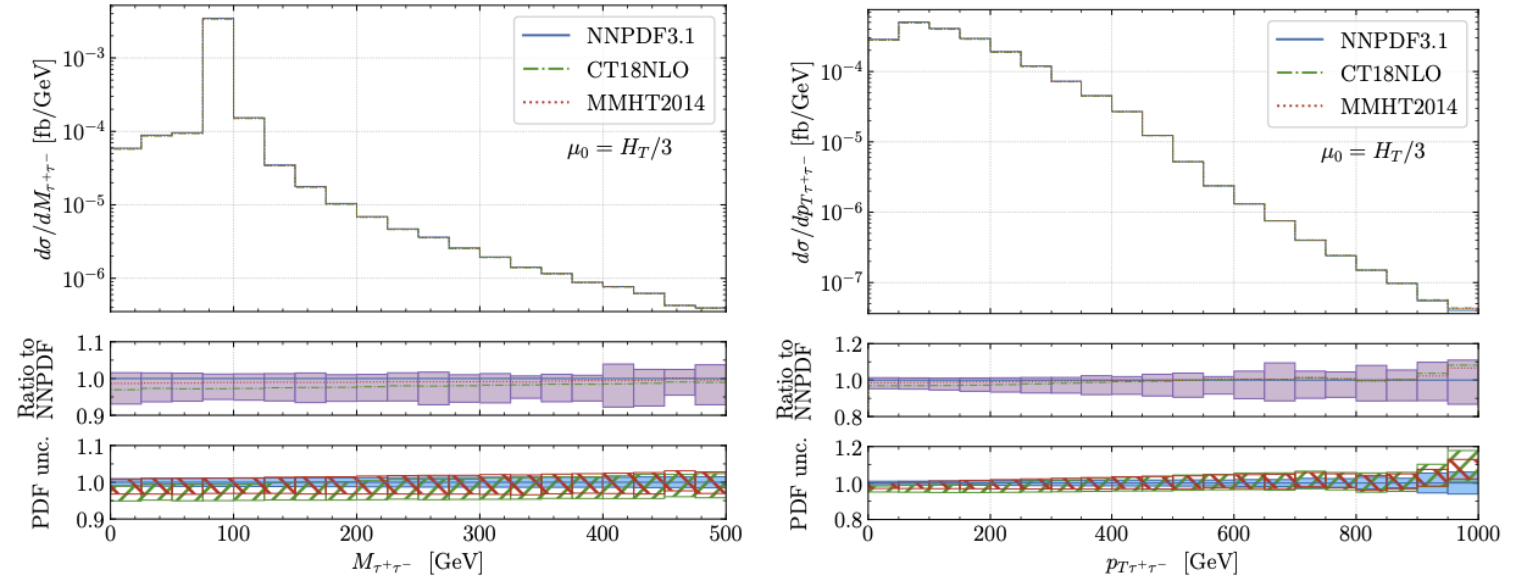
PDF UNCERTAINTIES

Bevilacqua, Hartanto, Kraus, Nasufi, Worek, JHEP 08 (2022) 060



INTEGRATED LEVEL

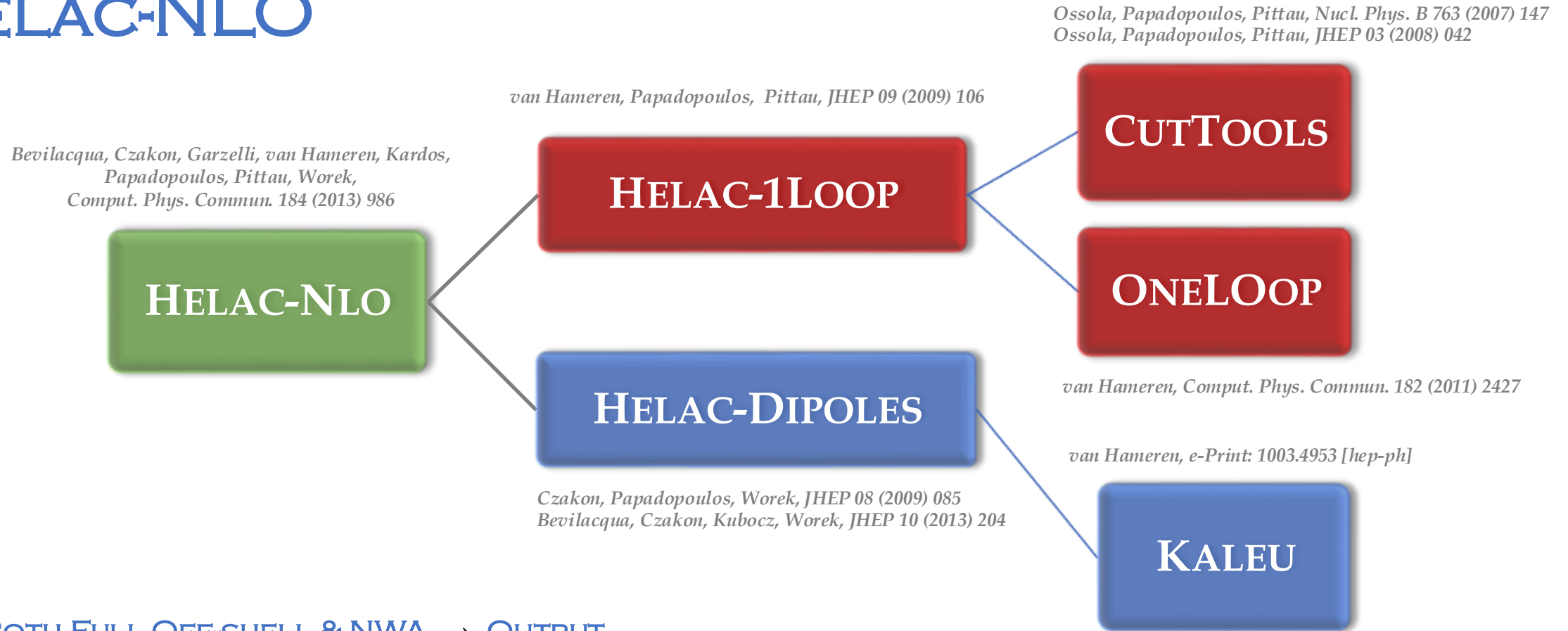
$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \tau^+ \tau^-$$



DIFFERENTIAL LEVEL

- PDF uncertainties for CT18 & MMHT14 similar
- Factor of 2 larger than PDF uncertainties for NNPDF3.1
- *PDF uncertainties smaller than scale variation → But are not constant over the phase space and can reach 10% for large p_T*

HELAC-NLO



■ BOTH FULL OFF-SHELL & NWA → OUTPUT

- Predictions stored as partially unweighted “events” → *ROOT-Ntuples Files* & *Les Houches Files*
- Each “event” provided with supplementary matrix element & PDF information
- Results for different scale settings & PDF choices by can be obtained by reweighting
- Different observables and/or binning can be provided + more exclusive cuts → With caveat

VARIOUS PHASE – SPACE REGIONS

- 3 different resonance histories $\Rightarrow$ Resolved jet at NLO gives 9 in total

(i)	$t = W^+(\rightarrow e^+\nu_e)b$	and	$\bar{t} = W^-(\rightarrow \mu^-\bar{\nu}_\mu)\bar{b}$,
(ii)	$t = W^+(\rightarrow e^+\nu_e)b\gamma$	and	$\bar{t} = W^-(\rightarrow \mu^-\bar{\nu}_\mu)\bar{b}$,
(iii)	$t = W^+(\rightarrow e^+\nu_e)b$	and	$\bar{t} = W^-(\rightarrow \mu^-\bar{\nu}_\mu)\bar{b}\gamma$

$$pp \rightarrow e^+\nu_e\mu^-\bar{\nu}_\mu b\bar{b}\gamma$$

Bevilacqua, Hartanto, Kraus, Weber, Worek, JHEP 03 (2020) 154

- Compute for each history Q and pick one that minimizes Q

$$Q = |M(t) - m_t| + |M(\bar{t}) - m_t|$$

- DOUBLE-RESONANT (DR)

$$|M(t) - m_t| < n\Gamma_t, \quad \text{and} \quad |M(\bar{t}) - m_t| < n\Gamma_t$$

- TWO SINGLE-RESONANT REGIONS (SR)

$$|M(t) - m_t| < n\Gamma_t, \quad \text{and} \quad |M(\bar{t}) - m_t| > n\Gamma_t$$

$$|M(t) - m_t| > n\Gamma_t, \quad \text{and} \quad |M(\bar{t}) - m_t| < n\Gamma_t$$

- NON-RESONANT REGION (NR)

$$|M(t) - m_t| > n\Gamma_t, \quad \text{and} \quad |M(\bar{t}) - m_t| > n\Gamma_t$$

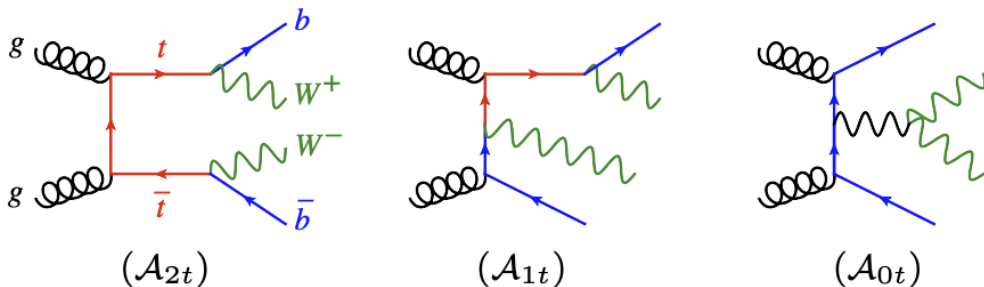
- BOUNDARY PARAMETER

- Determines size of resonant region for each reconstructed top quark
- $n = 5, 10, 15$
- For $n = 15$

$$M(t) \in (152.9, 193.5) \text{ GeV}$$

TWB

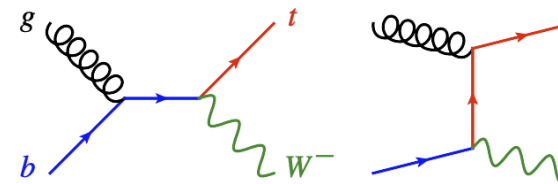
Demartin, Maier, Maltoni, Mawatari, Zaro, Eur. Phys. J. C 77 (2017) 1, 34



- *DS (diagram subtraction):*

$$|\mathcal{A}_{tWb}|_{\text{DS}}^2 = |\mathcal{A}_{1t} + \mathcal{A}_{2t}|^2 - \mathcal{C}_{2t},$$

- Local subtraction term $\mathcal{C}_{2t}$ by definition must cancel exactly the resonant matrix element $|\mathcal{A}_{2t}|^2$ when the kinematics is exactly on top of the resonant pole
- Be gauge invariant
- Decrease quickly away from the resonant region



- Squared matrix element for producing tWb

$$\begin{aligned} |\mathcal{A}_{tWb}|^2 &= |\mathcal{A}_{1t} + \mathcal{A}_{2t}|^2 \\ &= |\mathcal{A}_{1t}|^2 + 2\text{Re}(\mathcal{A}_{1t}\mathcal{A}_{2t}^*) + |\mathcal{A}_{2t}|^2, \end{aligned}$$

- *DR1 (without interference):*

$$|\mathcal{A}_{tWb}|_{\text{DR1}}^2 = |\mathcal{A}_{1t}|^2.$$

- *DR2 (with interference):*

$$|\mathcal{A}_{tWb}|_{\text{DR2}}^2 = |\mathcal{A}_{1t}|^2 + 2\text{Re}(\mathcal{A}_{1t}\mathcal{A}_{2t}^*).$$

- DR schemes based on removing contributions all over the phase space
- They are not gauge invariant