

Largely based on the lectures given by F. Tecker at the Graduate Accelerator Physics Course – John Adams Institute for Accelerator Science (Oxford), March 2025.

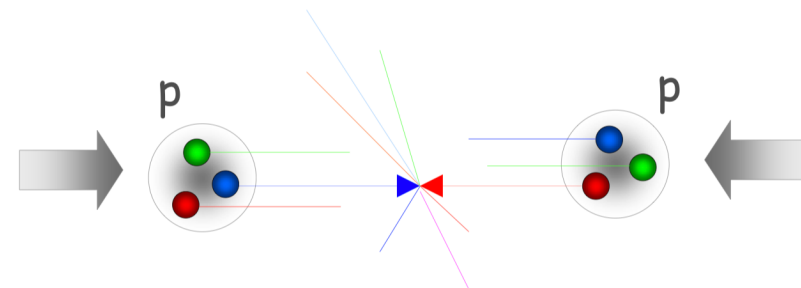
Linear Colliders

R. Corsini

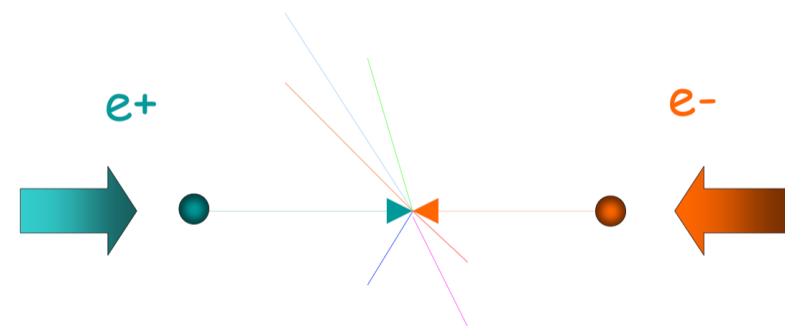
Outline of the lectures

- Introduction:
 - The basics
 - A bit of history: from SLC to the present LC projects
- Luminosity & parameters optimization
- Introduction to linear collider proposals, ILC & CLIC
- Subsystems:
 - Sources
 - Damping Ring
 - Bunch Compressors
 - Main linac
 - Beam Dynamics, wake-fields and alignment
 - RF System
 - Beam Delivery System
- The superconducting solution: ILC
- The Two-Beam solution: CLIC

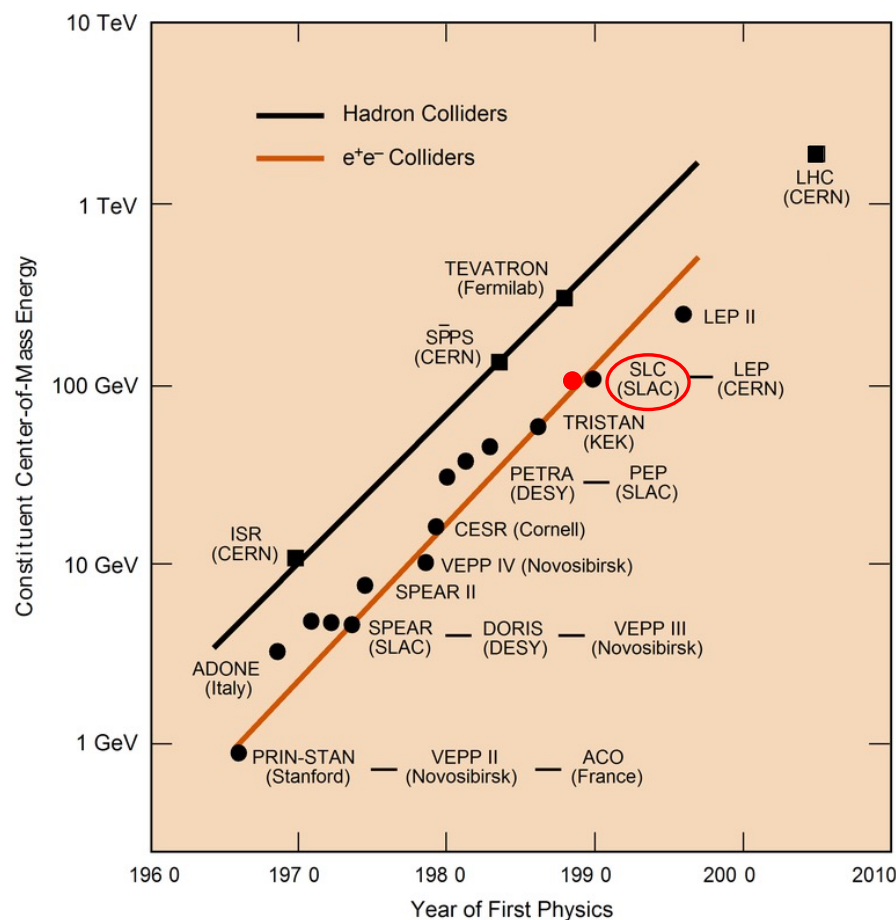
- Hadron collisions (p, ions):
 - Compound particles (mix of quarks, anti-quarks and gluons)
 - Parton energy spread, energy available $< E_{\text{cm}}$
 - Can only use P_T conservation
 - QCD processes produce large background



- Lepton collisions (e^- , e^+ , muons):
 - Elementary particles \Rightarrow all energy available
 - Well defined initial state
 - Momentum conservation eases decay product analysis
 - Less background
 - Polarization



- Photons also possible



History:

- Energy constantly increasing with time
- Hadron Colliders at the **energy frontier**
- Lepton Colliders for **precision physics**
- LHC has found the Higgs with $m_H = 126 \text{ GeV}/c^2$
- A future Lepton Collider (**Higgs factory**) would complement LHC physics \Rightarrow precision measurements of the Higgs boson characteristics
- Recommended in the 2020 Update of the European Strategy for Particle Physics

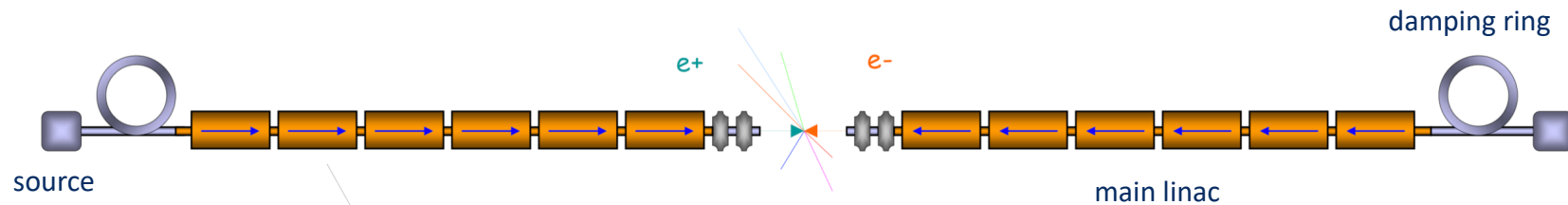
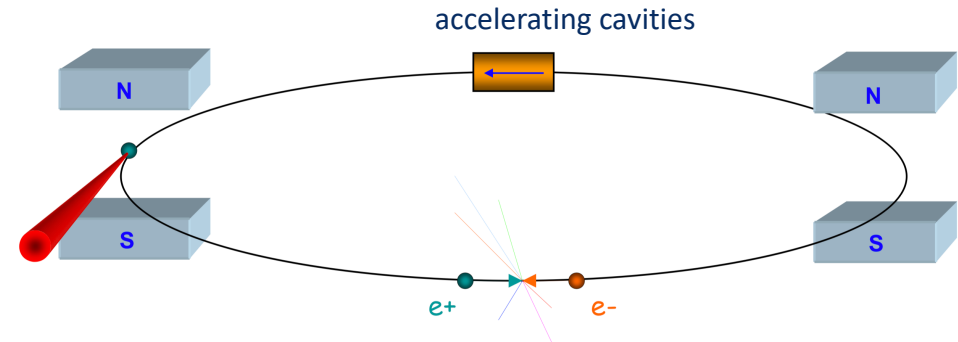
Accelerates beam over **many turns**
 Can use **beam many times** in collision

However, charged particles emit **synchrotron radiation**
 in a magnetic field

$$\Delta E_{turn} = \frac{4}{3} \pi \frac{r_e}{(m_o c^2)^3} \frac{E^4}{\rho}$$

For light particles synchrotron radiation can be large

- At LEP lost 2.75 GeV/turn for E = 105 GeV



Almost **no radiation** in a linac \Rightarrow **No energy loss!**

Beam has to achieve final **energy** in **single pass**
 Must achieve **luminosity** with **single beam collision**

Need a **larger** lepton storage ring to **compensate** for synchrotron radiation losses.
LEP had already a $L = 27$ km, for $E_{\text{cm}} = 200$ GeV

- Synchrotron radiation:

- Emitted power

$$P = \frac{2}{3} \frac{r_e c}{(m_o c^2)^3} \frac{E^4}{\rho^2}$$

scales with E^4 !!

- Energy loss/turn

$$\Delta E_{\text{turn}} = \frac{4}{3} \pi \frac{r_e}{(m_o c^2)^3} \frac{E^4}{\rho}$$

must be replaced
by the RF system

- RF costs:

$$\epsilon_{\text{RF}} \propto \Delta E_{\text{turn}} \propto E^4/\rho$$

- Linear costs (magnets, tunnel, etc.)

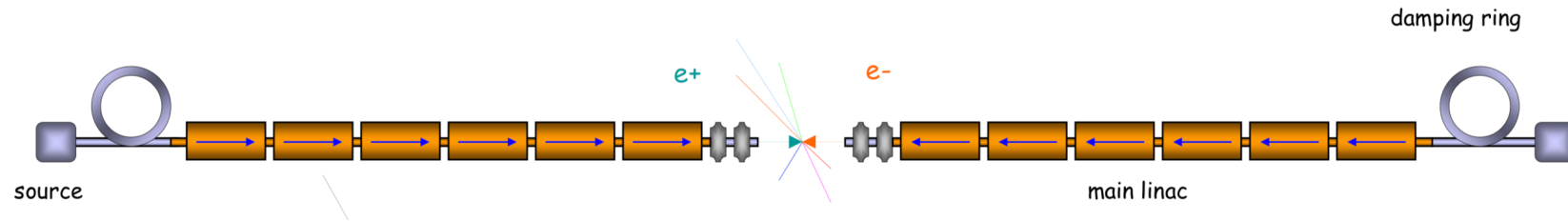
$$\epsilon_{\text{lin}} \propto \rho$$

⇒ Optimum when

$$\epsilon_{\text{lin}} \propto \epsilon_{\text{RF}} \Rightarrow \rho \propto E^2$$

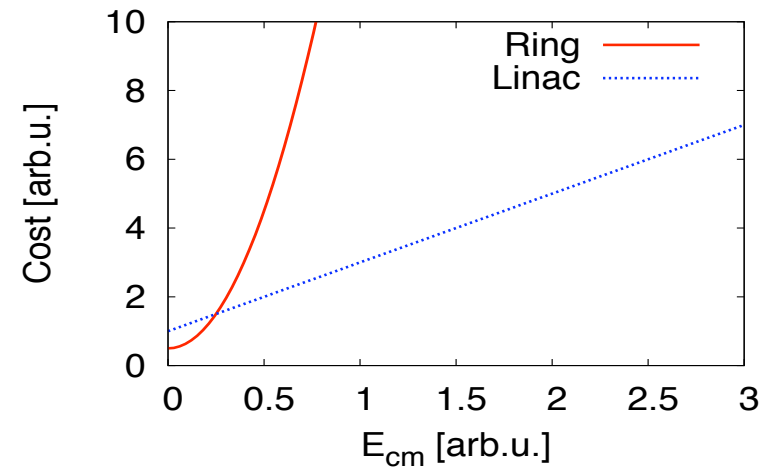
Must increase radius quadratically with energy

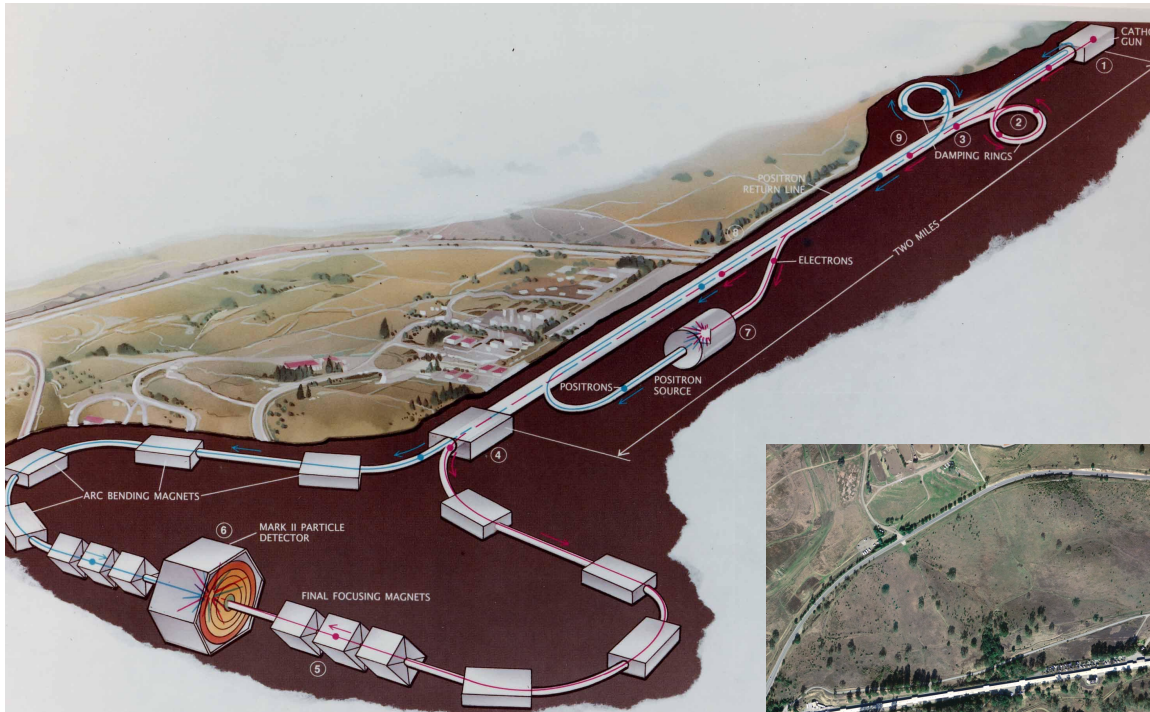
⇒ The **size** and the **optimized cost** scale as E^2 as well as the **energy loss per turn** (was already ~3% at LEP)



- NO bending magnets \Rightarrow NO synchrotron radiation
- Accelerating structures are used **only once** for each colliding beam
 \Rightarrow need **lots** of them !!!

\Rightarrow Cost and size scaling **linearly** with E





- Built to study the Z-boson Z_0 (and to demonstrate the feasibility of a linear collider)
- In order to reduce cost, used a **single linac** for both e^+ and e^- , followed by a long **double arc**



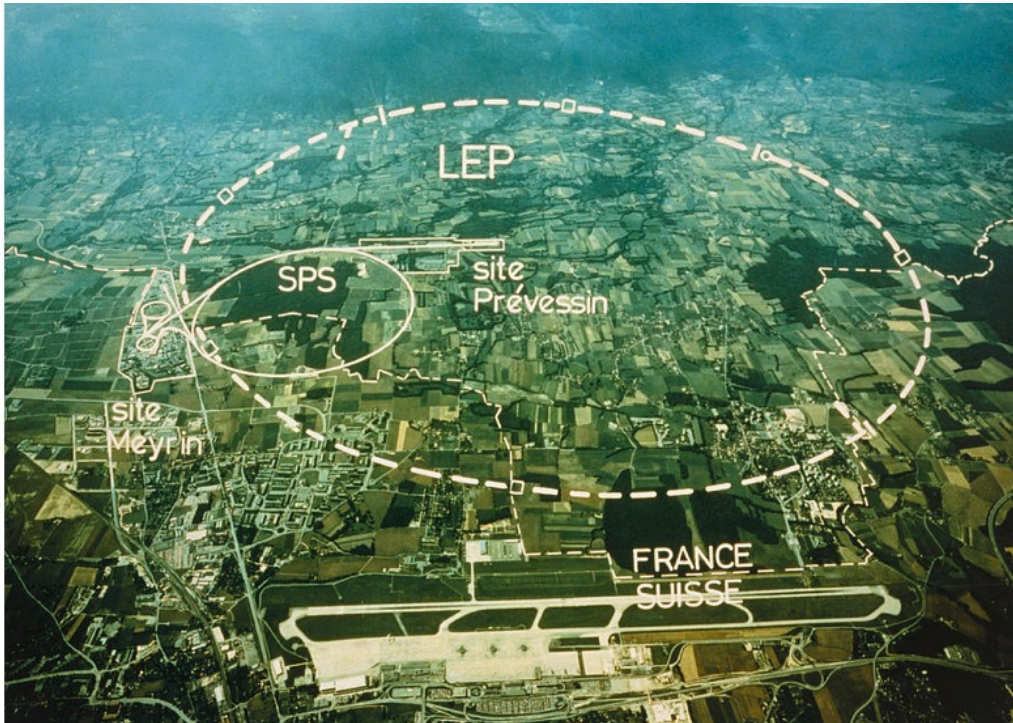
SLAC Linear Collider

Linac length = 3 km

Energy 92 GeV
Luminosity 1×10^{30}

SLAC NATIONAL
ACCELERATOR
LABORATORY

The Large Electron Positron (LEP) collider ring



Ring length = 27 km

- Operated initially at the Z_0 energy, later upgraded with superconducting cavities to allow for W bosons production



Energy
Luminosity

92 GeV \Rightarrow 209 GeV
 1×10^{32}

LEP I copper cavity



LEP II superconducting cavity



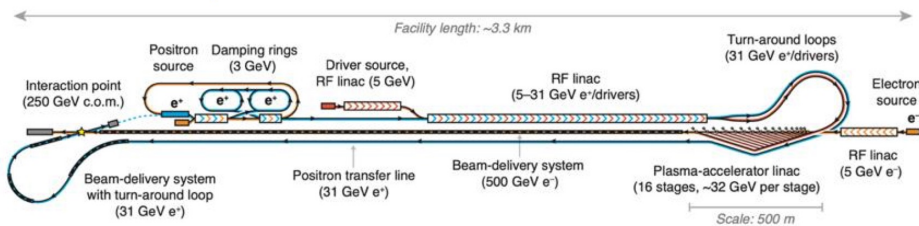
LEP – the largest electron-positron accelerator ever built – was dismantled in 2000
Its 27-kilometre tunnel now hosts the LHC

Linear Collider Projects, ~ 1990 to now

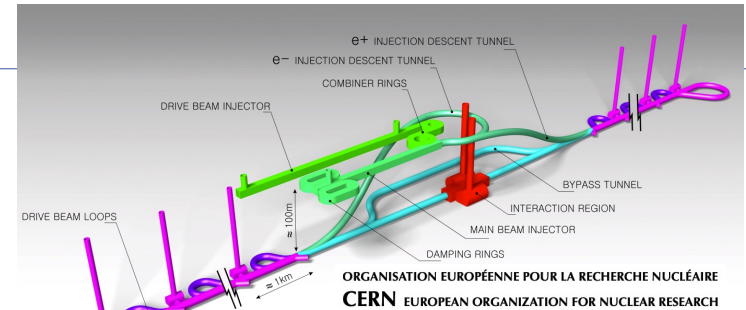
Linear Colliders: Overall and Final Focus Parameters – 500 GeV (c.m.)

	TESLA*	SBLCL	JLC (S)	JLC (C)	JLC (X)	NLC	VLEPP	CLIC
Initial energy (c.o.f.m.) (GeV)	500	500	500	500	500	500	500	500
RF frequency of main linac (GHz)	1.3	3	2.8	5.7	11.4	11.4	14	30
Nominal Luminosity ($10^{33} \text{ cm}^{-2} \text{ s}^{-2}$)†	2.6	2.2	5.2	7.3	5.1	5.3	12.3	0.7-3.4
Actual luminosity ($10^{33} \text{ cm}^{-2} \text{ s}^{-2}$)†	6.1	3.75	4.3	6.1	5.2	7.1	9.3	1.07-4.8
Linac repetition rate (Hz)	10	50	50	100	150	180	300	2530-1210
No. of particles/bunch at IP (10^{10})	5.15	2.9	1.44	1.0	.63	.65	20	.8
No. of bunches/pulse	800	125	50	72	85	90	1	1-10
Bunch separation (nsec)	1000	16.0	5.6	2.8	1.4	1.4	–	.67
Beam power/beam (MW)	16.5	7.26	1.3	2.9	3.2	4.2	2.4	.8-3.9
Damping ring energy (GeV)	4.0	3.15	2.0	2.0	2.0	2.0	3.0	2.15
Main linac gradient, unloaded/loaded†† (MV/m)	25/25	21/17	31/–	40/32	73/58	50/37	100/91	80/78
Total two-linac length (km)	29	33	22.1	18.8	10.4	15.6	7	8.8
Total beam delivery length (km)	3	3	3.6	3.6	3.6	4.4	3	2.4
$\gamma\epsilon_x/\gamma\epsilon_y$ ($m\text{-rad} \times 10^{-8}$)	2000/100	1000/50	330/4.8	330/4.8	330/4.8	500/5	2000/7.5	300/15
β_x^*/β_y^* (mm)	25/2	22/0.8	10/0.1	10/0.1	10/0.1	10/0.1	100/0.1	10/0.18
σ_x^*/σ_y^* (nm) before pinch	1000/64	670/28	260/3.0	260/3.0	260/3.0	320/3.2	2000/4	247/7.4
σ_x^* (μm)	1000	500	120	120	90	100	750	200
Crossing Angle at IP (mrad)	0	3	6.4	6.0	6.1	20	6	1
Disruptions D_x/D_y	0.56/8.7	.36/8.5	.29/25	.20/18	.096/8.3	.07/7.3	.4/215	0.29/9.8
H_D	2.3	1.8	1.6	1.4	1.4	1.34	2.0	1.42
Upsilon sub-zero	.02	.037	.20	.14	.12	.089	.059	0.07
Upsilon effective	.03	.042	.22	.144	.12	.090	.074	.075
δ_B (%)	3.3	3.2	12.7	6.5	3.5	2.4	13.3	3.6
n_γ (no. of γ 's per e)	2.7	1.9	2.2	1.5	.94	.8	5.0	1.35
$N_{pairs}(p_T^{min}=20 \text{ MeV}/c, \theta_{min}=0.15)$	19.0	8.8	31.6	10.3	2.9	2.0	1700	3.0
$N_{hadrons}/\text{crossing}$	0.17	0.10	0.98	0.23	0.05	0.03	45.9	0.05
$N_{jets} \times 10^{-2} (p_T^{min}=3.2 \text{ GeV}/c)$	0.16	0.14	3.4	0.66	0.14	0.08	56.4	0.10

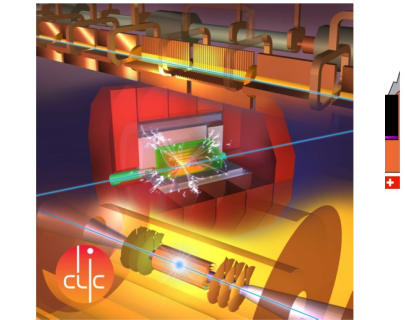
From the 1995 International Linear Collider (ILC) Technical Review Committee (TRC) Report (FERMILAB-PUB-95-438)



HALHF
Hybrid, Asymmetric,
Linear Higgs Factory

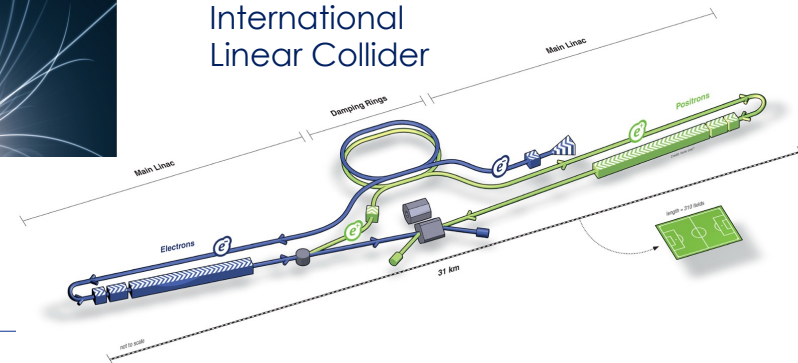


CLIC
Compact
Linear Collider



THE COMPACT LINEAR COLLIDER (CLIC)
READINESS REPORT

ILC
International
Linear Collider



- The performance of particle colliders is usually quantified by the center of mass beam energy E_{cm} and the luminosity L
- The **luminosity** is the quantity that measures the **ability** of a particle accelerator to **produce the required number of useful interactions**.
In particular, it is the proportionality factor between the number of events per second dR/dt and the cross section σ_p :

$$dR/dt = L \cdot \sigma_p$$

The unit of the luminosity is $\text{cm}^{-2}\text{s}^{-1}$

- A Collider luminosity is approximately given by

where:

n_b = bunches / train

N = particles per bunch

f_{rep} = repetition frequency

$\sigma_{x,y}$ = transverse beam size at IP

H_D = beam-beam enhancement factor (linear collider: typical value ~ 2)

$$L = \frac{n_b N^2 f_{rep}}{4\pi \sigma_x \sigma_y} H_D$$

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- LHC ring $f_{rep} = 11 \text{ kHz}$
- LC $f_{rep} = \text{few-100 Hz}$ (power limited)

\Rightarrow factor $\sim 100\text{-}1000$ in L already lost for the LC!

- Must push very hard on beam cross-section at collision:

factor of 10^6 gain! needed
to obtain high luminosity
of a few $10^{34} \text{ cm}^{-2}\text{s}^{-1}$

$$\text{LEP: } \sigma_x \sigma_y \approx 130 \times 6 \text{ } \mu\text{m}^2$$

$$\text{LC: } \sigma_x \sigma_y \approx (60\text{-}550) \times (1\text{-}5) \text{ nm}^2$$

Introduce centre-of-mass Energy E_{cm}

$$L = \frac{n_b N^2 f_{rep}}{4\pi \sigma_x \sigma_y} H_D \quad \rightarrow \quad L = \frac{\left(n_b N f_{rep} E_{cm} \right) N}{4\pi \sigma_x \sigma_y E_{cm}} H_D$$

$$\rightarrow L = \frac{\eta_{RF} P_{RF} N}{4\pi \sigma_x \sigma_y E_{cm}} H_D$$

Beam
power

- η_{RF} is the RF-to-beam power efficiency
- Luminosity L is proportional to the RF power P_{RF} and efficiency η_{RF} for a given E_{cm}


- Some numbers:

E_{cm}	= 500 GeV
N	= 10^{10}
n_b	= 100
f_{rep}	= 100 Hz

- Need to include efficiencies:

RF→beam	range 20-60%
Wall plug→RF	range 28-40%

AC power: a few hundred MW to accelerate beams for a high luminosity
 \Rightarrow This limits the practically achievable energy and luminosity

$$L = \frac{1}{4\pi E_{cm}} (\eta_{RF} P_{RF}) \left(\frac{N}{\sigma_x \sigma_y} H_D \right)$$


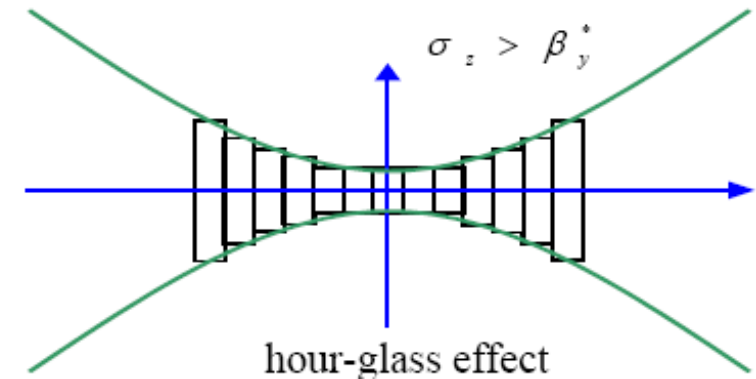
- Choice of acceleration technology (NC vs SC):
 - Efficiency
 - Available power
- Strong focusing needed for small beam size
 - Optical aberrations
 - Issues with stability and tolerances
- Beam-Beam effects:
 - Strong self focusing (pinch effect) \Rightarrow
 - increases Luminosity
 - Photon emission (Beamstrahlung) \Rightarrow
 - dilutes Luminosity spectrum
 - creates detector background

- β -function at the interaction point follows

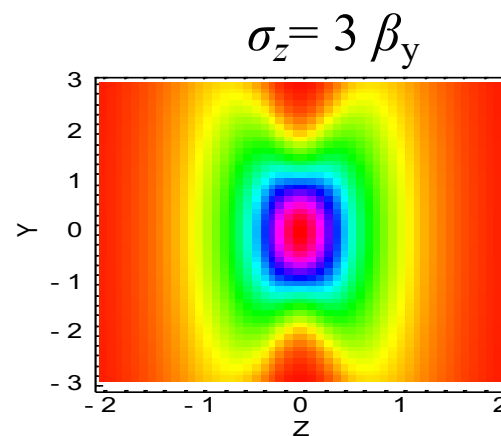
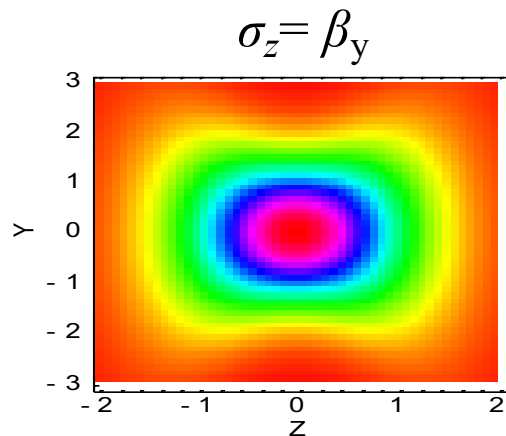
$$\beta(s) = \beta^* + \frac{s^2}{\beta^*}$$

β^* beta function at the IP

N.B.: $\sigma_{x,y} = \sqrt{\frac{\beta_{x,y} \epsilon_{x,y}}{\gamma}}$

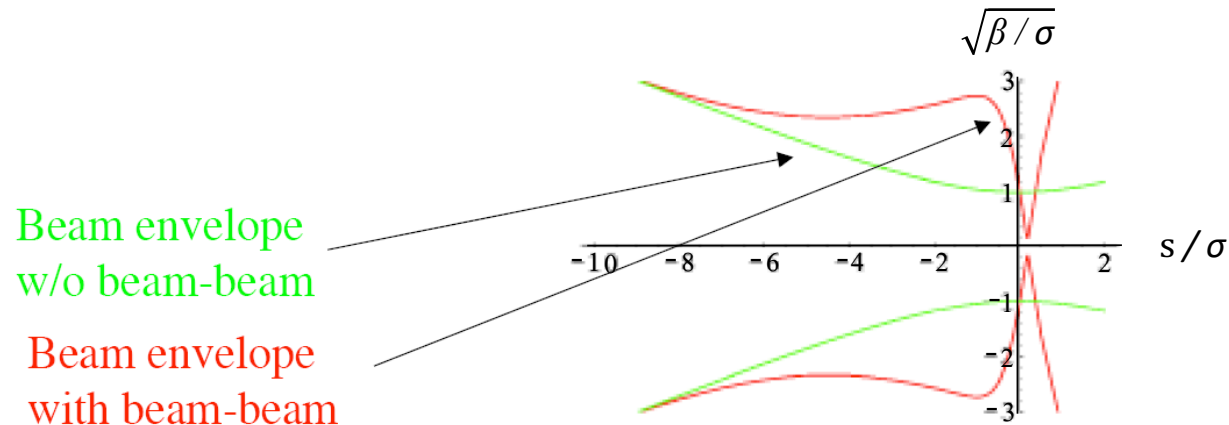
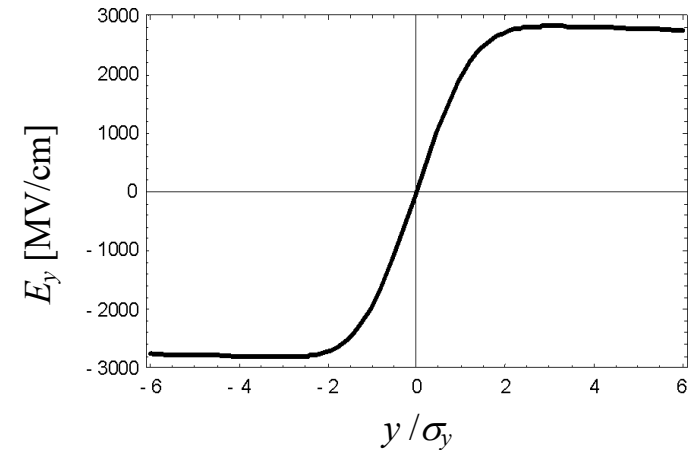


- Desirable to have $\sigma_z \leq \beta_y \Rightarrow$ short bunch length for high luminosity

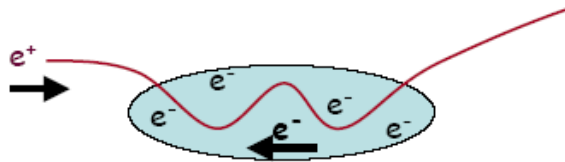


N.Walker

- Strong electromagnetic field of the opposing bunch:
 - Deflects the particles
“beam-beam kick”
 - Focuses the bunches
“pinch effect”
- Luminosity enhancement factor H_D



- “Synchrotron radiation” in the field of the opposing bunch (beamstrahlung)

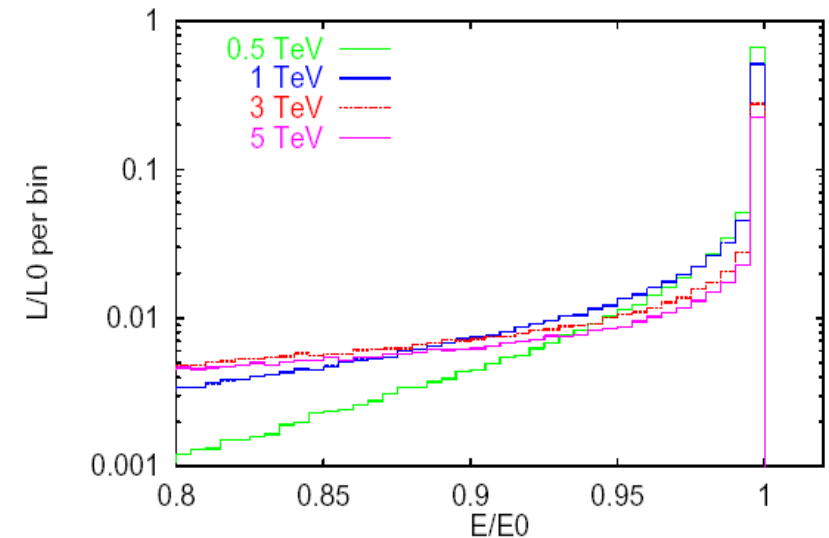


⇒ energy loss

- Smears out luminosity spectrum
- Creates e^+e^- pairs background in detector



- Quantified by Disruption parameter



$$D_{x,y} = \frac{2r_e N \sigma_z}{\gamma \sigma_{x,y} (\sigma_x + \sigma_y)}$$

- RMS relative **energy loss** by beamstrahlung

$$\delta_{BS} \approx 0.86 \frac{r_e^3}{2m_0 c^2} \left(\frac{E_{cm}}{\sigma_z} \right) \frac{N^2}{(\sigma_x + \sigma_y)^2}$$

- We want

- σ_x and σ_y **small** for **high luminosity**
- $(\sigma_x + \sigma_y)$ **large** for small δ_{BS} \Rightarrow better **luminosity spectrum**

- Use **flat beams** with $\sigma_x \gg \sigma_y$

increase luminosity

by **small** σ_y

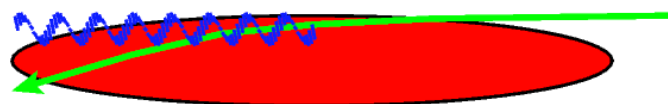
and minimise δ_{BS}

by (relatively) **large** σ_x

$$\delta_{BS} \propto \left(\frac{E_{cm}}{\sigma_z} \right) \frac{N^2}{\sigma_x^2}$$

Beam-beam Effect

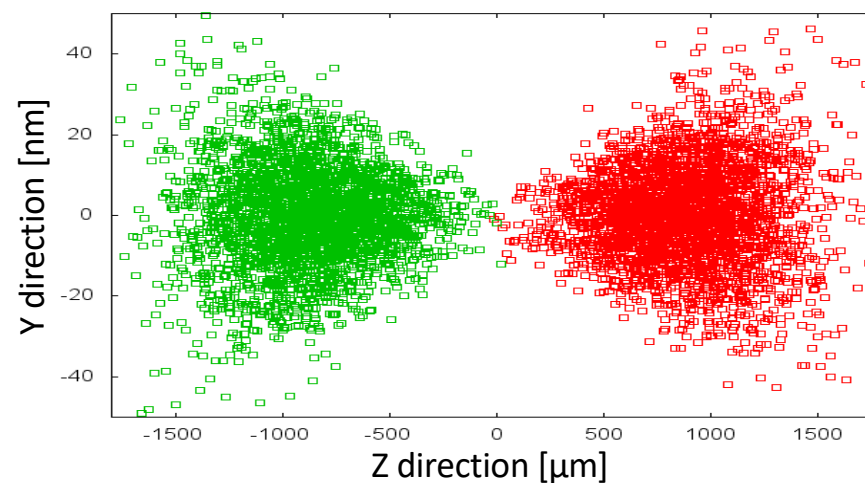
$$\mathcal{L} \propto H_D \left(\frac{N}{\sigma_x} \right) N n_b f_r \frac{1}{\sigma_y}$$



Intense beams to reach high luminosity

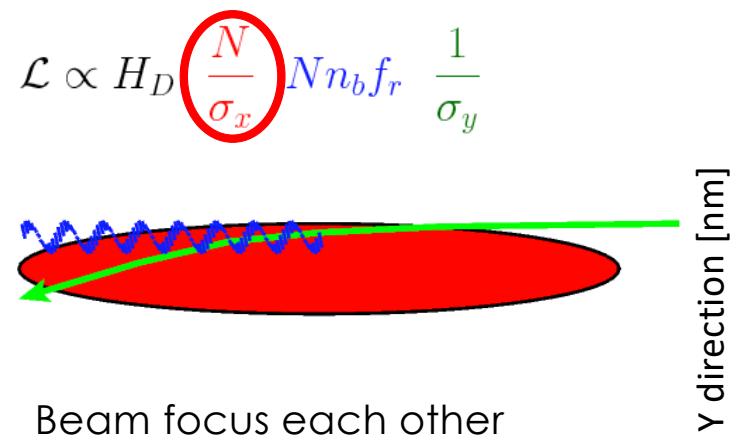
$$\mathcal{L} \propto \frac{N}{\sigma_x \sigma_y}$$

Beam-beam force switched off

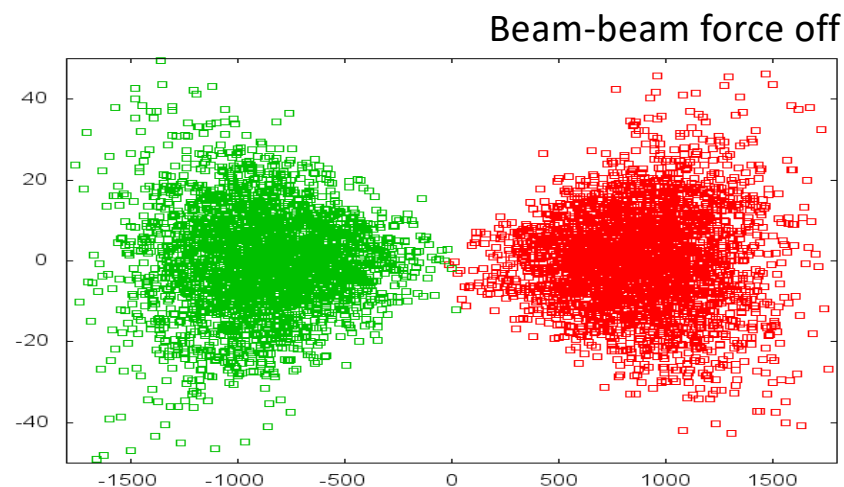


D. Schulte

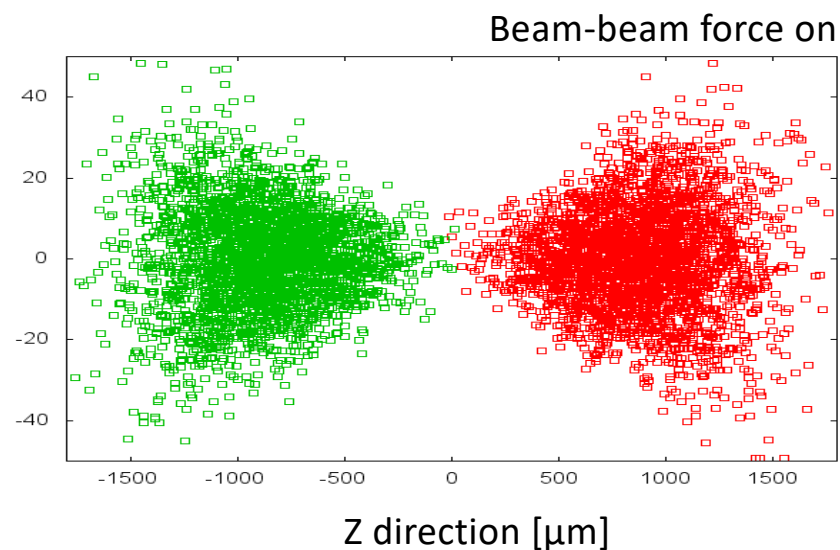
Beam-beam Effect



$$\mathcal{L} \propto \frac{N}{\sigma_x \sigma_y}$$

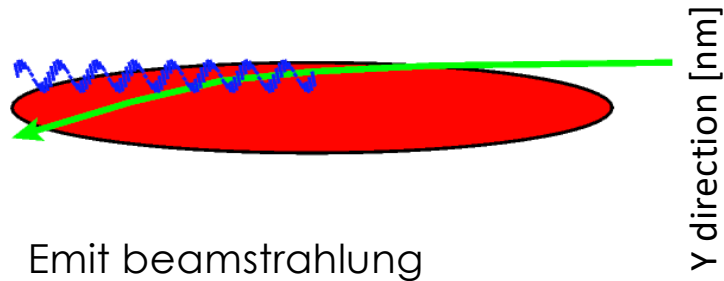


D. Schulte



Beam-beam Effect

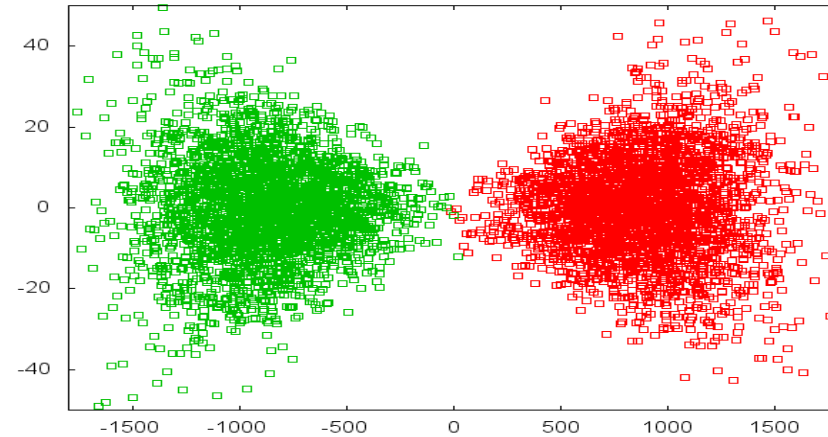
$$\mathcal{L} \propto H_D \left(\frac{N}{\sigma_x} \right) N n_b f_r \frac{1}{\sigma_y}$$



$$\mathcal{L} \propto \frac{N}{\sigma_x \sigma_y}$$

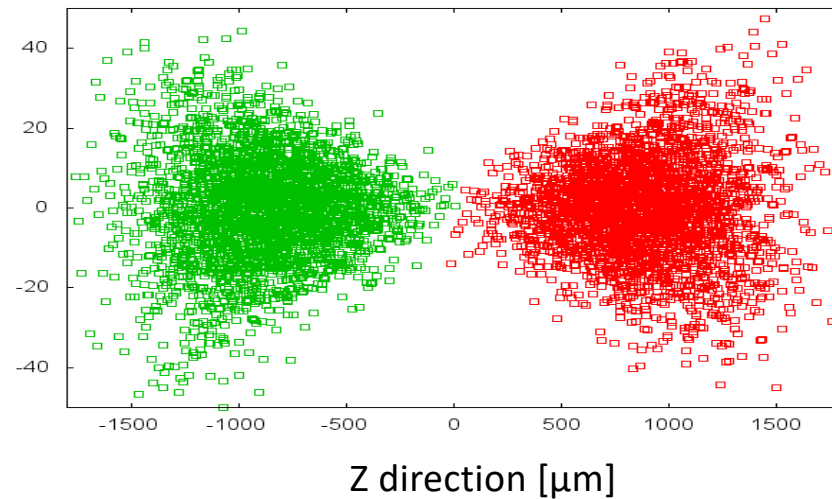
$$n_\gamma \propto E_\gamma \propto \frac{N}{\sigma_x + \sigma_y}$$

Beam-beam force off

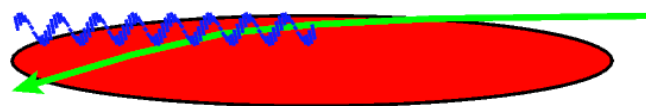


D. Schulte

Beam-beam force on



$$\mathcal{L} \propto H_D \left(\frac{N}{\sigma_x} \right) N n_b f_r \frac{1}{\sigma_y}$$

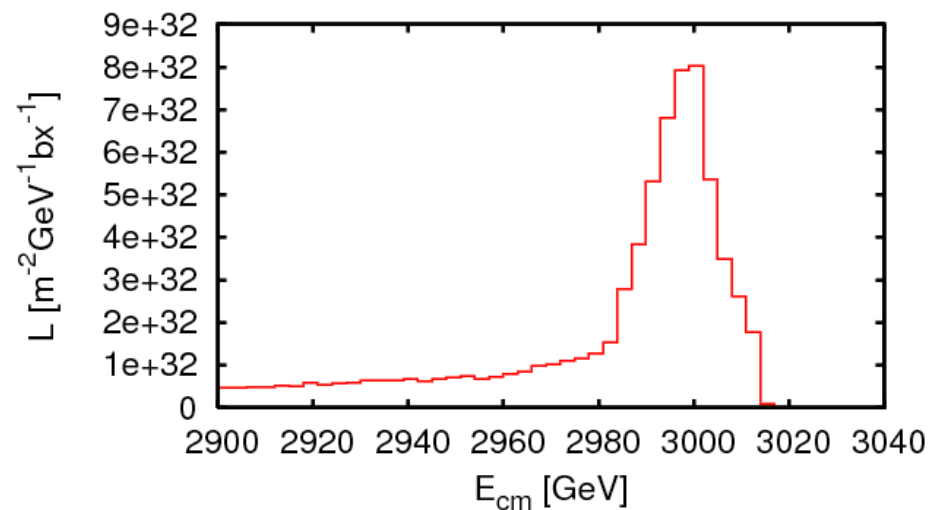


Develop luminosity spectrum

$$\mathcal{L} \propto \frac{N}{\sigma_x \sigma_y}$$

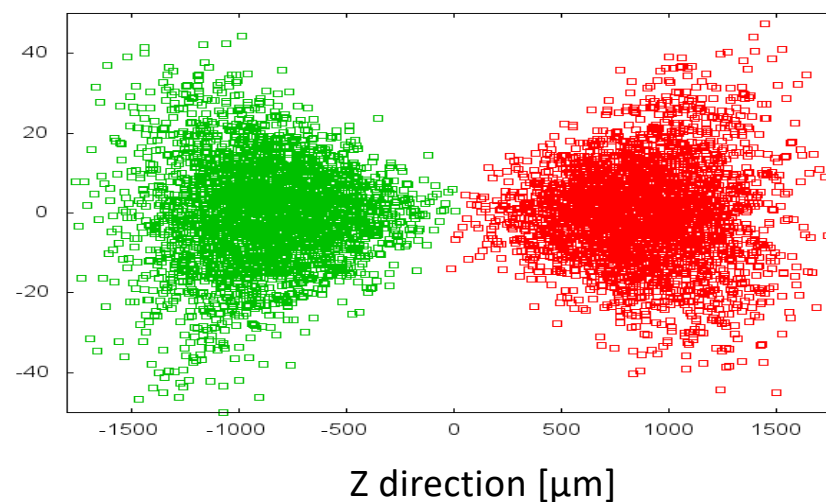
$$n_\gamma \propto E_\gamma \propto \frac{N}{\sigma_x + \sigma_y}$$

$$\sigma_x \gg \sigma_y \quad \sigma_x + \sigma_y \approx \sigma_x$$



D. Schulte

Beam-beam force on



• Substitute $\delta_{BS} \propto \left(\frac{E_{cm}}{\sigma_z} \right) \frac{N^2}{\sigma_x^2}$ into $L = \frac{1}{4\pi E_{cm}} (\eta_{RF} P_{RF}) \left(\frac{N}{\sigma_x \sigma_y} H_D \right)$

• We get
$$L \propto \frac{\eta_{RF} P_{RF}}{E_{cm}^{3/2}} \frac{\sqrt{\delta_{BS} \sigma_z}}{\sigma_y}$$

• Now use
$$\sigma_y = \sqrt{\frac{\beta_y \varepsilon_{n,y}}{\gamma}}$$

• Then
$$L \propto \frac{\eta_{RF} P_{RF}}{E_{cm}^{3/2}} \sqrt{\frac{\delta_{BS} \gamma}{\varepsilon_{n,y}}} \sqrt{\frac{\sigma_z}{\beta_y}} \propto \frac{\eta_{RF} P_{RF}}{E_{cm}} \sqrt{\frac{\delta_{BS}}{\varepsilon_{n,y}}} \underbrace{\sqrt{\frac{\sigma_z}{\beta_y}}}_{\sim 1 \text{ (hourglass effect)}}$$

$$L \propto \frac{\eta_{RF} P_{RF}}{E_{cm}} \sqrt{\frac{\delta_{BS}}{\epsilon_{n,y}}} H_D \quad \beta_y \approx \sigma_z$$

- We want **high** RF-beam conversion efficiency η_{RF}
- Need **high** RF power P_{RF}
- **Small** normalised vertical emittance $\epsilon_{n,y}$
- Strong focusing at IP is implied (i.e., **small** β_y and hence **small** σ_z)
- Could also allow higher beamstrahlung δ_{BS} if willing to live with the consequences (luminosity spread and background)
 - Above result is for the low beamstrahlung regime where $\delta_{BS} \sim \text{few } \%$
 - Slightly different result for high beamstrahlung regime

What matters in a linear collider ?

Energy reach

$$E_{cm} \approx L_{linac} G_{acc}$$



High gradient

Luminosity

$$L = \frac{n_b N^2 f_{rep}}{4\pi\sigma_x^* \sigma_y^*} \times H_D \propto \frac{\eta_{beam}^{AC} P_{AC}}{\epsilon_y^{1/2}} \frac{\delta_{BS}^{1/2}}{E_{cm}}$$

$$\text{N.B.: } \sigma_{x,y} = \sqrt{\frac{\beta_{x,y} \epsilon_{x,y}}{\gamma}}$$



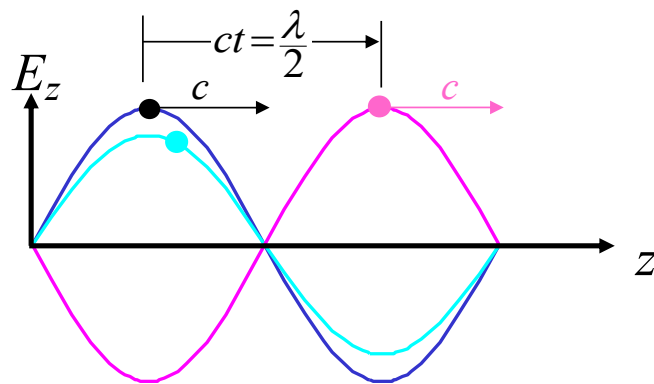
- Acceleration efficiency
- Generation of small emittance
- Conservation of small emittance
- Extremely small beam spot at IP

Superconducting RF (ILC) or Two-beam scheme (CLIC)

Damping rings

Wake-fields, alignment, stability

Beam delivery system, stability



Standing wave cavity:

bunch sees field:

$$E_z = E_0 \sin(\omega t + \varphi) \sin(kz)$$

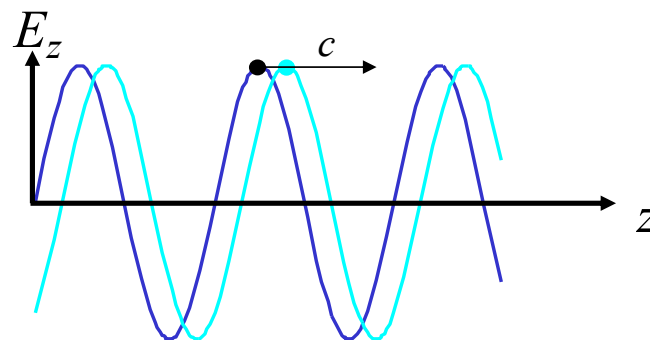
$$= E_0 \sin(kz + \varphi) \sin(kz)$$



Superconducting
(Niobium)



Normal
Conducting
(Copper)



Travelling wave structure:
need *phase velocity* = c
(*disk-loaded structure*)

bunch sees constant field:

$$E_z = E_0 \cos(\varphi)$$

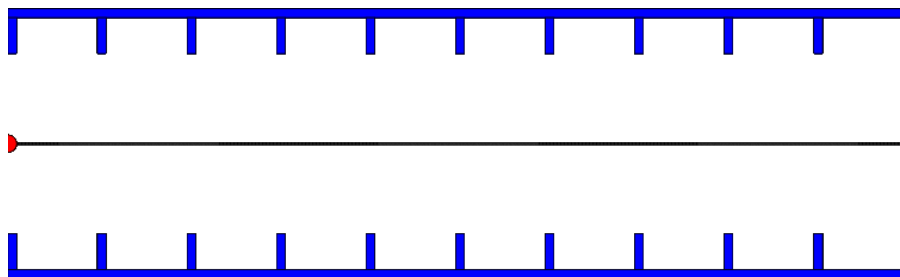
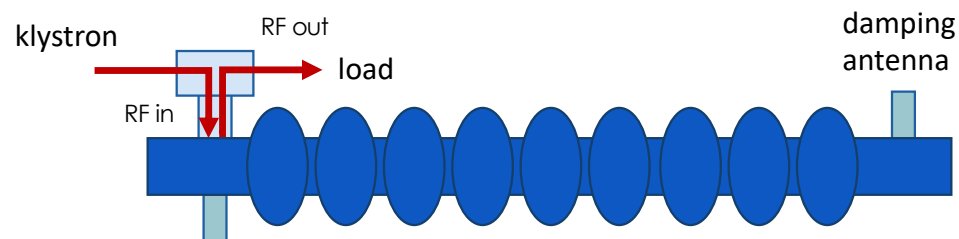


Superconducting cavity (Ni at 2 K)

RF frequency is 1.3 GHz, 23 cm wavelength

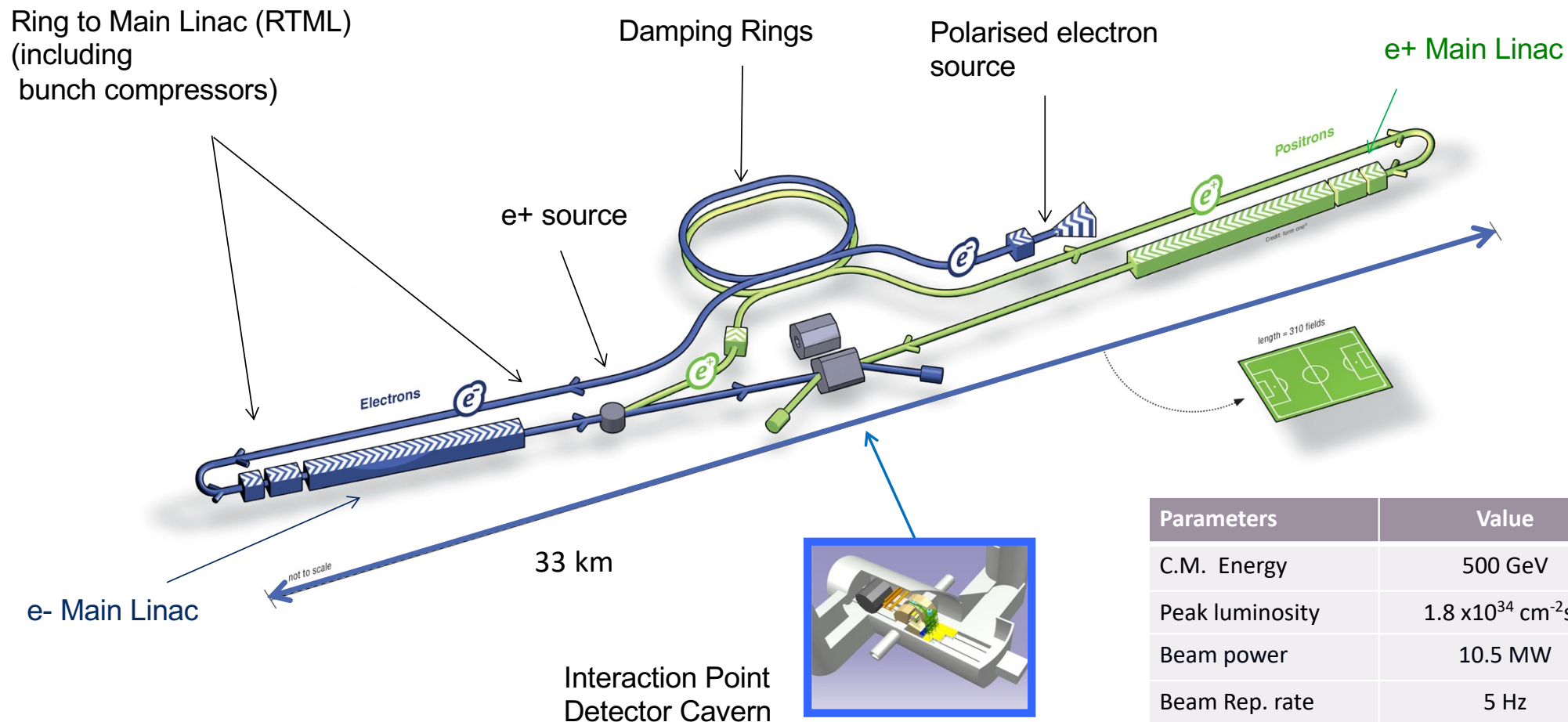
Length is 9 cells = 4.5 wavelengths = 1 m

Standing wave structure



Gradient is 31.5 MV/m

Need about 16000 cavities



Parameters	Value
C.M. Energy	500 GeV
Peak luminosity	$1.8 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
Beam power	10.5 MW
Beam Rep. rate	5 Hz
E gradient	31.5 MV/m +/-20%

12 GHz, 23 cm long, **normal conducting**
Loaded gradient 100MV/m

- ⇒ Allows to reach higher energies
- ⇒ 140,000 structures at 3TeV

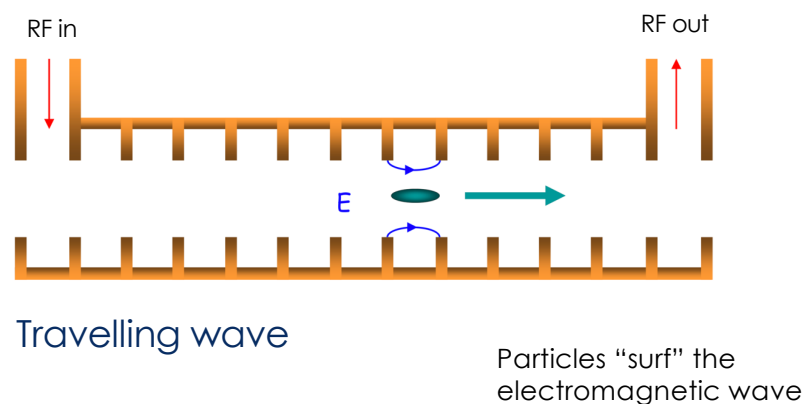
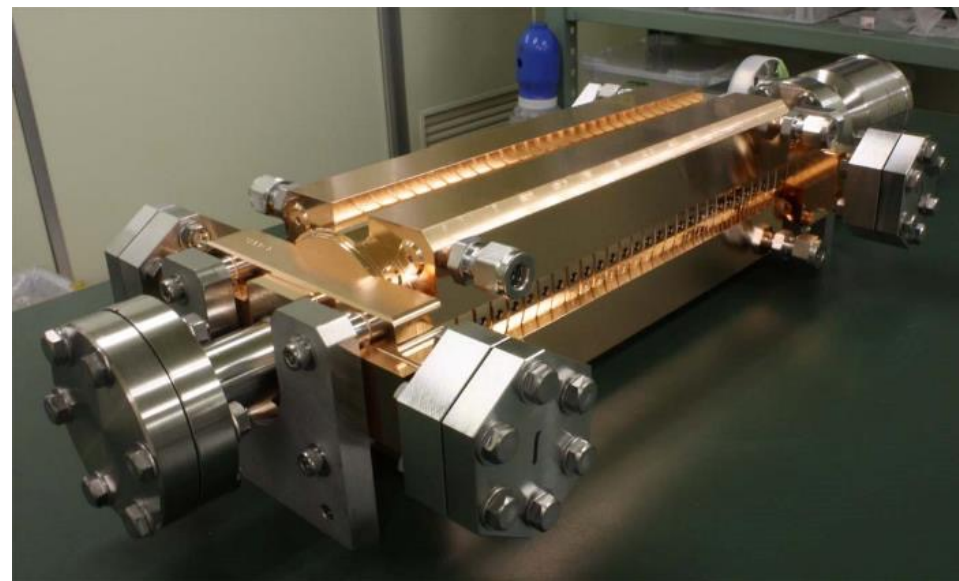
losses in the walls and in the load

- ⇒ 50 RF bursts per second
- ⇒ 240 ns, 60 MW, 312 bunches
- ⇒ **Power during pulse 8.5×10^6 MW (3000 x ILC)**

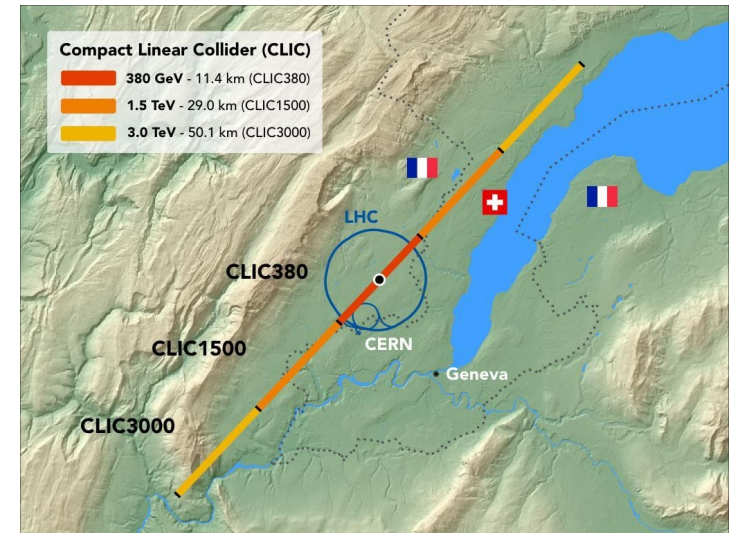
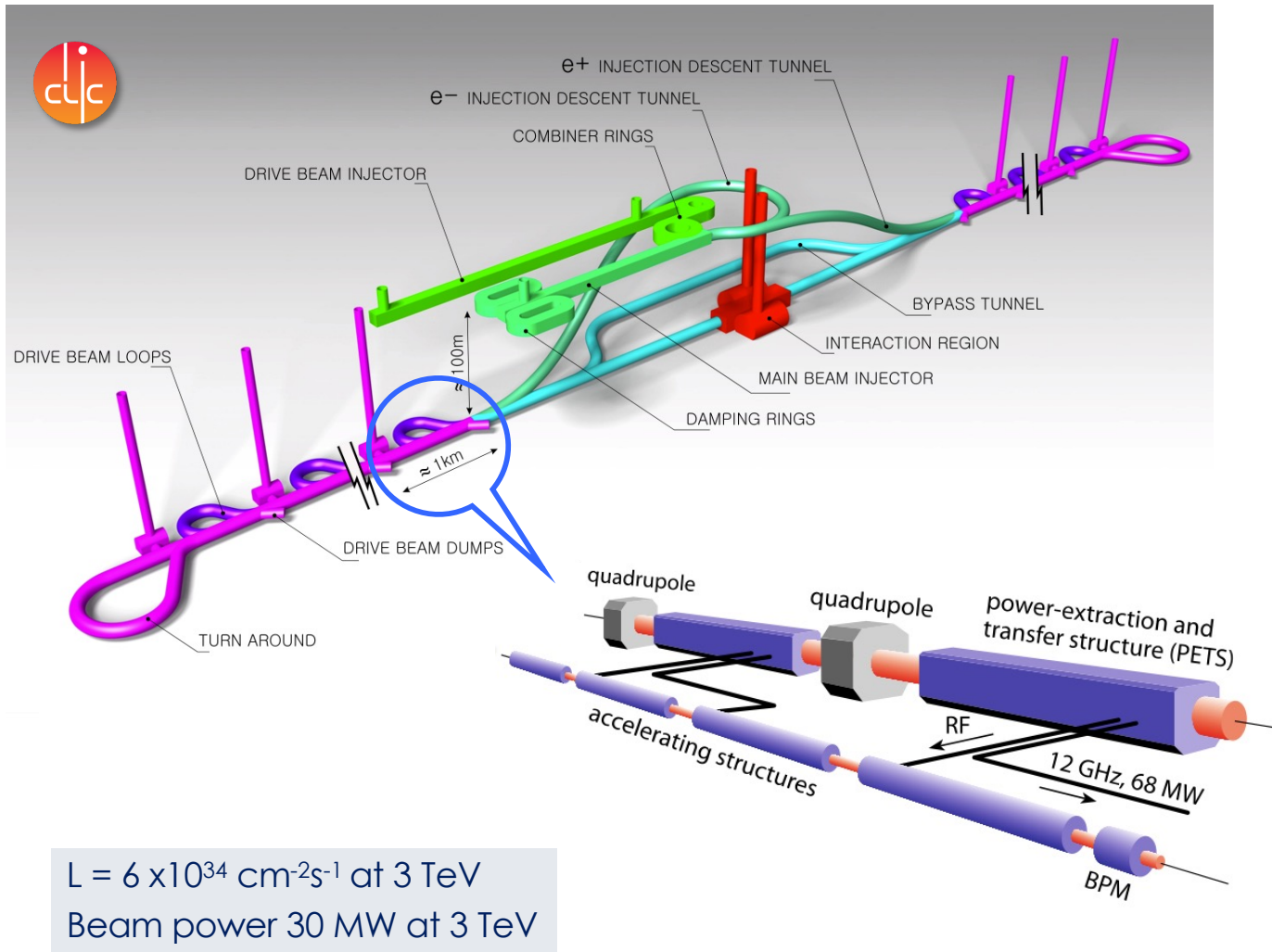
Power flow

- 1/3 lost in cavity walls
- 1/3 in filling the structure and into load
- 1/3 into the beam

Average RF power about 3kW/m
About 1kW/m into beam



The Compact Linear Collider - CLIC



CLIC can be built in stages of increasing collision energy: starting from 380 GeV, then ~ 1- 2 TeV, and up to a final energy of 3 TeV.

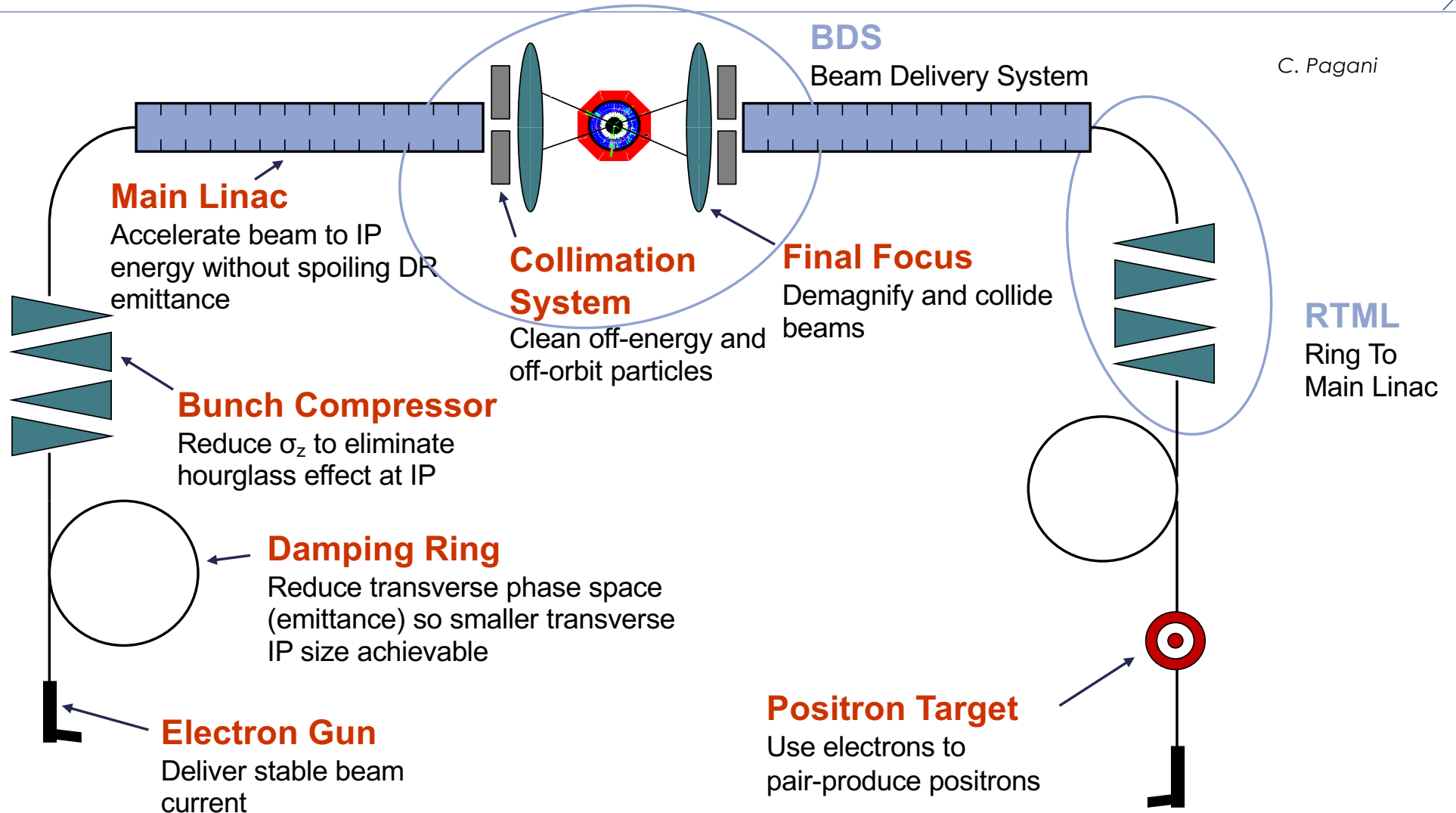
To limit the collider length, the accelerating gradient must be very high - CLIC aims at 100 MV/m, 20 times higher than the LHC.

CLIC is based on a two-beam acceleration scheme, in which a high current e^- beam (the drive beam) is decelerated in special structures (PETS), and the generated RF power is used to accelerate the main beam.

Parameter	Symbol [unit]	SLC	ILC	CLIC	CLIC
Centre of mass energy	E_{cm} [GeV]	92	500	380	3000
Luminosity	L [$10^{34}\text{cm}^{-2}\text{s}^{-1}$]	0.0003	1.8	1.5	6
Luminosity in peak	$L_{0.01}$ [$10^{34}\text{cm}^{-2}\text{s}^{-1}$]	0.0003	1	0.9	2
Gradient	G [MV/m]	20	31.5	72	100
Particles per bunch	N [10^9]	37	20	5.2	3.72
Bunch length	σ_z [μm]	1000	300	70	44
Collision beam size	$\sigma_{x,y}$ [nm/nm]	1700/600	474/5.9	143/2.9	40/1
Vertical emittance	$\epsilon_{x,y}$ [nm]	3000	35	30	20*
Bunches per pulse	n_b	1	1312	352	312
Bunch distance	Δz [mm]	-	554	0.5	0.5
Repetition rate	f_r [Hz]	120	5	50	50

End part I

C. Pagani

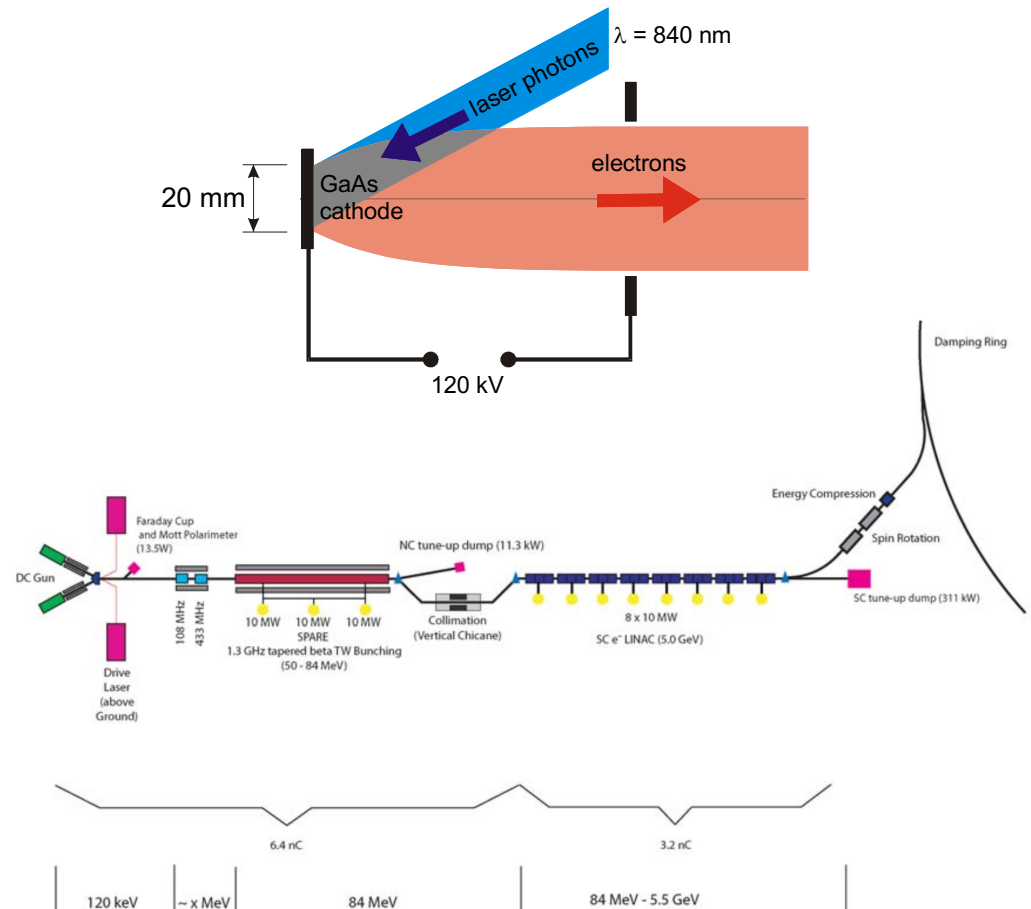


We need large number of bunches of (polarized) electrons – “standard” solution:

- laser-driven DC photo injector
 - circularly polarized photons on GaAs cathode (incompatible with RF gun)
 - $\epsilon_n \sim 50 \mu\text{m rad}$ too large by:
 - factor ~ 10 in x plane
 - factor ~ 500 in y plane
 - dominated by space charge

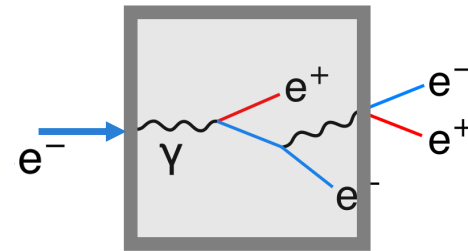
⇒ need a damping ring

- Laser + RF bunching system generate and capture the bunch structure adapted to the linac for further acceleration

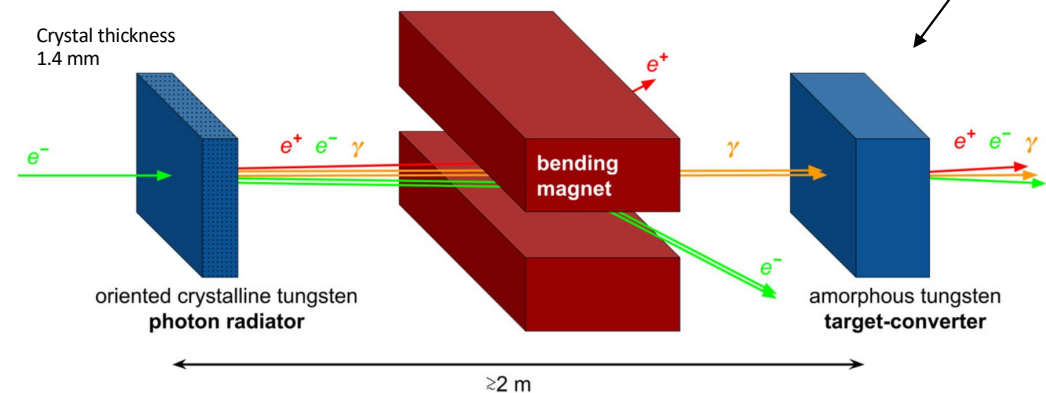


Basic mechanism: pair production in target material

- Standard method: 'thick' target
primary e⁻ generate photons
these convert into pairs



- Hybrid source:
 - Crystal + Amorphous target
 - Enhanced photon flux by channeling effect

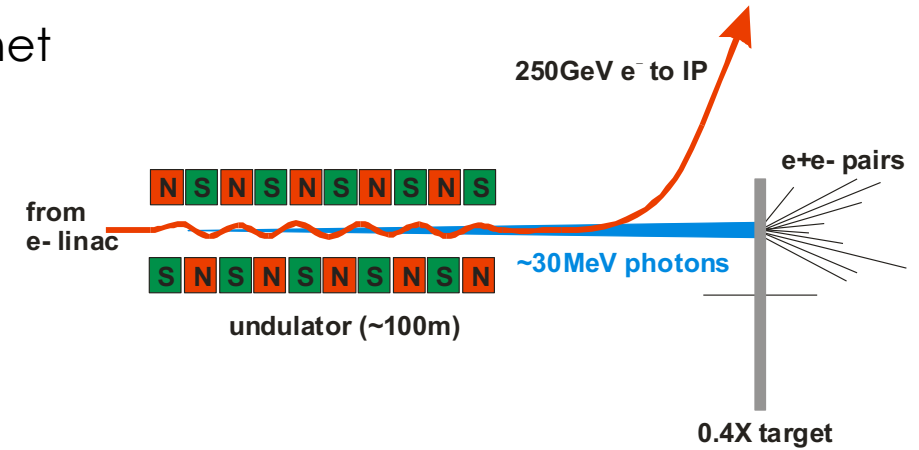


- Positrons are captured in accelerating structure inside solenoids and accelerated

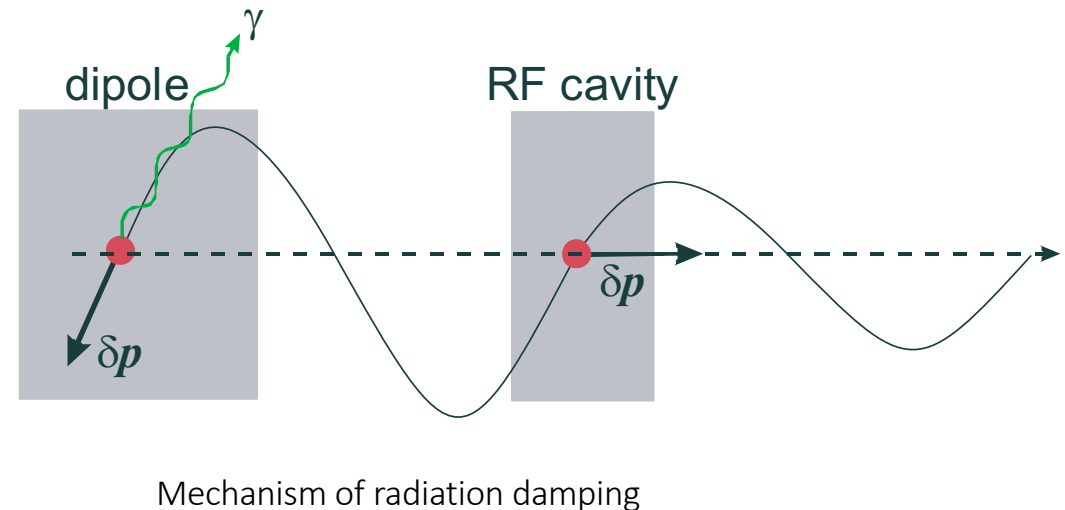
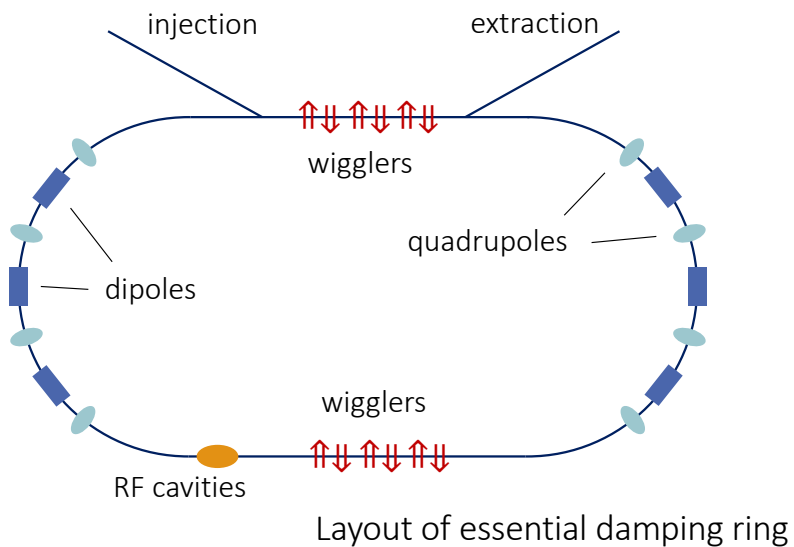
Undulator source:

high energy e⁻ produce photons in undulator magnet
+ thin conversion target

- ~0.4 rad. length ⇒ much less energy deposition in the target (5 kW compared to 20 kW)
⇒ no parallel targets needed
- Smaller emittance due to less coulomb scattering (factor ~2)
but still much bigger than needed $\epsilon_n \sim 10.000 \mu\text{m rad}$
- Could produce polarised e⁺ by helical undulator
- But: need very high initial electron energy > 150 GeV !
- Use primary e⁻ beam
- Consequences for the commissioning and operation!



- e^- and particularly e^+ from the source have a **much too high** transverse ε_n
 \Rightarrow we have to reduce it (**cooling**)
- Solution: use synchrotron radiation in a damping ring



- γ emission with **transverse** component
- **Acceleration** only in **longitudinal** direction

} **radiation
damping!!!**

- Exponential damping to equilibrium emittance:

initial emittance
(~0.01 m rad for e⁺)

$$\varepsilon_f = \varepsilon_{eq} + (\varepsilon_i - \varepsilon_{eq}) e^{-2T/\tau_D}$$

final emittance equilibrium emittance damping time

- For e⁺ we need emittance reduction by few 10⁵
- ~7-8 damping times required

- Damping time:

P - emitted radiation power

$$\tau_D = \frac{2E}{P} \quad P = \frac{2}{3} \frac{r_e c}{(m_o c^2)^3} \frac{E^4}{\rho^2}$$

$$\tau_D \propto \frac{\rho^2}{E^3}$$

LEP: $E \sim 90$ GeV, $P \sim 15000$ GeV/s, $\tau_D \sim 12$ ms

$\tau_D \propto \frac{\rho^2}{E^3}$ suggests high-energy for a small ring. But

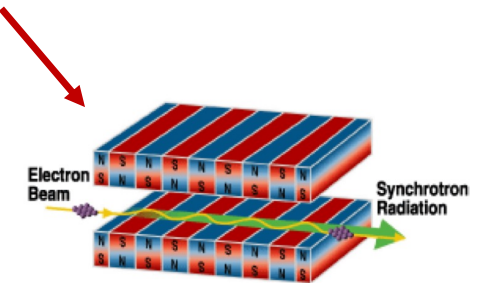
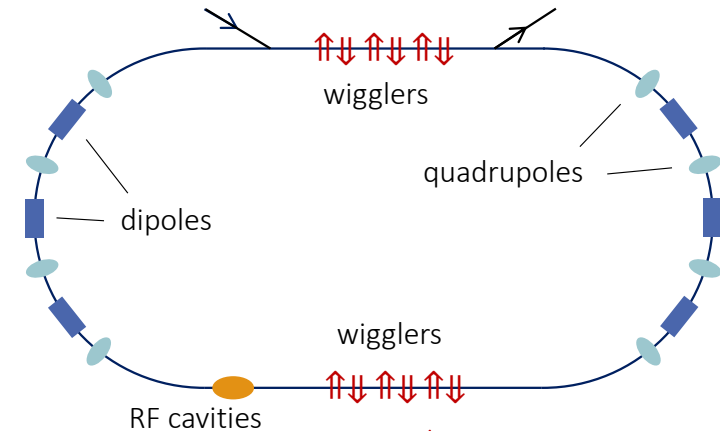
- required RF power: $P_{RF} \propto \frac{E^4}{\rho^2} \times n_b N$
- equilibrium emittance: $\epsilon_{n,x} \propto \frac{E^2}{\rho}$ limit E and ρ in practice
- DR example:
 - Take $E \approx 2$ GeV
 - $\rho \approx 50$ m
 - $P_\gamma = 27$ GeV/s [28 kV/turn]
 - hence $\tau_D \approx 150$ ms - we need 7-8 τ_D !!! \Rightarrow store time too long !!!
- Increase damping and P using wiggler magnets

Insert **wigglers** in straight sections
in the damping ring

- Average **power radiated per electron** with wiggler straight sections

$$P = c \frac{\Delta E_{\text{wiggler}} + \Delta E_{\text{arcs}}}{L_{\text{wiggler}} + 2\pi\rho_{\text{arcs}}}$$

$\Delta E_{\text{wiggler}}$ energy loss in wiggler
 ΔE_{arcs} energy loss in the arcs
 L_{wiggler} total length of wiggler

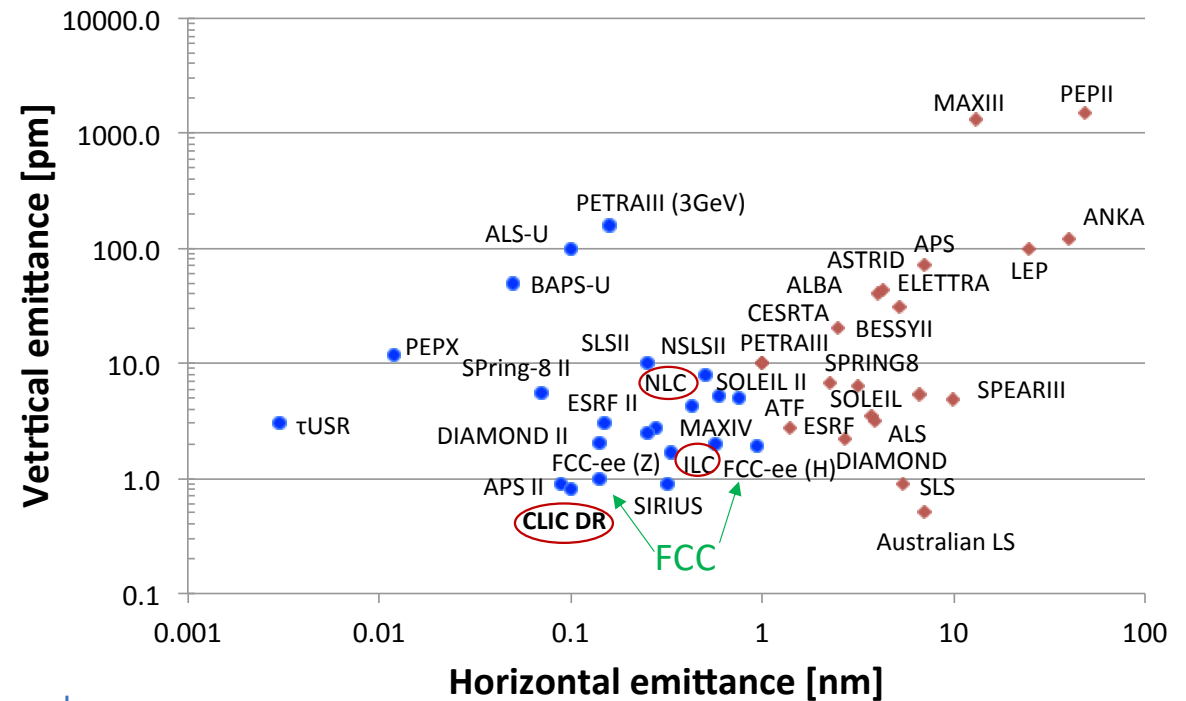


- Energy loss in wiggler:

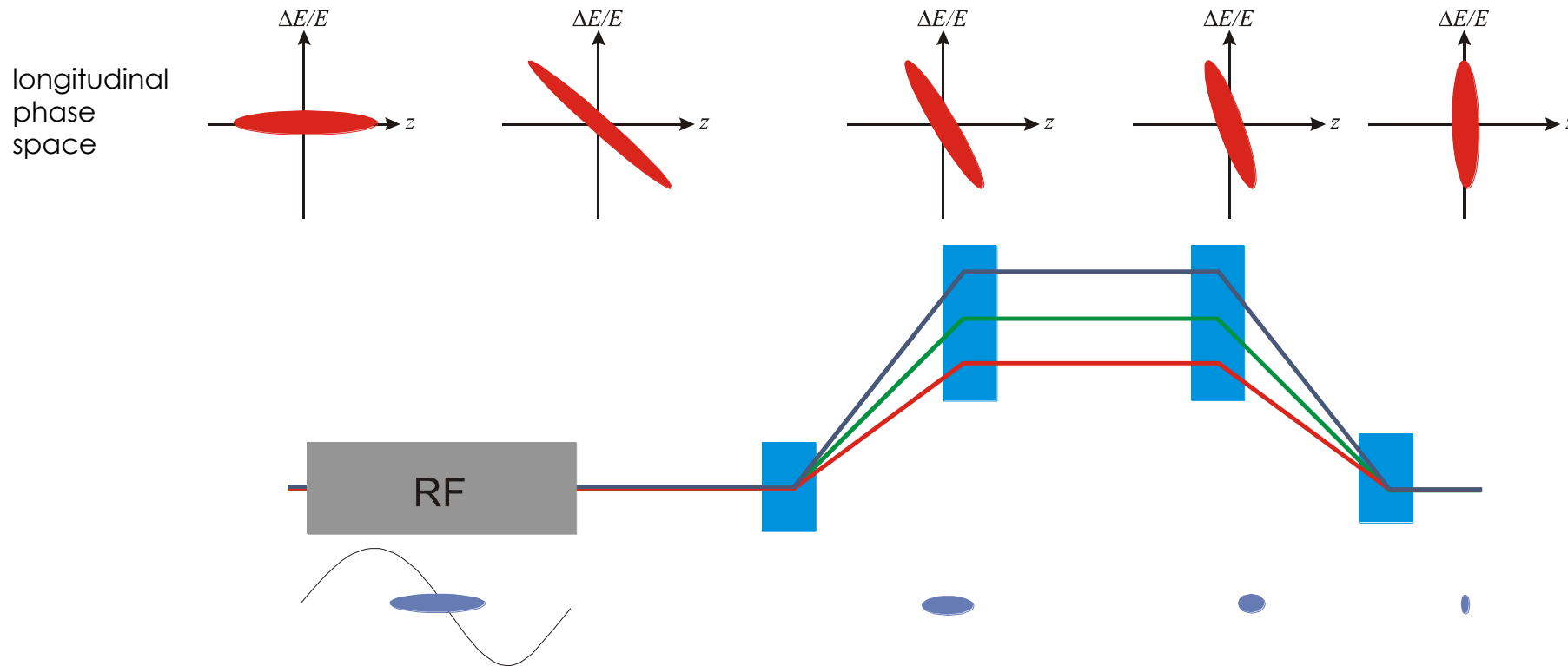
$$\Delta E_{\text{wiggler}} \approx \frac{K_{\gamma}}{2\pi} E^2 \langle B^2 \rangle L_{\text{wiggler}} \quad \text{with } K_{\gamma} \approx 8 \cdot 10^{-6} \text{ GeV}^{-1} \text{ Tesla}^{-2} \text{ m}^{-1}$$

$\langle B^2 \rangle$ is the field square averaged over the wiggler length

- Horizontal emittance ε_x defined by lattice
- Theoretical vertical emittance ε_y limited by
 - Space charge
 - Intra-beam scattering (IBS)
 - Photon emission opening angle
- In practice, ε_y limited by magnet alignment errors [cross plane coupling by tilted magnets]
- typical vertical alignment tolerance: $\Delta y \approx 30 \mu\text{m}$ \Rightarrow requires beam-based alignment techniques!
- DR emittance for LC in the range of existing/planned light sources

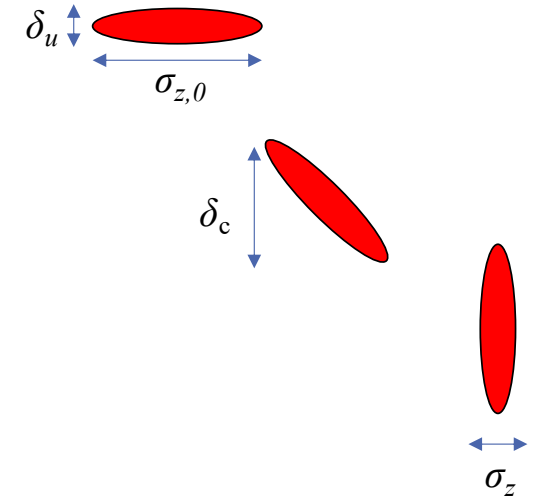


- Bunch length σ_z from damping ring: ~ few mm
- Required at IP: ~ few 100 μm or shorter
- Solution: introduce energy/time correlation and compress with magnetic chicane:



Initial (uncorrelated) momentum spread
 Initial bunch length
 Compression ratio
 Beam energy
 RF induced (correlated) momentum spread
 RF voltage
 RF wavelength
 Longitudinal dispersion (transfer matrix element)

$$\begin{aligned} \delta_u \\ \sigma_{z,0} \\ F_c = \sigma_{z,0} / \sigma_z \\ E \\ \delta_c \\ V_{RF} \\ \lambda_{RF} = 2\pi / k_{RF} \\ R_{56} \end{aligned}$$



conservation of longitudinal
 emittance ($\sigma_z \delta = \text{const}$)



$$F_c = \frac{\sqrt{\delta_c^2 + \delta_u^2}}{\delta_u} \Leftrightarrow \delta_c = \delta_u \sqrt{F_c^2 - 1}$$

fixed by DR

$$\text{RF cavity} \quad \delta_c \approx \frac{k_{RF} V_{RF} \sigma_{z,0}}{E} \Leftrightarrow V_{RF} = \frac{E \delta_c}{k_{RF} \sigma_{z,0}} = \frac{E}{k_{RF}} \left(\frac{\delta_u}{\sigma_{z,0}} \right) \sqrt{F_c^2 - 1}$$

compress at low energy

- Chicane (dispersive section) linear part $z_1 \approx z_0 + R_{56} \delta$

- Minimum bunch length for upright ellipse
 \Rightarrow correlation

$$\langle z\delta \rangle = 0 \quad \langle z\delta \rangle_f = \langle z\delta \rangle_i + R_{56} \delta^2 = 0$$

- Initial correlation

$$\langle z\delta \rangle_i = \frac{k_{RF} V_{RF}}{E} \sigma_{z,0}^2 = \delta_c \sigma_{z,0}$$

- With $\delta^2 = \delta_u^2 + \delta_c^2$ we get

$$R_{56} = -\frac{\delta_c \sigma_{z,0}}{\delta_c^2 + \delta_u^2}$$

- For high compression ratio ($\delta_c \gg \delta_u$)

$$R_{56} \approx -\frac{\sigma_{z,0}}{\delta_c}$$



$$\sigma_{z,0} = 2 \text{ mm}$$

$$\delta_u = 0.1\%$$

$$\sigma_z = 100 \mu\text{m} \Rightarrow F_c = 20$$

$$f_{RF} = 3 \text{ GHz} \Rightarrow k_{RF} = 62.8 \text{ m}^{-1}$$

$$E = 2 \text{ GeV}$$

$$\delta = 2\%$$

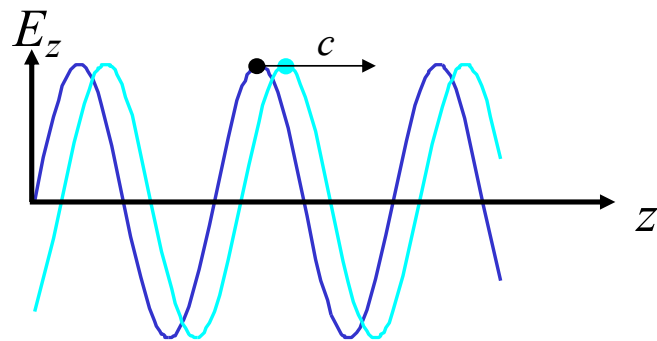
$$V_{RF} = 318 \text{ MV}$$

$$R_{56} = 0.1 \text{ m}$$

- Remark: we get a **large energy spread** after compression
 \Rightarrow large **chromatic effects** in the linac

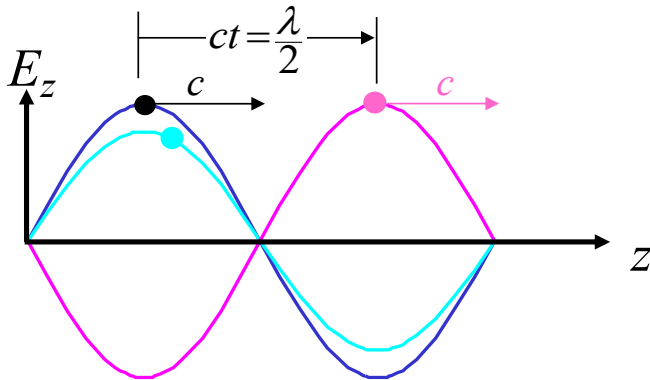
\Rightarrow use a **two-stage compression** with acceleration in between
to reduce relative energy spread along the line

- Now we got small, short bunches we "only" have to **accelerate** them to **collision energy**
- Reminder, **accelerating cavities**:



travelling wave structure:
need *phase velocity* = c
(*disk-loaded structure*)

bunch sees constant field:
 $E_z = E_0 \cos(\varphi)$

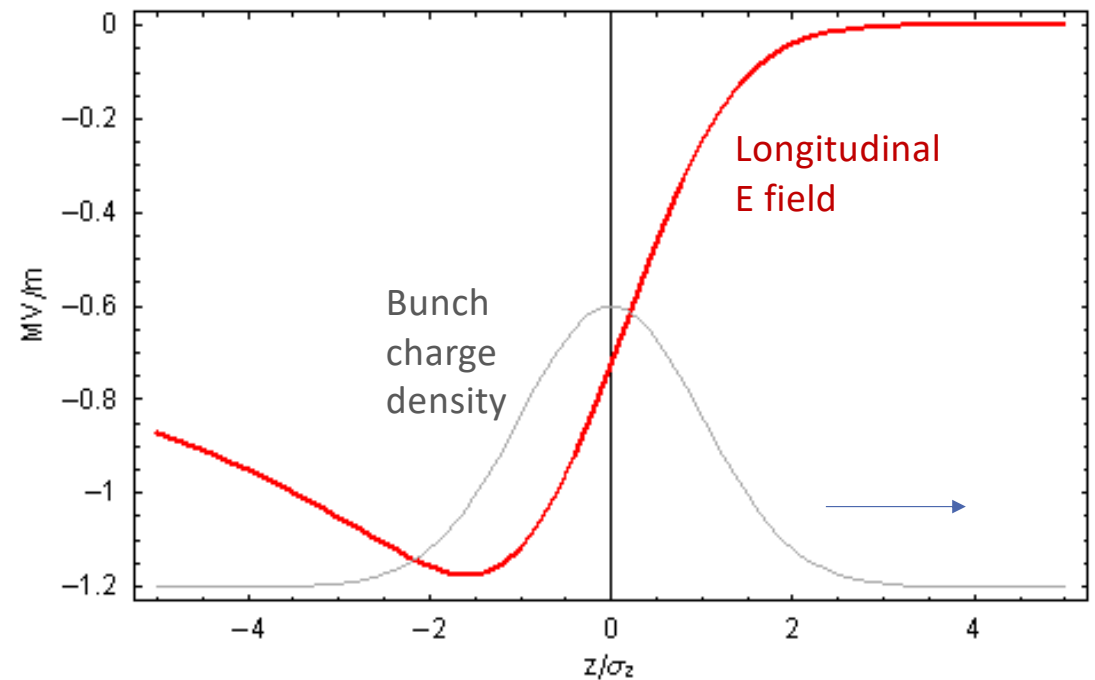


standing wave cavity:

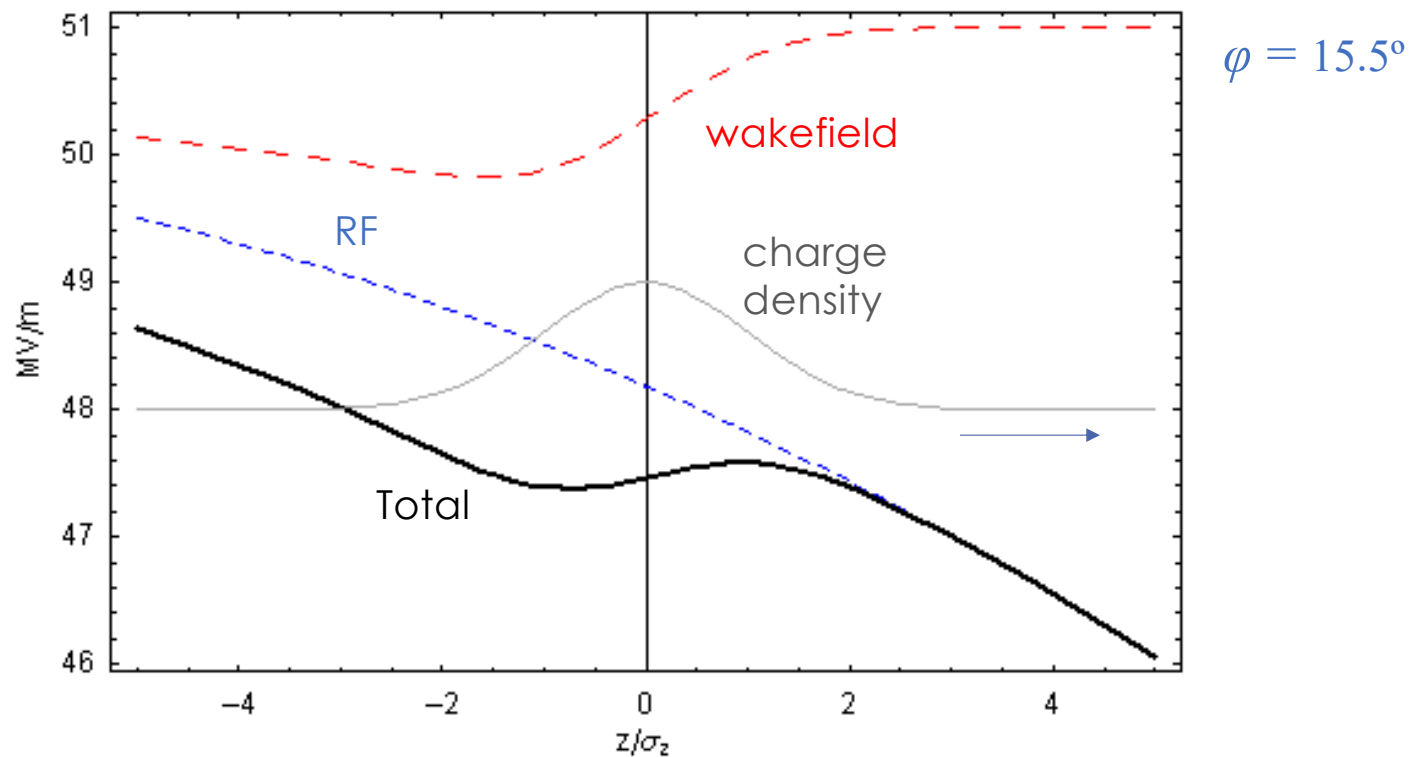
bunch sees field:
 $E_z = E_0 \sin(\omega t + \varphi) \sin(kz)$
 $= E_0 \sin(kz + \varphi) \sin(kz)$

Beam **absorbs** RF power \Rightarrow **decreasing RF field** in cavities

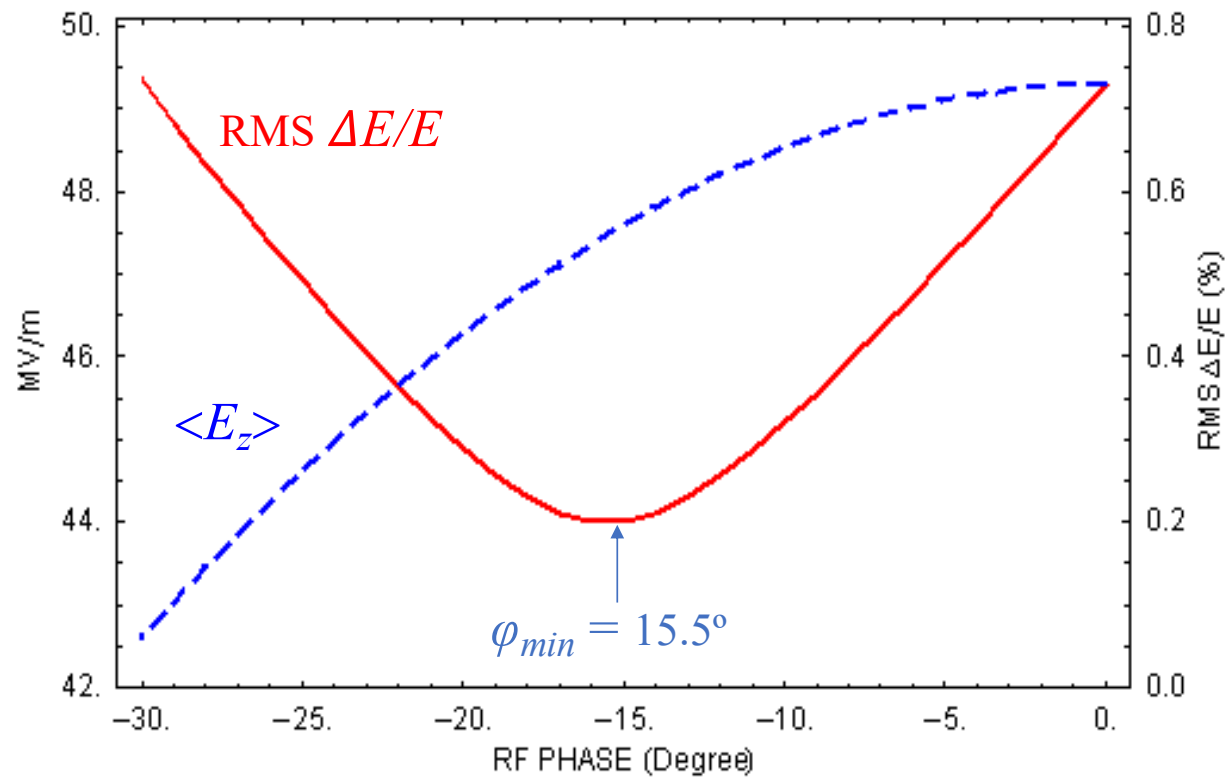
- Single bunch beam loading = single bunch longitudinal wake field
- Particles within a bunch see a decreasing field
 \Rightarrow energy gain **different within a bunch**



- Run **off-crest** and use **RF curvature** to compensate single bunch beam-loading
- Reduces the **effective gradient**



- Minimize momentum spread



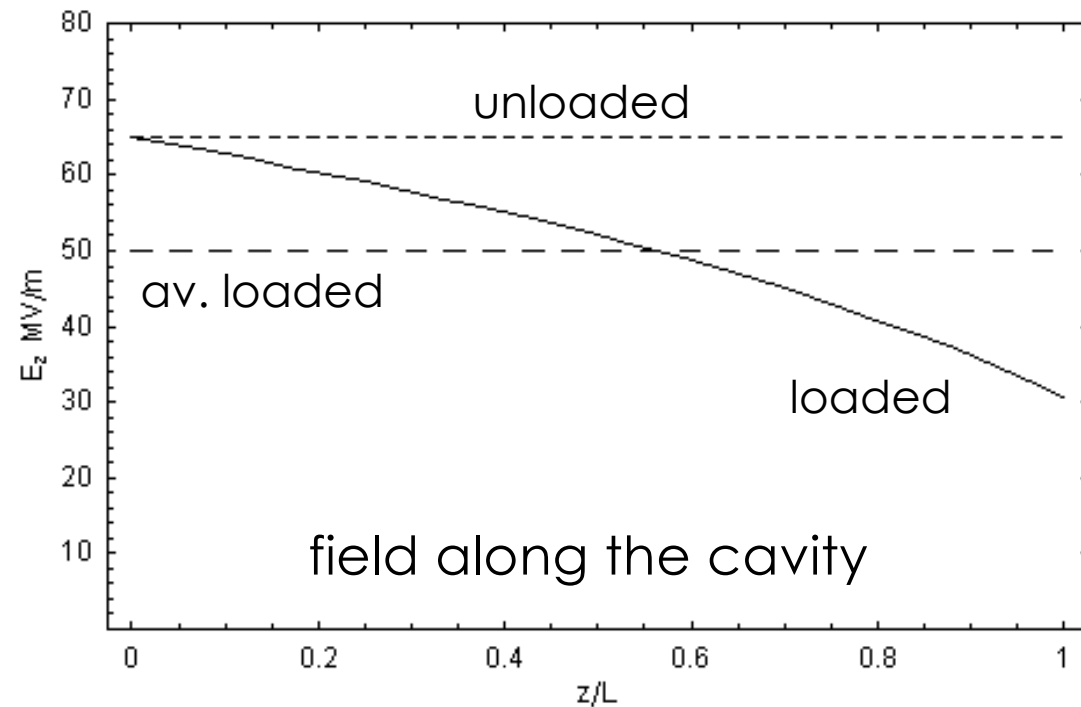
Beam absorbs RF power

⇒ gradient reduced along TW cavity for steady state

$$\frac{dP}{dz} = -\frac{E_z^2}{r_s} - I_b E_z$$

r_s shunt impedance

I_b peak beam current



- Transient beam loading (multi bunch effect):
 - First bunches see the **full unloaded field**, energy gain different from steady state
 - In the LC design, long bunch trains achieve steady state quickly, and previous results very good approximation.
 - However, transient over first bunches needs to be compensated
 - ‘Delayed filling’ of the structure



With **superconducting** standing wave (SW) cavities:

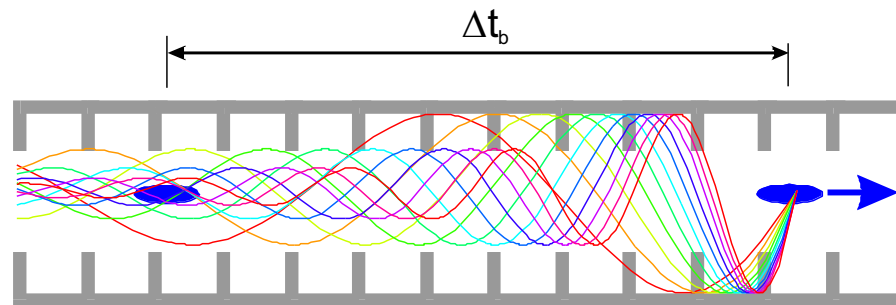
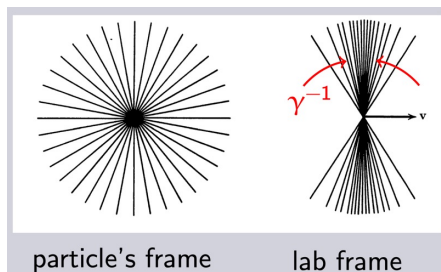
- Very **small losses** to cavity walls
- You can afford **long RF pulse** with
 - Many bunches
 - Large time between the bunches
- **RF feed-back** to compensate **beam-loading** before the next bunch arrives

⇒ **long bunch trains in SC linear collider design**

Linac must preserve the **small beam sizes** (and therefore the emittances), in particular in **vertical plane y**

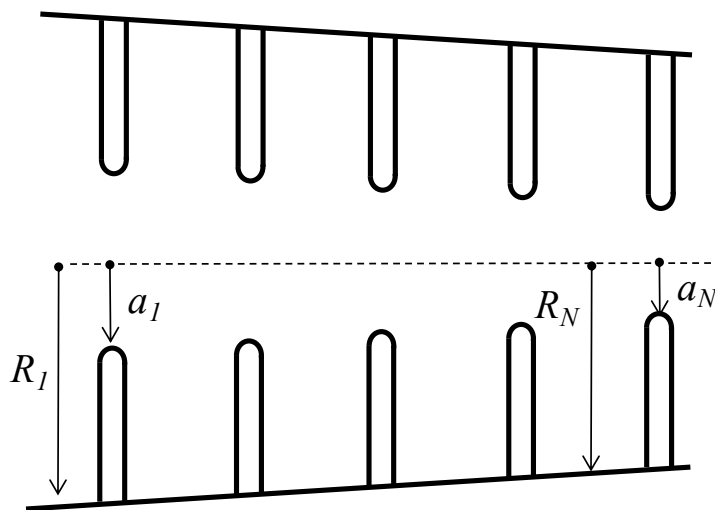
- Possible sources for emittance dilutions are:
 - Dispersive errors, chromaticity: $(\Delta E \rightarrow x, y)$
 - Transverse wakefields: $(z \rightarrow x, y)$
 - Betatron coupling: $(x \rightarrow y)$ and $(y \rightarrow x)$
 - Jitter: $(t \rightarrow x, y)$
- All these can increase the **beam size at the IP**
- Preserve beam size is fundamental to preserve the **luminosity**

Charged particles induce **electromagnetic fields** in the cavities
⇒ later particles are **perturbed** by these fields

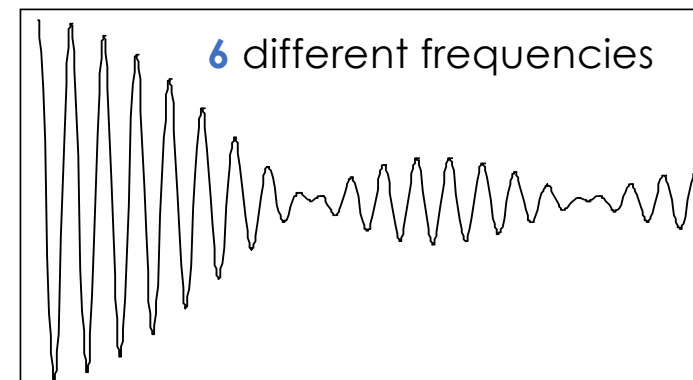
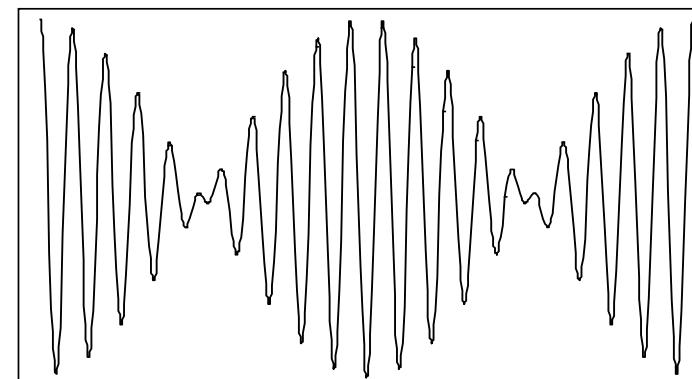


- Bunches passing **off-centre** excite **transverse higher order modes** (HOM)
- Fields can build up resonantly
- Later bunches are kicked transversely
⇒ multi-bunch and single-bunch **beam break-up** (MBBU, SBBU)
- Emittance growth!!!

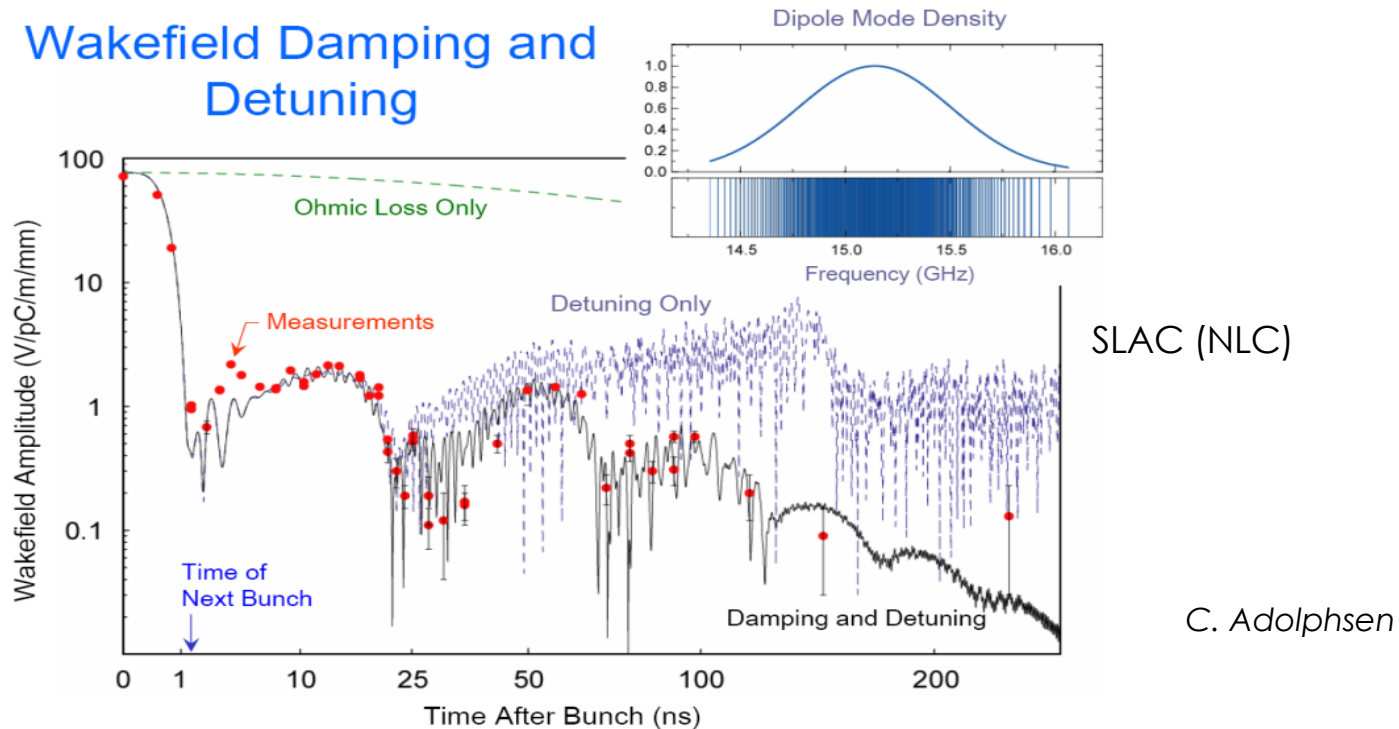
- Effect depends on a/λ (a iris aperture) and structure design details
- Transverse wakefields roughly scale as $W_{\perp} \propto f^3$
- **Less important** for **lower frequency**:
Superconducting (SW) cavities suffer less
- Long-range minimised by structure design
⇒ Dipole mode detuning



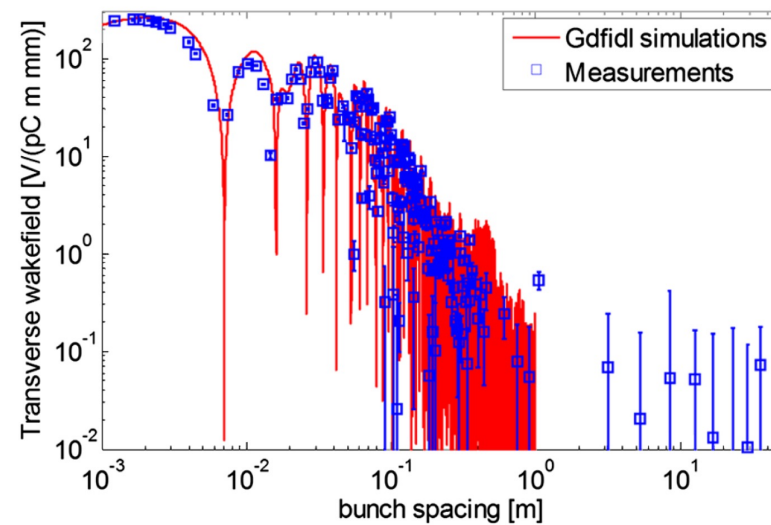
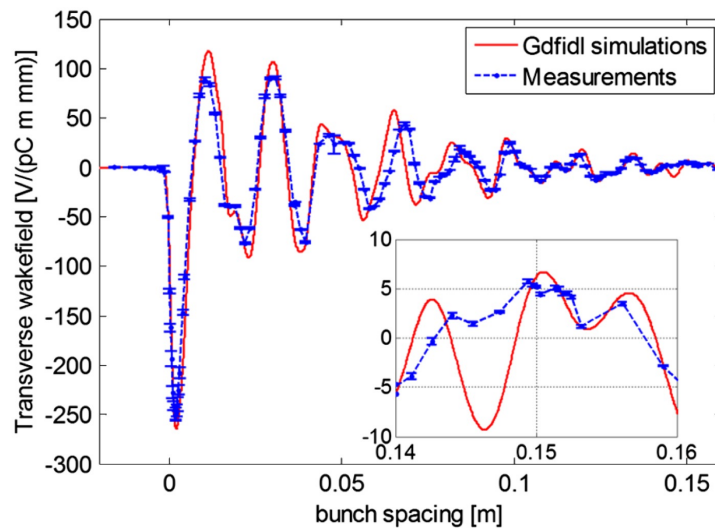
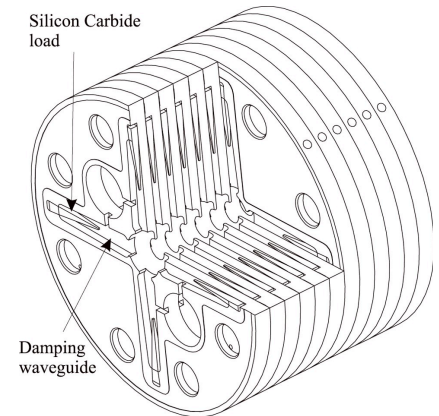
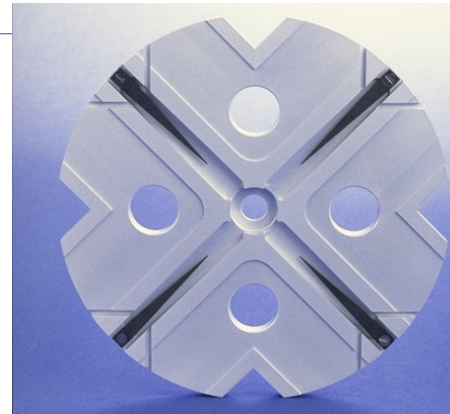
Long range wake of a dipole mode spread over **2** different frequencies



- Slight **detuning** between cells makes HOMs **decohere** quickly
- Will **recohere later**: for long trains need to be **damped** (HOM dampers)



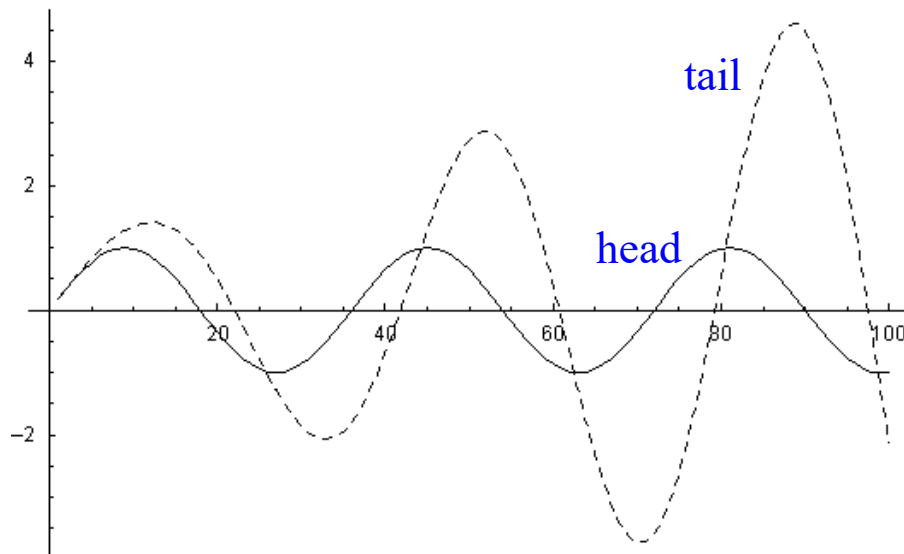
- Each cell damped by 4 radial WGs
- Terminated by SiC RF loads
- HOM enter WG
- Long-range wake efficiently damped



CERN (CLIC)
Measured at
FACET (SLAC)

A. Latina

- Head particle wakefields deflect tail particles
- Particles perform coherent betatron oscillations
- => head resonantly drives the tail



Tail particle
Equation of motion:

$$\frac{d^2 y_t}{ds^2} + k_1 y_t = f(W_\perp) y_h$$

Driven Oscillator !!

More explicit:

$$\frac{d^2 y(z)}{ds^2} + (1 - \delta) K_1 y(z) = \frac{Nr_0}{\gamma} \int_z^\infty dz' \rho(z') y(z') W_\perp(z' - z)$$

- Counteract effective defocusing of tail by wakefield by **increased focusing** on tail
BNS \Rightarrow Balakin, Novokhatski, and Smirnov
- Done by **decreasing tail energy** with respect to head
- Obtained by longitudinally correlated energy spread
(less off-crest than longitudinal wakefield compensation)
 \Rightarrow Transverse wakefields balanced by lattice chromaticity
- 2 particle model:

$$\Delta E = \frac{1}{8} \frac{W_{\perp}(2\sigma_z) Q L_{cell}^2}{\sin^2(\pi q_{\beta})}$$

q_{β} fractional β tune advance per cell
 L_{cell} FODO cell length

- W_{\perp} non-linear
- Good **compensation achievable at the price of larger energy spread**

- BNS damping does not cure random cavity misalignment

- Emittance growth:
$$\Delta\epsilon \approx \delta Y_{RMS}^2 \left[\pi \epsilon_0 N r_e W_{\perp} (2\sigma_z) \right]^2 \frac{L_{acc} \bar{\beta}_i}{2\alpha G} \left[\left(\frac{E_f}{E_i} \right)^{\alpha} - 1 \right]$$

L_{acc} structure length

$\bar{\beta}_i$ initial average beta function

α scaling of the focusing lattice (~ 0.5)

G accelerating gradient

$E_{i,f}$ initial and final energy

- For given (maximum allowed) $\Delta\epsilon$, it scales as
$$\delta Y_{RMS} \propto \frac{1}{NW_{\perp}} \sqrt{\frac{G}{\beta}} \propto \frac{1}{Nf^3} \sqrt{\frac{G}{\beta}}$$

- Higher frequency requires better structure alignment δY_{rms}
- Partially compensated by: higher G , lower β , lower N

End part II